

## Statistics 101A Homework Two

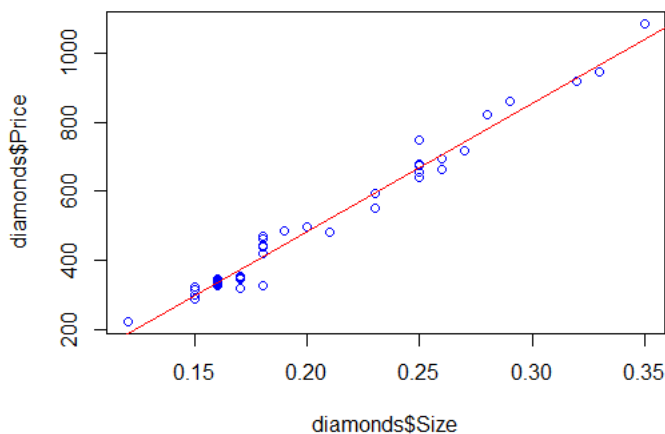
**Question One:** Problem one from chapter three 3.4 Exercises (The data file airfares.txt)

- a) Obviously the model is not a valid one, even though the  $R^2$  is very high. The standardized residuals are having a pattern which means they are not independent nor having a constant variance.
- b) The line seems to be fitting the pattern well but it does because of the large scale of the y variable. This is not a valid model; we can use transformations on the x or the y variables to try to fix the violations.

**Question Two:** Problem eight from chapter three 3.4 exercises (The Diamond stones data file)

**Part 1:**

**Part 1 a)**



```
> Dmod1<-lm(diamonds$Price~diamonds$Size)
> summary(Dmod1)
```

Call:

```
lm(formula = diamonds$Price ~ diamonds$Size)
```

Residuals:

Min	1Q	Median	3Q	Max
-85.654	-21.503	-1.203	16.797	79.295

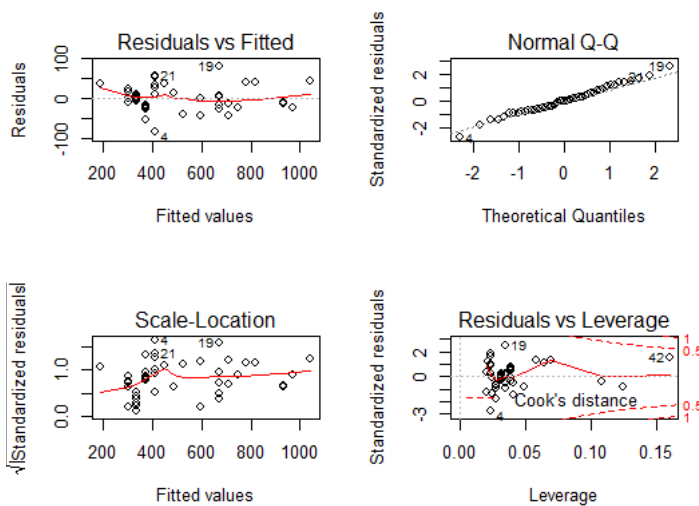
Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-258.05	16.94	-15.23	<2e-16 ***
diamonds\$Size	3715.02	80.41	46.20	<2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 31.6 on 47 degrees of freedom  
 Multiple R-squared: 0.9785, Adjusted R-squared: 0.978  
 F-statistic: 2135 on 1 and 47 DF, p-value: < 2.2e-16



Part 1 B: Slight pattern in the residual plot, and seem to violate the non-constant variance assumption.  $R^2$  is very high and significant, both the slope and the y-intercept estimates are significant

Part 2:

```
> summary(powerTransform(cbind(Size, Price) ~ 1, data=diamonds))
```

bcPower Transformations to Multinormality

	Est	Power	Rounded	Pwr	Wald	Lwr	Bnd	Wald	Upr	Bnd
Size	-0.2393			0		-1.0400			0.5615	
Price	-0.0172			0		-0.6114			0.5771	

Likelihood ratio test that transformation parameters are equal to 0  
(all log transformations)

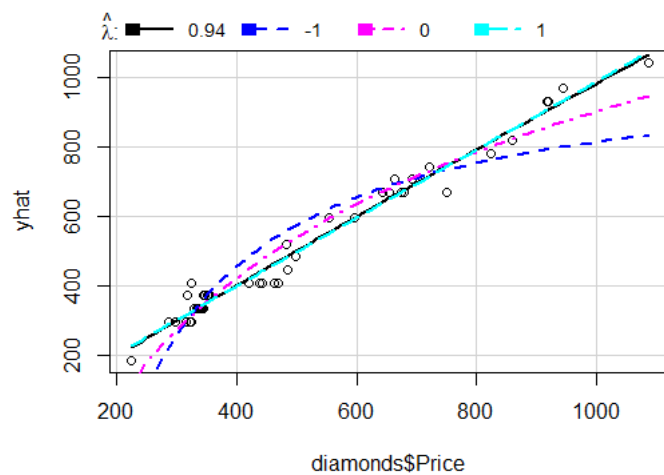
	LRT	df	pval
LR test, lambda = (0 0)	1.432924	2	0.48848

Likelihood ratio test that no transformations are needed

	LRT	df	pval
--	-----	----	------

```
> inverseResponsePlot(Dmod1)
```

	lambda	RSS
1	0.9376257	45670.12
2	-1.0000000	272143.61
3	0.0000000	101071.53
4	1.0000000	45918.17



Inverse response plot is suggesting power of 1 as the best transformation of the response variable.

Power transformation suggests *log of the response* and  $\frac{1}{Size^{0.25}}$  for the predictor.

```
> logpri ce<- log(di amonds$Pri ce)
> T. Si ze<- di amonds$Si ze^(-0. 25)
> Dmod2<-lm(logpri ce~T. Si ze)
> summary(Dmod2)
```

Call:  
lm(formula = logpri ce ~ T. Si ze)

Resi dual s:

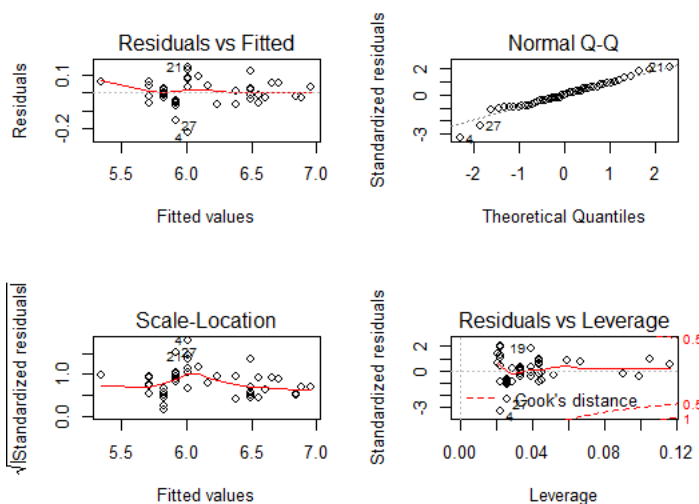
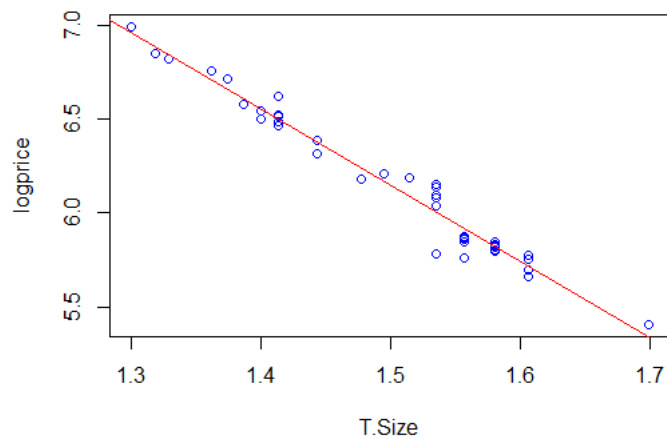
Min	1Q	Medi an	3Q	Max
-0.223411	-0.045628	0.001625	0.038482	0.141232

Coeffi ci ents:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	12.2252	0.1546	79.09	<2e-16 ***
T. Si ze	-4.0501	0.1025	-39.53	<2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.06816 on 47 degrees of freedom  
Multiple R-squared: 0.9708, Adjusted R-squared: 0.9702  
F-statistic: 1563 on 1 and 47 DF, p-value: < 2.2e-16



The diagnostics plots look better and less violation. More good leverage points. Almost a constant variance.

### Question Three:

- Using the stress echo UCLA data (see week four), fit a linear model to predict basal blood pressure from systolic blood pressure. Report the equation for the model. Report a residual plot and comment what it tells us about the assumption of linearity.
- Report the ANOVA table. Show how you can find the F value reported in the ANOVA table using  $R^2$ . What is the null hypothesis that you are testing through ANOVA? Compare the F value that you calculate with value that you find from the F table and decide whether you are going to reject or fail to reject the null hypothesis). Check if this equation is true:  $(Se)^2$  is approximately equal to  $var(Y) * (1 - r^2)$ .

c) Calculate  $R^2$  adjusted and compare it to  $R^2$ . Comment on the difference.

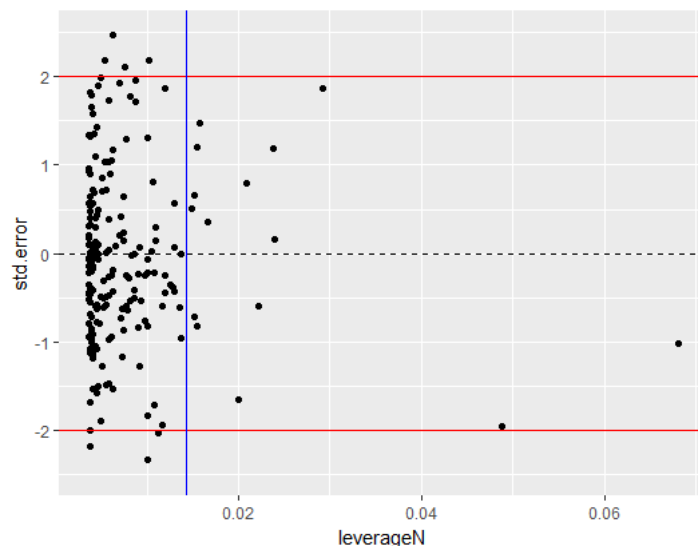
d) Check the diagnostic plots and comment on each one of them.

e) Create two new variables: one for the leverage of a point and one for the standardized residuals. Create a table from both variables to identify the following:

Leverage/Outliers	Yes	No
Yes	1	18
No	12	248

```
> table(LV)
LV
No Yes
260 19
> OL<- ifelse(abs(std.error)>=2, "Yes", "No")
> table(OL)
OL
No Yes
266 13
> table(LV, OL)
      OL
LV     No Yes
No    248 12
Yes   18  1
```

f) Use ggplot2 library to create a plot of Leverage Vs Standardizes residuals divided into regions to help you identify bad and good leverage points, outliers and not leverage points and all the ordinary points.



### Question 5:

Use the Echo data from question three to transform the data and compare the results to the SLR created in question three:

a) Use the inverse response plot to find the best  $\lambda$  to transform the y variable to minimize the SSE. Construct a SLR of the transformed y variable and systolic

blood pressure. Check diagnostics. Is this one better than the SLR in question three.

- b) Use the power transform function to find the best  $\lambda(s)$  to transform both the y variable and the x variable to make the densities of these two variables as close as possible to normal. Construct a SLR of the transformed variables. Check diagnostics. Is this one better than the SLR in question three.

### Q3 and Q5 Key:

```
> Em1<-lm(echo1$basebp~echo1$sbp)
> summary(Em1)
```

Call:

```
lm(formula = echo1$basebp ~ echo1$sbp)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-46.449	-12.456	-1.273	11.444	52.490

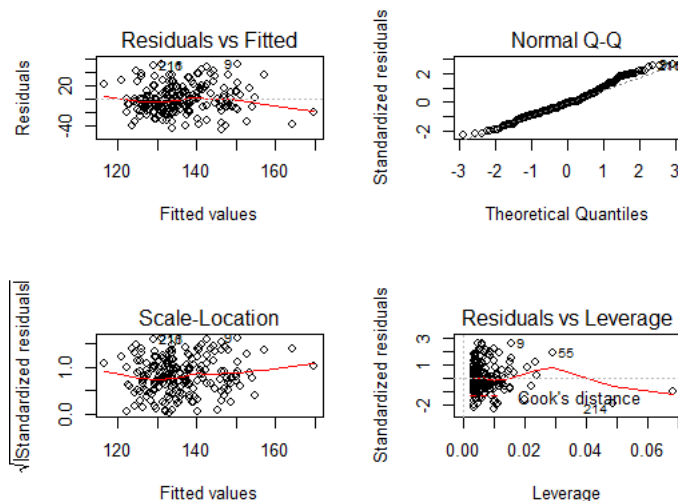
Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	103.70036	4.88943	21.21	< 2e-16 ***
echo1\$sbp	0.21374	0.03176	6.73	9.71e-11 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 19.97 on 277 degrees of freedom  
Multiple R-squared: 0.1405, Adjusted R-squared: 0.1374  
F-statistic: 45.3 on 1 and 277 DF, p-value: 9.705e-11

```
> par(mfrow=c(1, 1))
> plot(echo1$sbp, echo1$basebp)
> abline(Em1)
> par(mfrow=c(2, 2))
> plot(Em1)
```



```
> anova(Em1)
```

Analysis of Variance Table

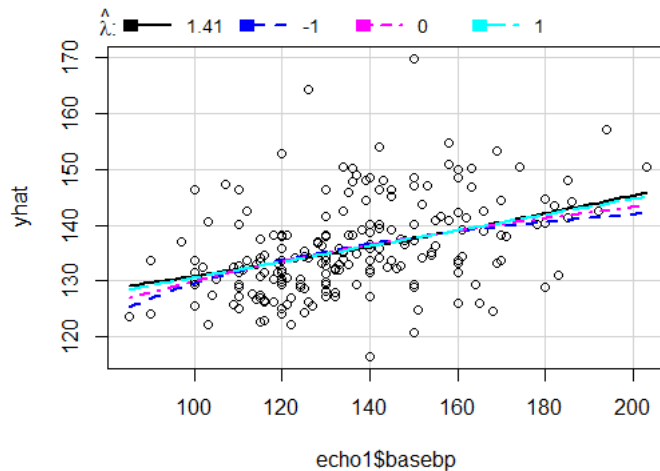
Response:	echo1\$basebp
	Df Sum Sq Mean Sq F value Pr(>F)

```
echo1$sbp    1  18065 18064.7  45.298 9.705e-11 ***
Residuals 277 110466    398.8
```

```
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
> library(car)
> par(mfrow=c(1, 1))
> inverseResponsePlot(Em1)
```

	lambda	RSS
1	1.413234	15521.43
2	-1.000000	15677.80
3	0.000000	15574.03
4	1.000000	15525.77



```
> Em2<-lm(echo1$basebp^(3/2)~echo1$sbp)
> summary(Em2)
```

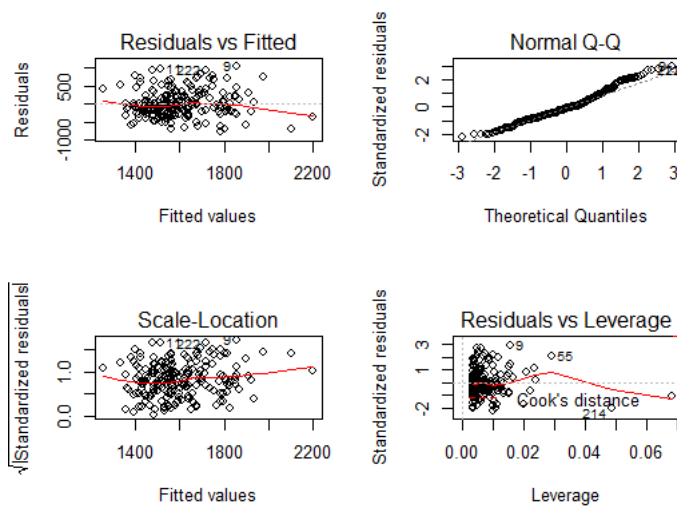
```
Call:
lm(formula = echo1$basebp^(3/2) ~ echo1$sbp)
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-786.35 -225.06  -34.72  199.56 1033.86
```

```
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 1027.4596    86.7166  11.848  < 2e-16 ***
echo1$sbp      3.7944     0.5632   6.737 9.35e-11 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 354.2 on 277 degrees of freedom
Multiple R-squared:  0.1408,    Adjusted R-squared:  0.1377
F-statistic: 45.38 on 1 and 277 DF,  p-value: 9.345e-11
```

```
> par(mfrow=c(2, 2))
> plot(Em2)
```



```
> summary(powerTransform(cbind(echo1$basebp, echo1$sbp) ~ 1, data=echo1))
bcPower Transformations to Multinormality
```

	Est	Power	Rounded	Pwr	Wald	Lwr	Bnd	Wald	Up	Bnd
Y1	0.0105			0	-0.6074			0.6283		
Y2	0.1356			0	-0.2080			0.4792		

Likelihood ratio test that transformation parameters are equal to 0  
(all log transformations)

	LRT	df	pval
LR test, lambda = (0 0)	0.6038973	2	0.73938

Likelihood ratio test that no transformations are needed

	LRT	df	pval
LR test, lambda = (1 1)	32.62618	2	8.2284e-08

```
> anova(Em2)
```

Analysis of Variance Table

Response: echo1\$basebp^(3/2)

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
echo1\$sbp	1	5693057	5693057	45.385	9.345e-11 ***
Residuals	277	34746894	125440		

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

```
> Em3<-lm(log(echo1$basebp)~log(echo1$sbp))
```

```
> summary(Em3)
```

Call:

```
lm(formula = log(echo1$basebp) ~ log(echo1$sbp))
```

Residuals:

Min	1Q	Median	3Q	Max
-0.38990	-0.08984	-0.00312	0.09195	0.34268

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.74996	0.17598	21.309	< 2e-16 ***
log(echo1\$sbp)	0.23064	0.03533	6.528	3.16e-10 ***

---

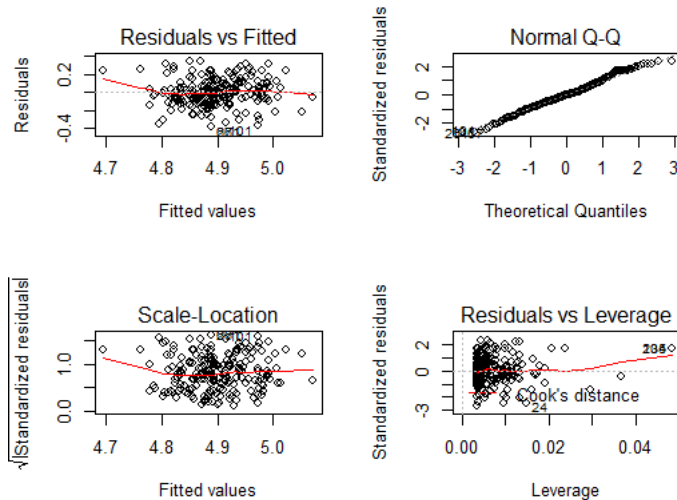
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.147 on 277 degrees of freedom



Multiple R-squared: 0.1333, Adjusted R-squared: 0.1302  
 F-statistic: 42.62 on 1 and 277 DF, p-value: 3.163e-10

```
> par(mfrow=c(2, 2))
> plot(Em3)
```



```
> anova(Em3)
```

Analysis of Variance Table

Response: log(echo1\$basebp)

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
log(echo1\$sbp)	1	0.9209	0.92089	42.619	3.163e-10 ***
Residuals	277	5.9852	0.02161		

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

#### Question Four:

Consider the following R output predicting Marine water growth from Freshwater growth in Salmon:

```
> SL1<- lm(salmon$Marine~salmon$Freshwater)
```

```
> summary(SL1)
```

Call:

```
lm(formula = salmon$Marine ~ salmon$Freshwater)
```

Residuals:

Min	1Q	Median	3Q	Max
-88.222	-27.382	-3.406	24.784	89.977

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	511.3656	18.2547	28.01	< 2e-16 ***
salmon\$Freshwater	-0.9602	0.1512	-6.35	6.75e-09 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 39.12 on 98 degrees of freedom

Multiple R-squared: 0.2915, Adjusted R-squared: 0.2843

F-statistic: 40.32 on 1 and 98 DF, p-value: 6.747e-09

```
> summary(salmon$Freshwater)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
53.0	99.0	117.5	117.9	140.0	179.0

```
> var(salmon$Freshwater)
```

```
[1] 676.0541
```

```
> summary(salmon$Marine)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
301.0	367.0	396.5	398.1	428.2	511.0

```
> var(salmon$Marine)
```

```
[1] 2138.142
```

a) Construct ANOVA table based on the given output.

```
> anova(SL1)
```

Analysis of Variance Table

Response: salmon\$Marine

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
salmon\$Freshwater	1	61706	61706	40.323	6.747e-09 ***
Residuals	98	149970	1530		

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Consider the three observations: 4, 41 and 53

Observation	SalmonOrigin	Freshwater	Marine
1	4	Alaska	86
2	41	Alaska	506 (outlier)
3	53	Canada	84
			511 (outlier)
			179
			407 (Good Leverage)

b) Which of these three points is a leverage point?

c) Which of these three points is an outlier?

d) Based on your answers of part b and c, classify these points as one of the following:

i) A bad leverage point

ii) An outlier but Not a leverage point.

iii) A good leverage point

iv) Not a leverage point nor an outlier (ordinary)

