



**Universidade do Minho**

Escola de Engenharia

Departamento de Informática

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## **Mobile Ray Tracing**

May 2018



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Master dissertation

Master Degree in Computer Science

Dissertation supervised by

**Professor Doutor Luís Paulo Peixoto dos Santos**

May 2018

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## ABSTRACT

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The technological advances and the massification of information technologies have allowed a huge and positive proliferation of the number of libraries and APIs. This large offer has made life easier for programmers in general, because they easily find a library, free or commercial, that helps them solve the daily challenges they have at hand.

One area of information technology where libraries are critical is in Computer Graphics, due to the wide range of rendering techniques it offers. One of these techniques is ray tracing. Ray tracing allows to simulate natural electromagnetic phenomena such as the path of light and mechanical phenomena such as the propagation of sound. Similarly, it also allows to simulate technologies developed by men, like Wi-Fi networks. These simulations can have a spectacular realism and accuracy, at the expense of a very high computational cost.

The constant evolution of technology allowed to leverage and massify new areas, such as mobile devices. Devices today are increasingly faster and replace and / or complement tasks that were previously performed only on computers or on dedicated hardware. However, the number of image rendering libraries available for mobile devices is still very scarce, and no ray tracing based image rendering library has been able to assert itself on these devices. This dissertation aims to explore the possibilities and limitations of using mobile devices to execute rendering algorithms that use ray tracing, such as progressive path tracing. Its main goal is to provide a rendering library for mobile devices based on ray tracing.

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## RESUMO

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Os avanços tecnológicos e a massificação das tecnologias de informação permitiu uma enorme e positiva proliferação do número de bibliotecas e APIs. Esta maior oferta permitiu facilitar a vida dos programadores em geral, porque facilmente encontram uma biblioteca, gratuita ou comercial, que os ajudam a resolver os desafios diários que têm em mãos.

Uma área das tecnologias de informação onde as bibliotecas são fundamentais é na Computação Gráfica, devido à panóplia de métodos de renderização que oferece. Um destes métodos é o ray tracing. O ray tracing permite simular fenómenos eletromagnéticos naturais como os percursos da luz e fenómenos mecânicos como a propagação do som. Da mesma forma também permite simular tecnologias desenvolvidas pelo homem, como por exemplo redes Wi-Fi. Estas simulações podem ter um realismo e precisão impressionantes, porém têm um custo computacional muito elevado.

A constante evolução da tecnologia permitiu alavancar e massificar novas áreas, como os dispositivos móveis. Os dispositivos são hoje cada vez mais rápidos e cada vez mais substituem e/ou complementam tarefas que anteriormente eram apenas realizadas em computadores ou em hardware dedicado. Porém, o número de bibliotecas para renderização de imagens disponíveis para dispositivos móveis é ainda muito reduzido e nenhuma biblioteca de renderização de imagens baseada em ray tracing conseguiu afirmar-se nestes dispositivos. Esta dissertação tem como objetivo explorar possibilidades e limitações da utilização de dispositivos móveis para a execução de algoritmos de renderização que utilizem ray tracing, como por exemplo, o path tracing progressivo. O objetivo principal é disponibilizar uma biblioteca de renderização para dispositivos móveis baseada em ray tracing.

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## INTRODUCTION

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### 1.1 CONTEXT

Programming is like building something with primitive blocks and it can be a very difficult task if we have to program every aspect of the application without some “blocks” already built for us to use. That’s why in the programming world there is a whole panoply of free and commercial libraries with APIs that provide a huge quantity of functions for the programmer to use.

In computer graphics, there are many libraries that provide functionalities to render images based in different techniques. Ray tracing is a technique for rendering an image by tracing the path of light through pixels in an image plane and simulating the effects of its interactions with virtual objects. This technique is capable of producing a very high degree of visual realism but at a great computational cost.

Since nowadays we have more and more mobile systems whose computational power increases every year, the need for more libraries to help the programmers develop applications for these systems is increasing too. However, there are not many options to choose from for developing a renderer based on ray tracing. That’s why this dissertation focuses on assessing and providing a ray tracer library for mobile systems.

It is important to mention that this dissertation is not focused on rendering techniques other than ray tracing. It is not focused in assess different integrators (numerical solutions to the rendering equation) and / or assess different approaches in ray tracing like Packet Traversal. It is also not focused on assess different quasi random numbers generators neither assess the performance of different computer systems.

These rendering algorithms based in ray tracing are very useful because they allow rendering photo-realistic images with a degree of realism much better than the graphics cards allow by default through rasterization. As previously stated, the computing power in mobile devices processors has been increasing and this may allow a mobile device with a mid-range processor to run these algorithms in a useful time.

Figure 1.: Illustration of the most common mobile devices - tablet and smartphone (du Net)



## 1.2 MOTIVATION

Among other factors, the productivity of a programmer depends on what libraries he can have access to. But, there are almost no rendering libraries based in ray tracing available today for mobile systems like Android, iOS or Windows 10 Mobile. And it is likely that these systems already have enough processing power to render images with fairly complex scenes in an acceptable time by using algorithms based in ray tracing.

It is also important to note that there is not much documentation about the advantages and limitations of executing different rendering algorithms in these devices.

## 1.3 GOALS

The main goal of this dissertation is to assess and demonstrate the advantages of running rendering algorithms in mobile devices.

It is also intended to promote and facilitate the development of applications for mobile systems that use ray tracing techniques, with special emphasis on rendering applications. To do this, will be developed a library that supports the fundamental operations of a ray tracing engine. This library will allow the agile development of diverse applications, by using components that invoke the functionality of the library itself.

Additionally, it is intended to supply rendering components at a higher abstraction level, like the camera, scene and the integrator that facilitates further the development of applications.

Finally, it is important to do a demonstration of the rendering application with some interface layer to let the user assess the performance of several functionalities provided by the library.

#### 1.4 DOCUMENT STRUCTURE

This dissertation is organized in 5 chapters: Introduction, State of the Art, Software Architecture, Demonstration: Global Illumination and Conclusion & Future work.

The first chapter describes the context and motivation behind this work, as well as its goals. Its main purpose is to identify the problem at hand and set up goals that should be accomplished.

The second chapter introduces the main concepts of ray tracing and compares different implementations of ray tracers already available in the world wide web. The reason behind this comparison is to show how many ray tracers are already available to mobile devices and highlight the differences between the features they have. It also provides some information about the processors of today that helps realize their ability to execute computationally demanding algorithms like ray tracing.

The third chapter explains the proposed approach and explains each module developed in the library and in the rendering components. This chapter ends with an explanation of some Android specifics, such as the user interface by characterizing its work flow and mentioning some of the challenges overcome during the development of the application.

The fourth chapter summarizes the key results obtained by executing different algorithms with different number of threads and different acceleration structures. And it will also contain a small comparison between the developed application and the Android CPU Ray-tracer (Dahlquist).

Finally, the fifth chapter ends this dissertation with the conclusions that can be withdrawn from this work and proposes some future work.

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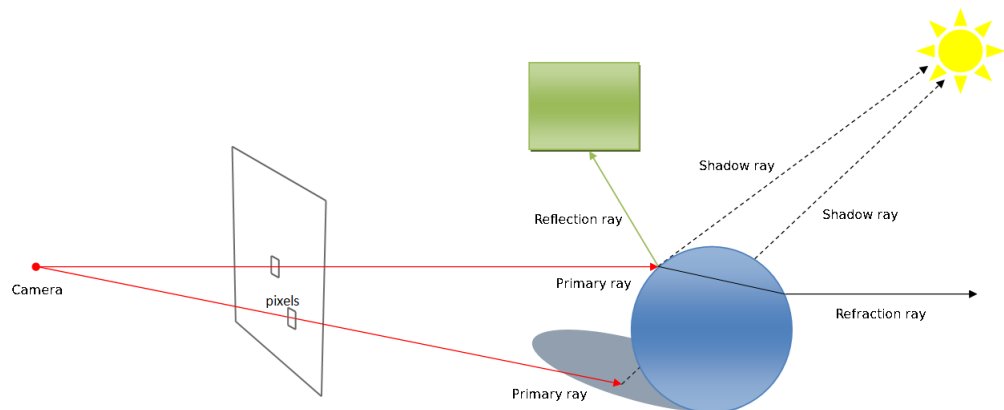
## STATE OF THE ART

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### 2.1 RAY TRACING

Ray tracing one frame can be, simultaneously, a computationally demanding task and an embarrassingly parallel task. As tracing rays is a recursive process which aims to calculate the luminance of light of each individual pixel separately. At least one ray is shot per pixel and in a naive approach each ray would be intersected with all the objects in the scene in order to determine which one is the closest primitive intersecting that given ray. To evaluate the light intensity that an object scatters towards the eye, the intensity of the light reaching that object has to be evaluated as well. Ray tracing achieves this by shooting additional secondary rays, because when a ray hits a reflecting or transparent surface, one or more secondary rays are cast from that point, simulating the reflection and refraction effects.

Figure 2.: Illustration of a typical ray tracer algorithm.



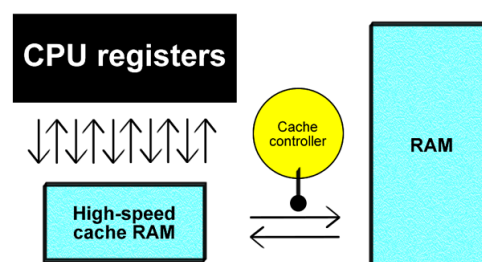
A typical image of  $1024 \times 1024$  pixels tends to cast at least a million primary rays and a multiple of that as shadow, reflection, refraction and secondary rays. This is why ray tracing can't provide interactive frame rates with ease.

## 2.2 TYPICAL CPU FEATURES

Fortunately, the present state of available technology provides affordable machines with multiple CPU cores that can work in parallel and with great performance. This is achieved thanks to features developed inside the processor like the cache, the multilevel pipeline, the hardware prefetching and SIMD instruction set already available in the current processors.

The cache is a very small and fast multilevel memory inside the processor that temporarily stores the data read from the main memory. This memory allows reading its content at a very low latency in the order of magnitude of around 1 nanosecond in the first level, 10 nanoseconds at second level and 50 nanoseconds at third level compared to the typical 100 nanoseconds of a DDR main memory. The downside is that it is very small because its cost are much higher than a typical RAM memory. Nowadays, the level 1 has 64kB, the level 2 has 256kB and the level 3 has 8 MB which is very little compared to the typical 16GB provided by the memory RAM.

Figure 3.: Illustration of a typical cache memory inside a microprocessor (Karbo and Aps.).



The multilevel pipeline is another feature inside a processor which allows to reduce the processor's own latency by allowing a form of parallelism called instruction-level parallelism within a single processor. Basically, one instruction is divided in some stages and it allows the possibility to execute different stages of different instructions simultaneously. In the early days, the Classic RISC pipeline were typically divided in 5 stages:

- Fetching the instruction
- Decoding the instruction
- Executing the instruction where the arguments can be fetched from registers (1 cycle latency) or from memory (2 cycle latency)
- Memory access where it ensured that writing in memory was always performed in the same stage and allowed to use that value in another instruction before it was written in memory
- Writing back the value in the register

Nowadays, the current microprocessors have a pipeline with 8-14 stages and can be more complex than the Classic RISC, but the operating principle is the same. This allows faster CPU throughput, which means the number of instructions that can be executed in a unit of time is greater, than it would otherwise be possible at a given clock rate.

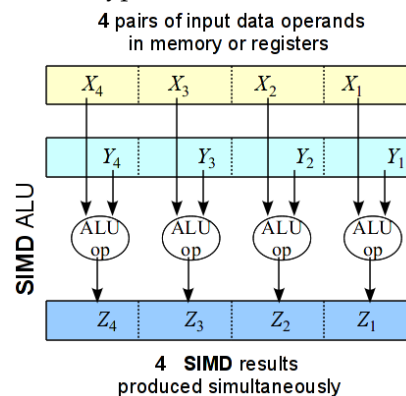
Figure 4.: Illustration of the Classic RISC multilevel CPU pipeline (Dictionaries and Encyclopedias).

Instr. No.	Pipeline Stage						
1	IF	ID	EX	MEM	WB		
2		IF	ID	EX	MEM	WB	
3			IF	ID	EX	MEM	WB
4				IF	ID	EX	MEM
5					IF	ID	EX
Clock Cycle	1	2	3	4	5	6	7

The hardware prefetching is, as the name implies, a feature in the processor that makes the processor fetch the data and the instructions before it really needs to execute. This allows to reduce the time that the processor waits for the data in the main memory.

Finally, SIMD instruction set is a set of special instructions that allows the processor to read or write bigger sizes of data. Typically, a 64 bit processor can only work with 64 bits of information at a time during the execution of an instruction. This feature can allow to read or write up to 512 bits by using special registers and additional ALUs provided in the processor.

Figure 5.: Illustration of a typical execution of SIMD extension (Bishop).



Nowadays, even mobile devices like smart phones and tablets have multiple CPU cores with features similar to those described above. This opens the possibility to execute more computationally demanding algorithms, like ray tracing, in these devices.

## 2.3 KEY FEATURES OF RAY TRACING FOR THIS WORK

Ray tracing is an algorithm that can have a panoply of features or optimizations in order to reduce the time required to trace all the rays and / or to show the results as fast as possible. It also, like any application, can have different types of software licenses and be executed in different platforms.

For this work, the most important features in a ray tracer are: the type of software license, the platform where can be executed, interactivity, progressive and the type of rendering components.

### 2.3.1 *Type of software license*

A software application can have different type of software license, but in order to simplify this dissertation, the software license were grouped into 3 types: Free, Commercial and Open Source. The license Free means that the user has the right to execute freely the application but cannot copy, modify or distribute the implemented code. The license Commercial means that the user cannot even execute the application without buying it first and cannot copy, modify or distribute the implemented code. The license Open Source means that the user has the right to execute freely the application and can even copy, modify and distribute the implemented code. The software license is very important in this work because it lets the user know if he can develop something over the provided software or if he can just use the application.

### 2.3.2 *Platform*

An application can only be executed in the platforms that the developers compiled the code for. So, a ray tracer that can be executed in a desktop may also or may not be executed on another platform, like a mobile device. This information is very important in this work because it inform us whether a ray tracer can be executed in a mobile device with the typical Operating System like Android, iOS or Windows 10 Mobile.

### 2.3.3 *Interactivity*

In ray tracing, interactivity means rendering an image with a very low response time, like a few milliseconds per frame. An interactive ray tracer can render a scene with multiple frames per second.



### 2.3.4 *Progressive*

A typical ray tracer shows the rendered image only after the whole process is complete. A progressive ray tracer is a ray tracer that updates the color of pixels in the screen as soon as the rays are traced, instead of waiting for the rendering process to complete. This means that an image is rendered quickly with some aliasing or noise and it is progressively improved over time.

### 2.3.5 *Types of Rendering Components*

A ray tracer can be developed with the different rendering components programmed separately. Some examples of rendering components are: Integrators, Cameras, Scenes, Samplers, Shapes, Lights and Accelerator Structures. In some ray tracers, these rendering components can even be programmable by the user. This is very important because it allows the user to develop his own renderer based in ray tracing without having to develop every feature in the ray tracer.

## 2.4 RELATED WORK

The possibility of rendering an image with ray tracing was demonstrated in 1980 by Whitted ([dos Santos](#)) and since then the number of libraries that provide basic ray tracing functionalities increased greatly. There is a wide range of different ray tracers available today for the programmer to use, yet the majority can only be used with the traditional personal computer hardware (desktop or laptop).

The table 1 shows some applications or frameworks that use ray tracing available today and compares them according to their type of license, platform compatibility, interactivity, progressive and whether they allow development of your own rendering components like the integrator and sampler. Note that some of these ray tracers provide only the engine with the basic ray tracing functions, such as creating rays and intersecting them with geometric primitives, so the rendering components are only programmable if the application that uses the engine supports it. During the research of the available ray tracers, others than the ones presented in the table were found, but they were excluded because the documentation was very poor without explaining the basic functionalities provided or because there was no documentation at all.

Table 1.: Comparison of different applications/frameworks that use ray tracing

Product	License	Platform	Mobile	Interactivity	Progressive	Programmable Components
Optix (Nvidia (a))	F	Nvidia GPU	N	Y	Y	Y
Optix Prime (Nvidia (b))	F	CPU & Nvidia GPU	N	Y	Y	Y
RenderMan RIS (Pixar)	C	CPU	N	Y	Y	Y
OctaneRender (Inc)	C	GPU	N	Y	Y	N
Embree (Intel)	O	Intel CPU	N	Y	Y	Y
Radeon Rays (AMD)	O	CPU & GPU	N	Y	Y	Y
PBRT (Matt Pharr)	O	CPU	N	N	N	N
Visionaray (Zellmann)	O	CPU & Nvidia GPU	N	Y	Y	N
YafaRay (Gustavo Pichorim Boiko)	O	CPU	N	N	N	N
tray_rust (Usher (c))	O	CPU	N	N	N	N
micro-packet (Usher (a))	O	Intel CPU	N	N	N	N
tray (Usher (b))	O	CPU	N	N	N	N
The G3D Innovation Engine (Morgan)	O	CPU	N	N	N	N
HRay (Kenneth)	O	CPU	N	N	N	N
Mitsuba (Jakob (2010))	O	CPU	N	N	N	N
Indigo RT (Limited)	O	CPU & GPU	N	Y	N	N
jsRayTracer (Chedeau)	O	CPU	N	Y	Y	N
Android CPU Raytracer (Dahlquist)	O	CPU	Y (Android)	Y	N	N

#### 2.4.1 Conclusions

As the table 1 shows, there is a lack of generic ray tracing libraries for the mobile devices. Although there are some closed-source ray tracing demo applications, only one ray tracer already available has some sort of documentation and is compatible with mobile devices, in this case with Android. This ray tracer is open source, uses only the CPU of the device and has a good performance. It even allows interactions with the objects during the render process. But, it doesn't support progressive rendering and also does not allow the programmers to use their own rendering components.

This dissertation aims to fix this lack of libraries, by providing one that contains ray tracing basic functionalities and the ability to let the programmer be able to develop their own rendering components like the sampler, integrator, camera and shapes of virtual objects. It also studies the drawbacks that these mobile devices may have comparing with the average multi-core personal computer hardware. And finally, a small comparison was made with the Android CPU Raytracer (Dahlquist) in order to illustrate the advantages and disadvantages of both. This comparison is important because it enriches all the work done, as it demonstrates if the performance of the provided features are relatively efficient.

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## SOFTWARE ARCHITECTURE

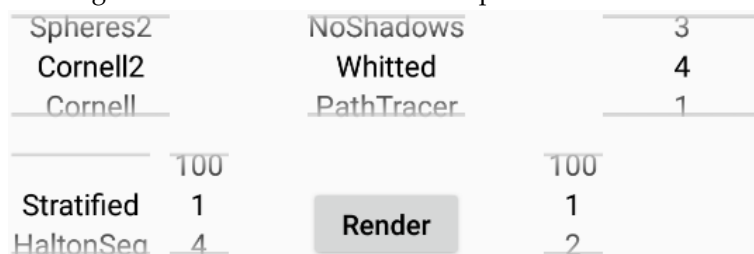
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### 3.1 APPROACH

The development of this demonstration application involves the distinction of three layers of abstraction: user interface, rendering components and the library itself.

The top layer is the User Interface which is obviously application, and eventually device, dependent. The user interface of this dissertation's demo application is very simple and just allows the user to see the rendered image and choose some rendering components to use, like the integrator, the sampler, the number of threads and samples and choose the scene to render. Although this layer is useful, this dissertation focuses only on the middle and bottom layers.

Figure 6.: Illustration of the developed User Interface.

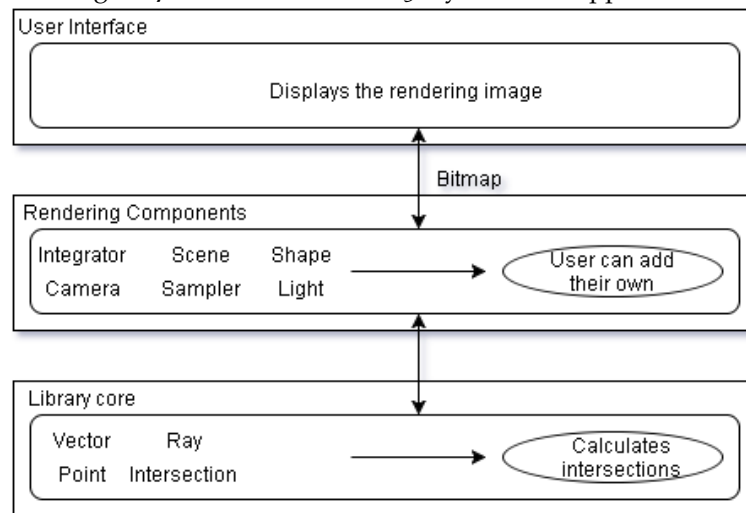


The middle layer provides the rendering components which are abstracted concepts about rendering that use functionalities that the library offers to the programmer. Some of these rendering components are the camera, the light, the sampler and the integrator. These rendering components are useful for the programmer since it allows them to use features without having the need to know how these were developed. And, of course, this facilitates and accelerates the development of new rendering applications.

Lastly, the bottom layer is the library itself, which contains the business logic of basic features in a renderer, that the rendering components use. These features are basic functionalities of a ray tracer engine like: create vectors and points, create different primitives with different materials, cast rays and intersect rays with the primitives.

It is also important to mention that the demo application was developed in order to show the developed features, the performance achieved in the mobile devices and also to help promote the library. This demo application is a good way to test it in several Android devices like a smart phone or a tablet.

Figure 7.: Illustration of the 3 layers in the application



Besides the abstraction layers, there are some important strategic decisions made in order to guide the progress of the development of this library.

The first decision was: the primary rays always have origin in the camera. This decision was made in order to not mix the code of the integrator with the ray tracer renderer engine.

Other decision made was to make the rendering process progressive, which means that the rendered image is incrementally refined with more and more traced rays. As the integrator will be converging to better values. This is important in order to give the user a fast rendered image, with some noise or aliasing, and converge it progressively to a better solution with higher details and practically without any visual noise or aliasing.

Another thought aspect that was studied is the permission of dynamic scenes and / or dynamic cameras, which means to let the programmer modify the camera or the scene while the ray tracer is rendering it. This makes possible to build challenging applications and also provide more interesting scenes and more eye candy applications for the final user.

Last, but not least, is that the code was developed in a modular way, in this case was programmed in an object oriented manner. This allows the programmers to code their own rendering components, like the integrator, camera, sampler and light, without having to develop the basic features in the renderer engine.

### 3.2 METHODOLOGY

In order to take advantage of most of the mobile CPU resources and give a good performance for the applications, the library and the rendering components were developed using the native programming language C++. This was achieved by using the Native Development Kit (NDK) provided by the Integrated Development Environment (IDE) Android Studio. The User Interface was developed in Java using the traditional Software Development Kit (SDK) provided by the Android Studio because there is no framework in the NDK that helps the programmer design his own user interface. Despite that, its performance is not very important because it doesn't interfere significantly with the others layers of the application.

### 3.3 LIBRARY

As stated above, this library was implemented in an object-oriented fashion. The most important classes that provide functionalities already developed for the user to use are:

- **Renderer:** class that starts the rendering process and stores the calculated pixels colors in a C style array.
- **Scene:** class that stores the geometry information in vectors and provides methods to trace rays in the scene without any acceleration structures.
- **Shapes:** set of classes that allows to create triangles, spheres and planes.
- **Material:** class that stores all 4 types of material color:
  - Emission light color
  - Diffuse reflection color
  - Specular reflection color
  - Specular refraction color
- **Primitive:** class that stores the shape and material of each primitive in the scene.
- **Ray:** class that represents a ray casted into the scene.

#### 3.3.1 *Third parties dependencies*

Before describing each functionality provided in each class developed, it is important to mention that this library uses 3 other libraries developed in C++ by third parties. Those libraries are:

- OpenGL Mathematics ([Creation](#)): used to create 3d points and vectors, perform geometry calculations and store pixels and primitives colors.
- tinyobjloader ([syoyo](#)): used to load scenes from wavefront obj files.
- Google Test ([Google \(b\)](#)): used to create some unit tests and to mock some classes.

All these libraries are Android compatible and are reliable in terms of performance and maintenance.

Besides being dependent on these 3 libraries, this library also depends on OpenGL ES 2.0 ([Inc.](#)) from Android SDK and depends on CMake ([kitware](#)) in order to compile the application.

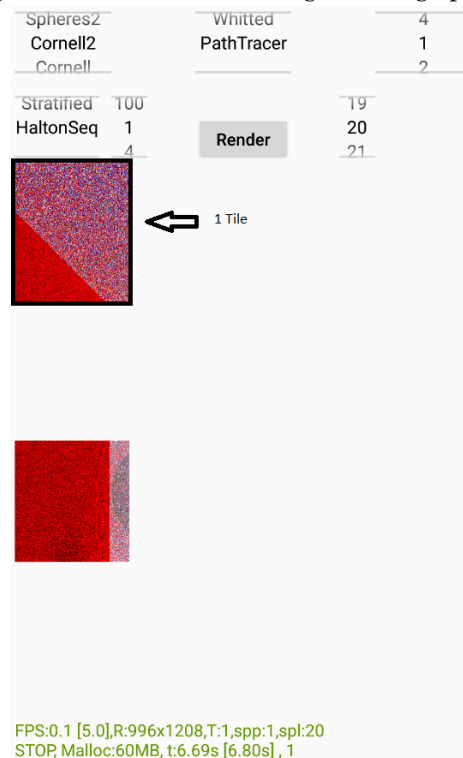
### 3.3.2 *Renderer*

The *Renderer* is the closest class to the application that starts the rendering process. This class provides two main methods:

```
void renderFrame (::std::uint32_t *bitmap, ::std::int32_t numThreads, ::std::uint32_t stride) noexcept;
void stopRender() noexcept;
```

The *renderFrame* method starts the rendering process and writes the calculated light luminance of each pixel in the parameter *bitmap*. This method also allows to choose the number of threads that will render the image into the bitmap, and needs the stride of that bitmap array. The image plane is divided into 16 tiles of pixels and it is traced one primary ray per pixel in each tile.

Figure 8.: Illustration of tiling the image plane.



The *stopRender* method only serves to stop the rendering process without cleaning the pixels' colors already calculated.

### 3.3.3 Scene

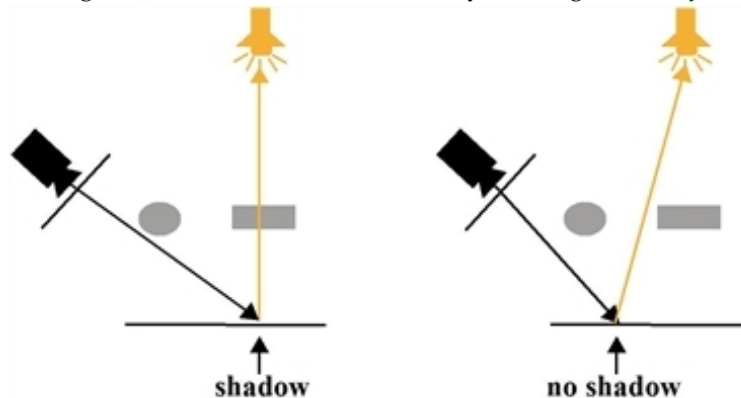
The Scene is the class that handles the process of intersecting a ray with the primitives and source lights in the scene. Besides providing a vector to add the light sources and a vector to add primitives to the scene, it also provides two main methods:

```
Intersection trace(Intersection intersection, const Ray &ray) noexcept;
Intersection shadowTrace(Intersection intersection, const Ray &ray) noexcept;
```

The *trace*, as the name implies, is a method that tries to intersect a ray with all the primitives and light sources in the scene. And It returns the closest intersection to the origin of that ray. This method is used to determine the intersection of the casted ray with the primitives in the scene.

The *shadowTrace*, is similar to the *trace* method but with the difference that returns the first intersection found. The purpose of this method is to simulate the shadows in the scene, like it is illustrated in figure 9.

Figure 9.: Illustration of shadow rays casting (Foundry).



#### 3.3.4 Shapes

In order to make possible to generate scenes with all kind of objects, it was developed 3 types of shapes: plane, sphere and triangle. All shapes provide only one method:

```
Intersection intersect(const Intersection &intersection, const Ray &ray) const
noexcept;
```

This method determines if a ray intersects the shape and returns the intersection. It is important to mention that, obviously, each shape was developed with different algorithm.

##### Plane

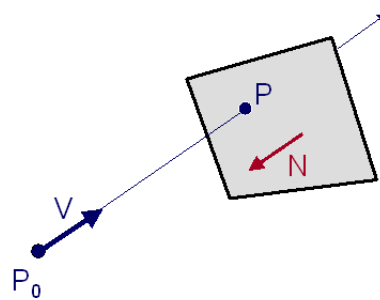
The plane is an essential primitive shape because it allows the user to build indoor scenes.

The construction of a plane requires just an arbitrary point in the plane and the normal of the plane. So, the intersect method implemented has the following algorithm:

```
projection = planeNormal . rayDirection
if (|projection| <= 0) return false
distance = planeNormal . (planePoint - rayOrigin) / projection
if (distance <= 0 || distance > rayMaxDistance) return false
intersectionPoint = rayOrigin + rayDirection * distance
return Intersection(intersectionPoint, planeNormal, material)
```



Figure 10.: Illustration of a ray intersecting a plane (Vink).



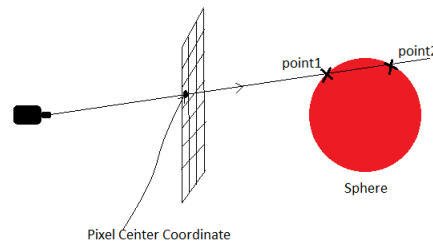
### Sphere

The sphere is also an important primitive shape because it allows the user to build some common objects with a shape of a ball.

The construction of a sphere requires just the point in the center and the radius of the sphere. It also should be noted that a ray can intersect a sphere at two points and therefore it is necessary to determine the closest intersection point to the origin of the ray. So, the intersect method implemented has the following algorithm:

```
centerToOrigin = rayOrigin - sphereCenter
B = 2 * centerToOrigin . rayDirection
C = centerToOrigin.magnitude - radius
discriminant = B^2 - 4*C
if (discriminant <= 0) return false
distance1 = (-B + sqrt{discriminant} * 0.5)
distance2 = (-B - sqrt{discriminant} * 0.5)
distance = min(distance1, distance2)
if (distance <= 0 || distance > rayMaxDistance) return false
intersectionPoint = rayOrigin + rayDirection * distance
sphereNormal = intersectionPoint - sphereCenter
return Intersection(intersectionPoint, sphereNormal, material)
```

Figure 11.: Illustration of a ray intersecting a sphere in two points (Chirag).



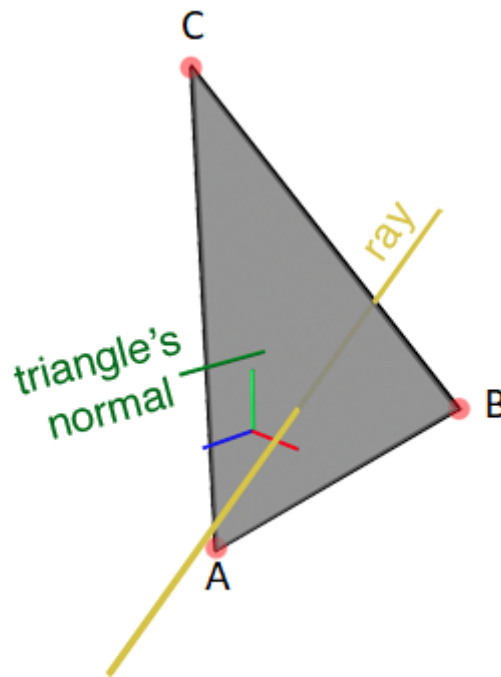
### Triangle

And finally, obviously the triangle has also been implemented because, as it is the simplest primitive with an area, it allows to build many different object shapes.

The construction of a triangle requires three points  $[A, B, C]$ , two vectors  $[AB, AC]$  and the normal of the triangle. So, the intersect method implemented has the following algorithm:

```
perpendicularVector = rayDirection x AC
projection = AB . perpendicularVector
if(|projection| <= 0) return false
vectorToRay = rayOrigin - A
u = (vectorToRay . perpendicularVector) / projection
if (u < 0 || u > 1) return false
perpendicularVector2 = vectorToRay x AB
v = (rayDirection . perpendicularVector2) / projection
if(v < 0 || (u + v) > 1) return false
distance = (AC . perpendicularVector2) / projection
intersectionPoint = rayOrigin + rayDirection * distance
return Intersection(intersectionPoint, triangleNormal, material)
```

Figure 12.: Illustration of a ray intersecting a triangle (Scratchapixel).



### 3.3.5 Acceleration Structures

As previously stated, the rendering algorithms based on ray tracing can be very computationally demanding, like Path Tracing and Bidirectional Path Tracing. These algorithms are very computationally demanding because if the scene is very complex, made with millions of primitives, it is necessary to try to intersect every ray thrown into the scene with those millions of primitives. This task is, obviously, very time consuming and can waste a lot of battery power on the mobile device. Luckily, there are already known techniques, called acceleration structures, that helps to accelerate this process by reducing the number of intersections.

There are 2 types of approaches that acceleration structures can have:

- Subdivision of Space: the 3D space of the scene is divided in smaller portions of space which the volume elements can be uniform or irregular:
  - Regular Grids
  - Octrees
  - Kd-trees
- Subdivision of Objects: the 3D space of the scene is divided by aggregating the 3D primitives in groups which are next to each others:

### – Bounding Volume Hierarchy (BVH)

The idea in Subdivision of Space is allowing the intersections to start with the nearest primitives of the ray and is only intersected with the further ones, if these are not in the same direction of the ray. These structures also allow the rapid and simultaneous rejection of groups of primitives.

In contrast, structures based on Subdivision of objects only allow the rapid and simultaneous rejection of groups of primitives.

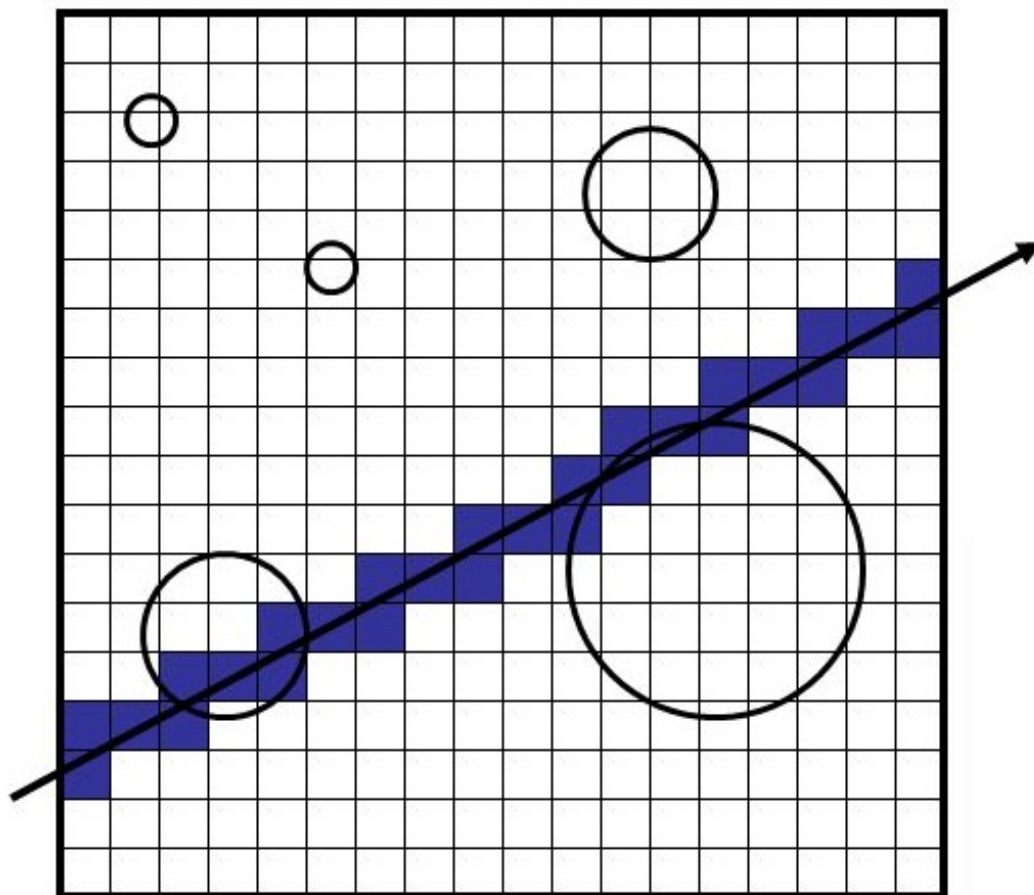
The developed library provides only 2 types of structures, 1 of each approach: the regular grid and the bounding volume hierarchy. Both structures are built with Axis Aligned Bounding Volumes (AABB), which are volume elements (voxels) that can cover, 1 or more primitives from the 3D scene. An AABB is a voxel, like the name implies, that is aligned to the axis of the scene. This type of voxels are great to use in acceleration structures because it is very fast to test whether or not a ray intersects that voxel and it only needs to store, in memory, 2 points of that box. Besides AABB, it is possible to build the structures with other types of voxels, like:

- Sphere: intersection with a sphere is simpler than AABB but covers more 3D space than the scene primitive needs.
- Oriented Bounding Volume: its like a AABB but rotated according to the orientation of the primitive.
- k-Discrete Oriented Prototype (k-DOP):
- Convex Hull:

#### *Regular Grid*

A regular grid is an acceleration structure where the scene space is subdivided into equal voxels. Each voxel is a volume element where it could have inside 1 or more primitives of the scene, if a ray intersects that voxel, then it tries to intersect the primitives inside it. The order of testing each voxel is from the nearest of the ray into the furthest in the direction of that ray. This type of structure is very fast to build but its traversal is poorly efficient due to poor distribution of primitives by voxels. The figure 13 shows the process of intersecting a ray with the primitives in a scene.

Figure 13.: Illustration of traversing a regular grid acceleration structure (Torsten Möller).



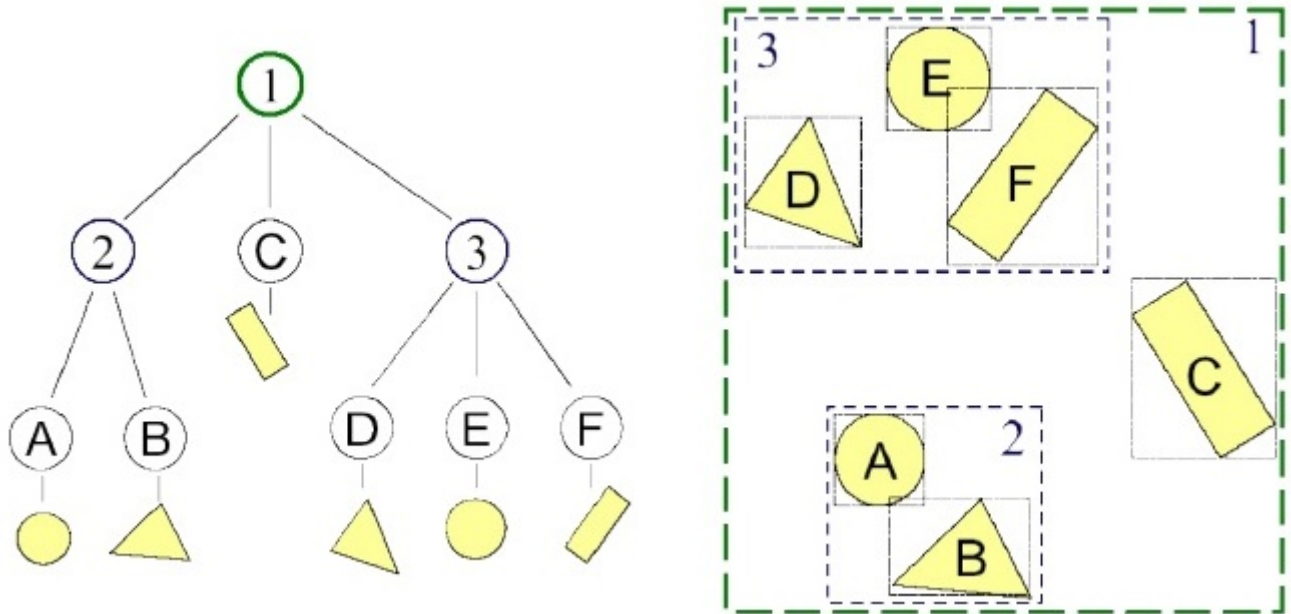
The ray tracer library provides a regular grid as an acceleration structure and its operation is as shown in the figure.

### *Bounding Volume Hierarchy*

Bounding Volume Hierarchy is another acceleration structure provided in the library. This structure is different from the regular grid because the space is not divided into voxels of the same size. The space is divided in a way where the primitives of the scene are grouped according to the nearest primitives of each. This allows to build a structure of voxels where a voxel has, for sure, 1 or more primitives inside.

The figure 14 shows an example of a BVH structure of a scene. As it can be seen, each primitive is covered by an AABB, and then 2 or more AABBs are covered by 1 larger AABB. In this library, this is built in a top down manner, where the scene is divided by a fake plane that divides the scene into 2 AABBs. The calculation of that plane is using the Surface Area Heuristic which is a very popular heuristic commonly used in ray tracers.

Figure 14.: Illustration of traversing a Bounding Volume Hierarchy acceleration structure (Kilgard).



### Surface Area Heuristic

As it was said above, the library uses the Surface Area Heuristic in order to split the scene. The algorithm used in the library is very simple, it just needs to calculate the minimum area surface of the sum of left and right subtrees, as following:

$$SAH_{optimal} = \min(S_L * N_L + S_R * N_R) \quad (1)$$

$N_L$  = number of polygons in left subtree

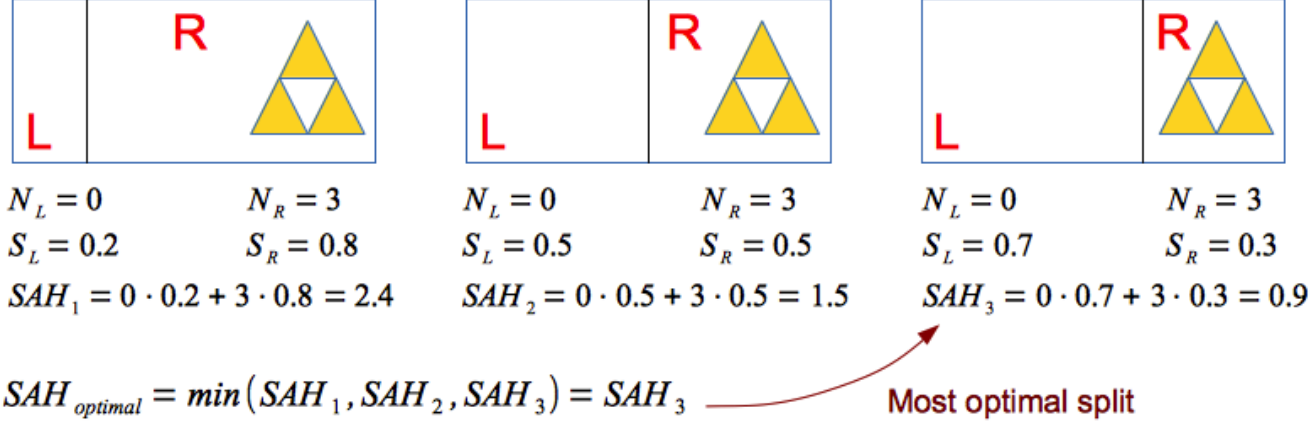
$N$  = number of polygons in right subtree

$S_L$  = surface area of left subtree

$S_R$  = surface area of right subtree

The figure 15 shows a very simple example of how the SAH algorithm works.

Figure 15.: Illustration of how Surface Area Heuristic works in Bounding Volume Hierarchy acceleration structure (Lahodiuk).



### 3.4 RENDERING COMPONENTS

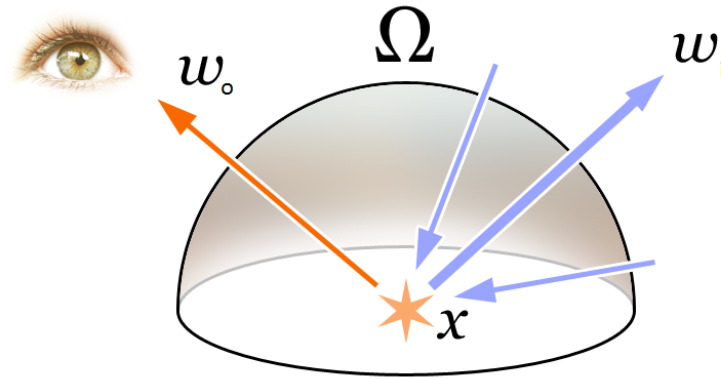
In order to show the functionalities provided by the library, it was developed a few Rendering Components. It is provided the perspective and orthographic cameras, the area and point lights, 6 Samplers, 5 Shaders and 1 OBJ loader.

#### 3.4.1 Shaders

The implemented ray tracer was programmed objected oriented, so each Rendering Component was developed separately. This allows the user to develop his own Rendering Components without having to develop the ray tracer engine.

In this context, a shader is the Rendering Component that describes how the Rendering Equation is approximated. The Rendering Equation describes how the total radiance reflected by any point  $p$  of a surface in a direction  $\omega_r$  is calculated. The Bidirectional Reflectance Distribution Function (BRDF) is a function that tries to approximate the Rendering Equation. In summary, a shader, in this context, is the algorithm of a BRDF.

Figure 16.: Illustration of the rendering equation describing the total amount of light emitted from a point  $x$  along a particular viewing direction and given a function for incoming light and a BRDF.



There was developed three shaders: NoShadows, Whitted and PathTracer. All shaders provide only one main method that allows the user to calculate the RGB color of a pixel with the information of a ray and the respective intersection.

```
void shade(RGB &rgb, Intersection &intersection, Ray &ray) const override;
```

The parameter *rgb* is where the color of the pixel will be calculated and the *intersection* contains the necessary information about the intersection of a ray with the primitive like the intersection point, its normal and the material of the intersected material. Finally the parameter *ray* is where the information about the ray like the origin of the ray and its direction is accessed.

### NoShadows

NoShadows is the simplest shader because, as the name implies, it does not synthesize the shadows and it only simulates the direct lighting. This BRDF only simulates direct lighting in primitives with diffuse surfaces and it does not take into account the light coming from other points. As already said, the indirect lighting is not fully simulated but rather simplified in a way of fixed ambient light of about 10% of the color of the objects.

The algorithm developed is as following:

```
if (intersected material is diffuse) {
    for each light source
        for each sample
            vectorToLight = lightPosition - intersectionPoint
            cos_N_L = vectorToLight . intersectionNormal
            if (cos_N_L > 0) rgb += kD * radLight * cos_N_L
```

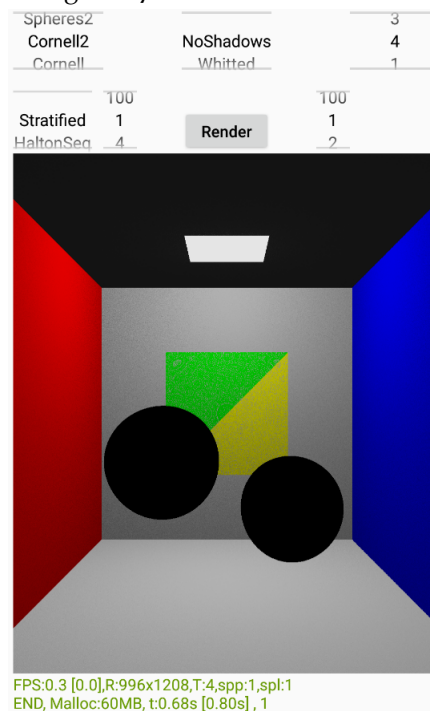


```

    rgb /= #samples
    rgb /= #lights
    rgb += kD * 0.1 //Ambient light
}

```

Figure 17.: NoShadows shader.



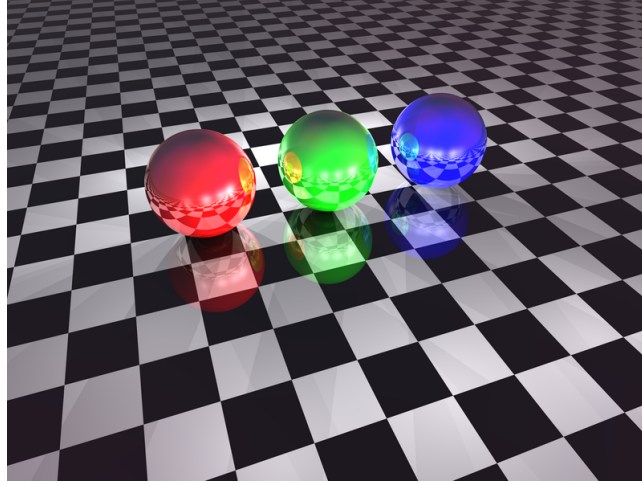
### Whitted

As the name of this shader implies, Whitted is the algorithm demonstrated by Whitted in 1980s. Like the previous shader, it doesn't simulate indirect lighting. This BRDF calculates the reflected light on diffuse and specular surfaces, as well as the light refracted on surfaces with a degree of transmission, such as water. In order to simulate a reflective and refractive surfaces, the algorithm was divided into each case. This makes it possible to simulate refractive surfaces, reflective surfaces and even refractive and reflective surfaces.

The reflected light in a diffuse surface is calculated by adding the casting rays in direction to the lights. These rays are called shadow rays and their radiance are multiplied by the dot product between vector to the light and the shading normal. At the end, the summation is multiplied by the diffuse color of the intersected primitive and divided by the number of samples taken.

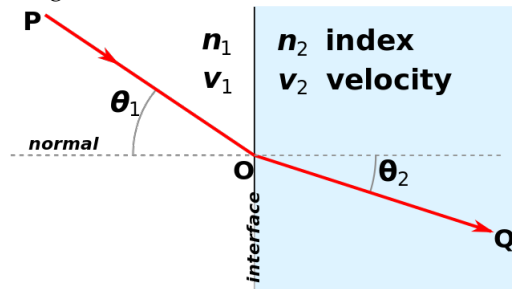
The reflected light in a specular surface is calculated in a different way. The specular ray is casted and ray traced, then the obtained radiance is multiplied by the specular color of the intersected primitive. The reflection direction is the subtraction between the double of dot product between the inverse of the ray direction and the shading normal multiplying by the shading normal, and the inverse of the ray direction.

Figure 18.: Reflections projected on the floor and on the spheres.



Finally, the refracted light in a transmission surface is calculated by using the refractive index of the intersected primitive and the ray direction and shading normal. First, the shading normal is inverted if the origin of the ray was inside a primitive, like a sphere, and if it was not then the refractive index is inverted. Then, it is calculated two auxiliary scalar projections:  $\cos\theta_1$  and  $\cos\theta_2$ .  $\cos\theta_1$  is the dot product of the inverse of the shading normal and the ray direction, and  $\cos\theta_2$  is the difference of 1 and refractive index squared multiplied by one minus  $\cos\theta_1$  squared. Then, if  $\cos\theta_2$  is greater than zero, then the direction of the transmission ray is ray direction multiplied with refractive index plus shading normal multiplied by refractive index multiplied  $\cos\theta_1$  minus square root of  $\cos\theta_2$ . Else, the direction of the transmission ray is just ray direction plus shading normal multiplied by the double of  $\cos\theta_1$ . And, as usual, the transmission ray is traced and its radiance is multiplied by the transmission component of the intersected primitive.

Figure 19.: Refraction of light at the interface of two media of different refractive indices.



The algorithm developed is as following:

```

if (intersected material is diffuse) {
  for each light source
    for each sample
      vectorToLight = lightPosition - intersectionPoint
      cos_N_L = vectorToLight . shadingNormal
      if (cos_N_L > 0) {
        Ray shadowRay(intersectionPoint, vectorToLight, distanceToLight,
                      rayDepth + 1)
        if (!shadowTrace(shadowRay)) rgb += radLight * cos_N_L
      }
    rgb *= kD
  rgb /= #samples
}

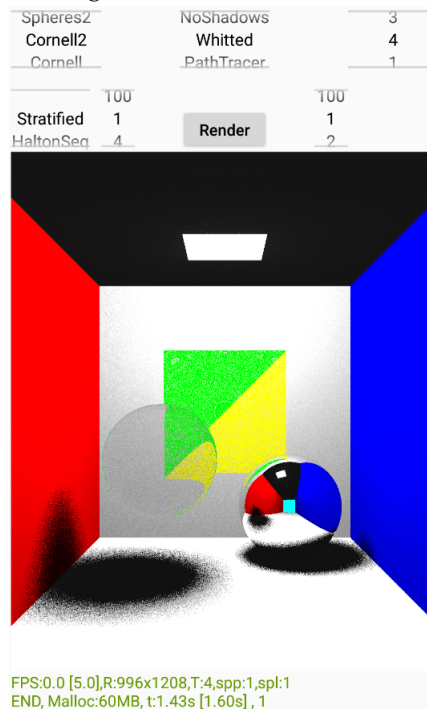
if (intersected material is specular reflective) {
  reflectionDir = (2 * symRayDirection . normal) * normal - symRayDirection
  Ray specularRay(intersectionPoint, reflectionDir, rayDepth + 1)
  rgb += rayTrace (specularRay) * kS
}

if (intersected material is specular refractive) {
  if (shadingNormal . rayDirection > 0) {
    //we are inside the medium
    shadingNormalT = -1 * shadingNormal
    n = 1 / n
  }
  n = 1 / n
  cosTheta1 = -shadingNormalT . rayDirection
  cosTheta2 = 1 - n^2*(1-cosTheta1^2)
  if (cosTheta2 > 0)
    transmissionRay.dir = ((rayDir*n) + (shadingNormalT*(n*cos1 - sqrt(cost2)
    )))
  else
    transmissionRay.dir = (rayDir + shadingNormalT*(cost1 * 2))
  rgb += rayTrace(transmissionRay) * kT
}

```

}

Figure 20.: Whitted shader.



### *PathTracer*

Finally, the last shader developed is the canon Path Tracer. Unlike the previous shaders, this one fully simulates both direct and indirect lighting. But, like the previous shader, this algorithm simulates the light reflected on diffuse and specular surfaces, as well as the light refracted on transparent primitives.

The light reflected on diffuse surfaces is divided in two parts: direct lighting and indirect lighting. The direct lighting is calculated in a similar way to the Whitted shader but with the difference that samples are not taken from all sources of light but rather only one. The light source in each sample is chosen randomly. Then the obtained light radiance is multiplied by the Probability Density Function (PDF) in order to approximate the expected value. In this case the PDF is as simple as  $1/\#lights$ .

Finally, the indirect lighting reflected in diffuse surfaces is calculated in a much more complex way. First it is generated, from the intersected point, a random direction on an unit hemisphere with a PDF proportional to cosine-weighted solid angle  
 $(PDF : p(\Theta) = \cos\theta/\pi, x = \cos(2\pi r1)\sqrt{1-r2}, y = \sin(2\pi r1)\sqrt{1-r2}, z = \sqrt{r2})$ . This

kind of PDF is one of the best ways to render images with path tracing that the rendering equation converges to the expected value as fast as possible.

Then to generate

And the indirect lighting on diffuse surfaces is then the multiplication of the ray traced light radiance with the color of the primitive and  $\pi$ , and divided by the probability of stopping the Russian roulette.

The reflected light in a specular surface and the refracted light are simulated in a similar way to the Whitted algorithm presented previously.

The algorithm developed is as following:

```

if (intersected material is diffuse) {
    for each light
        for each sample
            light = samplerLight.getSample()
            vectorToLight = lightPosition - intersectionPoint
            cos_N_L = vectorToLight . shadingNormal
            if (cos_N_L > 0) {
                Ray shadowRay(intersectionPoint, vectorToLight, distanceToLight,
                               rayDepth + 1)
                if (!shadowTrace(shadowRay)) rgb += radLight * cos_N_L
            }
        }
    rgb *= kD
    rgb /= #lights
    rgb /= #samples

    if (rayDepth <= RAY_DEPTH_MIN || uniform_dist(gen) > finish_probability) {
        local = Generate random direction on unit hemisphere
        proportional to cosine-weighted solid angle

        RotationMatrix = Rotation matrix from axis and angle

        Vector3D up = (0,1,0)
        Vector3D u = intersectionNormal x up
        if (u == 0) u.x = 1
        cosTheta = up . intersectionNormal
        sinTheta = 1 - cosTheta^2
        if (sinTheta < 0) sinTheta *= -1
        sinTheta = sqrt(sinTheta)

        global = local * rotationMatrix

        Ray secondaryRay (globalX, globalY, globalZ, intersectionPoint, rayDepth +
                           1)

        LiD = rayTrace(secondaryRay) * kD * PI
    }
}

```

```

    if (rayDepth > RAY_DEPTH_MIN) LiD /= continue_probability
    if(secondaryRay intersects light) LiD = 0

    rgb += LiD
}

}

if (intersected material is specular reflective) {
    reflectionDir = (2 * symRayDirection . normal) * normal - symRayDirection
    Ray specularRay(intersectionPoint, reflectionDir, rayDepth + 1)
    rgb += rayTrace (specularRay) * kS
}

if (intersected material is specular refractive) {
    if (shadingNormal . rayDirection > 0) {
        //we are inside the medium
        shadingNormalT = -1 * shadingNormal
        n = 1 / n
    }
    n = 1 / n

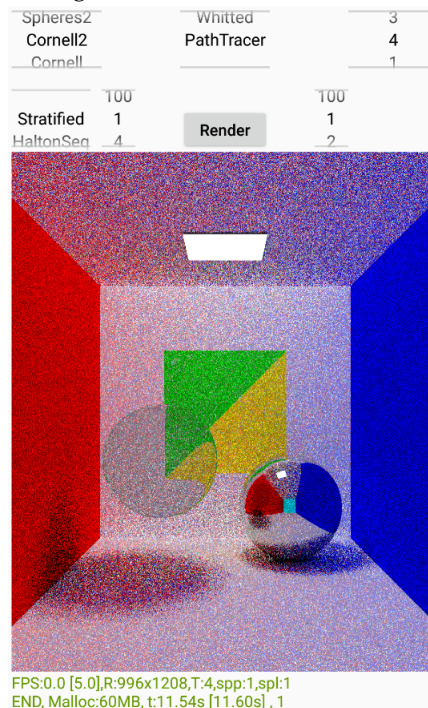
    cosTheta1 = -shadingNormalT . rayDirection
    cosTheta2 = 1 - n^2*(1-cosTheta1^2)

    if (cosTheta2 > 0)
        transmissionRay.dir = ((rayDir*n) + (shadingNormalT*(n*cosTheta1 - sqrt(
            cosTheta2))))
    else
        transmissionRay.dir = (rayDir + shadingNormalT*(cosTheta1 * 2))

    rgb += rayTrace(transmissionRay) * kT
}

```

Figure 21.: PathTracer shader.



### 3.4.2 Samplers

There were implemented four samplers: Constant, Stratified, HaltonSequence and Random.

All samplers just provide one method for the user to use:

```
float getSample(const unsigned int sample);
```

The *getSample* method receives as parameter the number of the current sampler and returns the the actual sample. An atomic variable *sample* is used to count the current index of the samples.

#### Constant

This sampler is the simplest because it always returns the same number passed to the constructor.

The algorithm of the *getSample* is just:

```
return value
```

### Stratified

This sampler makes each sample at equal distance ( $1/\text{domainSize}$ ) and in ascending order. For example, for a domain size of 4, the samples taken are going to be: 0, 0.25, 0.5 and 0.75.

The algorithm of the *getSample* is then:

```
//atomic operation
current = sample++
if (current >= (domainSize * (sampleParam + 1))) {
    sample--
    return 1
}
task = current - (sampleParam * domainSize)
return task / domainSize
```

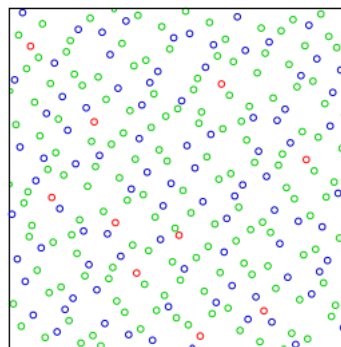
### HaltonSequence

As the name implies, this sampler generates the Halton sequence.

Halton sequence is a quasi random number sequence which is a deterministic sequence with low discrepancy.

These sequences are usually good for Rendering Algorithms like Path Tracing because it can make the rendering equation converge faster (with fewer samples).

Figure 22.: Halton sequence in a 2D image plane.



The algorithm of the *getSample* is as following:

```
//atomic operation
current = sample++
if (current >= (domainSize * (sampleParam + 1))) {
    sample--
```



```

    return 1
}
task = current - (sampleParam * domainSize)

f = 1
result = 0
while (task > 0) {
    f = f / base
    result = result + f * (index % base)
    task = floor(index / base)
}
return result

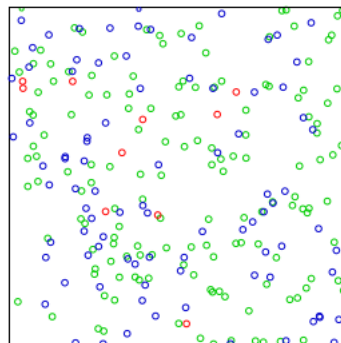
```

### *Random*

This sampler is just a wrapper to call the function `rand()` of the standard C library.

This function is a pseudo random number generator (PRNG), which is an algorithm for generating a sequence of numbers whose properties approximate the properties of sequences of random numbers. Although the PRNG-generated sequence is not truly random, because it is completely determined by an initial value, called the PRNG's seed. These sequences are usually used in simulations that use Monte Carlo methods like the Monte Carlo Ray Tracing.

Figure 23.: Pseudorandom sequence in a 2D image plane.



So the algorithm of the *getSample* is just:

```
return rand() / RAND_MAX
```

### 3.4.3 Lights

There were implemented two types of light sources: `PointLight` and `AreaLight`. These light sources provide the user two main methods:

```
const Point3D getPosition(void);
bool intersect(Intersection &intersection, const Ray &ray, const Material &)
    const;
```

The *getPosition* method just returns the position of the light source and the *intersect* method determines whether a given *ray* as a parameter intersects this light source and, if it intersects, writes the result to the *intersection* parameter.

#### *PointLight*

The `PointLight` is the simplest form of a light because, as the name implies, is just a point of light.

Therefore, the *getPosition* method is very simple because it only returns the position of the light source determined in its constructor:

```
return position;
```

And the *intersect* method is also quite simple because it always returns false. This is because the probability of a ray intersecting a single 3D point in the world is practically nil.

#### *AreaLight*

The `AreaLight` implemented has a shape of a triangle. This shape is intended as it allows to generate a random point in a triangle with barycentric coordinates.

A triangle with 3 points: A, B and C. We get vectors AB and AC, being:

```
AB=[Bx-Ax,By-Ay,Bz-Az] and AC=[Cx-Ax,Cy-Ay,Cz-Az].
```

These vectors tell how to get from point A to the other two points in the triangle, by telling us what direction to go and how far. So, with barycentric coordinates  $R=1/3$ ,  $S=1/3$  and  $T=1/3$ , we get the point in the center of the triangle. To generate a random point in the triangle, we have to generate 2 random numbers between 0 and 1 (R and S). Then we have to make sure we stay inside the triangle by checking if they are larger than one:

```

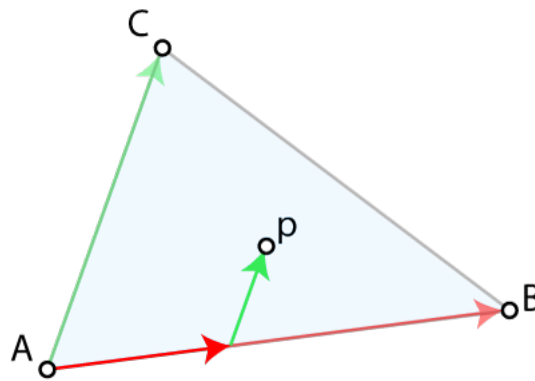
if (R + S >= 1) {
    R = 1 - R
    S = 1 - S
}

```

Finally we can obtain a random point in the triangle by starting at point A, then getting a random percentage along vector AB and a random percentage along vector AC:

```
RandomPointPosition = A + R*AB + S*AC
```

Figure 24.: Calculation of point P by using barycentric coordinates starting at point A and adding a vector AB and a vector AC.



So, the *getPosition* algorithm is as following:

```

R = samplerPointLight.getSample(0)
S = samplerPointLight.getSample(0)
if (R + S >= 1) {
    R = 1 - R
    S = 1 - S
}
x = A.x + R * AB.x + S * AC.x
y = A.y + R * AB.y + S * AC.y
z = A.z + R * AB.z + S * AC.z
return Point3D(x, y, z)

```

And the *intersect* method is equal to the intersection of a ray with a triangle presented earlier.

### 3.4.4 Cameras

Only 2 types of cameras were implemented: perspective and orthographic cameras.

The camera only provides one method for the user to cast a ray from the camera position in direction to the image plane:

```
Ray generateRay(const float u, const float v,
               const float deviationU, const float deviationV) const;
```

The method *generateRay* needs four parameters to create a ray. The *u* and *v* are used to choose the targeted pixel in the image plane. Being *u* the inverse of the index of the pixel in its line, that is,  $x/width$ , and *v* the inverse of the index of the pixel in its column, that is,  $y/height$ . In order to allow the reduction of aliasing in the generated images of the scene, the camera also accepts two extra parameters *deviationU* and *deviationV* which are variances inside a pixel. The *deviationU* is a horizontal variance of the pixel, that is,  $[-0.5 * pixelWidth, 0.5 * pixelWidth]$  and *deviationV* the variance in the vertical of the pixel  $[-0.5 * pixelHeight, 0.5 * pixelHeight]$ . This technique is called jittering, as shown in figure 25, and allows to reduce the aliasing effect by introducing noise into the output image. Although the final image gets some noise, this effect turns out to be visually more appealing than aliasing because it is an effect without patterns that are easily detectable by the human eye. It is important to reduce the aliasing effect because, it is an effect that the human eyes can detect very fast because the generated image will have quite regular patterns, as shown in figure 26.

Figure 25.: Illustration of how sampling the plane image with jittering works.

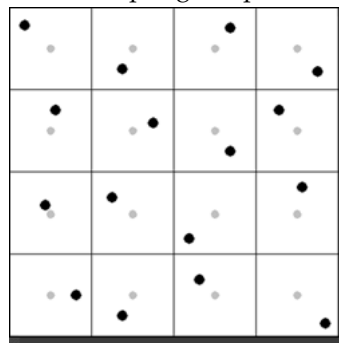


Figure 26.: Aliasing effect.



Sampling with jittering is, as previously stated, a good technique to avoid aliasing in the image. The figure 27 shows an example of stratified sampling with 1 and 256 samples per pixel. As can be seen in the figure on the left, there is a noticeably aliasing in the image, and we can't even perceive the correct positions of the black squares on the background. Of course, with 256 samples per pixel, the aliasing effect is greatly reduced, but also, the execution time is linearly increased, which is a downside to the user experience.



(a) Stratified sampling with 1 sample per pixel.



(b) Stratified sampling with 256 samples per pixel.

Figure 27.: Stratified sampling.

Sampling with jittering is, obviously not perfect, as shown in the figure 28. But, it produces more visually appealing images, although it introduces some noise. Even, with just 1 sample per pixel, the generated image is less "jaggy" in the background. And, with 4 samples per pixel, the noise is greatly reduced and its quality is visually comparable to the stratified sampling with 256 samples per pixel. This means that by using jittering it is possible to obtain images pleasing to the human eye with fewer samples per pixel, and consequently in less execution time.



(a) Jittered sampling with 1 sample per pixel.



(b) Jittered sampling with 4 samples per pixel.

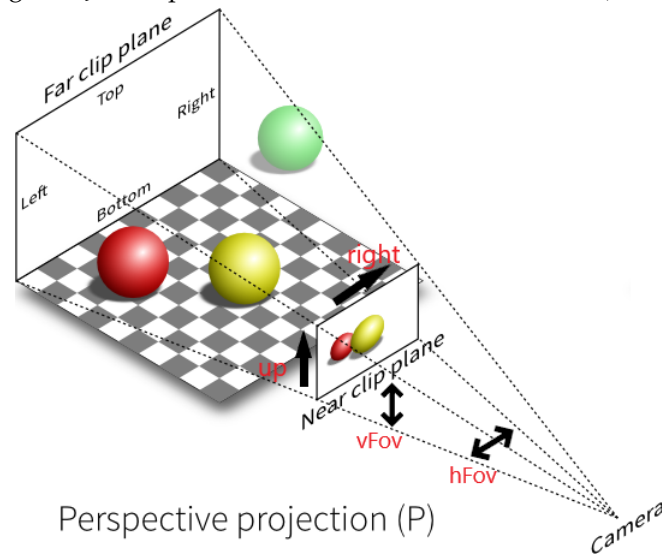
Figure 28.: Jittered sampling.

### Perspective Camera

With this type of camera we can simulate images being seen by the human eyes, which means, it simulates the depth of the objects, and produces 2D images with a 3D projection.

To obtain an image plane with perspective is necessary to have a Field of View. In order to accept any resolution of the image plane, we have to divide the field of view in 2 parts: horizontal and vertical. This way, we can obtain the aspect ratio of the image plane we want.

Figure 29.: Perspective camera with hFov and vFov (Schim).



The algorithm to generate a ray from the perspective camera is very simple. By knowing the horizontal Field of View and vertical Field of View in radians, and with  $u$  and  $v$  as parameters, it is possible to calculate the direction of that ray.

It starts to calculate the distance to go through the right vector and the up vector of the camera. That can be done with the arctangent of each Field of View of the camera (horizontal and vertical) and multiplying it with  $u - 0.5$  in the right vector and with  $0.5 - v$  in the up vector. This makes sure that we go through every pixel, starting with the pixel from the upper left corner to the lower right corner of the image plane. Then the destination point of the ray is just the sum:

$destinationPoint = cameraPosition + cameraDirection + rightVector + upVector$ , and so its direction is just:

$rayDirection = destinationPoint - cameraPosition$ . The origin of the ray is the position of the camera, because in a perspective camera, all rays come from the same point: the point where the camera is located.

```
rightFactor = arctan(hFov * (u - 0.5)) + deviationU
rightVector = right * rightFactor
```

```

upFactor = arctan(vFov * (0.5 - v)) + deviationV
upVector = up * upFactor
destinationPoint = cameraPosition + cameraDirection + rightVector + upVector
rayDirection = destinationPoint - cameraPosition
return Ray (rayDirection, cameraPosition)

```

### *Orthographic Camera*

The orthographic camera removes the sense of perspective by drawing the image plane without simulating the depth of the objects, making all the objects looking flat. This is achieved by inverting the logic of the perspective camera. Instead of calculating the direction and always having the same origin, in the orthographic camera, the direction is always the same for all rays, and the origin of the ray varies.

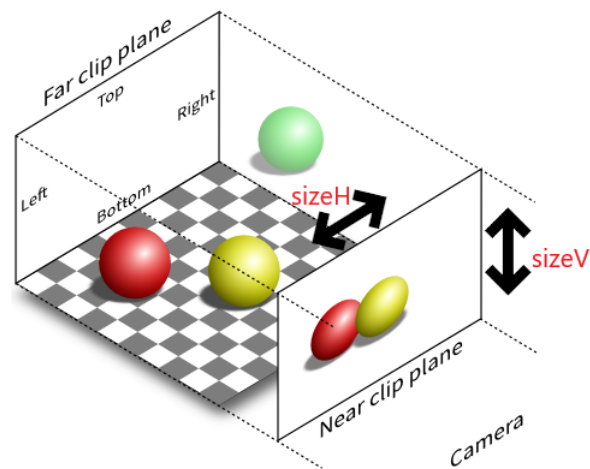
It starts to calculate the distance to go through the right vector and up vector of the camera, like the perspective camera. But, instead of using the Field of View, we now use the *sizeH* and *sizeV*, which are the horizontal and vertical sizes of the image plane. Then, to make sure that we go through all pixels from upper left pixel to lower right, we need to use the *u* and *v* values from the parameters. Then, the origin of the ray is:  $rayOrigin = cameraPosition + rightVector + upVector$ .

```

rightFactor = (u - 0.5) * sizeH
rightVector = right * rightFactor + right * deviationU
upFactor = (0.5f - v) * sizeV
upVector = up * upFactor + up * deviationV
rayOrigin = cameraPosition + rightVector + upVector
return Ray (cameraDirection, rayOrigin)

```

Figure 30.: Orthographic camera with sizeH and sizeV (Schim).



Orthographic projection (O)

#### 3.4.5 Object Loaders

Last, but not least, the library allows to develop different Object Loaders. An Object Loader is, as the name implies, a class that allows the ray tracer to import meshes from different Model file formats. There are many different types of file formats for storing meshes:

- 3ds
- FBX
- Wavefront .obj file
- COLLADA
- SketchUp
- AutoCAD DXF

All these file formats allows the user to store the positions of many triangles in a file, which together form the geometry of the scene.

This library only provides an Object Loader that allows loading the scene geometry from Wavefront obj files. This type of Model file format is a good choice because, besides being simple, it is open and has been adopted by many 3D graphics application vendors, like, 3ds Max and Blender.



*OBJ Loader*

The OBJ file format is a simple data format that allows to store only the position of each vertex, the UV position of each texture coordinate vertex, vertex normals, and the faces that make each polygon defined as a list of vertices, and texture vertices. Vertices are stored in a counter-clockwise order by default, making explicit declaration of face normals unnecessary.

```
# This is a comment

# List of geometric vertices
# x   y   z   w
v 1.0 2.0 3.0 1.0
v 5.0 6.0 7.0 1.0
...

# List of texture coordinates
#   x   y   w
vt 0.5 1.0 0.0
vt 0.1 0.3 0.0
...

# List of vertex normals
#   x   y   z
vn 0.3 0.0 0.7
vn 0.2 1.0 0.3
...

# List of polygonal face elements
# v1/vt1/vn1  v2/vt2/vn2  v3/vt3/vn3
f 3/1/1        4/2/3        5/3/4
f 6/6/3        7/1/2        8/2/6
...
```

Listing 3.1: .OBJ file format

The Wavefront OBJ file format is described as shown in 3.1, and is accompanied by another file, Material Template Library (MTL), that describes the visual aspects of the polygons. It is this file that describes surface shading (material) properties of objects within one or more .OBJ files. It allows to define multiple materials, with, ambient color, diffuse color, specular reflective color and specular refractive color. And even allows to load texture maps stored in TGA files. The Listing 3.2 shows an example of a description of a material.

```
# This is a comment

# Define a material named 'Colored'
newmtl Colored
```

```

# Ambient color
Ka 1.0 0.0 0.0 # red

# Diffuse color
Kd 0.0 1.0 0.0 # green

# Specular color
Ks 0.0 0.0 1.0 # blue

# Dissolved (transparency)
d 0.4

```

Listing 3.2: .MTL file format

### 3.5 ANDROID SPECIFICS AND CHALLENGES

#### 3.5.1 Specifics

Before developing the ray tracer to Android, it is necessary to understand how an Android application works.

A typical Android application is programmed in Java programming language. And it usually needs to communicate with an User Interface which also is programmed in Java. The code is compiled with Android Software Development Kit (SDK) along with any data and resource files into an Android package (APK). But, in order to avoid using the Java Emulator in our code and program it in native code, it is necessary to use Android Native Development Kit (NDK). Unfortunately, the NDK tool-chain doesn't provide any User Interface libraries like Qt that facilitates the build of a User Interface in native code. So, in order to obtain the best performance possible in a mobile device, the ray tracer library and components were programmed in C++ and the User Interface was programmed in Java.

#### 3.5.2 User Interface

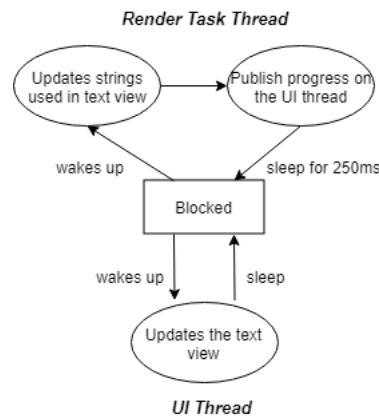
The Android User Interface is programmed in Java and only one thread can refresh the User Interface (UI thread).

There are only 2 goals in the User Interface: should be as simple as possible and should be able to allow progressive ray tracing, which means, refreshing the image while it is being rendered.

In order to allow progressive ray tracing, it was used a pool of 1 thread called Render Task thread that every 250 ms wakes up the thread and updates the strings used in the

text view. Before it finishes, it publishes the progress on the UI thread. Then the UI thread wakes up and updates the text view.

Figure 31.: Execution flow of UI thread and Render Task thread.



### 3.5.3 Challenges

Developing applications for mobile devices have different challenges compared with the traditional personal computer hardware.

The Android User Interface has some particularities like only 1 thread can modify the UI, and is usually called the UI thread.

The size of RAM available for executing programs is typically smaller and the CPU microarchitecture is generally simpler and with smaller computational power. Also the Operating System (OS) is shaped for the mobile world, making a lot of restrictions in the performance of the applications in order to save battery. The amount of main memory available for the applications can also be affected by the OS.

Other challenges are related with the communication mechanism between the SDK and the NDK, because two different languages need to "communicate" in runtime (GUI in Java and the library in C++). This involves learning how to use the Java Native Interface (JNI), so that the native code can send and receive information from Java Virtual Machine (JVM).

Because ray tracing may involve rendering complex scenes, placing all this information in the main memory may not be possible, and so this memory management can be a worthy challenge.

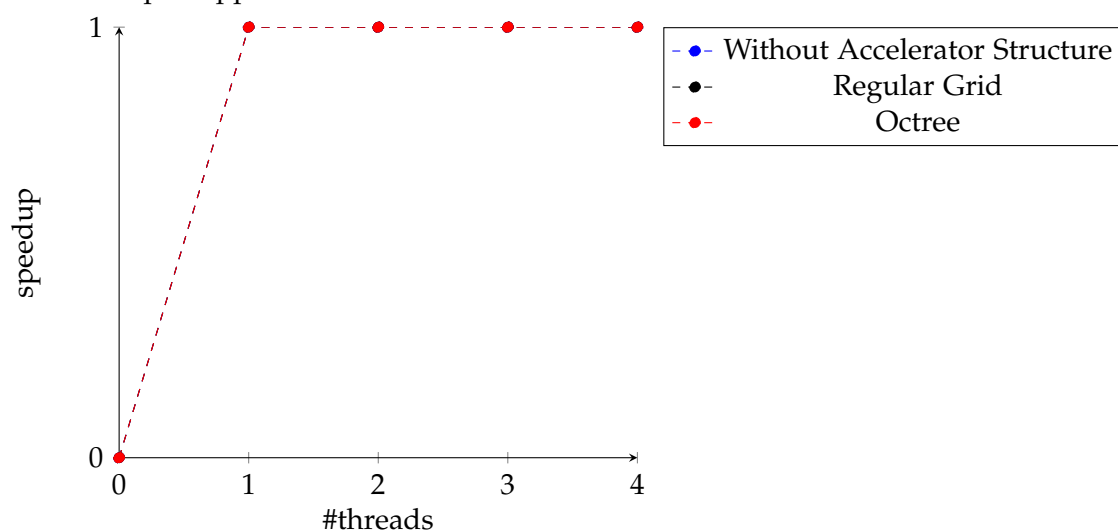
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## DEMONSTRATION: GLOBAL ILLUMINATION

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### 4.1 RESULTS OBTAINED

The developed application ...



### 4.2 COMPARISON WITH ANDROID CPU RAYTRACER (DAHLQUIST)

Comparison ...

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## CONCLUSION & FUTURE WORK

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### 5.1 CONCLUSIONS

The constant evolution of technology allowed to leverage and massify the mobile devices. With, more and increasingly powerful, mobile devices, it is possible to perform more and more complex and useful tasks in them. This is a huge market where the programmers can develop their applications to, and where the development time can be a huge factor in their career success.

But as noted in the section [2.4](#), there is clearly a lack of well documented rendering libraries for mobile systems. There is then the need to change this reality, since more and more the Internet of Things is more present each passing year, because there are increasingly powerful mobile systems.

During the development of this ray tracer library, it was identified some challenges caused by the fact that it was developed for an Android mobile device, like, the smaller amount of RAM available for the software applications. And, also, the simpler CPUs microarchitectures and smaller computational power available from these devices can make computational demanding applications, like ray tracers, difficult to perform the required calculations in a useful time for the user. This fact is corroborated by the obtained results as demonstrated in section [4.1](#).

### 5.2 FUTURE WORK

With respect to future work, it should be the development of the library for Android and the analysis of possibilities and challenges that may arise. Upon completion of the development process, besides writing the dissertation and the article, it is expected to provide a demo application in order to illustrate the functionalities and performance that the library will offer.

The library was implemented as planned, having been developed:

- 2 acceleration structures

- 3 primitive shapes
- intersection
- material
- primitive
- ray
- renderer
- scene
- possibility to develop different types of cameras
- possibility to develop different types of lights
- possibility to develop different types of object loaders
- possibility to develop different types of samplers
- possibility to develop different types of shaders

All these developed components allow the execution of the basic features of a ray tracer, such as the intersection of rays with the different shapes of primitives. Besides that, it allows the user the possibility to develop several types of rendering components, like cameras, lights, object loaders, samplers and shaders. With this, the user can create simple rendering applications that just use the rendering components offered together with the library, or even very complex applications, that use rendering components developed by the user.

Besides the library, it was also developed several rendering components:

- 2 cameras
- 2 lights
- 1 object loader
- 6 samplers
- 5 shaders

This allows the user to develop rendering applications in an easy, safe and fast way, as was intended in this dissertation. Unfortunately, this does not allow rapid development of all kinds of rendering applications. One of the things that can be improved in this library is allowing to put more than one camera in the scene, so that you can cast rays to the scene from more than one different point. And thus open the possibility of allowing the user to develop more different shaders, such as Bidirectional Path Tracing, or even allowing to render the 3D scene into a 3D image.

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## USER DOCUMENTATION

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