



Universidade do Minho

Escola de Engenharia

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Mobile Ray Tracing

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ABSTRACT

The technological advances and the massification of information technologies have allowed a huge and positive proliferation of the number of libraries and APIs. This large offer has made life easier for programmers in general, because they easily find a library, free or commercial, that helps them solve the daily challenges they have at hand.

One area of information technology where libraries are critical is in Computer Graphics, due to the wide range of rendering techniques it offers. One of these techniques is ray tracing. Ray tracing allows to simulate natural electromagnetic phenomena such as the path of light and mechanical phenomena such as the propagation of sound. Similarly, it also allows to simulate technologies developed by men, like Wi-Fi networks. These simulations can have a spectacular realism and accuracy, at the expense of a very high computational cost.

The constant evolution of technology allowed to leverage and massify new areas, such as mobile devices. Devices today are increasingly faster and replace and / or complement tasks that were previously performed only on computers or on dedicated hardware. However, the number of image rendering libraries available for mobile devices is still very scarce, and no ray tracing based image rendering library has been able to assert itself on these devices. This dissertation aims to explore the possibilities and limitations of using mobile devices to execute rendering algorithms that use ray tracing, such as progressive path tracing. Its main goal is to provide a rendering library for mobile devices based on ray tracing.

RESUMO

Os avanços tecnológicos e a massificação das tecnologias de informação permitiu uma enorme e positiva proliferação do número de bibliotecas e APIs. Esta maior oferta permitiu facilitar a vida dos programadores em geral, porque facilmente encontram uma biblioteca, gratuita ou comercial, que os ajudam a resolver os desafios diários que têm em mãos.

Uma área das tecnologias de informação onde as bibliotecas são fundamentais é na Computação Gráfica, devido à panóplia de métodos de renderização que oferece. Um destes métodos é o ray tracing. O ray tracing permite simular fenómenos eletromagnéticos naturais como os percursos da luz e fenómenos mecânicos como a propagação do som. Da mesma forma também permite simular tecnologias desenvolvidas pelo homem, como por exemplo redes Wi-Fi. Estas simulações podem ter um realismo e precisão impressionantes, porém têm um custo computacional muito elevado.

A constante evolução da tecnologia permitiu alavancar e massificar novas áreas, como os dispositivos móveis. Os dispositivos são hoje cada vez mais rápidos e cada vez mais substituem e/ou complementam tarefas que anteriormente eram apenas realizadas em computadores ou em hardware dedicado. Porém, o número de bibliotecas para renderização de imagens disponíveis para dispositivos móveis é ainda muito reduzido e nenhuma biblioteca de renderização de imagens baseada em ray tracing conseguiu afirmar-se nestes dispositivos. Esta dissertação tem como objetivo explorar possibilidades e limitações da utilização de dispositivos móveis para a execução de algoritmos de renderização que utilizem ray tracing, como por exemplo, o path tracing progressivo. O objetivo principal é disponibilizar uma biblioteca de renderização para dispositivos móveis baseada em ray tracing.

CONTENTS

1	INTRODUCTION	1
1.1	Context	1
1.2	Motivation	2
1.3	Goals	2
1.4	Document Structure	3
2	STATE OF THE ART	4
2.1	Ray Tracing	4
2.2	Typical CPU features	5
2.3	Key features of Ray Tracing for this work	7
2.3.1	Type of software license	7
2.3.2	Platform	7
2.3.3	Interactivity	7
2.3.4	Progressive	8
2.3.5	Types of Rendering Components	8
2.4	Related work	8
2.4.1	Conclusions	9
3	SOFTWARE ARCHITECTURE	10
3.1	Approach	10
3.2	Methodology	12
3.3	Library	12
3.3.1	Third parties dependencies	12
3.3.2	Renderer	13
3.3.3	Scene	14
3.3.4	Shapes	15
3.3.5	Acceleration Structures	18
3.4	Rendering Components	18
3.4.1	Shaders	18
3.4.2	Samplers	26
3.4.3	Lights	29
3.4.4	Cameras	31
3.5	Android specifics and challenges	32
3.5.1	Specifics	32
3.5.2	User Interface	33
3.5.3	Challenges	33

4	DEMONSTRATION: GLOBAL ILLUMINATION	35
4.1	Results obtained	35
4.2	Comparison with Android CPU Raytracer (Dahlquist)	35
5	CONCLUSION & FUTURE WORK	36
5.1	Conclusions	36
5.2	Future Work	36
6	BIBLIOGRAPHY	37
A	USER DOCUMENTATION	40
	Appendices	40

LIST OF FIGURES

Figure 1	Illustration of the most common mobile devices - tablet and smart-phone (du Net)	2
Figure 2	Illustration of a typical ray tracer algorithm.	4
Figure 3	Illustration of a typical cache memory inside a microprocessor (Karbo and Aps.).	5
Figure 4	Illustration of the Classic RISC multilevel CPU pipeline (Dictionaries and Encyclopedias).	6
Figure 5	Illustration of a typical execution of SIMD extension (Bishop).	6
Figure 6	Illustration of the developed User Interface.	10
Figure 7	Illustration of the 3 layers in the application	11
Figure 8	Illustration of tiling the image plane.	14
Figure 9	Illustration of shadow rays casting (Foundry).	15
Figure 10	Illustration of a ray intersecting a plane (Vink).	16
Figure 11	Illustration of a ray intersecting a sphere in two points (Chirag).	17
Figure 12	Illustration of a ray intersecting a triangle (Scratchapixel).	18
Figure 13	Illustration of the rendering equation describing the total amount of light emitted from a point x along a particular viewing direction and given a function for incoming light and a BRDF.	19
Figure 14	NoShadows shader.	20
Figure 15	Reflections projected on the floor and on the spheres.	21
Figure 16	Refraction of light at the interface of two media of different refractive indices.	22
Figure 17	Whitted shader.	23
Figure 18	Rotation matrix from an arbitrary axis and an angle.	24
Figure 19	PathTracer shader.	26
Figure 20	Halton sequence in a 2D image plane.	27
Figure 21	Pseudorandom sequence in a 2D image plane.	28
Figure 22	Calculation of point P by using barycentric coordinates starting at point A and adding a vector AB and a vector AC.	30
Figure 23	Jittering in a plane image.	31
Figure 24	Perspective camera with hFov, vFov and dFov.	32
Figure 25	Execution flow of UI thread and Render Task thread.	33

LIST OF TABLES

Table 1	Comparison of different applications/frameworks that use ray tracing	9
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INTRODUCTION

1.1 CONTEXT

Programming is like building something with primitive blocks and it can be a very difficult task if we have to program every aspect of the application without some “blocks” already built for us to use. That’s why in the programming world there is a whole panoply of free and commercial libraries with APIs that provide a huge quantity of functions for the programmer to use.

In computer graphics, there are many libraries that provide functionalities to render images based in different techniques. Ray tracing is a technique for rendering an image by tracing the path of light through pixels in an image plane and simulating the effects of its interactions with virtual objects. This technique is capable of producing a very high degree of visual realism but at a great computational cost.

Since nowadays we have more and more mobile systems whose computational power increases every year, the need for more libraries to help the programmers develop applications for these systems is increasing too. However, there are not many options to choose from for developing a renderer based on ray tracing. That’s why this dissertation focuses on assessing and providing a ray tracer library for mobile systems.

It is important to mention that this dissertation is not focused on rendering techniques other than ray tracing. It is not focused in assess different integrators (numerical solutions to the rendering equation) and / or assess different approaches in ray tracing like Packet Traversal. It is also not focused on assess different quasi random numbers generators neither assess the performance of different computer systems.

These rendering algorithms based in ray tracing are very useful because they allow rendering photo-realistic images with a degree of realism much better than the graphics cards allow by default through rasterization. As previously stated, the computing power in mobile devices processors has been increasing and this may allow a mobile device with a mid-range processor to run these algorithms in a useful time.

Figure 1.: Illustration of the most common mobile devices - tablet and smartphone (du Net)



1.2 MOTIVATION

Among other factors, the productivity of a programmer depends on what libraries he can have access to. But, there are almost no rendering libraries based in ray tracing available today for mobile systems like Android, iOS or Windows 10 Mobile. And it is likely that these systems already have enough processing power to render images with fairly complex scenes in an acceptable time by using algorithms based in ray tracing.

It is also important to note that there is not much documentation about the advantages and limitations of executing different rendering algorithms in these devices.

1.3 GOALS

The main goal of this dissertation is to assess and demonstrate the advantages of running rendering algorithms in mobile devices.

It is also intended to promote and facilitate the development of applications for mobile systems that use ray tracing techniques, with special emphasis on rendering applications. To do this, will be developed a library that supports the fundamental operations of a ray tracing engine. This library will allow the agile development of diverse applications, by using components that invoke the functionality of the library itself.

Additionally, it is intended to supply rendering components at a higher abstraction level, like the camera, scene and the integrator that facilitates further the development of applications.

Finally, it is important to do a demonstration of the rendering application with some interface layer to let the user assess the performance of several functionalities provided by the library.

1.4 DOCUMENT STRUCTURE

This dissertation is organized in 5 chapters: Introduction, State of the Art, Software Architecture, Demonstration: Global Illumination and Conclusion & Future work.

The first chapter describes the context and motivation behind this work, as well as its goals. Its main purpose is to identify the problem at hand and set up goals that should be accomplished.

The second chapter introduces the main concepts of ray tracing and compares different implementations of ray tracers already available in the world wide web. The reason behind this comparison is to show how many ray tracers are already available to mobile devices and highlight the differences between the features they have. It also provides some information about the processors of today that helps realize their ability to execute computationally demanding algorithms like ray tracing.

The third chapter explains the proposed approach and explains each module developed in the library and in the rendering components. This chapter ends with an explanation of some Android specifics, such as the user interface by characterizing its work flow and mentioning some of the challenges overcome during the development of the application.

The fourth chapter summarizes the key results obtained by executing different algorithms with different number of threads and different acceleration structures. And it will also contain a small comparison between the developed application and the Android CPU Ray-tracer (Dahlquist).

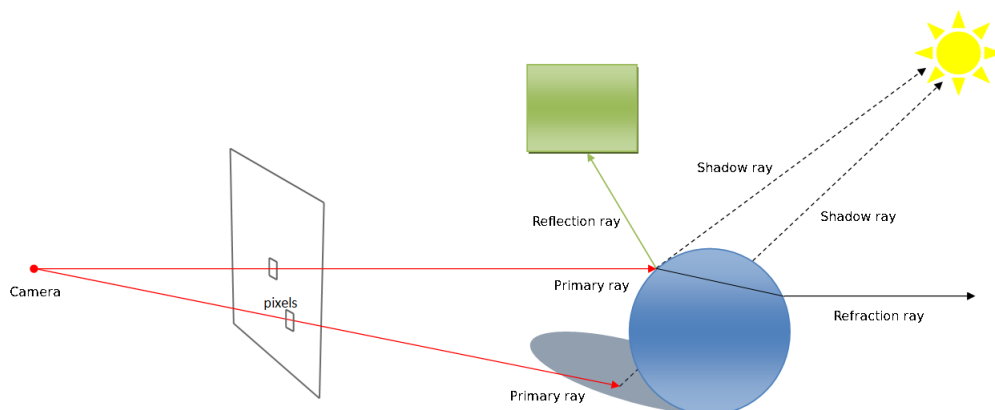
Finally, the fifth chapter ends this dissertation with the conclusions that can be withdrawn from this work and proposes some future work.

STATE OF THE ART

2.1 RAY TRACING

Ray tracing one frame can be, simultaneously, a computationally demanding task and an embarrassingly parallel task. As tracing rays is a recursive process which aims to calculate the luminance of light of each individual pixel separately. At least one ray is shot per pixel and in a naive approach each ray would be intersected with all the objects in the scene in order to determine which one is the closest primitive intersecting that given ray. To evaluate the light intensity that an object scatters towards the eye, the intensity of the light reaching that object has to be evaluated as well. Ray tracing achieves this by shooting additional secondary rays, because when a ray hits a reflecting or transparent surface, one or more secondary rays are cast from that point, simulating the reflection and refraction effects.

Figure 2.: Illustration of a typical ray tracer algorithm.



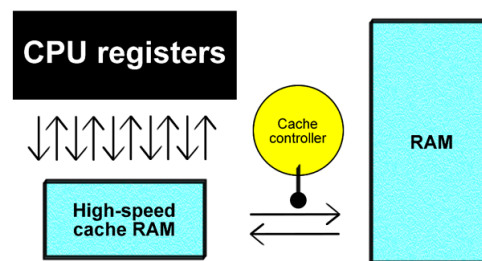
A typical image of 1024×1024 pixels tends to cast at least a million primary rays and a multiple of that as shadow, reflection, refraction and secondary rays. This is why ray tracing can't provide interactive frame rates with ease.

2.2 TYPICAL CPU FEATURES

Fortunately, the present state of available technology provides affordable machines with multiple CPU cores that can work in parallel and with great performance. This is achieved thanks to features developed inside the processor like the cache, the multilevel pipeline, the hardware prefetching and SIMD instruction set already available in the current processors.

The cache is a very small and fast multilevel memory inside the processor that temporarily stores the data read from the main memory. This memory allows reading its content at a very low latency in the order of magnitude of around 1 nanosecond in the first level, 10 nanoseconds at second level and 50 nanoseconds at third level compared to the typical 100 nanoseconds of a DDR main memory. The downside is that it is very small because its cost are much higher than a typical RAM memory. Nowadays, the level 1 has 64kB, the level 2 has 256kB and the level 3 has 8 MB which is very little compared to the typical 16GB provided by the memory RAM.

Figure 3.: Illustration of a typical cache memory inside a microprocessor (Karbo and Aps.).



The multilevel pipeline is another feature inside a processor which allows to reduce the processor's own latency by allowing a form of parallelism called instruction-level parallelism within a single processor. Basically, one instruction is divided in some stages and it allows the possibility to execute different stages of different instructions simultaneously. In the early days, the Classic RISC pipeline were typically divided in 5 stages:

- Fetching the instruction
- Decoding the instruction
- Executing the instruction where the arguments can be fetched from registers (1 cycle latency) or from memory (2 cycle latency)
- Memory access where it ensured that writing in memory was always performed in the same stage and allowed to use that value in another instruction before it was written in memory
- Writing back the value in the register

Nowadays, the current microprocessors have a pipeline with 8-14 stages and can be more complex than the Classic RISC, but the operating principle is the same. This allows faster CPU throughput, which means the number of instructions that can be executed in a unit of time is greater, than it would otherwise be possible at a given clock rate.

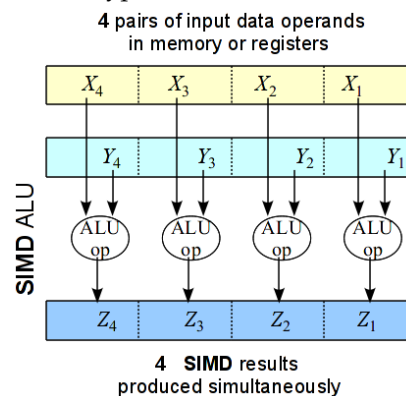
Figure 4.: Illustration of the Classic RISC multilevel CPU pipeline (Dictionaries and Encyclopedias).

Instr. No.	Pipeline Stage						
1	IF	ID	EX	MEM	WB		
2		IF	ID	EX	MEM	WB	
3			IF	ID	EX	MEM	WB
4				IF	ID	EX	MEM
5					IF	ID	EX
Clock Cycle	1	2	3	4	5	6	7

The hardware prefetching is, as the name implies, a feature in the processor that makes the processor fetch the data and the instructions before it really needs to execute. This allows to reduce the time that the processor waits for the data in the main memory.

Finally, SIMD instruction set is a set of special instructions that allows the processor to read or write bigger sizes of data. Typically, a 64 bit processor can only work with 64 bits of information at a time during the execution of an instruction. This feature can allow to read or write up to 512 bits by using special registers and additional ALUs provided in the processor.

Figure 5.: Illustration of a typical execution of SIMD extension (Bishop).



Nowadays, even mobile devices like smart phones and tablets have multiple CPU cores with features similar to those described above. This opens the possibility to execute more computationally demanding algorithms, like ray tracing, in these devices.

2.3 KEY FEATURES OF RAY TRACING FOR THIS WORK

Ray tracing is an algorithm that can have a panoply of features or optimizations in order to reduce the time required to trace all the rays and / or to show the results as fast as possible. It also, like any application, can have different types of software licenses and be executed in different platforms.

For this work, the most important features in a ray tracer are: the type of software license, the platform where can be executed, interactivity, progressive and the type of rendering components.

2.3.1 *Type of software license*

A software application can have different type of software license, but in order to simplify this dissertation, the software license were grouped into 3 types: Free, Commercial and Open Source. The license Free means that the user has the right to execute freely the application but cannot copy, modify or distribute the implemented code. The license Commercial means that the user cannot even execute the application without buying it first and cannot copy, modify or distribute the implemented code. The license Open Source means that the user has the right to execute freely the application and can even copy, modify and distribute the implemented code. The software license is very important in this work because it lets the user know if he can develop something over the provided software or if he can just use the application.

2.3.2 *Platform*

An application can only be executed in the platforms that the developers compiled the code for. So, a ray tracer that can be executed in a desktop may also or may not be executed on another platform, like a mobile device. This information is very important in this work because it inform us whether a ray tracer can be executed in a mobile device with the typical Operating System like Android, iOS or Windows 10 Mobile.

2.3.3 *Interactivity*

In ray tracing, interactivity means rendering an image with a very low response time, like a few milliseconds per frame. An interactive ray tracer can render a scene with multiple frames per second.

2.3.4 *Progressive*

A typical ray tracer shows the rendered image only after the whole process is complete. A progressive ray tracer is a ray tracer that updates the color of pixels in the screen as soon as the rays are traced, instead of waiting for the rendering process to complete. This means that an image is rendered quickly with some aliasing or noise and it is progressively improved over time.

2.3.5 *Types of Rendering Components*

A ray tracer can be developed with the different rendering components programmed separately. Some examples of rendering components are: Integrators, Cameras, Scenes, Samplers, Shapes, Lights and Accelerator Structures. In some ray tracers, these rendering components can even be programmable by the user. This is very important because it allows the user to develop his own renderer based in ray tracing without having to develop every feature in the ray tracer.

2.4 RELATED WORK

The possibility of rendering an image with ray tracing was demonstrated in 1980 by Whitted ([dos Santos](#)) and since then the number of libraries that provide basic ray tracing functionalities increased greatly. There is a wide range of different ray tracers available today for the programmer to use, yet the majority can only be used with the traditional personal computer hardware (desktop or laptop).

The table 1 shows some applications or frameworks that use ray tracing available today and compares them according to their type of license, platform compatibility, interactivity, progressive and whether they allow development of your own rendering components like the integrator and sampler. Note that some of these ray tracers provide only the engine with the basic ray tracing functions, such as creating rays and intersecting them with geometric primitives, so the rendering components are only programmable if the application that uses the engine supports it. During the research of the available ray tracers, others than the ones presented in the table were found, but they were excluded because the documentation was very poor without explaining the basic functionalities provided or because there was no documentation at all.

Table 1.: Comparison of different applications/frameworks that use ray tracing

Product	License	Platform	Mobile	Interactivity	Progressive	Programmable Components
Optix (Nvidia (a))	F	Nvidia GPU	N	Y	Y	Y
Optix Prime (Nvidia (b))	F	CPU & Nvidia GPU	N	Y	Y	Y
RenderMan RIS (Pixar)	C	CPU	N	Y	Y	Y
OctaneRender (Inc)	C	GPU	N	Y	Y	N
Embree (Intel)	O	Intel CPU	N	Y	Y	Y
Radeon Rays (AMD)	O	CPU & GPU	N	Y	Y	Y
PBRT (Matt Pharr)	O	CPU	N	N	N	N
Visionaray (Zellmann)	O	CPU & Nvidia GPU	N	Y	Y	N
YafaRay (Gustavo Pichorim Boiko)	O	CPU	N	N	N	N
tray_rust (Usher (c))	O	CPU	N	N	N	N
micro-packet (Usher (a))	O	Intel CPU	N	N	N	N
tray (Usher (b))	O	CPU	N	N	N	N
The G3D Innovation Engine (Morgan)	O	CPU	N	N	N	N
HRay (Kenneth)	O	CPU	N	N	N	N
Mitsuba (Jakob (2010))	O	CPU	N	N	N	N
Indigo RT (Limited)	O	CPU & GPU	N	Y	N	N
jsRayTracer (Chedeau)	O	CPU	N	Y	Y	N
Android CPU Raytracer (Dahlquist)	O	CPU	Y (Android)	Y	N	N

2.4.1 Conclusions

As the table 1 shows, there is a lack of generic ray tracing libraries for the mobile devices. Although there are some closed-source ray tracing demo applications, only one ray tracer already available has some sort of documentation and is compatible with mobile devices, in this case with Android. This ray tracer is open source, uses only the CPU of the device and has a good performance. It even allows interactions with the objects during the render process. But, it doesn't support progressive rendering and also does not allow the programmers to use their own rendering components.

This dissertation aims to fix this lack of libraries, by providing one that contains ray tracing basic functionalities and the ability to let the programmer be able to develop their own rendering components like the sampler, integrator, camera and shapes of virtual objects. It also studies the drawbacks that these mobile devices may have comparing with the average multi-core personal computer hardware. And finally, a small comparison was made with the Android CPU Raytracer (Dahlquist) in order to illustrate the advantages and disadvantages of both. This comparison is important because it enriches all the work done, as it demonstrates if the performance of the provided features are relatively efficient.

The development of this demonstration application involves the distinction of three layers of abstraction: user interface, rendering components and the library itself.

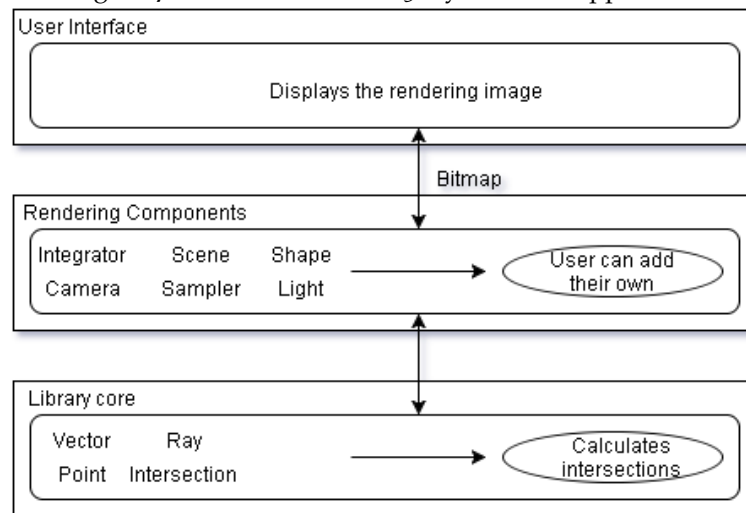
Figure 6.: Illustration of the developed User Interface.

The middle layer provides the rendering components which are abstracted concepts about rendering that use functionalities that the library offers to the programmer. Some of these rendering components are the camera, the light, the sampler and the integrator. These rendering components are useful for the programmer since it allows them to use features without having the need to know how these were developed. And, of course, this facilitates and accelerates the development of new rendering applications.

10

It is also important to mention that the demo application was developed in order to show the developed features, the performance achieved in the mobile devices and also to help promote the library. This demo application is a good way to test it in several Android devices like a smart phone or a tablet.

Figure 7.: Illustration of the 3 layers in the application



Besides the abstraction layers, there are some important strategic decisions made in order to guide the progress of the development of this library.

The first decision was: the primary rays always have origin in the camera. This decision was made in order to not mix the code of the integrator with the ray tracer renderer engine.

Other decision made was to make the rendering process progressive, which means that the rendered image is incrementally refined with more and more traced rays. As the integrator will be converging to better values. This is important in order to give the user a fast rendered image, with some noise or aliasing, and converge it progressively to a better solution with higher details and practically without any visual noise or aliasing.

Another thought aspect that was studied is the permission of dynamic scenes and / or dynamic cameras, which means to let the programmer modify the camera or the scene while the ray tracer is rendering it. This makes possible to build challenging applications and also provide more interesting scenes and more eye candy applications for the final user.

Last, but not least, is that the code was developed in a modular way, in this case was programmed in an object oriented manner. This allows the programmers to code their own rendering components, like the integrator, camera, sampler and light, without having to develop the basic features in the renderer engine.

3.2 METHODOLOGY

In order to take advantage of most of the mobile CPU resources and give a good performance for the applications, the library and the rendering components were developed using the native programming language C++. This was achieved by using the Native Development Kit (NDK) provided by the Integrated Development Environment (IDE) Android Studio. The User Interface was developed in Java using the traditional Software Development Kit (SDK) provided by the Android Studio because there is no framework in the NDK that helps the programmer design his own user interface. Despite that, its performance is not very important because it doesn't interfere significantly with the others layers of the application.

3.3 LIBRARY

As stated above, this library was implemented in an object-oriented fashion. The most important classes that provide functionalities already developed for the user to use are:

- **Renderer:** class that starts the rendering process and stores the calculated pixels colors in a C style array.
- **Scene:** class that stores the geometry information in vectors and provides methods to trace rays in the scene without any acceleration structures.
- **Shapes:** set of classes that allows to create triangles, spheres and planes.
- **Material:** class that stores all 4 types of material color:
 - Emission light color
 - Diffuse reflection color
 - Specular reflection color
 - Specular refraction color
- **Primitive:** class that stores the shape and material of each primitive in the scene.
- **Ray:** class that represents a ray casted into the scene.

3.3.1 *Third parties dependencies*

Before describing each functionality provided in each class developed, it is important to mention that this library uses 3 other libraries developed in C++ by third parties. Those libraries are:

- OpenGL Mathematics (**Creation**): used to create 3d points and vectors, perform geometry calculations and store pixels and primitives colors.
- tinyobjloader (**syoyo**): used to load scenes from wavefront obj files.
- Google Test (**Google (b)**): used to create some unit tests and to mock some classes.

All these libraries are Android compatible and are reliable in terms of performance and maintenance.

Besides being dependent on these 3 libraries, this library also depends on OpenGL ES 2.0 (**Inc.**) from Android SDK and depends on CMake (**kitware**) in order to compile the application.

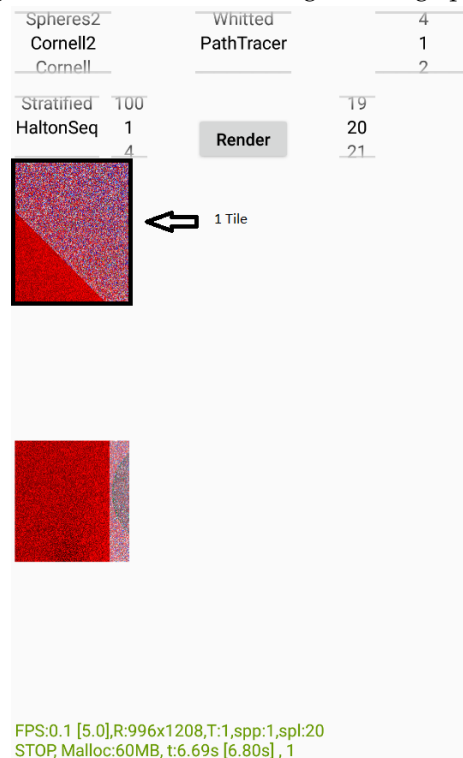
3.3.2 *Renderer*

The *Renderer* is the closest class to the application that starts the rendering process. This class provides two main methods:

```
void renderFrame (::std::uint32_t *bitmap, ::std::int32_t numThreads, ::std::uint32_t stride) noexcept;
void stopRender() noexcept;
```

The *renderFrame* method starts the rendering process and writes the calculated light luminance of each pixel in the parameter *bitmap*. This method also allows to choose the number of threads that will render the image into the bitmap, and needs the stride of that bitmap array. The image plane is divided into 16 tiles of pixels and it is traced one primary ray per pixel in each tile.

Figure 8.: Illustration of tiling the image plane.



The *stopRender* method only serves to stop the rendering process without cleaning the pixels' colors already calculated.

3.3.3 Scene

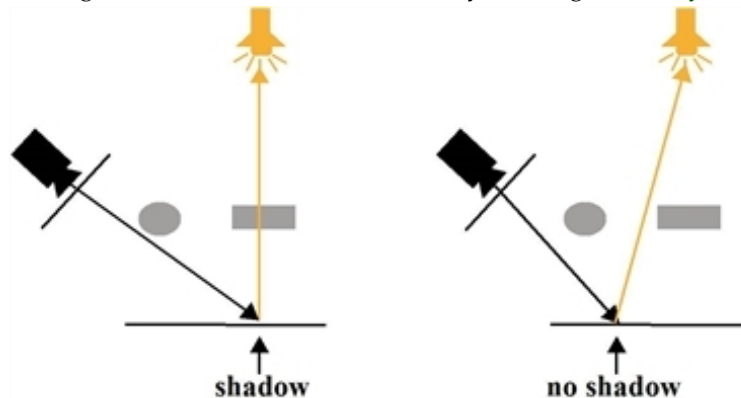
The Scene is the class that handles the process of intersecting a ray with the primitives and source lights in the scene. Besides providing a vector to add the light sources and a vector to add primitives to the scene, it also provides two main methods:

```
Intersection trace(Intersection intersection, const Ray &ray) noexcept;
Intersection shadowTrace(Intersection intersection, const Ray &ray) noexcept;
```

The *trace*, as the name implies, is a method that tries to intersect a ray with all the primitives and light sources in the scene. And It returns the closest intersection to the origin of that ray. This method is used to determine the intersection of the casted ray with the primitives in the scene.

The *shadowTrace*, is similar to the *trace* method but with the difference that returns the first intersection found. The purpose of this method is to simulate the shadows in the scene, like it is illustrated in figure 9.

Figure 9.: Illustration of shadow rays casting (Foundry).



3.3.4 Shapes

In order to make possible to generate scenes with all kind of objects, it was developed 3 types of shapes: plane, sphere and triangle. All shapes provide only one method:

```
Intersection intersect(const Intersection &intersection, const Ray &ray) const
noexcept;
```

This method determines if a ray intersects the shape and returns the intersection. It is important to mention that, obviously, each shape was developed with different algorithm.

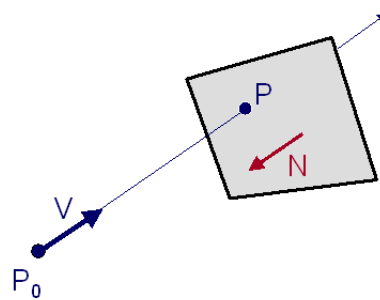
Plane

The plane is an essential primitive shape because it allows the user to build indoor scenes.

The construction of a plane requires just an arbitrary point in the plane and the normal of the plane. So, the intersect method implemented has the following algorithm:

```
projection = planeNormal . rayDirection
if (|projection| <= 0) return false
distance = planeNormal . (planePoint - rayOrigin) / projection
if (distance <= 0 || distance > rayMaxDistance) return false
intersectionPoint = rayOrigin + rayDirection * distance
return Intersection(intersectionPoint, planeNormal, material)
```

Figure 10.: Illustration of a ray intersecting a plane (Vink).



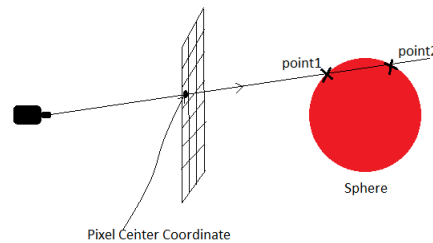
Sphere

The sphere is also an important primitive shape because it allows the user to build some common objects with a shape of a ball.

The construction of a sphere requires just the point in the center and the radius of the sphere. It also should be noted that a ray can intersect a sphere at two points and therefore it is necessary to determine the closest intersection point to the origin of the ray. So, the intersect method implemented has the following algorithm:

```
centerToOrigin = rayOrigin - sphereCenter
B = 2 * centerToOrigin . rayDirection
C = centerToOrigin.magnitude - radius
discriminant = B^2 - 4*C
if (discriminant <= 0) return false
distance1 = (-B + sqrt{discriminant} * 0.5)
distance2 = (-B - sqrt{discriminant} * 0.5)
distance = min(distance1, distance2)
if (distance <= 0 || distance > rayMaxDistance) return false
intersectionPoint = rayOrigin + rayDirection * distance
sphereNormal = intersectionPoint - sphereCenter
return Intersection(intersectionPoint, sphereNormal, material)
```


Figure 11.: Illustration of a ray intersecting a sphere in two points (Chirag).



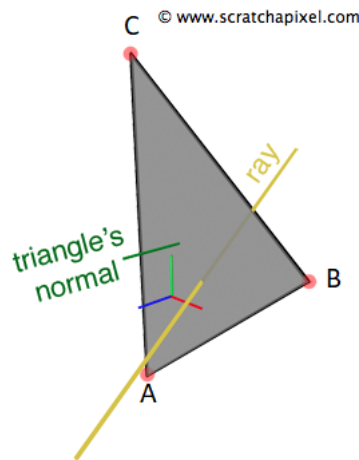
Triangle

And finally, obviously the triangle has also been implemented because, as it is the simplest primitive with an area, it allows to build many different object shapes.

The construction of a triangle requires three points $[A, B, C]$, two vectors $[AB, AC]$ and the normal of the triangle. So, the intersect method implemented has the following algorithm:

```
perpendicularVector = rayDirection x AC
projection = AB . perpendicularVector
if(|projection| <= 0) return false
vectorToRay = rayOrigin - A
u = (vectorToRay . perpendicularVector) / projection
if (u < 0 || u > 1) return false
perpendicularVector2 = vectorToRay x AB
v = (rayDirection . perpendicularVector2) / projection
if(v < 0 || (u + v) > 1) return false
distance = (AC . perpendicularVector2) / projection
intersectionPoint = rayOrigin + rayDirection * distance
return Intersection(intersectionPoint, triangleNormal, material)
```

Figure 12.: Illustration of a ray intersecting a triangle (Scratchapixel).



3.3.5 Acceleration Structures

Acceleration Structures ...

Regular Grid

Regular Grid ...

Bounding Volume Hierarchy

Bounding Volume Hierarchy ...

3.4 RENDERING COMPONENTS

In order to show the functionalities provided by the library, it was developed a few Rendering Components. It is provided the perspective camera, an area light and point light, four Samplers and three Shaders.

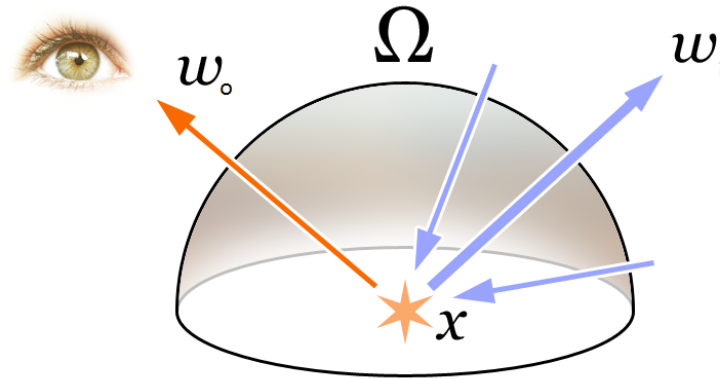
3.4.1 Shaders

The implemented ray tracer was programmed objected oriented, so each Rendering Component was developed separately. This allows the user to develop his own Rendering Components without having to develop the ray tracer engine.

In this context, a shader is the Rendering Component that describes how the Rendering Equation is approximated. The Rendering Equation describes how the total radiance

reflected by any point p of a surface in a direction ω_r is calculated. The Bidirectional Reflectance Distribution Function (BRDF) is a function that tries to approximate the Rendering Equation. In summary, a shader, in this context, is the algorithm of a BRDF.

Figure 13.: Illustration of the rendering equation describing the total amount of light emitted from a point x along a particular viewing direction and given a function for incoming light and a BRDF.



There was developed three shaders: NoShadows, Whitted and PathTracer. All shaders provide only one main method that allows the user to calculate the RGB color of a pixel with the information of a ray and the respective intersection.

```
void shade(RGB &rgb, Intersection &intersection, Ray &ray) const override;
```

The parameter *rgb* is where the color of the pixel will be calculated and the *intersection* contains the necessary information about the intersection of a ray with the primitive like the intersection point, its normal and the material of the intersected material. Finally the parameter *ray* is where the information about the ray like the origin of the ray and its direction is accessed.

NoShadows

NoShadows is the simplest shader because, as the name implies, it does not synthesize the shadows and it only simulates the direct lighting. This BRDF only simulates direct lighting in primitives with diffuse surfaces and it does not take into account the light coming from other points. As already said, the indirect lighting is not fully simulated but rather simplified in a way of fixed ambient light of about 10% of the color of the objects.

The algorithm developed is as following:

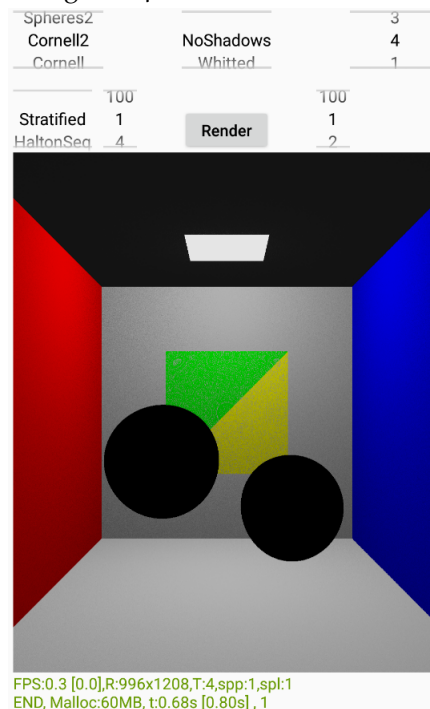
```
if (intersected material is diffuse) {
    for each light source
```

```

    for each sample
        vectorToLight = lightPosition - intersectionPoint
        cos_N_L = vectorToLight . intersectionNormal
        if (cos_N_L > 0) rgb += kD * radLight * cos_N_L
    rgb /= #samples
    rgb /= #lights
    rgb += kD * 0.1 //Ambient light
}

```

Figure 14.: NoShadows shader.



Whitted

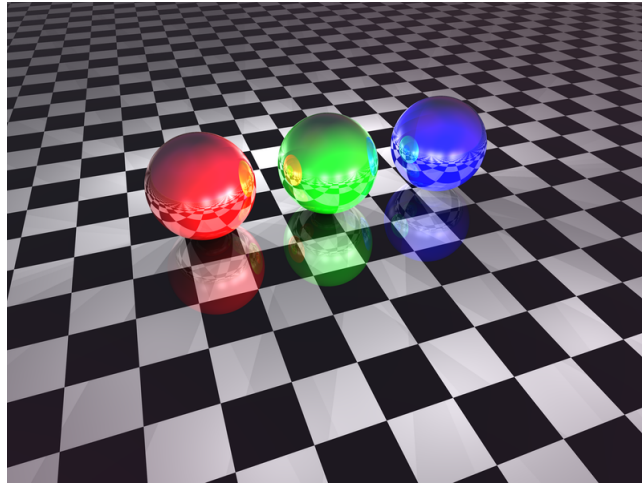
As the name of this shader implies, Whitted is the algorithm demonstrated by Whitted in 1980s. Like the previous shader, it doesn't simulate indirect lighting. This BRDF calculates the reflected light on diffuse and specular surfaces, as well as the light refracted on surfaces with a degree of transmission, such as water. In order to simulate a reflective and refractive surfaces, the algorithm was divided into each case. This makes it possible to simulate refractive surfaces, reflective surfaces and even refractive and reflective surfaces.

The reflected light in a diffuse surface is calculated by adding the casting rays in direction to the lights. These rays are called shadow rays and their radiance are multiplied by the dot product between vector to the light and the shading normal. At the end, the summation is

multiplied by the diffuse color of the intersected primitive and divided by the number of samples taken.

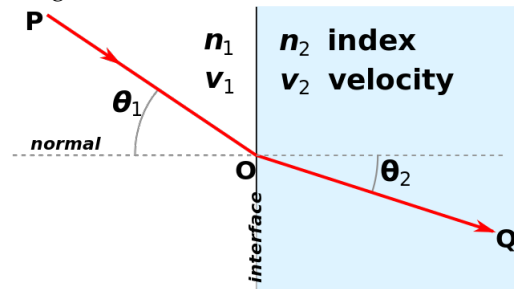
The reflected light in a specular surface is calculated in a different way. The specular ray is casted and ray traced, then the obtained radiance is multiplied by the specular color of the intersected primitive. The reflection direction is the subtraction between the double of dot product between the inverse of the ray direction and the shading normal multiplying by the shading normal, and the inverse of the ray direction.

Figure 15.: Reflections projected on the floor and on the spheres.



Finally, the refracted light in a transmission surface is calculated by using the refractive index of the intersected primitive and the ray direction and shading normal. First, the shading normal is inverted if the origin of the ray was inside a primitive, like a sphere, and if it was not then the refractive index is inverted. Then, it is calculated two auxiliary scalar projections: $\cos\theta_1$ and $\cos\theta_2$. $\cos\theta_1$ is the dot product of the inverse of the shading normal and the ray direction, and $\cos\theta_2$ is the difference of 1 and refractive index squared multiplied by one minus $\cos\theta_1$ squared. Then, if $\cos\theta_2$ is greater than zero, then the direction of the transmission ray is ray direction multiplied with refractive index plus shading normal multiplied by refractive index multiplied $\cos\theta_1$ minus square root of $\cos\theta_2$. Else, the direction of the transmission ray is just ray direction plus shading normal multiplied by the double of $\cos\theta_1$. And, as usual, the transmission ray is traced and its radiance is multiplied by the transmission component of the intersected primitive.

Figure 16.: Refraction of light at the interface of two media of different refractive indices.



The algorithm developed is as following:

```

if (intersected material is diffuse) {
  for each light source
    for each sample
      vectorToLight = lightPosition - intersectionPoint
      cos_N_L = vectorToLight . shadingNormal
      if (cos_N_L > 0) {
        Ray shadowRay(intersectionPoint, vectorToLight, distanceToLight,
                      rayDepth + 1)
        if (!shadowTrace(shadowRay)) rgb += radLight * cos_N_L
      }
    rgb *= kD
  rgb /= #samples
}

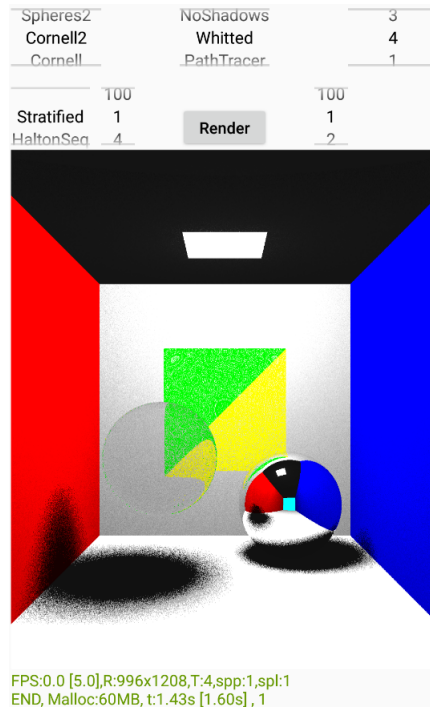
if (intersected material is specular reflective) {
  reflectionDir = (2 * symRayDirection . normal) * normal - symRayDirection
  Ray specularRay(intersectionPoint, reflectionDir, rayDepth + 1)
  rgb += rayTrace (specularRay) * kS
}

if (intersected material is specular refractive) {
  if (shadingNormal . rayDirection > 0) {
    //we are inside the medium
    shadingNormalT = -1 * shadingNormal
    n = 1 / n
  }
  n = 1 / n
  cosTheta1 = -shadingNormalT . rayDirection
  cosTheta2 = 1 - n^2*(1-cosTheta1^2)
  if (cosTheta2 > 0)
    transmissionRay.dir = ((rayDir*n) + (shadingNormalT*(n*cos1 - sqrt(cost2)
    )))
  else
    transmissionRay.dir = (rayDir + shadingNormalT*(cost1 * 2))
  rgb += rayTrace(transmissionRay) * kT
}

```

}

Figure 17.: Whitted shader.

*PathTracer*

Finally, the last shader developed is the canon Path Tracer. Unlike the previous shaders, this one fully simulates both direct and indirect lighting. But, like the previous shader, this algorithm simulates the light reflected on diffuse and specular surfaces, as well as the light refracted on transparent primitives.

The light reflected on diffuse surfaces is divided in two parts: direct lighting and indirect lighting. The direct lighting is calculated in a similar way to the Whitted shader but with the difference that samples are not taken from all sources of light but rather only one. The light source in each sample is chosen randomly. Then the obtained light radiance is multiplied by the Probability Density Function (PDF) in order to approximate the expected value. In this case the PDF is as simple as $1/\#lights$.

Finally, the indirect lighting reflected in diffuse surfaces is calculated in a much more complex way. First it is generated, from the intersected point, a random direction on an unit hemisphere with a PDF proportional to cosine-weighted solid angle ($PDF : p(\Theta) = \cos\theta / \pi$, $x = \cos(2\pi r1)\sqrt{1-r2}$, $y = \sin(2\pi r1)\sqrt{1-r2}$, $z = \sqrt{r2}$). This kind of PDF is one of the

best ways to render images with path tracing that the rendering equation converges to the expected value as fast as possible. Then a rotation matrix is built, where it lets rotate a vector around an arbitrary axis with a given angle.

Figure 18.: Rotation matrix from an arbitrary axis and an angle.

$$R = \begin{bmatrix} \cos \theta + u_x^2 (1 - \cos \theta) & u_x u_y (1 - \cos \theta) - u_z \sin \theta & u_x u_z (1 - \cos \theta) + u_y \sin \theta \\ u_y u_x (1 - \cos \theta) + u_z \sin \theta & \cos \theta + u_y^2 (1 - \cos \theta) & u_y u_z (1 - \cos \theta) - u_x \sin \theta \\ u_z u_x (1 - \cos \theta) - u_y \sin \theta & u_z u_y (1 - \cos \theta) + u_x \sin \theta & \cos \theta + u_z^2 (1 - \cos \theta) \end{bmatrix}$$

Then the proper coordinates in the world view is just: $globalCoordinates = localCoordinates * rotationMatrix$. And the indirect lighting on diffuse surfaces is then the multiplication of the ray traced light radiance with the color of the primitive and π , and divided by the probability of stopping the Russian roulette.

The reflected light in a specular surface and the refracted light are simulated in a similar way to the Whitted algorithm presented previously.

The algorithm developed is as following:

```
if (intersected material is diffuse) {
    for each light
        for each sample
            light = samplerLight.getSample()
            vectorToLight = lightPosition - intersectionPoint
            cos_N_L = vectorToLight . shadingNormal
            if (cos_N_L > 0) {
                Ray shadowRay(intersectionPoint, vectorToLight, distanceToLight,
                               rayDepth + 1)
                if (!shadowTrace(shadowRay)) rgb += radLight * cos_N_L
            }
        }
    rgb *= kD
    rgb *= #lights
    rgb /= #samples

    if (rayDepth <= RAY_DEPTH_MIN || uniform_dist(gen) > finish_probability) {
        local = Generate random direction on unit hemisphere
        proportional to cosine-weighted solid angle

        RotationMatrix = Rotation matrix from axis and angle

        Vector3D up = (0,1,0)
        Vector3D u = intersectionNormal x up
        if (u == 0) u.x = 1
        cosTheta = up . intersectionNormal
        sinTheta = 1 - cosTheta^2
        if (sinTheta < 0) sinTheta *= -1
        sinTheta = sqrt(sinTheta)
```



```

    global = local * rotationMatrix

    Ray secondaryRay (globalX, globalY, globalZ, intersectionPoint, rayDepth +
        1)

    LiD = rayTrace(secondaryRay) * kD * PI

    if (rayDepth > RAY_DEPTH_MIN) LiD /= continue_probability
    if(secondaryRay intersects light) LiD = 0

    rgb += LiD
}

}

if (intersected material is specular reflective) {
    reflectionDir = (2 * symRayDirection . normal) * normal - symRayDirection
    Ray specularRay(intersectionPoint, reflectionDir, rayDepth + 1)
    rgb += rayTrace (specularRay) * kS
}

if (intersected material is specular refractive) {
    if (shadingNormal . rayDirection > 0) {
        //we are inside the medium
        shadingNormalT = -1 * shadingNormal
        n = 1 / n
    }
    n = 1 / n

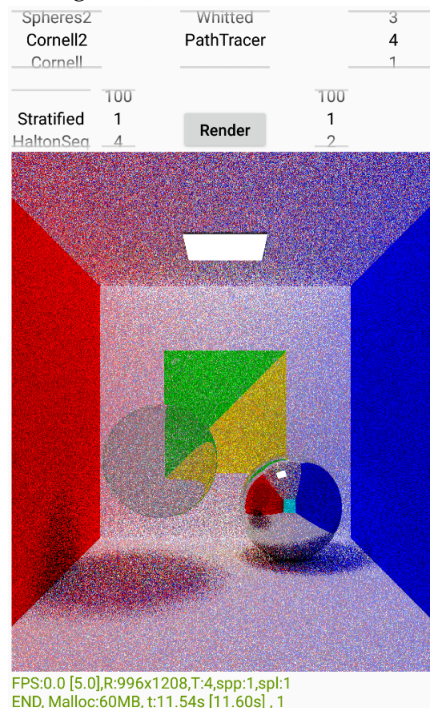
    cosTheta1 = -shadingNormalT . rayDirection
    cosTheta2 = 1 - n^2*(1-cosTheta1^2)

    if (cosTheta2 > 0)
        transmissionRay.dir = ((rayDir*n) + (shadingNormalT*(n*cosTheta1 - sqrt(
            cosTheta2))))
    else
        transmissionRay.dir = (rayDir + shadingNormalT*(cosTheta1 * 2))

    rgb += rayTrace(transmissionRay) * kT
}

```

Figure 19.: PathTracer shader.



3.4.2 Samplers

There were implemented four samplers: Constant, Stratified, HaltonSequence and Random.

All samplers just provide one method for the user to use:

```
float getSample(const unsigned int sample);
```

The *getSample* method receives as parameter the number of the current sampler and returns the the actual sample. An atomic variable *sample* is used to count the current index of the samples.

Constant

This sampler is the simplest because it always returns the same number passed to the constructor.

The algorithm of the *getSample* is just:

```
return value
```

Stratified

This sampler makes each sample at equal distance ($1/\text{domainSize}$) and in ascending order. For example, for a domain size of 4, the samples taken are going to be: 0, 0.25, 0.5 and 0.75.

The algorithm of the *getSample* is then:

```
//atomic operation
current = sample++
if (current >= (domainSize * (sampleParam + 1))) {
    sample--
    return 1
}
task = current - (sampleParam * domainSize)
return task / domainSize
```

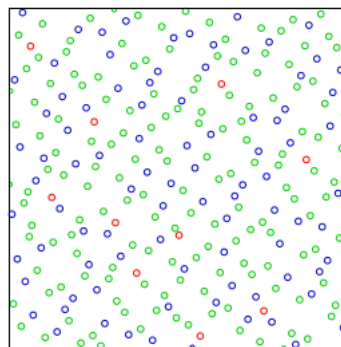
HaltonSequence

As the name implies, this sampler generates the Halton sequence.

Halton sequence is a quasi random number sequence which is a deterministic sequence with low discrepancy.

These sequences are usually good for Rendering Algorithms like Path Tracing because it can make the rendering equation converge faster (with fewer samples).

Figure 20.: Halton sequence in a 2D image plane.



The algorithm of the *getSample* is as following:

```
//atomic operation
current = sample++
if (current >= (domainSize * (sampleParam + 1))) {
    sample--
```

```

    return 1
}
task = current - (sampleParam * domainSize)

f = 1
result = 0
while (task > 0) {
    f = f / base
    result = result + f * (index % base)
    task = floor(index / base)
}
return result

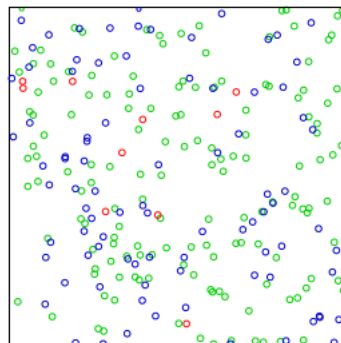
```

Random

This sampler is just a wrapper to call the function `rand()` of the standard C library.

This function is a pseudo random number generator (PRNG), which is an algorithm for generating a sequence of numbers whose properties approximate the properties of sequences of random numbers. Although the PRNG-generated sequence is not truly random, because it is completely determined by an initial value, called the PRNG's seed. These sequences are usually used in simulations that use Monte Carlo methods like the Monte Carlo Ray Tracing.

Figure 21.: Pseudorandom sequence in a 2D image plane.



So the algorithm of the *getSample* is just:

```

return rand() / RAND_MAX

```

3.4.3 Lights

There were implemented two types of light sources: `PointLight` and `AreaLight`. These light sources provide the user two main methods:

```
const Point3D getPosition(void);
bool intersect(Intersection &intersection, const Ray &ray, const Material &)
    const;
```

The *getPosition* method just returns the position of the light source and the *intersect* method determines whether a given *ray* as a parameter intersects this light source and, if it intersects, writes the result to the *intersection* parameter.

PointLight

The `PointLight` is the simplest form of a light because, as the name implies, is just a point of light.

Therefore, the *getPosition* method is very simple because it only returns the position of the light source determined in its constructor:

```
return position;
```

And the *intersect* method is also quite simple because it always returns false. This is because the probability of a ray intersecting a single 3D point in the world is practically nil.

AreaLight

The `AreaLight` implemented has a shape of a triangle. This shape is intended as it allows to generate a random point in a triangle with barycentric coordinates.

A triangle with 3 points: A, B and C. We get vectors AB and AC, being:

```
AB=[Bx-Ax,By-Ay,Bz-Az] and AC=[Cx-Ax,Cy-Ay,Cz-Az].
```

These vectors tell how to get from point A to the other two points in the triangle, by telling us what direction to go and how far. So, with barycentric coordinates $R=1/3$, $S=1/3$ and $T=1/3$, we get the point in the center of the triangle. To generate a random point in the triangle, we have to generate 2 random numbers between 0 and 1 (R and S). Then we have to make sure we stay inside the triangle by checking if they are larger than one:

```

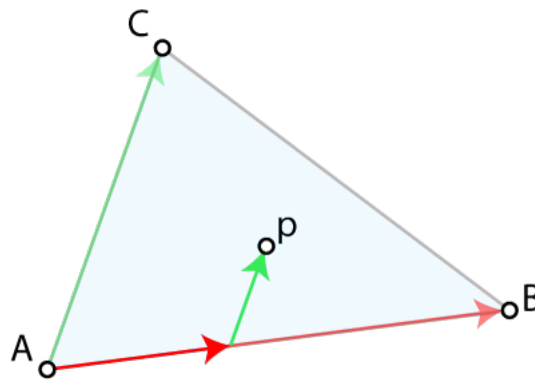
if (R + S >= 1) {
    R = 1 - R
    S = 1 - S
}

```

Finally we can obtain a random point in the triangle by starting at point A, then getting a random percentage along vector AB and a random percentage along vector AC:

```
RandomPointPosition = A + R*AB + S*AC
```

Figure 22.: Calculation of point P by using barycentric coordinates starting at point A and adding a vector AB and a vector AC.



So, the *getPosition* algorithm is as following:

```

R = samplerPointLight.getSample(0)
S = samplerPointLight.getSample(0)
if (R + S >= 1) {
    R = 1 - R
    S = 1 - S
}
x = A.x + R * AB.x + S * AC.x
y = A.y + R * AB.y + S * AC.y
z = A.z + R * AB.z + S * AC.z
return Point3D(x, y, z);

```

And the *intersect* method is equal to the intersection of a ray with a triangle presented earlier.

3.4.4 Cameras

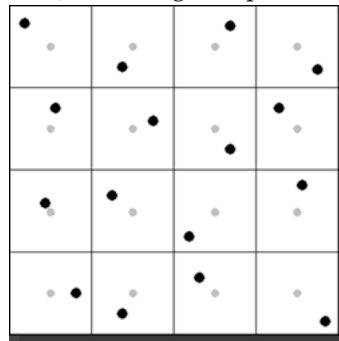
There was implemented one type of Camera: Perspective Camera.

The camera only provides one method for the user to generate a ray from the camera position in direction to the image plane:

```
Ray generateRay(const float u, const float v,
               const float deviationU, const float deviationV) const;
```

The method *generateRay* needs four parameters to create a ray. The *u* and *v* are used to choose the pixel in the image plane. Being *u* the inverse of the index of the pixel in its line, that is, $x/width$, and *v* the inverse of the index of the pixel in its column, that is, $y/height$. In order to allow the reduction of aliasing in the generated images of the scene, the camera also accepts two extra parameters *deviationU* and *deviationV* which are variances inside a pixel. The *deviationU* is a horizontal variance of the pixel, that is, $[-0.5 * pixelWidth, 0.5 * pixelWidth]$ and *deviationV* the variance in the vertical of the pixel $[-0.5 * pixelHeight, 0.5 * pixelHeight]$.

Figure 23.: Jittering in a plane image.

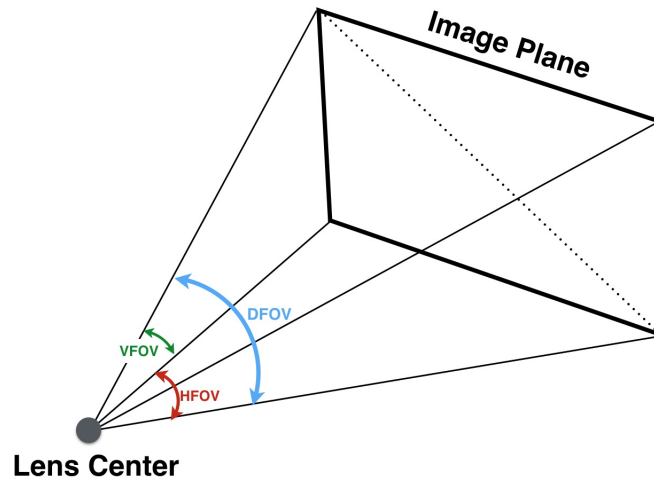


Perspective Camera

With this type of camera we can simulate images being seen by the human eyes.

To obtain an image plane with perspective is necessary to have a Field of View. In order to accept any resolution of the image plane, we have to divide the field of view in 2 parts: horizontal and vertical. This way, we can obtain the aspect ratio of the image plane we want.

Figure 24.: Perspective camera with hFov, vFov and dFov.



The algorithm to generate a ray from the camera is very simple.

...

3.5 ANDROID SPECIFICS AND CHALLENGES

3.5.1 Specifics

Before developing the ray tracer to Android, it is necessary to understand how an Android application works.

A typical Android application is programmed in Java programming language. And it usually needs to communicate with an User Interface which also is programmed in Java. The code is compiled with Android Software Development Kit (SDK) along with any data and resource files into an Android package (APK). But, in order to avoid using the Java Emulator in our code and program it in native code, it is necessary to use Android Native Development Kit (NDK). Unfortunately, the Android Studio IDE doesn't provide any support like libraries like Qt that facilitates the build of a User Interface in native code. So, in order to obtain the best performance possible in a mobile device, the User Interface was programmed in Java and the ray tracer library and components were programmed in C++.

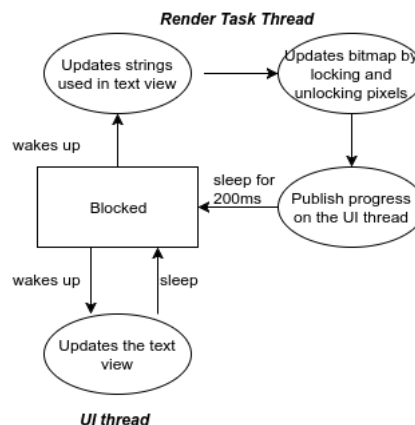
3.5.2 User Interface

The Android User Interface is programmed in Java and only one thread can refresh the User Interface (UI thread).

There are only 2 goals about the User Interface: should be as simple as possible and should be able to allow progressive ray tracing (refresh the image while it is being rendered).

In order to allow progressive ray tracing, it was used a pool of 1 thread called Render Task thread that every 200 ms wakes up the thread and updates the strings used in the text view and updates the bitmap of the rendering image by locking and unlocking the pixels. Locking pixels means that will be ensured that the memory for the pixels will not move until the pixels is unlocked. Before it finishes, it publishes the progress on the UI thread. Then the UI thread wakes up and updates the text view.

Figure 25.: Execution flow of UI thread and Render Task thread.



3.5.3 Challenges

Developing applications for mobile devices have different challenges compared with the traditional personal computer hardware.

The Android User Interface has some particularities like only one thread can modify the UI (UI thread).

The memory size is typically lower, the CPU microarchitecture is different and also the Operating System (OS) is shaped for the mobile world, making a lot of restrictions in the performance in order to save battery. The amount of main memory available for the applications can also be affected by the OS.

Other challenges are related with the communication mechanism between the SDK and the NDK, because two different languages need to “communicate” in runtime (GUI in Java

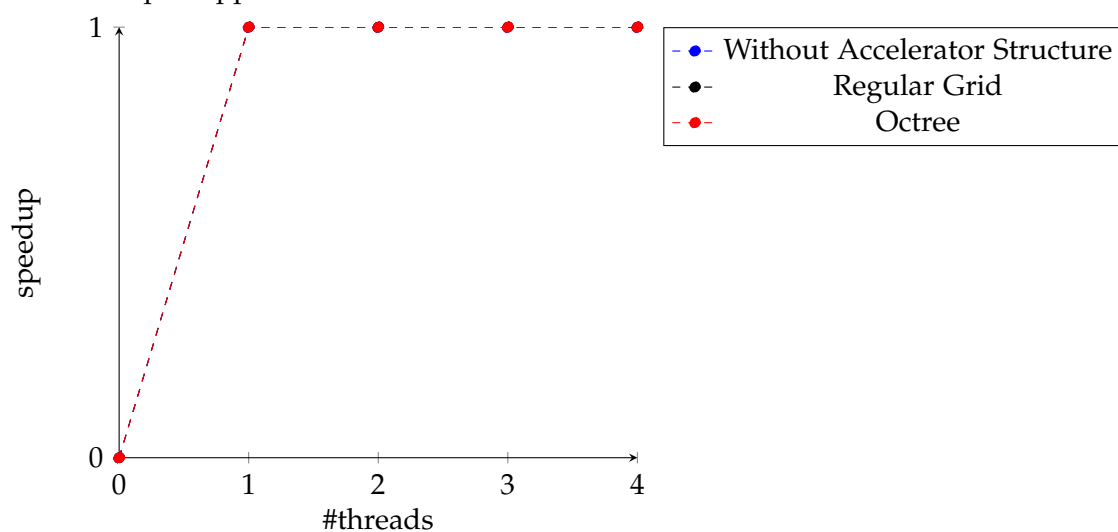
and C++ for the library). This involves learning how to use the Java Native Interface (JNI), so that both can “communicate” with each other.

Because ray tracing may involve rendering complex scenes, putting all this information in the main memory may not be possible, and so this memory management can be a worthy challenge.

DEMONSTRATION: GLOBAL ILLUMINATION

4.1 RESULTS OBTAINED

The developed application ...



4.2 COMPARISON WITH ANDROID CPU RAYTRACER (DAHLQUIST)

Comparison ...

CONCLUSION & FUTURE WORK

5.1 CONCLUSIONS

The constant evolution of technology allowed to leverage and massify the mobile devices. With more and increasingly powerful mobile devices, it is possible to perform more and more complex and useful tasks in them. This is a huge market where the programmers can develop their applications to and where the development time can be a huge factor in their career success.

But as noted in this pre-dissertation report, there is clearly a lack of well documented rendering libraries for mobile systems. There is then the need to change this reality, since more and more the Internet of Things is more present each passing year, because there are increasingly powerful mobile systems.

As it is possible to address a huge number of challenges while developing the ray tracer, this pre-dissertation identified some of the strategic decisions to be performed in this dissertation project and its related challenges that may arise during the development.

5.2 FUTURE WORK

With respect to future work, it should be the development of the library for Android and the analysis of possibilities and challenges that may arise. Upon completion of the development process, besides writing the dissertation and the article, it is expected to provide a demo application in order to illustrate the functionalities and performance that the library will offer.

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