# **Attention-based Recursive Neural Networks for Semantic Representation**

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#### **Abstract**

The attention mechanism has succeeded in many NLP tasks. While existing attention-based models exert attention on sequential memories, we attempt to focus attention recursively on local tree structures. Specially, we use the attention mechanism to select semantically more relevant modifier words to construct a sentence representation on a dependency tree using LSTM and GRU, respectively. Our attention-based recursive neural networks outperform the non-attention counterparts in semantic relatedness and sentiment classification, and achieve the state-of-the-art performance.

# 1 Introduction

It has been shown that distributed representation of word achieves superior performance in many high-level NLP tasks. However, with word vectors, it is still challenging to obtain a good sentence representation due to the diversity in the sentence length and word order. There are two typical approaches for sentence-level semantic representations: sequence-based and tree-based models. The sequence-based models, such as the recurrent neural networks (RNNs) (Elman, 1990; Mikolov, 2012), treat composing a sentence representation as a sequential composition of words from left to right. On the other hand, the tree-based models, such as the recursive neural networks (Goller and Kuchler, 1996; Socher et al., 2011), compose a representation button up based on the parse tree of the sentence.

Amongst the tree-based neural networks (Tree-NNs), the Tree-LSTMs (Tai et al., 2015) recursively applies the LSTM to derive the representations for the internal nodes in the parse trees. Specifically, they propose an *N-ary Tree-LSTM* 

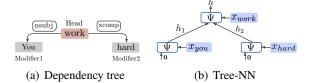


Figure 1: A tree-based neural network (Tree-NN), e.g. tree-LSTM, derives a sentence representation h using the word vector  $x_{work}$  and the recursive input  $h_1$  and  $h_2$  from the children based on the dependency tree.

for constituent trees as well as a *Child-Sum Tree-LSTM* for dependency trees. Experiment results show that the Tree-LSTMs are effective for semantic representations.

In this paper, we extend the Child-Sum Tree-LSTM by using the *attention mechanism*. As shown in Figure 1(b), a Tree-NN derives the representation of each head word in the dependency tree from the representations of the head word's modifier words. The attention mechanism enables our model to derive better sentence representation by attaching difference emphases to the recursive input from the modifier words in forms of weights, which are obtained from a trained neural network. Our contributions are summarized as follows:

- 1. We firstly apply the attention mechanisms to the recursive Tree-NNs, and propose extensions to both GRU and LSTM.
- We conduct extensive experiments on two semantic tasks: semantic relatedness (SemEval 2014, Task 1) and sentiment classification (Stanford Sentiment Treebank).
- 3. Our attention-based Tree-NNs outperform the non-attention counterparts and achieve the state-of-the-art performance.

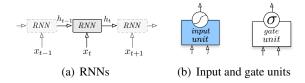


Figure 2: RNNs, input unit and gate unit in LSTM.

# 2 Preliminaries

In this section, we will briefly discuss RNN, LSTM, GRU, Tree-LSTM, as well as Tree-GRU, a simple variant of the Tree-LSTM.

## 2.1 Recurrent neural network (RNN)

Given an input sequence of T words, an RNN (Figure 2(a)) iteratively computes an output  $h_t$  using word  $x_t$  ( $1 \le t \le T$ ) and the RNN's previous output  $h_{t-1}$ . The output  $h_T$  for the last word in the sentence will be used as the representation of the whole sentence. Unfortunately, in such an RNN, the propagation of the memory of earlier part of the sentence diminishes in long sentences.

## 2.2 Long short-term memory (LSTM)

The LSTM (Hochreiter and Schmidhuber, 1997; Zaremba and Sutskever, 2014) preserves long-term memory by adding a recurrent memory cell. As shown in Figure 3(a), an LSTM has a memory cell  $c_t$  and three gates: the input gate  $i_t$ , the forget gate  $f_t$  and the output gate  $o_t$  at a time step t. The input  $u_t$  is computed by the *input unit I*, and the three gates,  $i_t$ ,  $f_t$ , and  $o_t$ , are all computed by the same kind of *gate unit G* but with different parameter  $\theta = (W, U, b)$ . The input unit and the gate unit are shown in Figure 2(b) and defined in Equations 1.

$$I(x,h) = \tanh(W^{(u)}x + U^{(u)}h + b^{(u)}),$$
  

$$G_{\theta}(x,h) = \sigma(Wx + Uh + b).$$
(1)

The LSTM is illustrated in Figure 3(a) and formally defined in Equations 2.

$$u_{t} = I(x_{t}, h_{t-1}), f_{t} = G_{\theta_{f}}(x_{t}, h_{t-1}),$$

$$i_{t} = G_{\theta_{i}}(x_{t}, h_{t-1}), o_{t} = G_{\theta_{o}}(x_{t}, h_{t-1}),$$

$$c_{t} = i_{t} \odot u_{t} + f_{t} \odot c_{t-1},$$

$$h_{t} = LSTM(x_{t}, h_{t-1}, c_{t-1})$$

$$= o_{t} \odot \tanh(c_{t}).$$
(2)

## 2.3 Gated recurrent unit (GRU)

The GRU (Chung et al., 2014) is one of the simplified variants of the LSTM that has only two gates

and the memory cell removed. As shown in Figure 3(d) and defined in Equations 3, in a GRU, the reset get  $r_t$  is similar to the  $f_t$  in LSTM, and the update gate  $z_t$  is similar to  $i_t$  and  $o_t$  in LSTM.

$$r_{t} = G_{\theta_{r}}(x_{t}, h_{t-1}), \quad z_{t} = G_{\theta_{z}}(x_{t}, h_{t-1}),$$

$$\tilde{h}_{t} = I(x_{t}, r_{t} \odot h_{t-1}),$$

$$h_{t} = GRU(x_{t}, h_{t-1})$$

$$= z_{t} \odot h_{t-1} + (1 - z_{t}) \odot \tilde{h}_{t}.$$
(3)

## 2.4 Child-Sum Tree-LSTM

While conventional LSTM has a single pair of recurrent input  $h_t$  and  $c_t$ , being a Tree-NN (Figure 1(b)), the Tree-LSTM has multiple recursive input,  $h_1, h_2, \ldots, h_k, c_1, c_2, \ldots, c_k$ , where k is the number of children of the current node. The  $Child-Sum\ Tree-LSTM$  (Tai et al., 2015), as illustrated in Figure 3(b) and defined in Equations 4, handles multiple recursive input  $h_i$  by summing them, besides using multiple forget gates  $f_i$  for the recursive memory cells  $c_i$ . For clarity, in all of the Tree-NNs described thereafter, we omit the subscript for the current node.

$$h = LSTM_{sum}^{tree}(x, h_1 \dots h_k, c_1 \dots c_k)$$

$$= LSTM(x, \hat{h}, \{c_1 \dots c_k\}),$$
where:
$$\hat{h} = \sum_{1 \le i \le k} h_i, \quad f_i = G_{\theta_{f,i}}(x, h_i),$$

$$\hat{c} = i \odot u + \sum_{1 \le i \le k} f_i \odot c_i.$$
(4)

The *Child-Sum Tree-LSTM* is well suited for dependency trees, where the children (modifiers) are order-insensitive.

## 2.5 Child-Sum Tree-GRU

Similar to the way that *Child-Sum Tree-LSTM* extends the conventional LSTM in dependency trees, we define a *Child-Sum Tree-GRU*. As illustrated in Figure 3(e) and defined in Equations 5, the *Child-Sum Tree-GRU* defines multiple reset gates  $r_i$  for each recursive input  $h_i$ .

$$h = GRU_{sum}^{tree}(x, h_1 \dots h_k) = GRU(x, \hat{h}),$$
where:
$$\hat{h} = \sum_{1 \le i \le k} h_i, \quad r_i = G_{\theta_{r,i}}(x, h_i),$$

$$\tilde{h} = I(x, \sum_{1 \le i \le k} r_i \odot h_i).$$
(5)

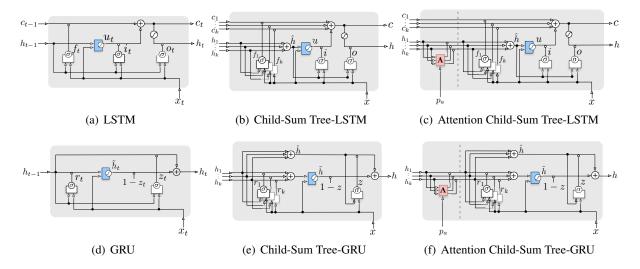


Figure 3: Illustrations of different architectures.

## 3 Attention-based Tree-NNs

### 3.1 The attention unit

Our attention mechanism for Tree-NNs is implemented by an *attention unit* A, which is defined below in Equations 6. Given the memory input from k children nodes,  $h_1^{(in)}, h_2^{(in)}, \ldots, h_k^{(in)}$ , the attention unit A first computes a weight vector  $w \in \mathbb{R}^k$  using a two-layer neural network, and then multiply each input  $h_i^{(in)}$  with the weight  $w_i$  to produce each of its k output  $h_i^{(out)}$ .

$$\alpha_{i} = V_{i}^{(a)} \tanh(W^{(a)} h_{i}^{(in)} + U^{(a)} p_{a}),$$

$$w = \operatorname{softmax}([\alpha_{1}, \alpha_{2}, \dots, \alpha_{k}]), \qquad (6)$$

$$h_{i}^{(out)} = w_{i} h_{i}^{(in)}, \qquad (1 \leq i \leq k).$$

In Equations 6,  $V^{(a)}$ ,  $W^{(a)}$  and  $U^{(a)}$  are the hyperparameters in the two-layer neural network;  $p_a$  is called the *attention parameter*, which is used to affect the weight  $w_i$  that is computed for each memory input  $h_i^{(in)}$ . We will discuss different implementations of  $p_a$  in Section 3.3.

## 3.2 Attention-based Tree-LSTM and GRU

Our attention-based Tree-LSTM (Figure 3(c)) and attention-based Tree-GRU (Figure 3(f)) are implemented by appending the Tree-LSTM and Tree-GRU to the attention unit, respectively. Concretely, the memory input  $h_1, h_2, \ldots, h_k$  from the children are weighted by the attention unit before entering a Tree-LSTM or Tree-GRU. Thus, different emphases are placed to different children inputs by the attention unit via the attention parameter.

For space limitations, this paper only proposed the attention-based extension to the Child-Sum Tree-LSTM and GRU. With the attention unit, it is straightforward to extend other RNNs, such as the *N-ary Tree-LSTM* (Tai et al., 2015).

### 3.3 Variants of the attention Tree-NN

The two attention-based Tree-NNs adopt different *attention parameter* implementations.

**Static-attention Tree-NNs**. In this implementation, the value of the *attention parameter*  $p_a$  is simply fixed to a constant. Since the weight w is computed by the attention unit, the value of  $p_a$  can be a small floating number.

**Dynamic-attention Tree-NNs.** This implementation uses the sentence representation from a simpler model (i.e. a sequential RNN) as  $p_a$ , and then feeds  $p_a$  to the attention-based Tree-NN to produce the final representation. In this implementation, the sequential RNN and the attention Tree-NN are trained jointly.

## 3.4 Training

We use the 300-dimensional *Glove vectors* (Pennington et al., 2014) as the initial word representations. Out-of-vocabulary words are randomly initialized for a uniform distribution.

We used AdaGrad (Duchi et al., 2011) for optimization, with a learning rate of 0.05, and a minibatch size of 25. We also apply the L2 regularization to our model parameters with  $\lambda=10^{-4}$ . In our evaluations, the sentiment classifier used is regularized using *dropout* (Hinton et al., 2012) with a dropout rate of 0.5.

Method	r	$\rho$	MSE	Method
Illinois-LH (Lai and Hockenmaier, 2014)	0.7993	0.7538	0.3692	Paragraph-Vec (Le and Mikolov, 2014)
UNAL-NLP (Jimenez et al., 2014)	0.8070	0.7489	0.3550	CNN-non-static (Kim, 2014)
Meaning Factory (Bjerva et al., 2014)	0.8268	0.7721	0.3324	CNN-multichannel (Kim, 2014)
ECNU (Zhao et al., 2014)	0.8414	-	-	DRNN (Irsoy and Cardie, 2014)
LSTM (Tai et al., 2015)	0.8528	0.7911	0.2831	LSTM (Tai et al., 2015)
Bidirectional LSTM (Tai et al., 2015)	0.8567	0.7966	0.2736	Bidirectional LSTM (Tai et al., 2015)
Child-Sum Tree-LSTM (Tai et al., 2015)	0.8676	0.8083	0.2532	Child-Sum Tree-LSTM (Tai et al., 2015)
combine-skip+COCO (Kiros et al., 2015)	0.8655	0.7995	0.2561	N-ary Tree-LSTM (Tai et al., 2015)
GRU	0.8595	0.7974	0.2689	GRU
Bidirectional GRU	0.8662	0.8025	0.2603	Bidirectional GRU
Child-Sum Tree-GRU	0.8672	0.8116	0.2573	Child-Sum Tree-GRU
Static-attention Child-Sum Tree-GRU	0.8730	0.8117	0.2426	Static-attention Child-Sum Tree-GRU
Static-attention Child-Sum Tree-LSTM	0.8692	0.8106	0.2528	Static-attention Child-Sum Tree-LSTM
Dynamic-attention Child-Sum Tree-GRU	0.8684	0.8106	0.2548	Dynamic-attention Child-Sum Tree-GRU
Dynamic-attention Child-Sum Tree-LSTM	0.8701	0.8085	0.2524	Dynamic-attention Child-Sum Tree-LSTM

Table 1: The evaluation metrics of the SICK semantic relatedness subtask are Pearson's r, Spearman's  $\rho$  and MSE. The first group is the SemEval 2014 baselines, and the last group is our results.

# 4 Experiments

## 4.1 Semantic relatedness

First we conduct our experiment on the semantic relatedness SICK dataset (Marelli et al., 2014). This task is to predict a similarity score of a pair of sentences, based on human generated scores. The score values range from 1 to 5, and higher score indicates that the pair of sentences are semantically related. This dataset consists of 9927 sentence pairs with the split of 4500 training pairs, 500 development pairs and 4927 testing pairs. The similarity score  $\hat{y}$  is computed by a neural network whose input is a representation pair  $(h_L, h_R)$ :

$$h_{\times} = h_{L} \odot h_{R}, \quad h_{+} = |h_{L} - h_{R}|,$$

$$h_{s} = \sigma(W^{(x)}h_{\times} + W^{(+)}h_{+} + b^{(h)}),$$

$$\hat{p}_{\theta} = softmax(W^{(p)}h_{s} + b^{(p)}),$$

$$\hat{y} = r^{\mathsf{T}}\hat{p}_{\theta},$$
(7)

where  $r^{\mathsf{T}} = [1, 2, ..., 5]$  is an integer vector. We compute target distribution p as a function of prediction scores y given by  $p_i = y - \lfloor y \rfloor$  if  $i = \lfloor y \rfloor + 1$ ,  $p_i = \lfloor y \rfloor - y + 1$  if  $i = \lfloor y \rfloor$ , and 0 otherwise. The cost function is the regularized KL-divergence between p and  $\hat{p}_{\theta}$ .

The SemEval results are summarized in Table 1. All of our models are able to outperform the best submission in the SemEval 2014 competition. Our attention-based Tree-LSTM performs better than the Child-Sum Tree-LSTM (Tai et al., 2015) thanks to the attention mechanism. Our Static-attention Tree-GRU achieves the state-of-the-art performance in all of the three metrics. All results shows that our attention-based Tree-NNs

Table 2: The test set accuracies on the Stanford Sentiment Treebank. **Fine-grained**: 5-class classification. **Binary**: 2-class classification.

Binary(%)

87.2

88.1

86.6

84 9

87.5 85.7

85.6

85.1

85.5

86.2

87.5

Fine-grained(% 48.7 48.0

47.4

498

46.4

49.1

48.4

46.8

47.8

48.1

50.3

49.1

learn better representations for semantic relatedness.

### 4.2 Sentiment classification

The Stanford Sentiment Treebank (SST) is a benchmark for sentiment classification. Each sentence from a movie review is parsed as a constituency tree. Each node in a tree is annotated with a sentiment polarity label. This dataset contains two classification tasks: (1) binary classification: positive, negative, and (2) finegrained classification: very negative, negative, neutral, positive, and very positive. In this experiment, we use the predefined train/dev/test splits of 6920/872/1821 for the binary classification subtask and 8544/1101/2210 for the fine-grained classification subtask. The classification criterion used is the *Negative Log Likelihood*.

The results on sentiment classification task are presented in Table 2. Our attention-based Child-Sum Tree-LSTM obtains the state-of-the-art performance in binary classification. Again, comparison to the corresponding non-attention models, each of our attention-based model achieves better accuracy. In the fine-gained classification task, the Static-attention Tree-LSTM precedes the Child-Sum Tree-LSTM nearly two percents.

## 5 Conclusion

In this paper, we proposed the attention-based recursive neural networks for better semantic representation. In our experiments, our models outperformed non-attention counterparts and demonstrated the state-of-the-art performance in semantic relatedness and sentiment classification.

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