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% SIO 229 Homework 3, Magnetism HW # 1
clear all; close all; clc
```

Question 1: Plot magnetic field elements against latitude

Suppose we have a magnetic dipole with dipole moment m at Earth's center and oriented along Earth's axis. Calculate (i) the magnetic field elements B_r , B_{θ} , B_{ϕ} , and (ii) the declination, inclination, and intensity as a function of latitude.

```
% Calculate the magnetic field as a function of latitude

rEarth = 6371000; % Earth's radius in m
mu0 = 4*pi*1e-7; % Permeability of vacuum in henries/
meters
m = 8e22; % Dipole moment in ampere*m^2
theta = 0:180; % colatitude in degrees
phi = 0:360; % longitude in degrees
B_r = mu0*m*(2*cosd(theta))/(4*pi*rEarth^3); % Magnetic field in tesla
for unit r
B_theta = mu0*m*(sind(theta))/(4*pi*rEarth^3); % Magnetic field in
tesla for unit theta
B_phi = zeros(1,length(theta)); % Magnetic field in tesla
for unit phi

figure(1)
plot(theta, B_r, 'LineWidth',1)
hold on
plot(theta, B_theta, 'LineWidth',1)
plot(theta, B_phi, 'LineWidth',1)
title('B_r, B_{\theta}, B_{\phi} vs. Colatitude','FontSize',15)
xlabel('Colatitude \theta in degrees','FontSize',15)
ylabel('B components T','FontSize',15)
set(gcf,'color','w');
legend('B_r', 'B_{\theta}', 'B_{\phi}')
hold off

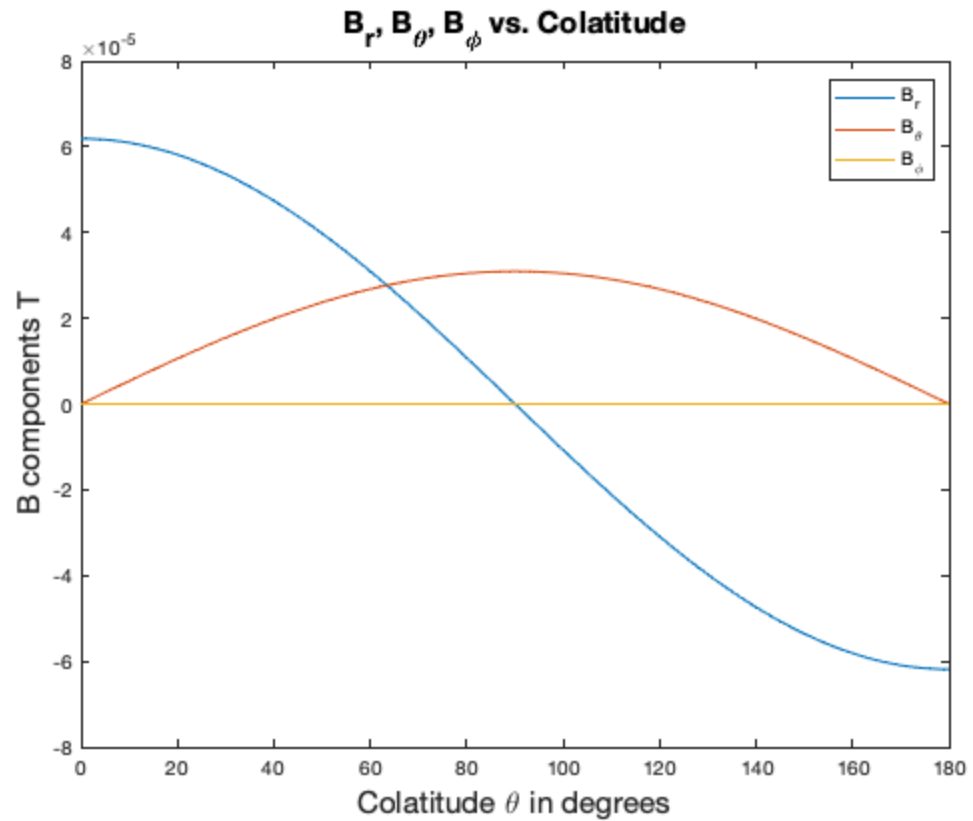
% Convert B to inclination in degrees
inclin = atand(-B_r./sqrt(B_theta.^2+B_phi.^2));
% Convert B to declination in degrees
declin = atand(B_r./-B_theta);
% Convert B to intensity in teslas
inten = sqrt(B_r.^2+B_theta.^2+B_phi.^2);

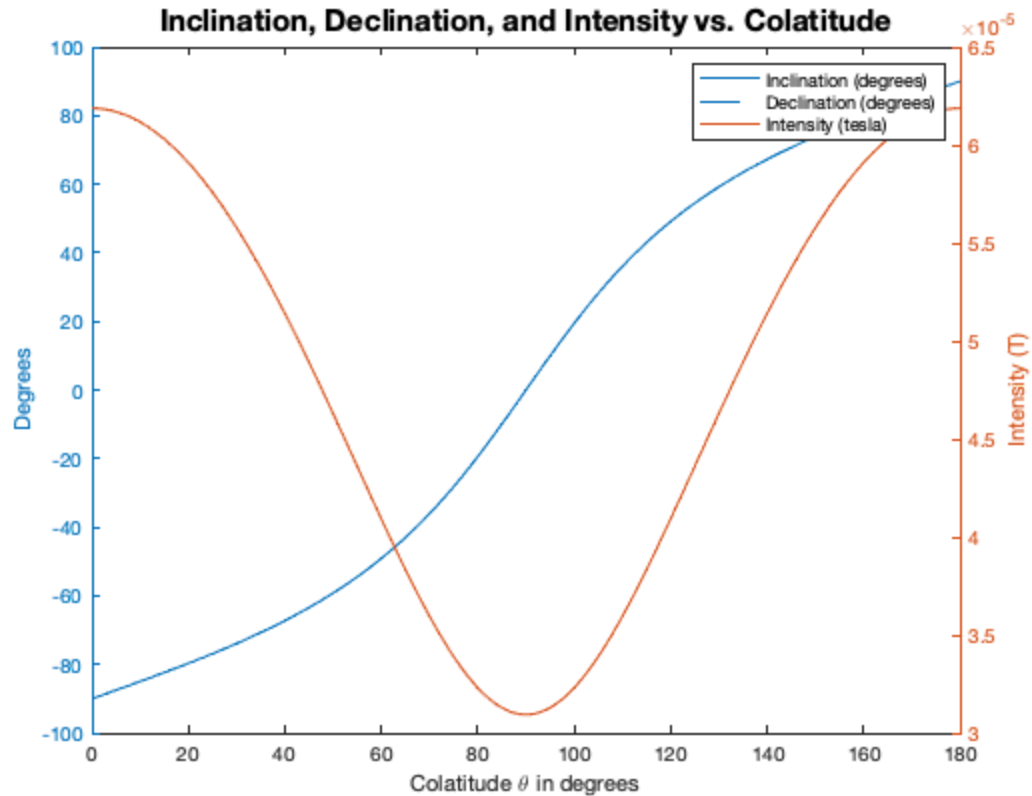
figure(2)
yyaxis left
plot(theta, inclin, 'LineWidth',1)
hold on
plot(theta, declin, 'LineWidth',1)
ylabel('Degrees')
```

```

yyaxis right
plot(theta, inten, 'LineWidth', 1)
title('Inclination, Declination, and Intensity vs.
Colatitude', 'FontSize', 15)
xlabel('Colatitude \theta in degrees')
ylabel('Intensity (T)')
legend('Inclination (degrees)', 'Declination (degrees)', 'Intensity
(tesla)')
set(gcf, 'color', 'w');
hold off

```





Question 2c: Calculate the magnetic dipole from Gauss Coefficients

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% Gauss Coefficients from IGRF-2000
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g10_2000 = -29615e-9;
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```
g11_2000 = -1728e-9;
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h11_2000 = 5186e-9;
```

```
% Gauss Coefficients from IGRF-2020
```

```
g10_2020 = -29404.8e-9;
```

```
g11_2020 = -1450.9e-9;
```

```
h11_2020 = 4652.5e-9;
```

```
% Dipole moment
```

```
m_2000=4*pi*rEarth^3*norm([g10_2000 g11_2000 h11_2000])/mu0
```

```
m_2020=4*pi*rEarth^3*norm([g10_2020 g11_2020 h11_2020])/mu0
```

```
m_2000 =
```

```
7.7877e+22
```

```
m_2020 =
```

$7.7077\text{e}+22$

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