# Trabalho Computacional - Otimização Multiobjetivo

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### Modelo

$$\min_{\mathbf{x}} \mathcal{L}(\mathbf{x}) = [M(\mathbf{x}), F(\mathbf{x})]^{T}$$
$$x_{i} = \{1, 2, 3\}$$

 $M(\mathbf{x}) = \sum x_i - 1$ 

 $F(\mathbf{x}) = \sum p(x_i) f_i$ 

 $p(x_i) = \frac{w(t_0 + k\Delta t) - w(t_0)}{1 - w(t_0)}$ 

 $p(x_i; k) = \frac{w(t_0 + k\Delta t) - priori}{1 - priori}$ 

 $w(t) = 1 - \exp(-\frac{t^{\beta}}{n})$ 

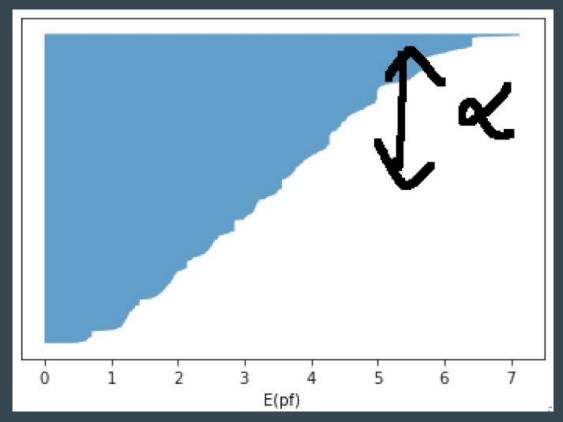
#### Heurística

# Solução Intuitiva

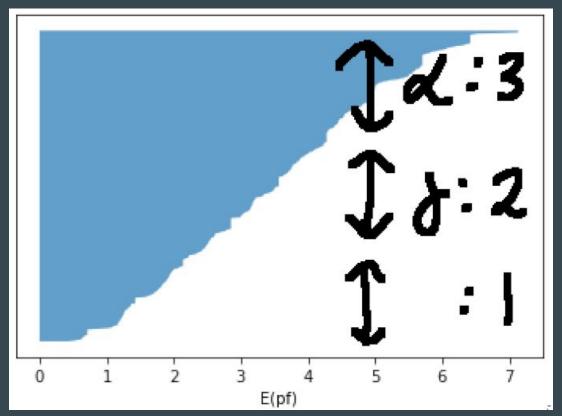
Aplique manutenção em equipamentos caros e antigos

- M e F são conflitantes e monotônicas
- NP-Hard para polinomial, linear (naive) ou quadrático
- Ordene pelo custo priori ou custo esperado de nenhuma manutenção

#### Solução *Naive*



#### Solução Composta



 $\min \mathcal{L} = [M(\alpha, \gamma), F(\alpha, \gamma)]^T$  $\alpha, \gamma$  $\alpha, \gamma \in [0, 1]$ 

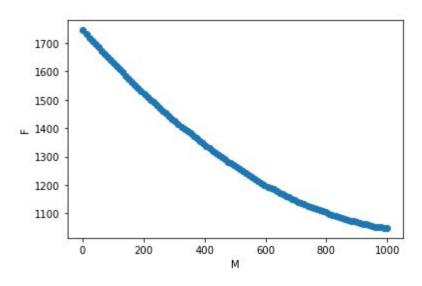
 $\alpha + \gamma \leq 1$ 

$$\min_{\alpha, \gamma}$$

#### Resultados

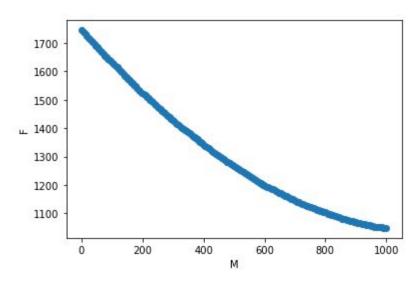
# Solução *Naive*

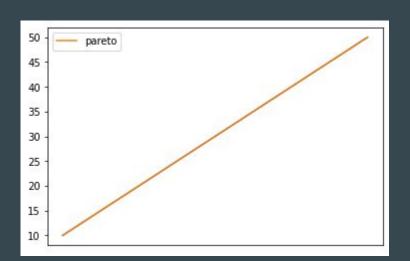
 $\delta = 1e-2$ HV = 0.620407
n = 100

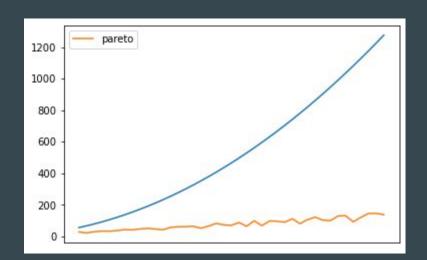


# Solução Composta

 $\delta = 1e-2$  HV = 0.622683 n = 208



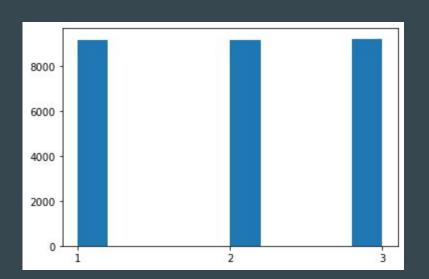


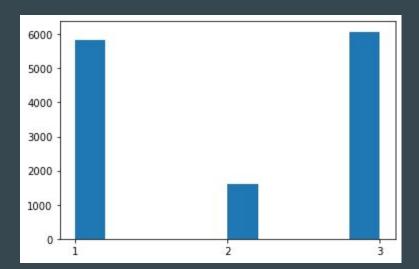


Tomada de Decisão

$$U(\mathbf{x}) = M(\mathbf{x}) + \tau F(\mathbf{x})$$
$$\tau = 1.25$$

$$lpha=0.574$$
 $\gamma=0$ 





## Obrigado