

$y_{i+1}^{(0)}$  is prediction from Euler method,  $y_{i+1}^{(n)}$  are subsequent guesses

$$\begin{aligned}
y_{i+1}^{(1)} &= y_i + \frac{\Delta t}{2} [f(y_i) + f(y_{i+1}^{(0)})] \\
y_{i+1}^{(2)} &= y_i + \frac{\Delta t}{2} [f(y_i) + f(y_{i+1}^{(1)})] & \rightarrow & y_{i+1}^{(2)} - y_{i+1}^{(1)} = \frac{\Delta t}{2} [f(y_{i+1}^{(1)}) - f(y_{i+1}^{(0)})] \\
y_{i+1}^{(3)} &= y_i + \frac{\Delta t}{2} [f(y_i) + f(y_{i+1}^{(2)})] & \rightarrow & y_{i+1}^{(3)} - y_{i+1}^{(2)} = \frac{\Delta t}{2} [f(y_{i+1}^{(2)}) - f(y_{i+1}^{(1)})] \\
&\vdots & & \vdots
\end{aligned}$$

$$\begin{aligned}
y_{i+1}^{(n+1)} - y_{i+1}^{(n)} &= \frac{\Delta t}{2} [f(y_{i+1}^{(n)}) - f(y_{i+1}^{(n-1)})] & \frac{df}{dy} &\approx \frac{f(y_{i+1}^{(n)}) - f(y_{i+1}^{(n-1)})}{y_{i+1}^{(n)} - y_{i+1}^{(n-1)}} \\
y_{i+1}^{(n+1)} - y_{i+1}^{(n)} &= \frac{\Delta t}{2} \frac{df}{dy} [y_{i+1}^{(n)} - y_{i+1}^{(n-1)}]
\end{aligned}$$

If  $\left| \frac{y_{i+1}^{(n+1)} - y_{i+1}^{(n)}}{y_{i+1}^{(n)} - y_{i+1}^{(n-1)}} \right| > 1$ , corrector will not converge

$$\text{system diverges if } \Delta t > \frac{2}{|df/dy|}, \quad \frac{df}{dy} = \frac{\cos y}{\sqrt{y}} - \frac{\sin y}{2y^{3/2}}$$

maximum value for  $y > 1$  :  $|df/dy|_{\max} = 0.5992425\dots$  occurs at  $y = 2.759363\dots$

system converges for  $\Delta t \lesssim 3.3375$