

What is the concentration in blood?

$$\frac{dm}{dt} = D$$

$$\frac{d \text{ m/v}}{dt} = \frac{dc}{dt}$$

$$\frac{dc}{dt} = \frac{D}{V}$$

$$C = \int \frac{D}{V} \cdot t \quad \text{Indefinite integral}$$

$$C(t) = \frac{D}{V} \cdot t \quad [=] \quad \frac{\text{mg} \cdot \text{min}}{\text{max} \cdot \text{L}}$$

But the body can clear the toxin/drug...

Include liver conversion with enzymes to eliminate the drug.

$$\frac{dm}{dt} = D - kC$$

↑  
drug delivery rate  
or  
toxin

↙ rate constant  
↘ drug conc.

$$\frac{dm/v}{dt} = \frac{dC}{dt} = \frac{D}{V} - k'C \quad \frac{k}{V} = k'$$

$$\frac{dC}{dt} = A - bC \quad \text{Integrate by substitution}$$

$$\int \frac{dx}{A - bx} = \int dt \quad \begin{aligned} z &= A - bx \\ dz &= -b dx \end{aligned}$$

$$\int \frac{dz}{-bz} = -\frac{1}{b} \int \frac{1}{z} = -\frac{1}{b} \ln|z|$$

$$-\frac{1}{b} \ln|A - bx| + E = t$$

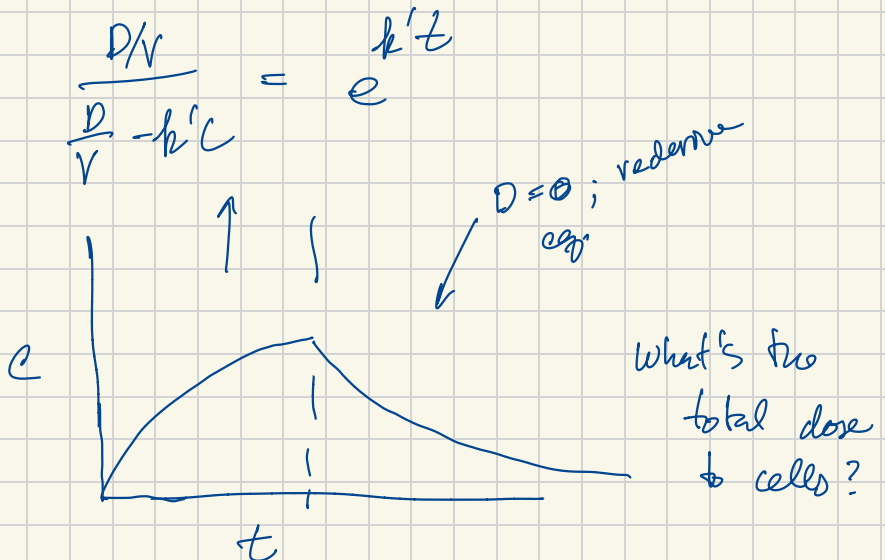
$$-\frac{1}{b} \ln |A - bx| + E = t$$

$$-\frac{1}{k'} \ln \left| \frac{D}{V} - k' C \right| + E = t$$

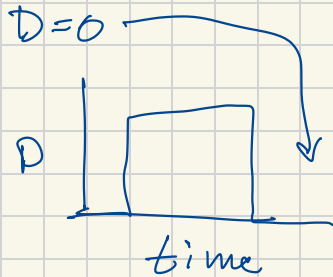
$$@ t = 0 \quad C = 0$$

$$E = \frac{1}{k'} \ln \left| \frac{D}{V} \right|$$

$$\frac{1}{k'} \left[ \ln \frac{D/V}{D/V - k' C} \right] = t$$



What about the condition when



after the dose, what  
is the concentration  
in the blood?

$$\frac{dc}{dt} = \cancel{\frac{D}{V}} - k'c$$

$$\int_{c_0}^c \frac{dc}{-k'c} = \int_{t_d}^t dt$$

$$-\frac{1}{k'} \left[ \ln \frac{c}{c_0} \right] = t - t_d$$

$$c = c_0 e^{-k'(t-t_d)}$$

