Clinton Hawkes CS-225: Discrete Structures in CS Homework 10 Exercise Set 10.7, Problem# 14, 15

## 14. Shortest path from a to z has length L(z) = 7

Step	V(T)	E(T)	F	L(a)	L(b)	L(c)	L(d)	L(e)	L(f)	L(g)	L(z)
0	{a}	Ø	{a}	0	$\infty$						
1	{a}	Ø	{b,e}	0	1	$\infty$	$\infty$	4	$\infty$	$\infty$	$\infty$
2	{a,b}	{{a,b}}	{c,e,f}	0	1	2	$\infty$	4	8	$\infty$	$\infty$
3	{a,b,c}	{{a,b},{b,c}}	{d,e,f,g}	0	1	2	3	4	8	10	$\infty$
4	{a,b,c,d}	{{a,b},{b,c},{c,d}}	{e,f,g,z}	0	1	2	3	4	8	10	23
5	{a,b,c,d,e}	{{a,b},{b,c},{c,d},{a,e}}	{f,g,z}	0	1	2	3	4	5	10	23
6	{a,b,c,d,e,f}	{{a,b},{b,c},{c,d},{a,e},{e,f}}	{g,z}	0	1	2	3	4	5	6	23
7	{a,b,c,d,e,f,g}	{{a,b},{b,c},{c,d},{a,e},{e,f},{f,g}}	{z}	0	1	2	3	4	5	6	7
8	{a,b,c,d,e,f,g,z}	$\{\{a,b\},\{b,c\},\{c,d\},\{a,e\},\{e,f\},\{f,g\},\{g,z\}\}$									

## 15. Shortest path from a to z (where a = a and z = f) has length L(z) = 5

Step	V(T)	E(T)	F	L(a)	L(b)	L(c)	L(d)	L(e)	L(g)	L(z)
0	{a}	Ø	{a}	0	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$
1	{a}	Ø	{b,e,g}	0	3	$\infty$	$\infty$	3	4	$\infty$
2	{a,b,e}	{{a,b},{a,e}}	{c,d,g,z}	0	3	10	14	3	4	7
3	{a,b,e,g}	{{a,b},{a,e},{a,g}}	{c,d,z}	0	3	10	14	3	4	5
4	{a,b,e,g,z}	{{a,b},{a,e},{a,g},{g,z}}								

<sup>\*\*\*</sup>algorithm terminates before finding shortest path to  $\boldsymbol{c}$  and  $\boldsymbol{d}$