Clinton Hawkes CS-225: Discrete Structures in CS Homework 9 Part 2 Exercise Set 10.2, Problem# 2, 9.b, 13, 20

2.

- a) Walk does not start/end on same vertex, uses e2 twice, v1 twice and v2 twice
- b) Simple Circuit start/end on same vertex and uses every other edge/vertex once
- c) Closed Walk start/end on same vertex, but uses v2, v4 and e5 twice
- d) Circuit start/end on same vertex, but uses v2 three times
- e) Trail does not start/end on same vertex. Does not use any edges twice, but uses v2 twice.
- f) Path does not start/end on same vertex and does not use any edge/vertex twice.

9.b

Yes, G has a Euler circuit. Theorem 10.2.4 states a graph has a Euler circuit if it is connected and every vertex has a positive even degree.

13.

No, this does not have a Euler circuit because vertices v1, v7, v8, and v9 have odd degree. This goes against theorem 10.2.4

20.

No, this does not have a Euler path. Though u and w have odd degree, e and h also have odd degrees. This goes against theorem 10.2.5 that states u and w must have odd degree, but all other vertices must be positive and even.