

# RStan Codes

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*29/08/19*

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# 1 Normal distribution without covariates in Stan

$Y \sim N(\mu, \sigma^2)$ . Therefore,  $\theta = (\mu, \sigma^2)^\top$ . Here, we do not specify the prior distribution for each parameter

```
rm(list = ls())
load("normal_dist_fit1.RData")
#ajuste<- lm(stack.loss~1, data=stackloss)
```

## 1.1 Classic inference: MLE for $\mu$

```
summary(ajuste)$coef[,1]#mean(stackloss$stack.loss)
```

```
## [1] 17.52381
```

## 1.2 Classic inference: MLE for $\sigma$

```
summary(ajuste)$sigma#sd(stackloss$stack.loss)
```

```
## [1] 10.17162
```

## 1.3 Bayesian Inference: Stan code (default prior)

```
normal_dist_example<- '
data {
  int<lower=0> N;
  vector[N] y;
}
parameters {
  //defines the sampling space
  real mu;
  real<lower=0> sigma;
}
model {
  //defines the log-likelihood
  y ~ normal(mu, sigma);
}
'
```

```
normal_dist_fit <- stan(model_code = normal_dist_example,
init=list(list(mu=-500,sigma=3),
          list(mu=500,sigma=2),
          list(mu=0,sigma=1)),
data = list(N = dim(stackloss)[1],
            y = stackloss$stack.loss),
chain = 3,
iter = 300,#11000
warmup = 10,#1000
thin = 1,#10
refresh = 0,seed=123)#refresh=-1

#save.image(file = "normal_dist_fit.RData")
```

## 1.4 MCMC diagnostics using the bayesplot package

```
parametros<- c("mu", "sigma")

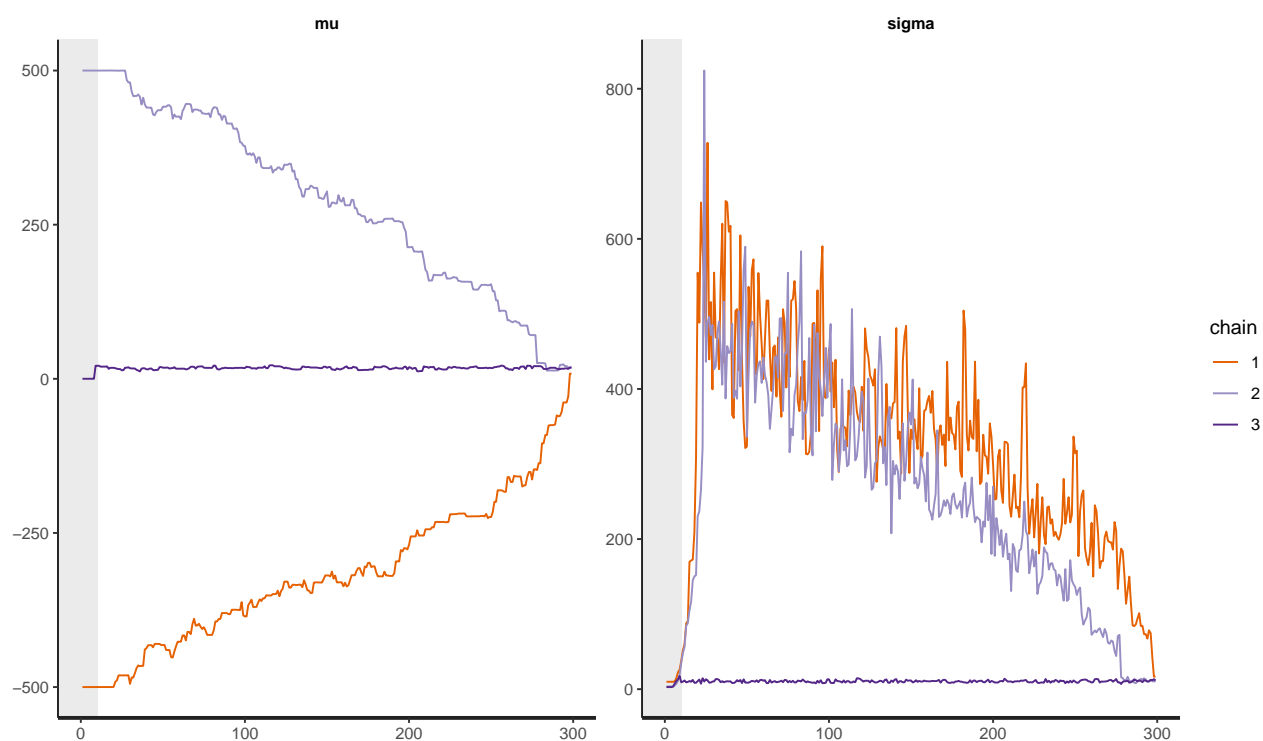
CI_theta <- summary(normal_dist_fit,
                    pars = parametros,
                    probs = c(0.025, 0.975))$summary

print(CI_theta)
```

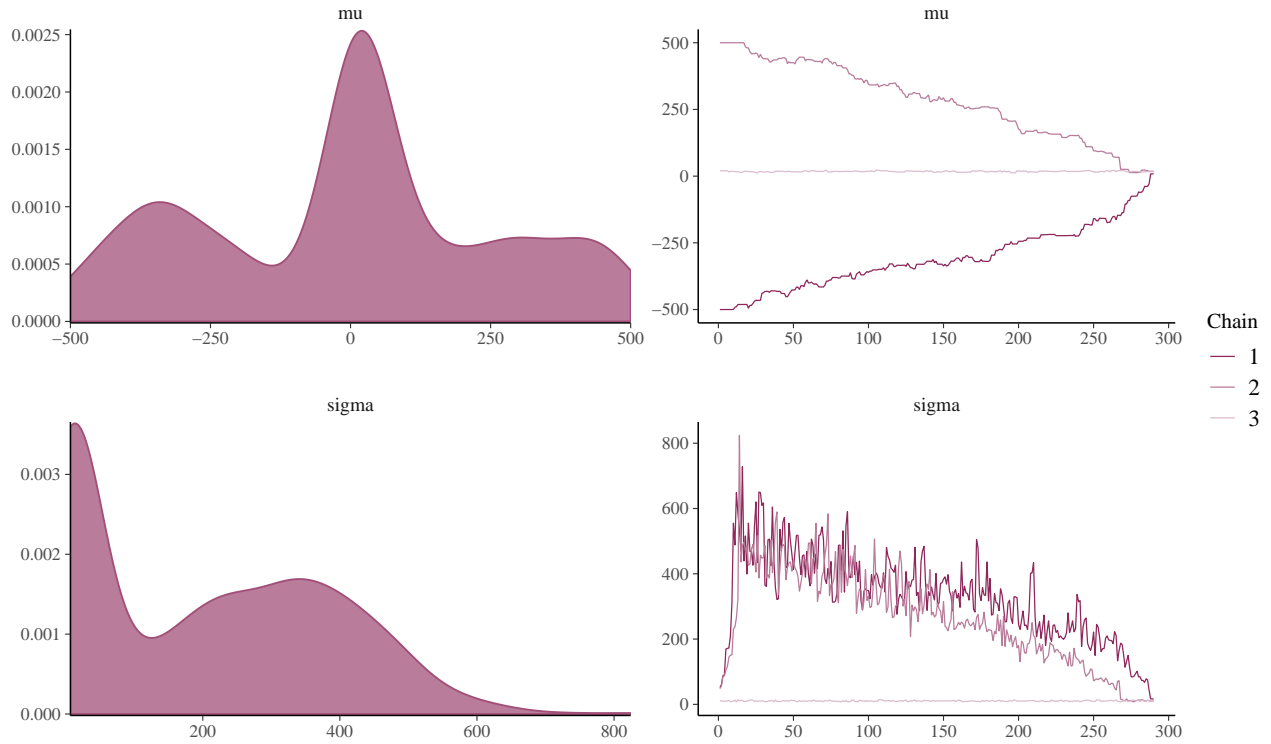
```
##           mean se_mean      sd      2.5%   97.5%   n_eff   Rhat
## mu      -3.494559 193.1230 263.4258 -478.22140 459.4751 1.860580 4.707568
## sigma  201.145878 108.8411 179.5661   8.46037 542.6115 2.721845 2.298128
```

```
mcmc_cadeia <- as.array(normal_dist_fit)
```

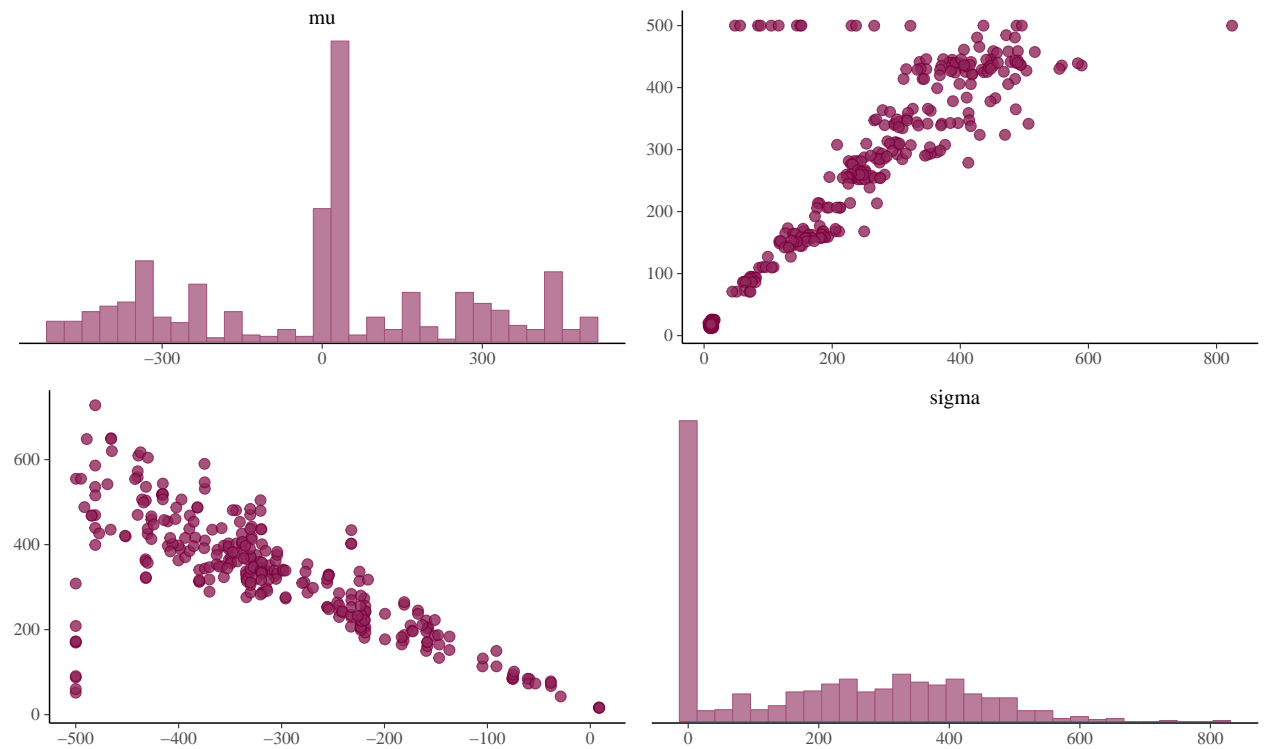
```
traceplot(normal_dist_fit, pars = parametros, inc_warmup = TRUE)
```



```
color_scheme_set("pink")
mcmc_combo(mcmc_cadeia, pars = parametros, n_warmup=0)
```



```
mcmc_pairs(mcmc_cadeia, pars = parametros)
```



## 2 Normal distribution without covariates in Stan

$Y \sim N(\mu, \sigma^2)$ . Therefore,  $\theta = (\mu, \sigma^2)^\top$ . Here, we specify the prior distribution for each parameter.

```
rm(list = ls())
load("normal_dist_fit2.RData")
#ajuste<- lm(stack.loss~1, data=stackloss)
```

## 2.1 Classic inference: MLE for $\mu$

```
summary(ajuste)$coef[,1]#mean(stackloss$stack.loss)

## [1] 17.52381
```

## 2.2 Classic inference: MLE for $\sigma$

```
summary(ajuste)$sigma#sd(stackloss$stack.loss)

## [1] 10.17162
```

## 2.3 Bayesian Inference: Stan code (specific prior)

```
normal_dist_example<- '
data {
  int<lower=0> N;
  vector[N] y;
}
parameters {
  real mu;
  real<lower=0> sigma;
}
model {
  y ~ normal(mu, sigma); //defines the log-likelihood
  mu~ normal(0,1e6); //defines Prior for mu
  sigma ~ student_t(3,0,1); //defines Prior sigma
}
'
```

```
normal_dist_fit <- stan(model_code = normal_dist_example,
data = list(N = dim(stackloss)[1],
            y = stackloss$stack.loss),
            chain = 3,
            iter = 11000,
            warmup = 1000,
            thin = 10,
            refresh = 0)#refresh=-1
#save.image(file = "normal_dist_fit2.RData")
```

## 2.4 MCMC diagnostics using the bayesplot package

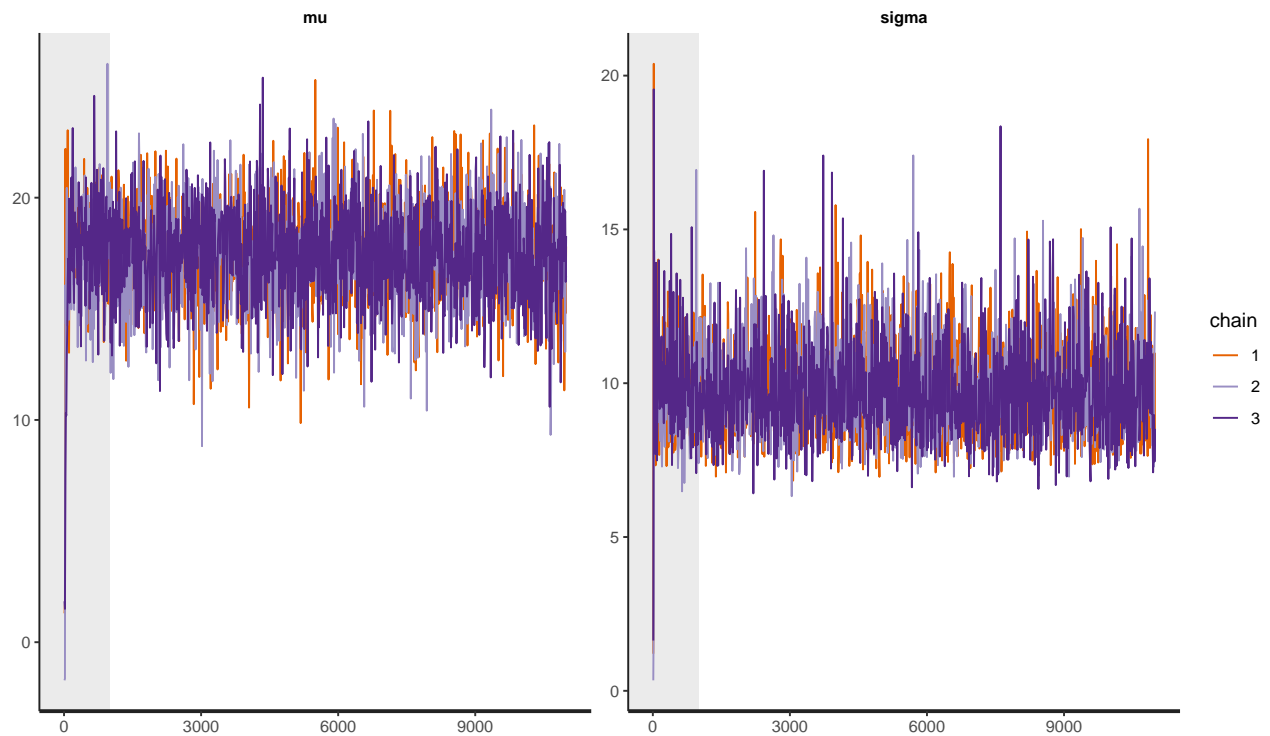
```
parametros<- c("mu", "sigma")
```

```
CI_theta <- summary(normal_dist_fit,
                    pars = parametros,
                    probs = c(0.025, 0.975))$summary
print(CI_theta)
```

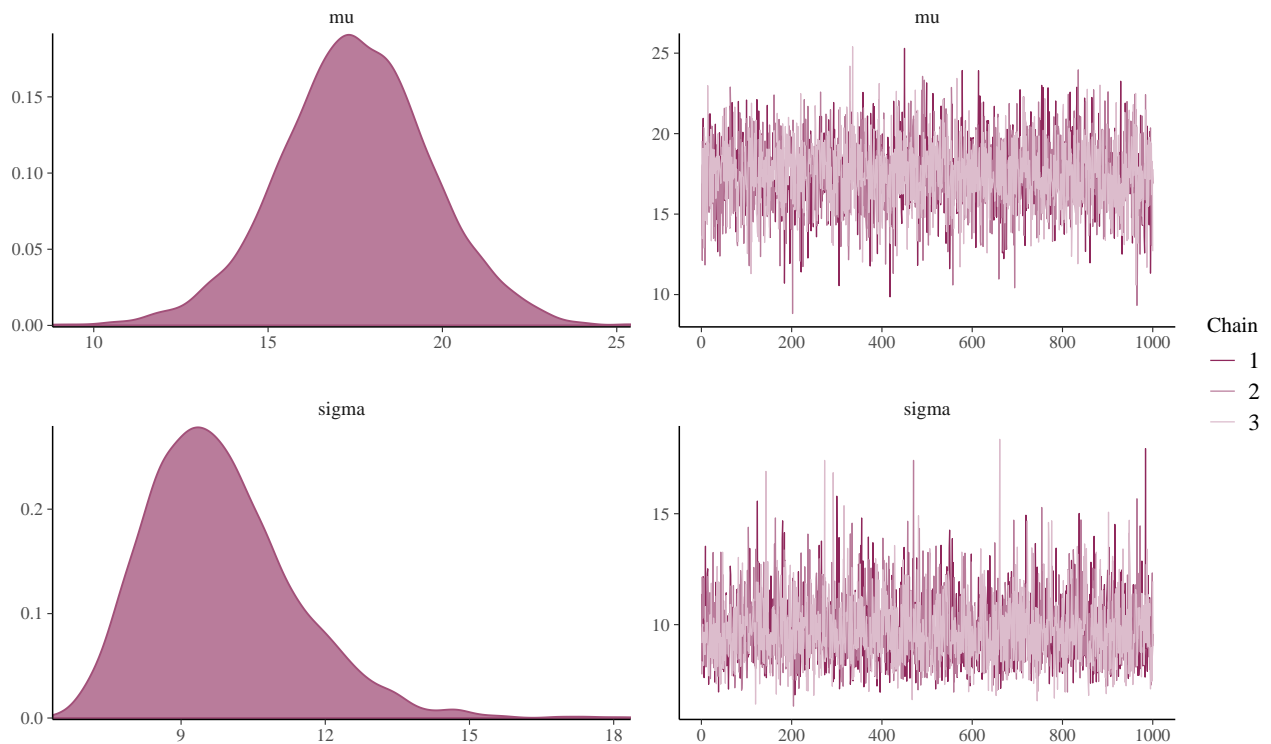
```
##           mean    se_mean      sd    2.5%   97.5%   n_eff    Rhat
## mu      17.503207 0.03946205 2.150759 13.183245 21.80289 2970.463 1.0001178
## sigma   9.821392 0.02801285 1.527582  7.404955 13.26666 2973.684 0.9997358
```

```
mcmc_cadeia <- as.array(normal_dist_fit)
```

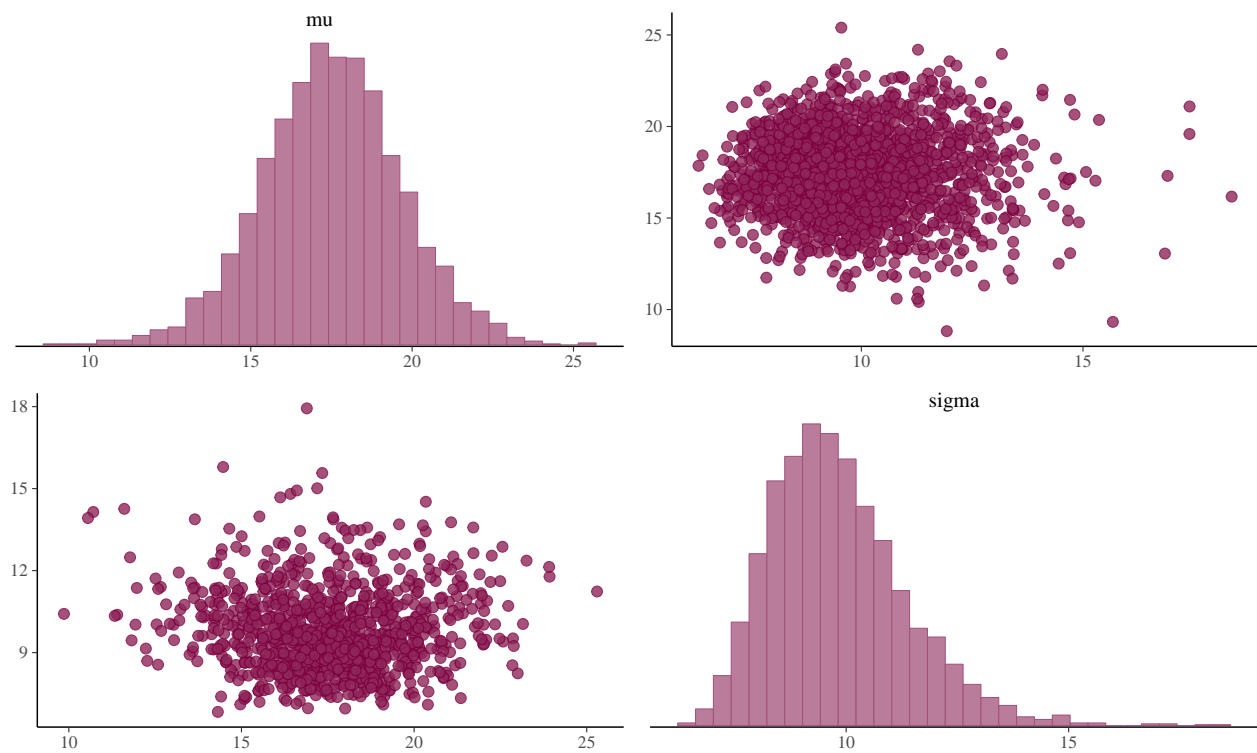
```
traceplot(normal_dist_fit, pars = parametros, inc_warmup = TRUE)
```



```
color_scheme_set("pink")
mcmc_combo(mcmc_cadeia, pars = parametros, n_warmup=0)
```



```
mcmc_pairs(mcmc_cadeia, pars = parametros)
```



### 3 Normal Linear Model

$$stackloss_i = \beta_1 + \beta_2 * AirFlow_i + \varepsilon_i$$

with  $\varepsilon_i \sim N(0, \sigma^2)$ . Therefore  $\theta = (\beta_1, \beta_2, \sigma^2)^\top$ . Here, we do not specify the prior distribution for each parameter.

### 3.1 Classic inference: MLE for $\beta$

```
rm(list = ls())
ajuste<- lm(stack.loss~Air.Flow, data=stackloss)
load("lm_fit1.RData")
```

### 3.2 Classic inference: MLE for $\beta$

```
summary(ajuste)$coef[,1]
```

```
## (Intercept)    Air.Flow
## -44.132025    1.020309
```

### 3.3 Classic inference: MLE for $\sigma$

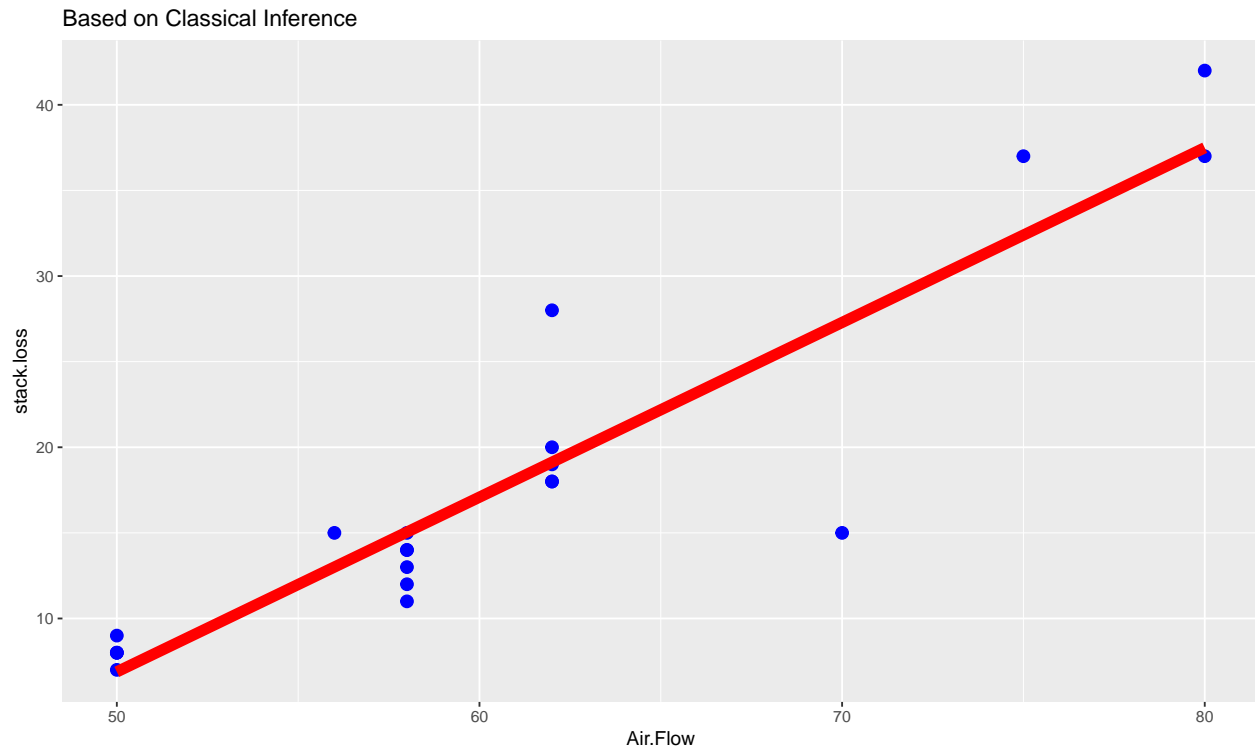
```
summary(ajuste)$sigma#sd(stackloss$stack.loss)
```

```
## [1] 4.098242
```

#### 3.3.1 Fitted curve

```
ggplot(stackloss, aes(Air.Flow, stack.loss))+geom_point(col="blue", size=3)+
  geom_smooth(method="lm", col="red", se=FALSE, size=3)+
  ggtitle("Based on Classical Inference")
```





### 3.4 Bayesian Inference: Stan code

```
lm_example<- '
data {
  int<lower=0> N;
  vector[N] x;
  vector[N] y;
}
parameters {
  real beta1;
  real beta2;
  real<lower=0> sigma;
}
model {
  y ~ normal(beta1+beta2*x, sigma);
}
'

lm_fit <- stan(model_code = lm_example,
data = list(N = dim(stackloss)[1],
            x = stackloss$Air.Flow,
y = stackloss$stack.loss),
            chain = 3,
            iter = 11000,
            warmup = 1000,
            thin = 10,
            refresh=0)
#save.image(file = "lm_fit1.RData")
```

### 3.5 MCMC diagnostics using the bayesplot package

```
parametros<- c(paste('beta',1:2, sep=""), 'sigma')

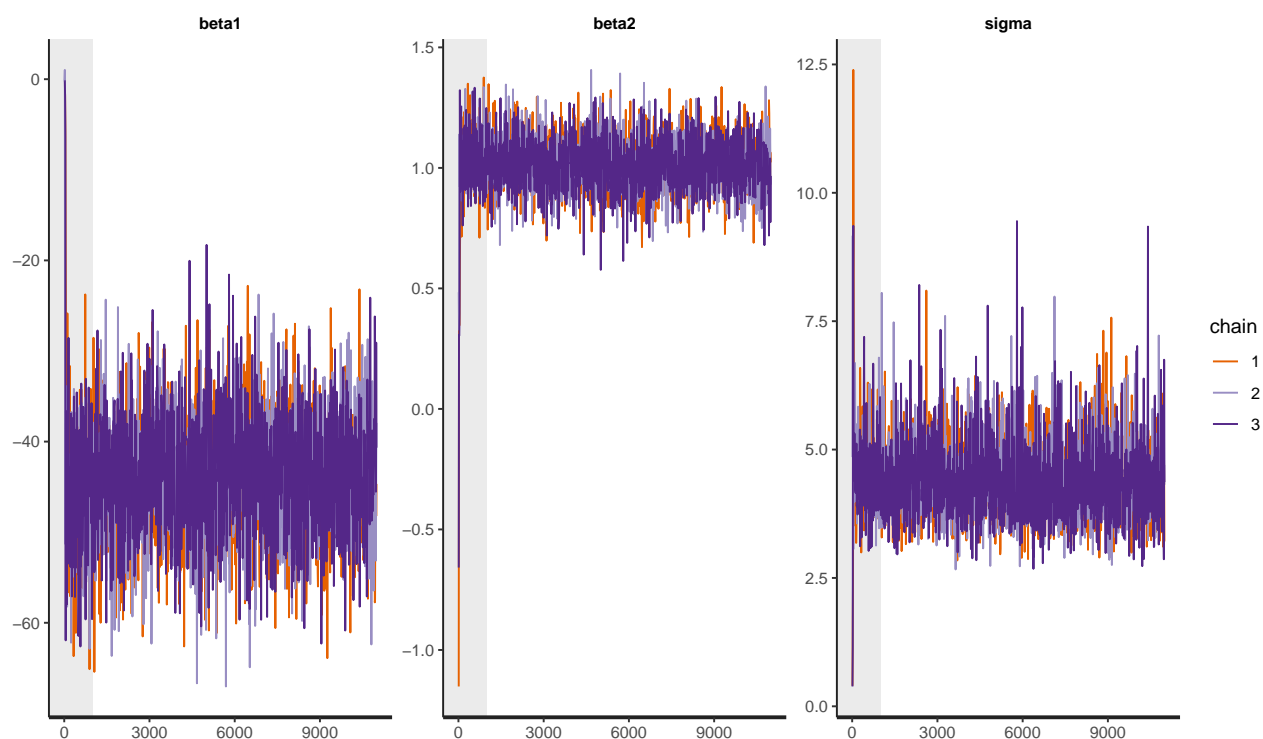
CI_theta <- summary(lm_fit,
                    pars = parametros,
                    probs = c(0.025, 0.975))$summary

print(CI_theta)
```

```
##           mean      se_mean      sd      2.5%      97.5%    n_eff
## beta1 -43.847882 0.123731167 6.5662771 -56.8302195 -30.913163 2816.308
## beta2  1.015100 0.002019555 0.1074735  0.7983867  1.229148 2831.987
## sigma  4.393619 0.014107408 0.7696754  3.1979503  6.144547 2976.602
##           Rhat
## beta1 1.000541
## beta2 1.000703
## sigma 1.000270
```

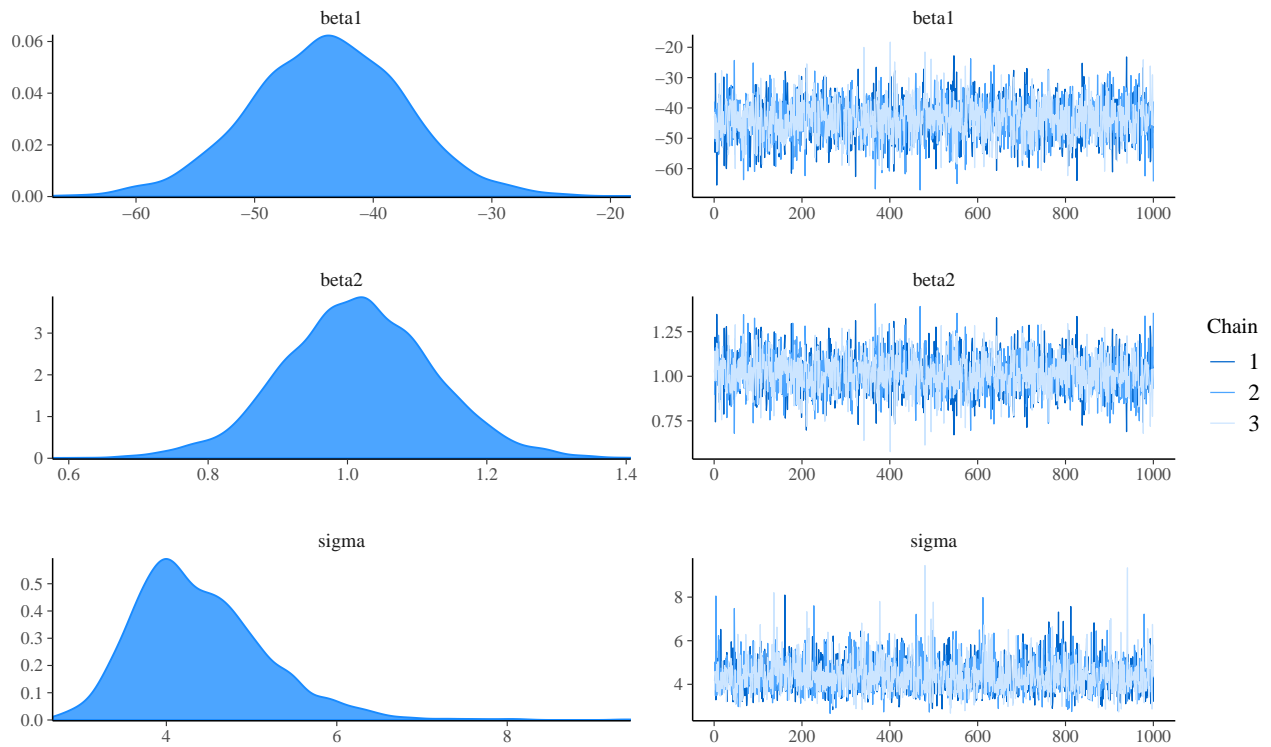
```
mcmc_cadeia <- as.array(lm_fit)
```

```
traceplot(lm_fit, pars = parametros, inc_warmup = TRUE)
```

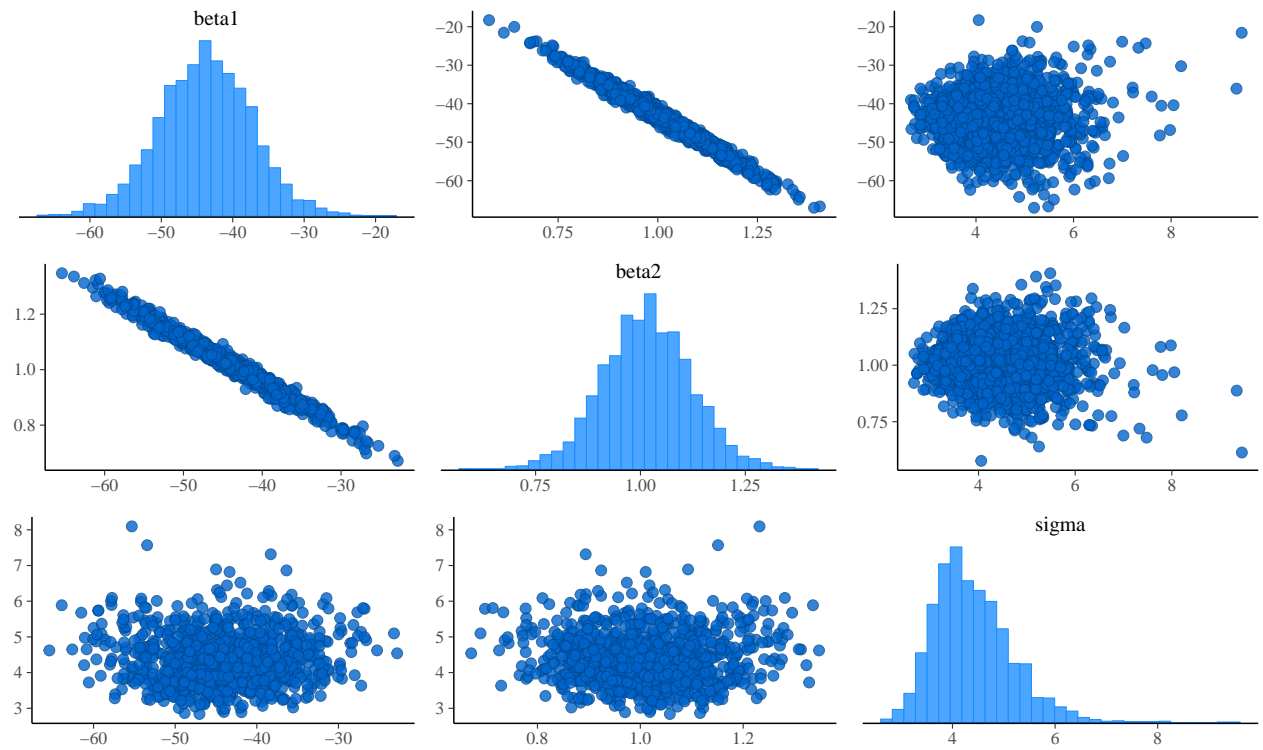


```
color_scheme_set("brightblue")
```

```
mcmc_combo(mcmc_cadeia,pars = parametros,n_warmup=0)
```



```
mcmc_pairs(mcmc_cadeia, pars = parametros)
```



### 3.5.1 Fitted curve

```

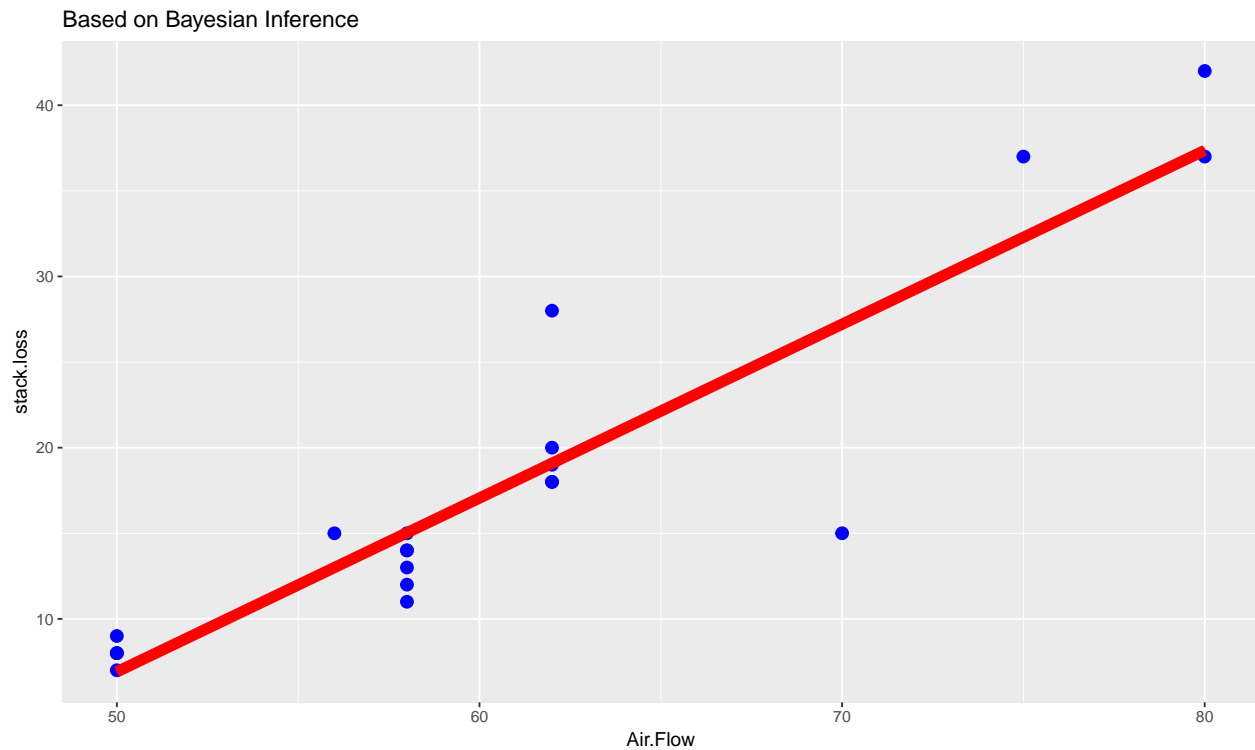
LM.function<- function(x,beta1, beta2){
  beta1+beta2*x
}

parametros<- c(paste('beta',1:2, sep=""), 'sigma')

CI_theta <- summary(lm_fit,
                    pars = parametros,
                    probs = c(0.025, 0.975))$summary

ggplot(stackloss, aes(Air.Flow,stack.loss))+geom_point(col="blue",size=3)+
  geom_smooth(method="lm", col="red", se=FALSE)+
  ggtitle("Based on Bayesian Inference")+
  stat_function(data=stackloss,aes(x=Air.Flow),fun = LM.function,
args = list(beta1=CI_theta[1,1],
            beta2=CI_theta[2,1]),
col="red", size=3)

```



## 4 Logistic Regression

Binomial response with logit link function. Here, we do not specify the prior distribution for each parameter.

```

rm(list = ls())
load("logistic_fit1.RData")

```

## 4.1 Classic inference for $\beta$

```
fitLogistic$coefficients
```

```
## (Intercept)      lDose  
##   -60.74013     34.28593
```

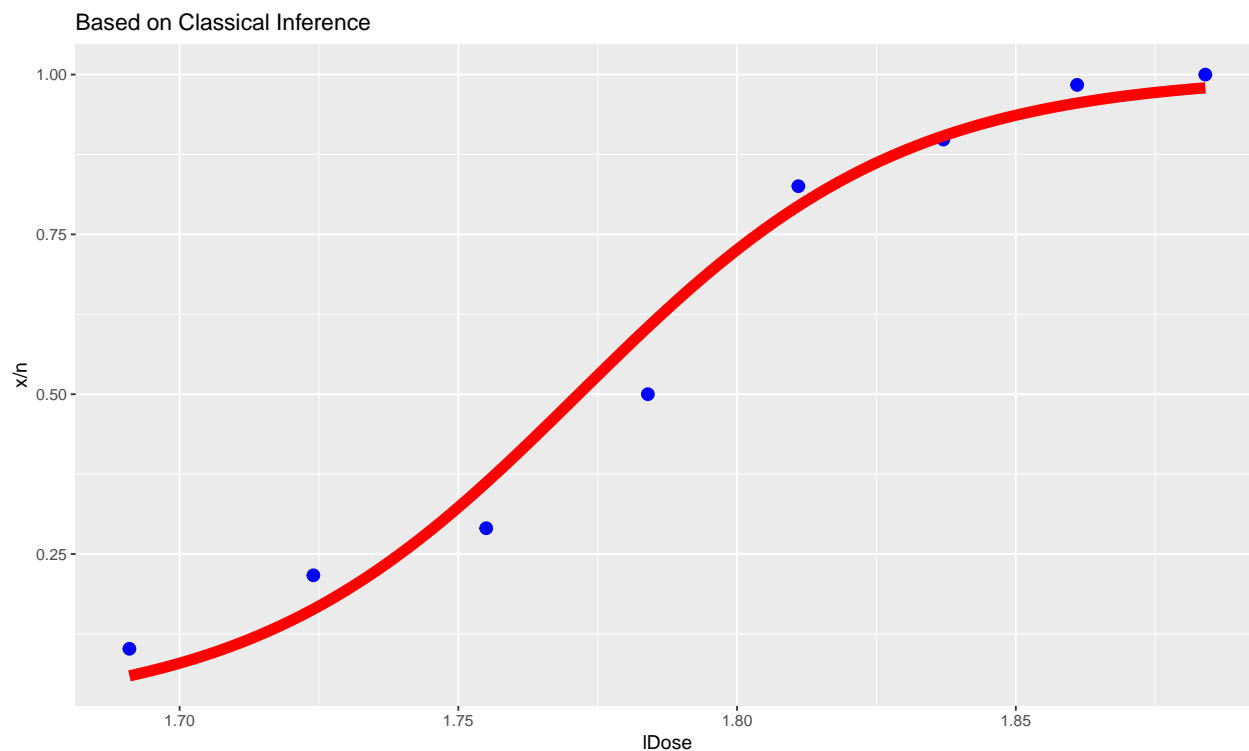
## 4.2 Predicted values for probabilities

```
fitLogistic$fitted.values
```

```
##           1           2           3           4           5           6  
## 0.05937747 0.16366723 0.36162283 0.60490961 0.79440490 0.90405532  
##           7           8  
## 0.95546748 0.97925643
```

## 4.3 Fitted curve based on Classical Inference

```
Logit_prob<-function(x,beta1, beta2){  
  eta<- beta1+beta2*x  
  exp(eta)/(1+exp(eta))  
}  
  
ggplot(beetleDat, aes(lDose,x/n))+geom_point(col="blue",size=3)+  
stat_function(data=beetleDat,aes(x=lDose),  
fun = Logit_prob,  
args = list(beta1=coef(fitLogistic)[1], beta2=coef(fitLogistic)[2]),  
col="red", size=3)+  
ggtitle("Based on Classical Inference")
```



#### 4.4 Bayesian Inference: Stan code

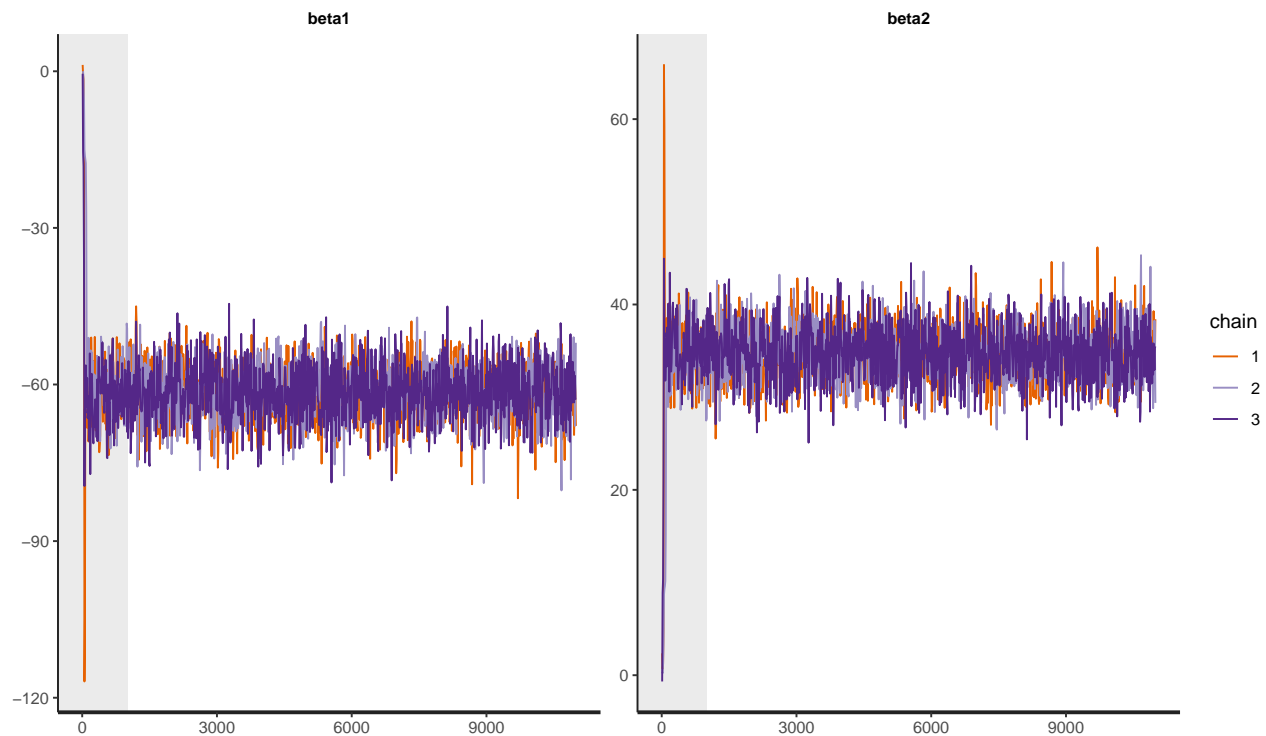
```
logistic_example<- '
data {
  int<lower=0> N;
  vector[N] x;      // lDose
  int<lower=0> y[N]; // Counts
  int<lower=0> n[N]; // Binomial Totals
}
parameters {
  real beta1;
  real beta2;
}
transformed parameters {
  // Probability transformation from linear predictor
  real exp_eta[N];
  real<lower=0, upper=1> prob[N];
  for (i in 1:N) {
    exp_eta[i] = exp(beta1 + beta2*x[i]);
    prob[i] = exp_eta[i]/(exp_eta[i] + 1);
  }
}
model {
  y ~ binomial_logit(n, beta1 + beta2 * x);
}
'
```

```
logistic_fit <- stan(model_code = logistic_example,
  data = list(N = dim(beetleDat)[1],
    n = beetleDat$n,
    x = beetleDat$lDose,
    y = beetleDat$x),
  chain = 3,
  iter = 11000,
  warmup = 1000,
  thin = 10,
  refresh=0)

#save.image(file = "logistic_fit1.RData")
```

## 4.5 MCMC diagnostics using the bayesplot package

```
parametros<- c(paste('beta',1:2, sep=""))
traceplot(logistic_fit, pars = parametros, inc_warmup = TRUE)
```

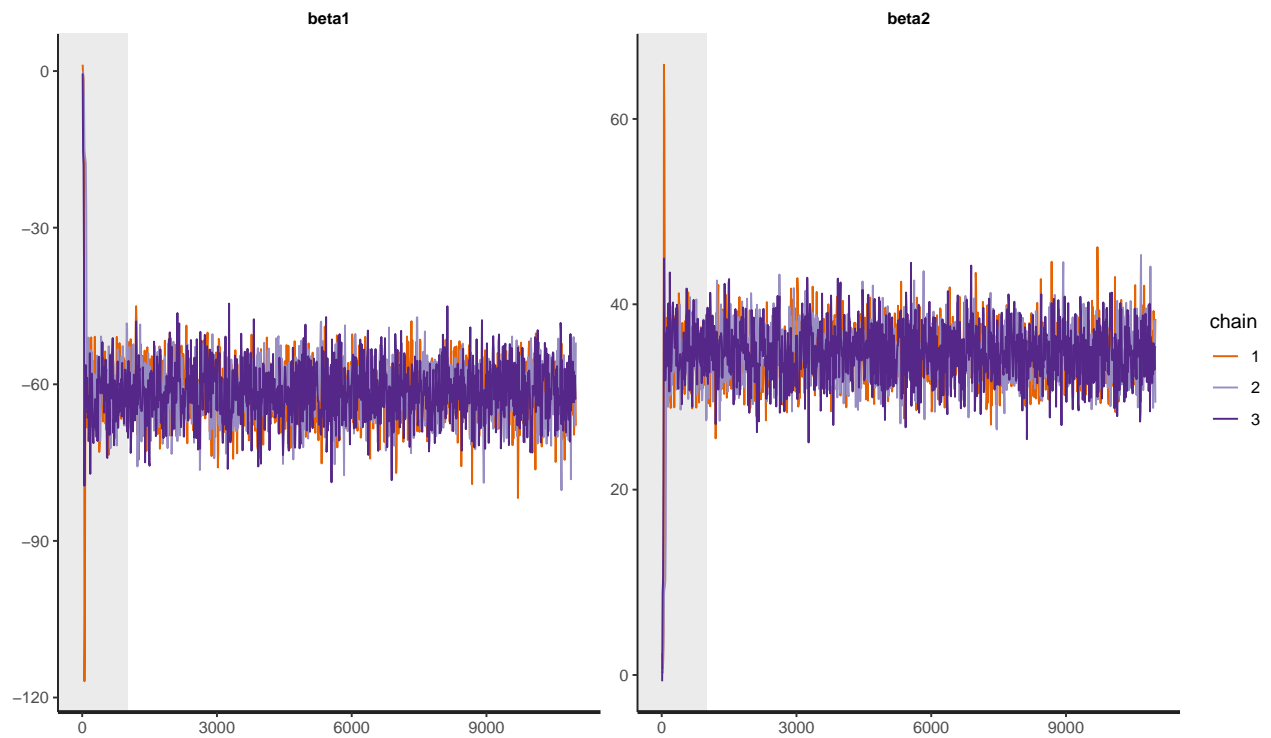


```
CI_theta <- summary(logistic_fit,
  pars = parametros,
  probs = c(0.025, 0.975))$summary
print(CI_theta)
```

```
##           mean  se_mean      sd   2.5%   97.5%  n_eff    Rhat
## beta1 -61.37130 0.1066553 5.247504 -72.01086 -51.42912 2420.699 0.9997729
## beta2  34.64121 0.0599260 2.949725  29.07175  40.58387 2422.883 0.9997907
```

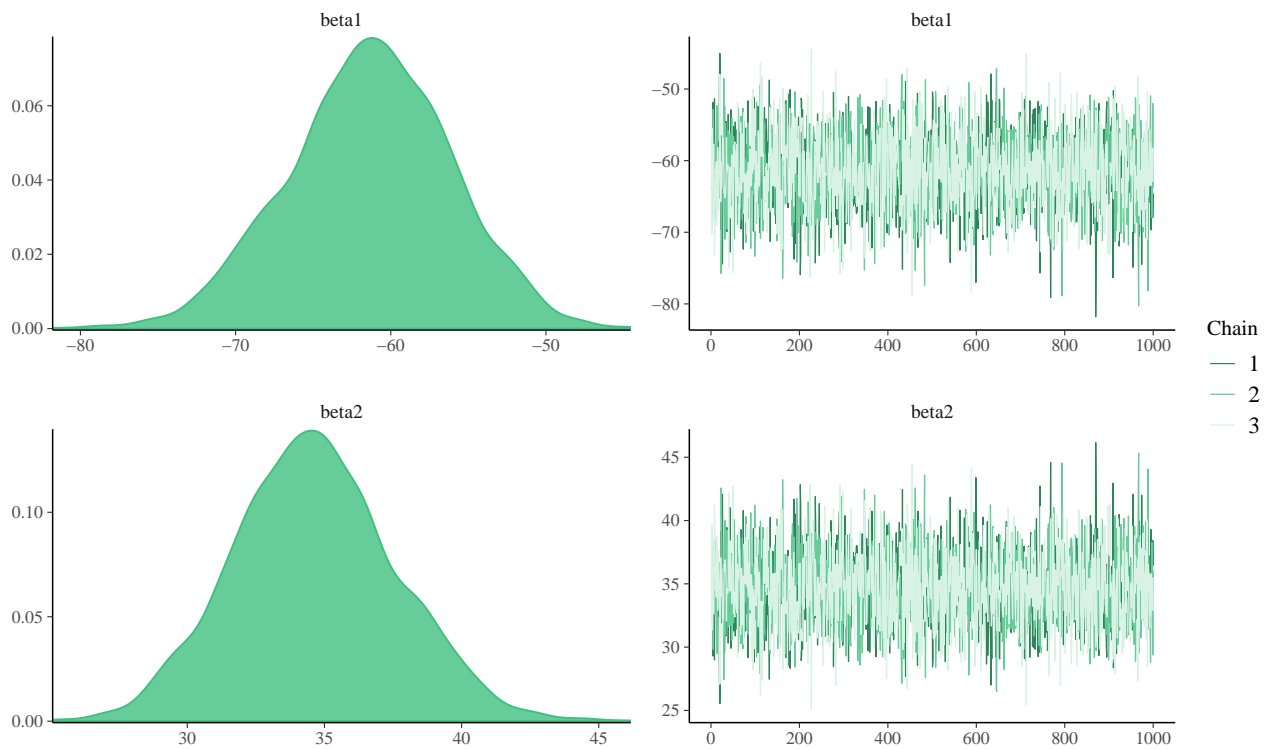
```
mcmc_cadeia <- as.array(logistic_fit)
```

```
traceplot(logistic_fit, pars = parametros, inc_warmup = TRUE)
```



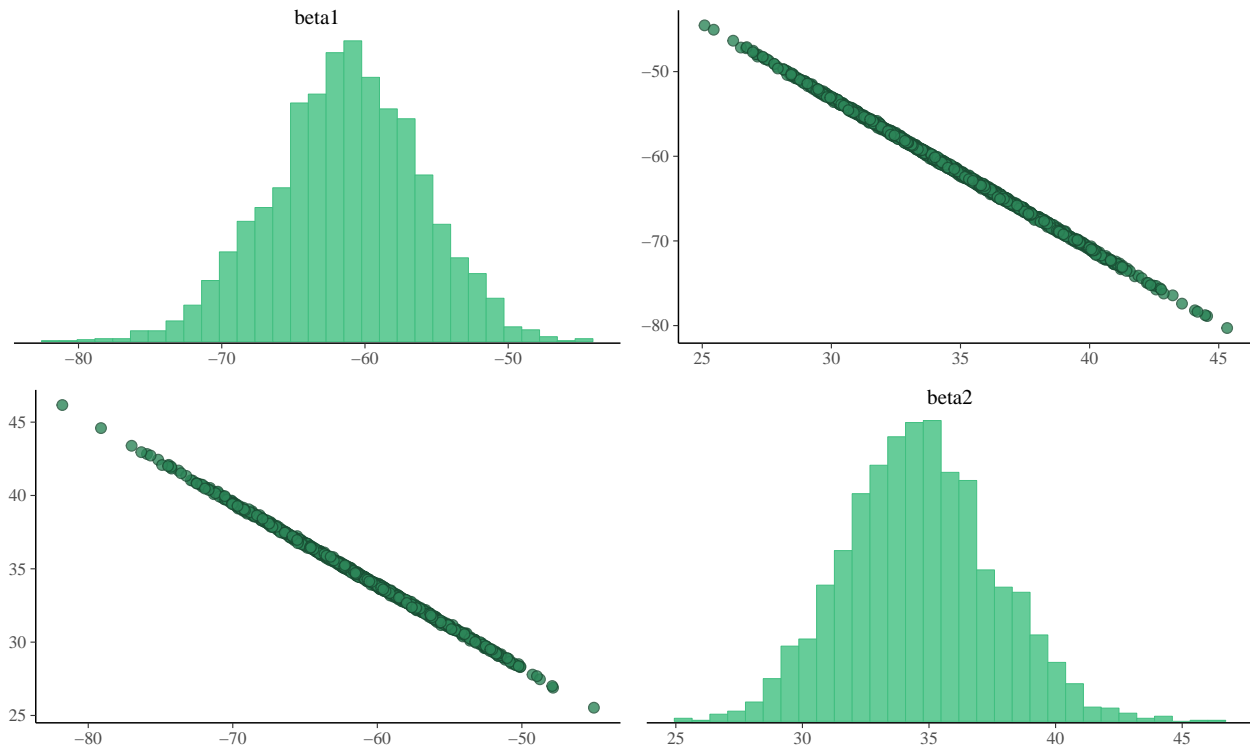
```
color_scheme_set("green")
```

```
mcmc_combo(mcmc_cadeia, pars = parametros, n_warmup=0)
```





```
mcmc_pairs(mcmc_cadeia,pars = parametros)
```



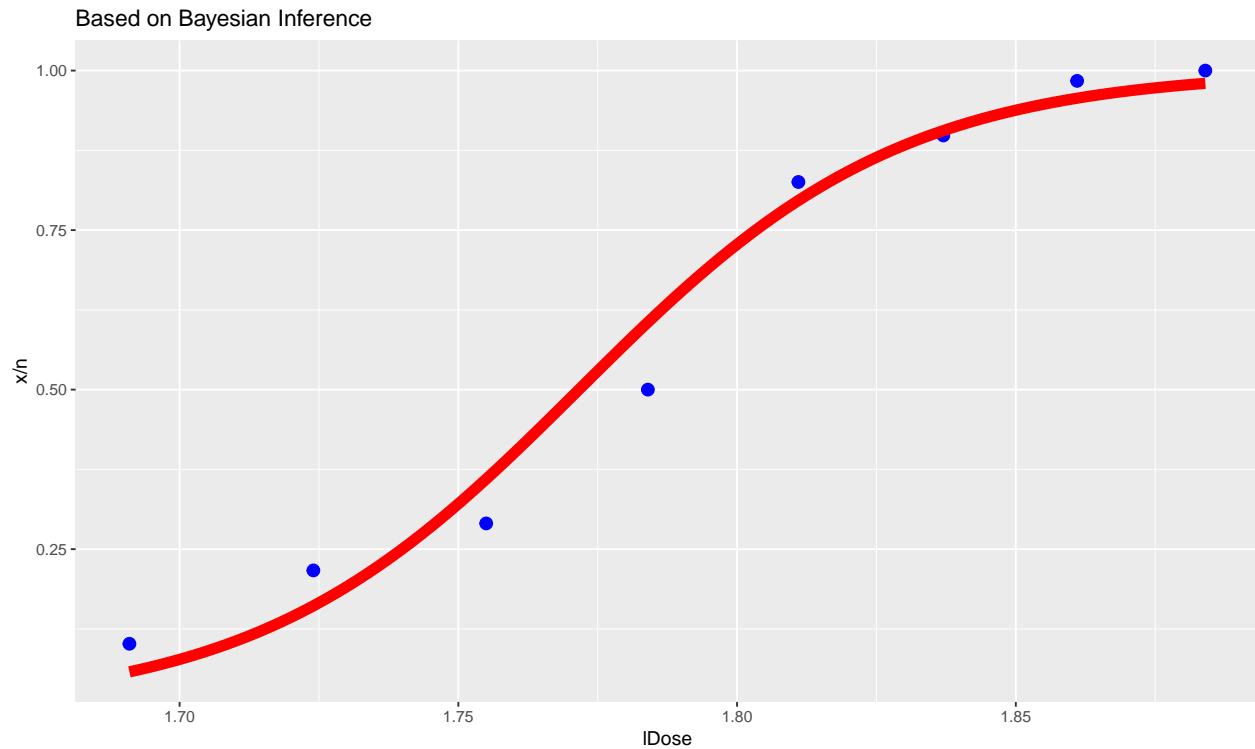
<https://www.youtube.com/watch?v=uSjsJg8fcwY>

## 4.6 Fitted curve based on Bayesian Inference

```
Logit_prob<-function(x,beta1, beta2){
  eta<- beta1+beta2*x
  exp(eta)/(1+exp(eta))
}

parametros<- paste('beta',1:2, sep=" ")
CI_theta <- summary(logistic_fit,
  pars = parametros,
  probs = c(0.025, 0.975))$summary

ggplot(beetleDat, aes(lDose,x/n))+geom_point(col="blue",size=3)+
  ggtitle("Based on Bayesian Inference")+
  stat_function(data=beetleDat,aes(x=lDose),
    fun = Logit_prob,
    args = list(beta1=CI_theta[1,1], beta2=CI_theta[2,1]),
    col="red", size=3)
```



## 5 Von Bertalanffy

```
rm(list=ls())
load("modelo_Von_Bertalanffy.RData")
#set.seed(123)
#dados.amostra<- dados[sample(x=dim(dados)[1], size=1000),]
```

### 5.1 Classic inference for $\beta$

```
LVB<-function(x,beta1, beta2, beta3){
  beta1*(1-exp(-beta2*(x-beta3)))
}

ajuste_LVB <- nls(Length ~ LVB(Age, beta1, beta2, beta3),
start = list(beta1 = max(dados.amostra$Length),
              beta2 = 0.5,
              beta3= 0),
data = dados.amostra)
coef(ajuste_LVB)

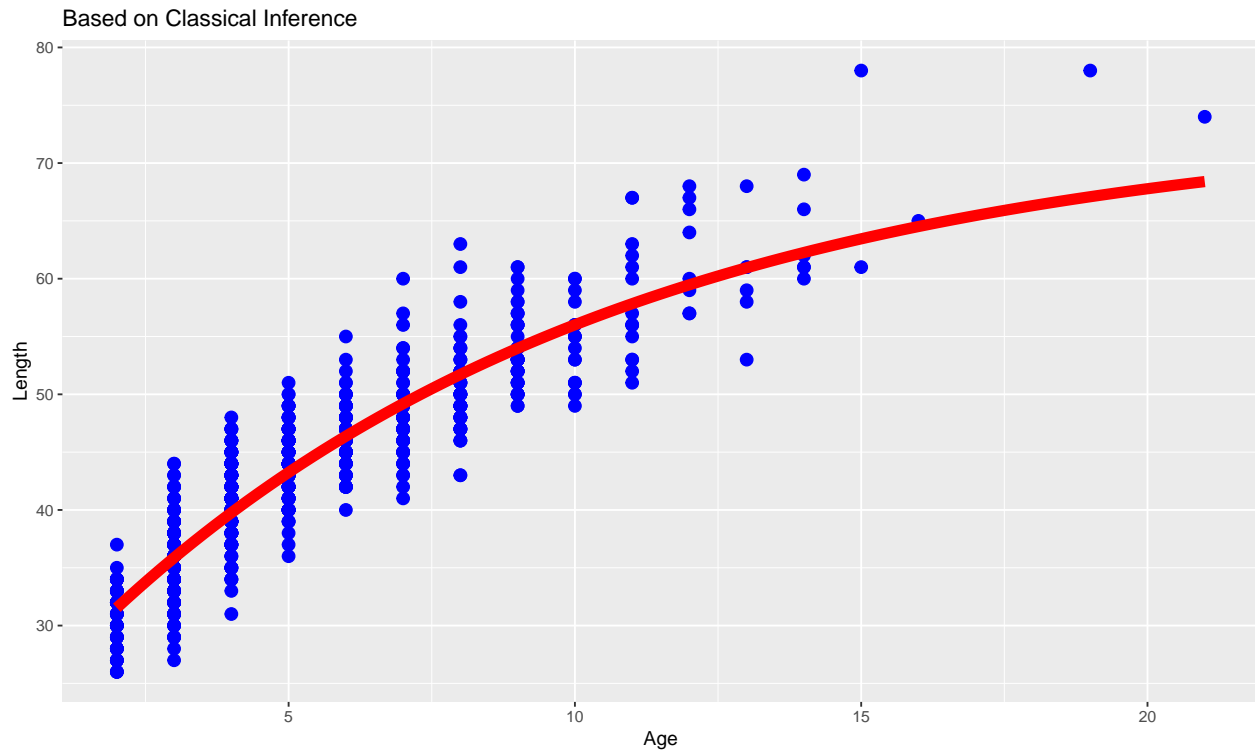
##      beta1      beta2      beta3
## 73.8227693  0.1080882 -3.1551711

sigma(ajuste_LVB)

## [1] 3.247594
```

## 5.2 Fitted curve based on Classical Inference

```
ggplot(dados.amostra, aes(Age, Length))+geom_point(col="blue", size=3)+  
stat_function(data=dados.amostra, aes(x=Age), fun = LVB,  
args = list(beta1=coef(ajuste_LVB)[1], beta2=coef(ajuste_LVB)[2], beta3=coef(ajuste_LVB)[3]),  
col="red", size=3) +ggtitle("Based on Classical Inference")
```



## 5.3 Bayesian Inference

```
Von_Bertanlanffy_mcmc <- '  
data {  
  int<lower = 0> N ;  
  vector[N] x ;  
  vector[N] y ;  
}  
parameters {  
  real<lower = .0> beta1 ;  
  real<lower = .0> beta2 ;  
  real beta3 ;  
  real<lower = .0> sigma ;  
}  
  
model {  
  y ~ normal(beta1*(1-exp(-beta2*(x-beta3))), sigma) ;  
}  
,  
  
ajuste_Von_Bertanlanffy <- stan(model_code = Von_Bertanlanffy_mcmc,
```

```
data = list(N = nrow(dados.amostra),
x = dados.amostra$Age,y = dados.amostra$Length),
chain = 3,
iter = 11000,
warmup = 1000,
thin = 10,
refresh=0)

#save.image("modelo_Von_Bertanlanffy_sem_convergencia.RData")
#save.image("modelo_Von_Bertanlanffy.RData")
```

## 5.4 MCMC diagnostics using the bayesplot package

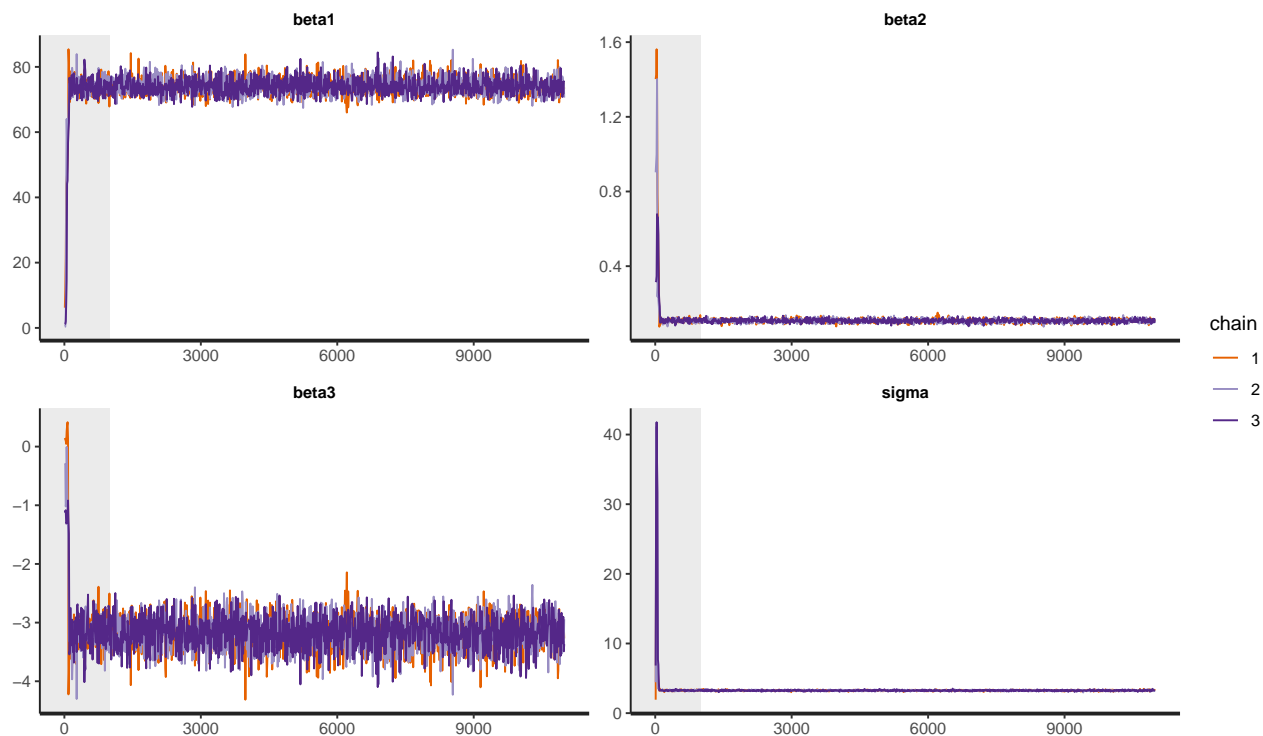
```
parametros<- c(paste('beta',1:3, sep=""), 'sigma')

CI_theta <- summary(ajuste_Von_Bertanlanffy,
                    pars = parametros,
                    probs = c(0.025, 0.975))$summary
print(CI_theta)
```

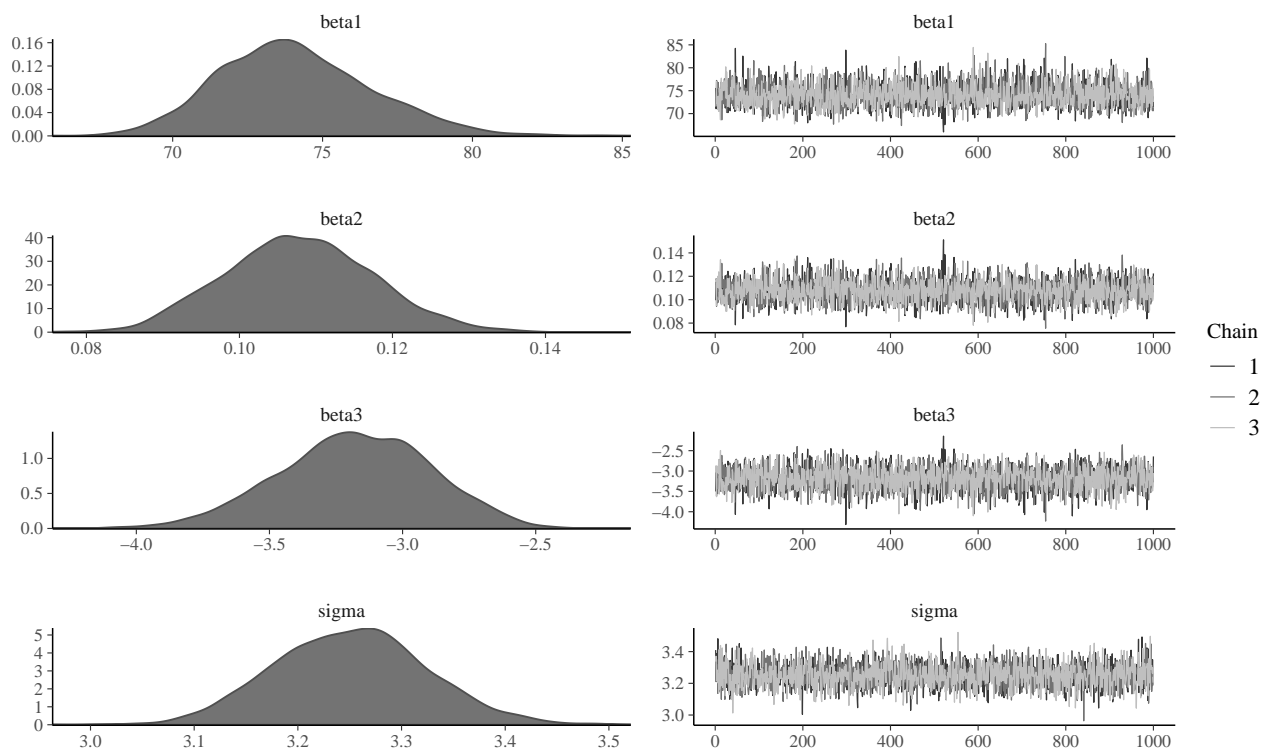
##		mean	se_mean	sd	2.5%	97.5%	n_eff
##	beta1	74.0883836	0.0475594521	2.538043586	69.63012718	79.494074	2847.898
##	beta2	0.1077937	0.0001796031	0.009648242	0.08971907	0.127173	2885.815
##	beta3	-3.1803626	0.0052332900	0.283401344	-3.75675263	-2.659727	2932.609
##	sigma	3.2509435	0.0013174606	0.072781075	3.11379297	3.397478	3051.839
##		Rhat					
##	beta1	1.0008503					
##	beta2	1.0006212					
##	beta3	1.0005698					
##	sigma	0.9994522					

```
mcmc_cadeia <- as.array(ajuste_Von_Bertanlanffy)

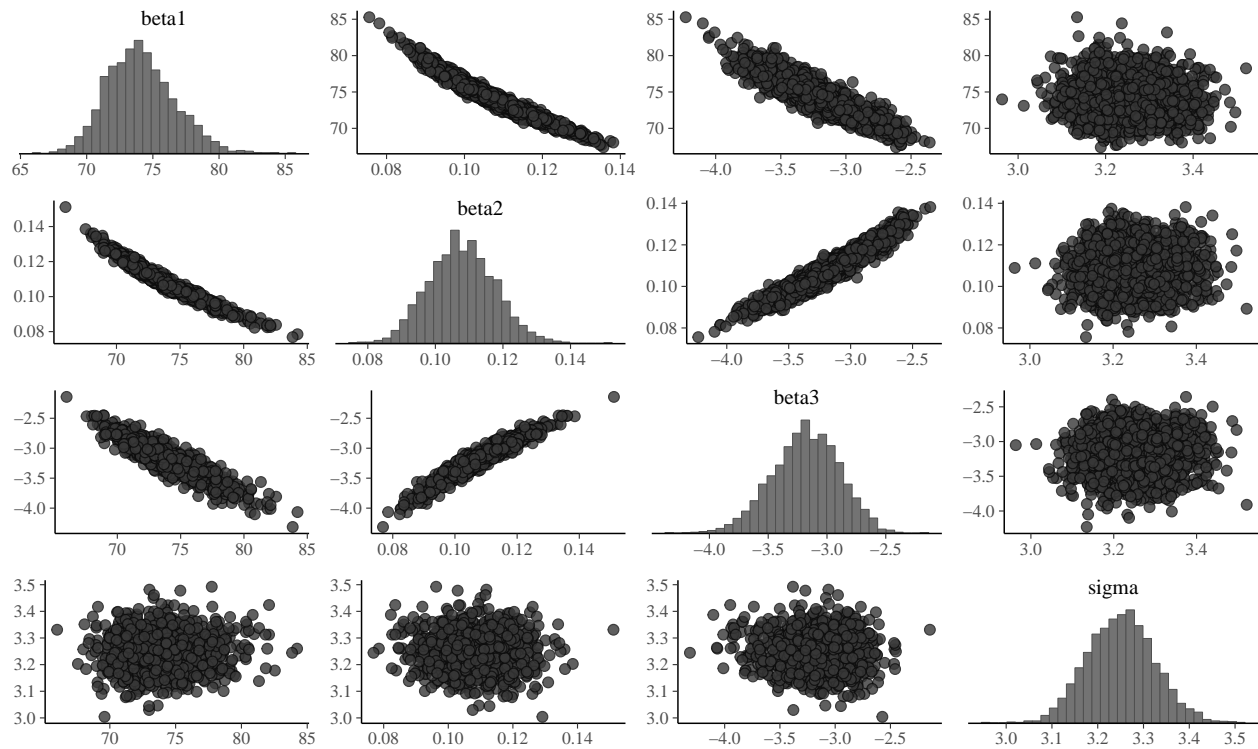
traceplot(ajuste_Von_Bertanlanffy, pars = parametros, inc_warmup = TRUE)
```



```
color_scheme_set("darkgray")
mcmc_combo(mcmc_cadeia, pars = parametros, n_warmup=0)
```

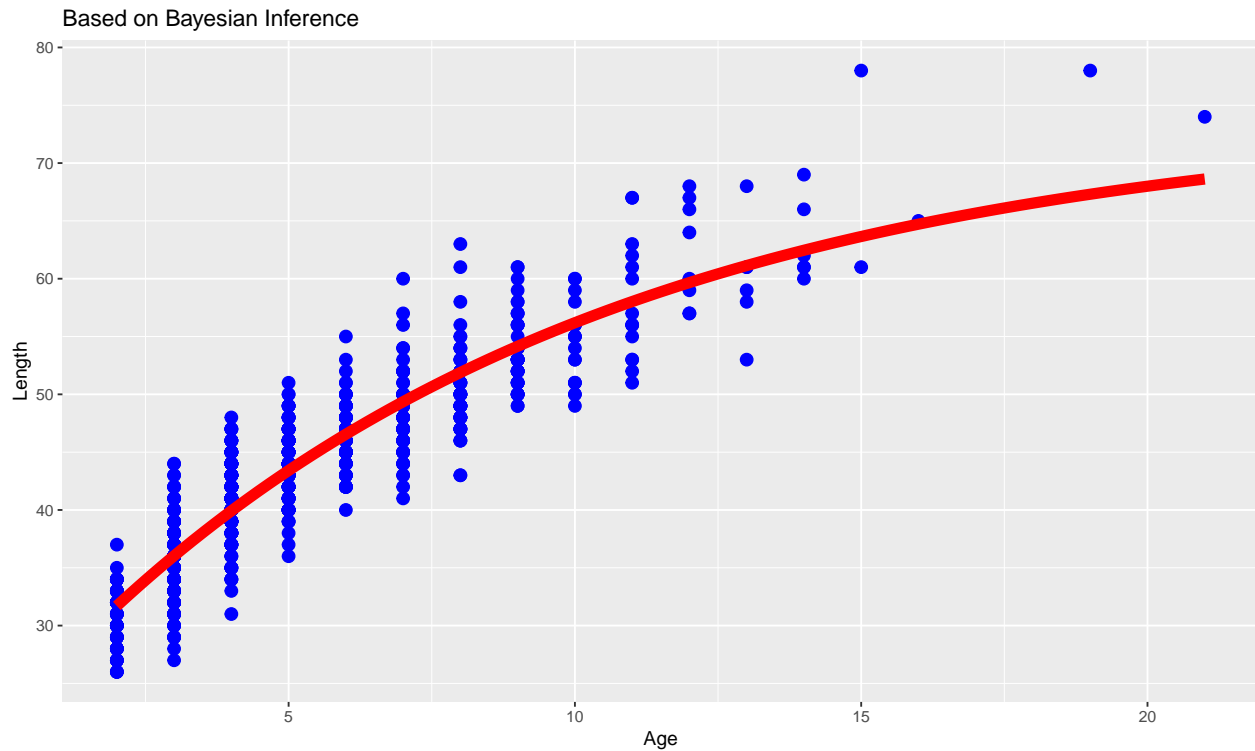


```
mcmc_pairs(mcmc_cadeia, pars = parametros)
```



## 5.5 Fitted curve based on Bayesian Inference

```
ggplot(dados.amostra, aes(Age,Length))+geom_point(col="blue",size=3)+
stat_function(data=dados.amostra,aes(x=Age),fun = LVB,
args = list(beta1=CI_theta[1,1],
            beta2=CI_theta[2,1],
            beta3=CI_theta[3,1]),
col="red", size=3) +ggtitle("Based on Bayesian Inference")
```



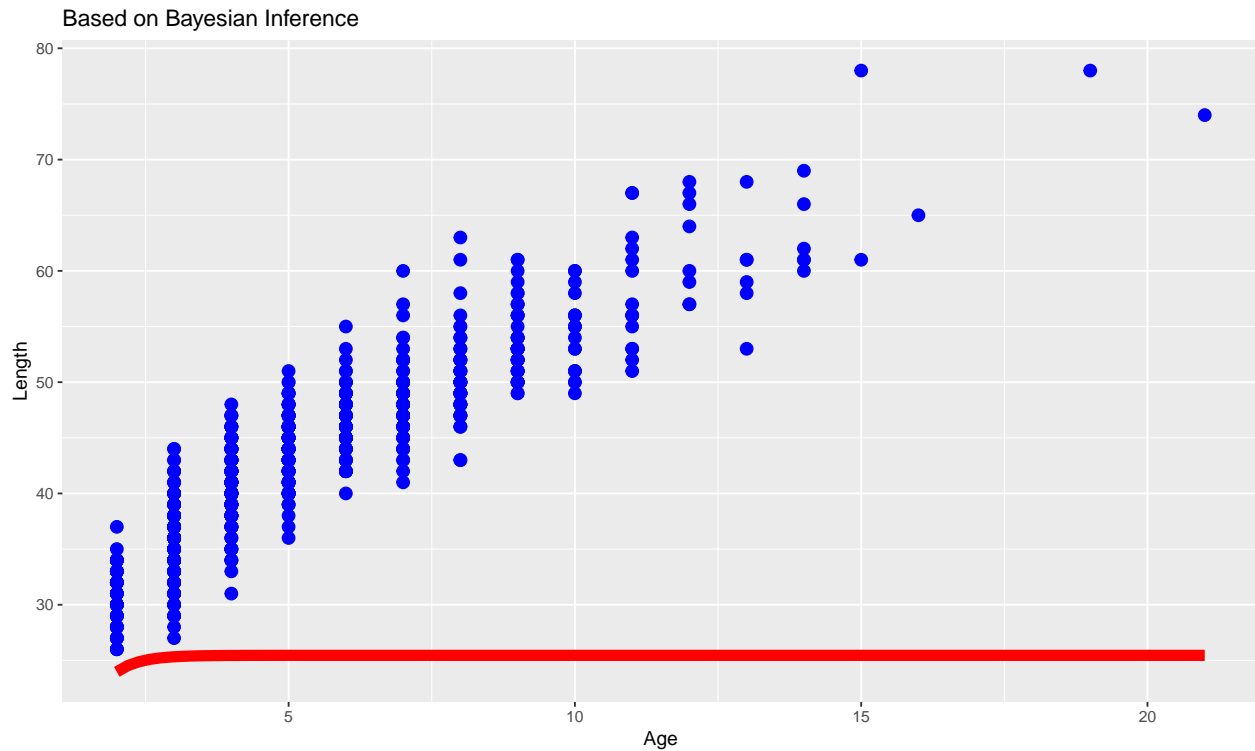
## 5.6 Fitted curve based on Bayesian Inference (without convergence)

```
rm(list=ls())
load("modelo_Von_Bertalanffy_sem_convergencia.RData")

LVB<-function(x,beta1, beta2, beta3){
  beta1*(1-exp(-beta2*(x-beta3)))
}

parametros<- c(paste('beta',1:3, sep=""), 'sigma')
CI_theta <- summary(ajuste_Von_Bertalanffy,
  pars = parametros,
  probs = c(0.025, 0.975))$summary

ggplot(dados.amostra, aes(Age,Length))+geom_point(col="blue",size=3)+
stat_function(data=dados.amostra,aes(x=Age),fun = LVB,
args = list(beta1=CI_theta[1,1],
  beta2=CI_theta[2,1],
  beta3=CI_theta[3,1]),
col="red", size=3) +ggtitle("Based on Bayesian Inference")
```



## 5.7 MCMC diagnostics using the bayesplot package

```
parametros<- c(paste('beta',1:3, sep=""), 'sigma')

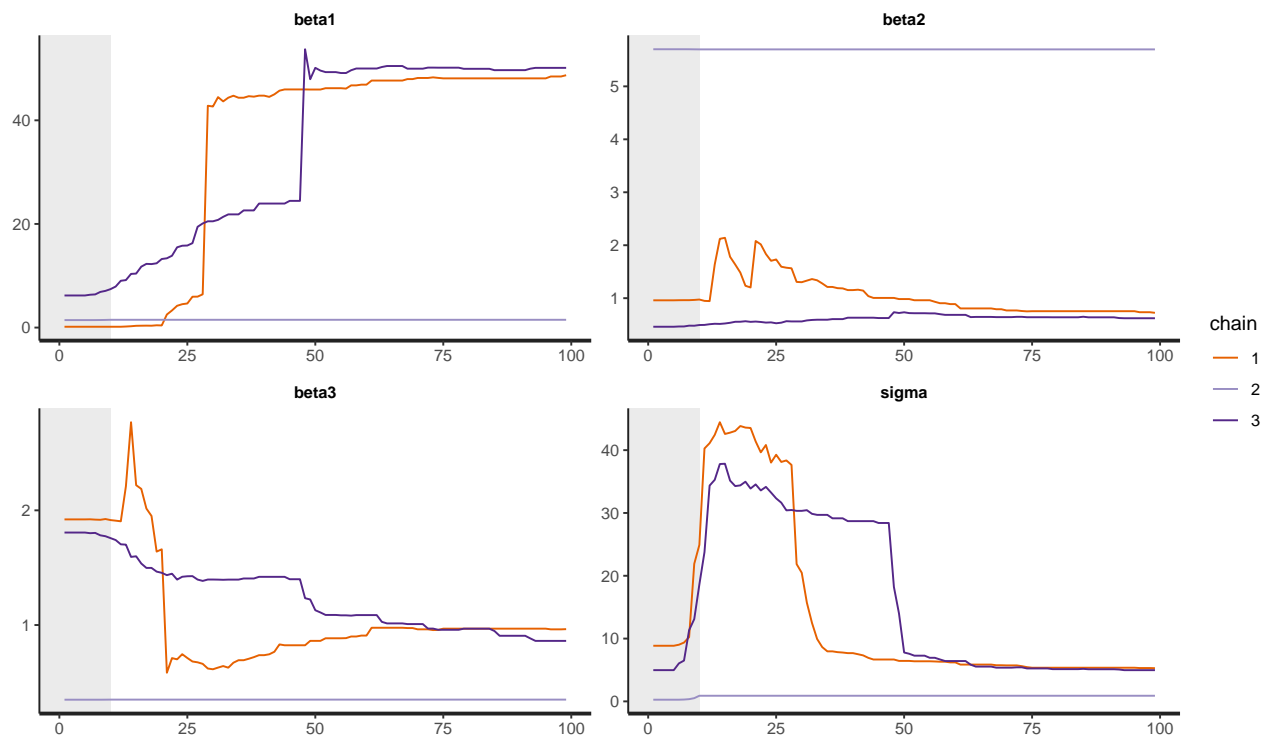
CI_theta <- summary(ajuste_Von_Bertanlanffy,
  pars = parametros,
  probs = c(0.025, 0.975))$summary
print(CI_theta)
```

##		mean	se_mean	sd	2.5%	97.5%	n_eff
##	beta1	25.4525584	13.4586171	21.9457933	0.3701932	50.176142	2.658898
##	beta2	2.4567863	1.8754883	2.3129298	0.5367772	5.698166	1.520884
##	beta3	0.8429762	0.2975077	0.4496281	0.3495844	1.905890	2.284075
##	sigma	10.3197269	5.1653622	12.8660239	0.8990780	42.475302	6.204220
##		Rhat					
##	beta1	2.302762					
##	beta2	16.999568					
##	beta3	1.968142					
##	sigma	1.783695					

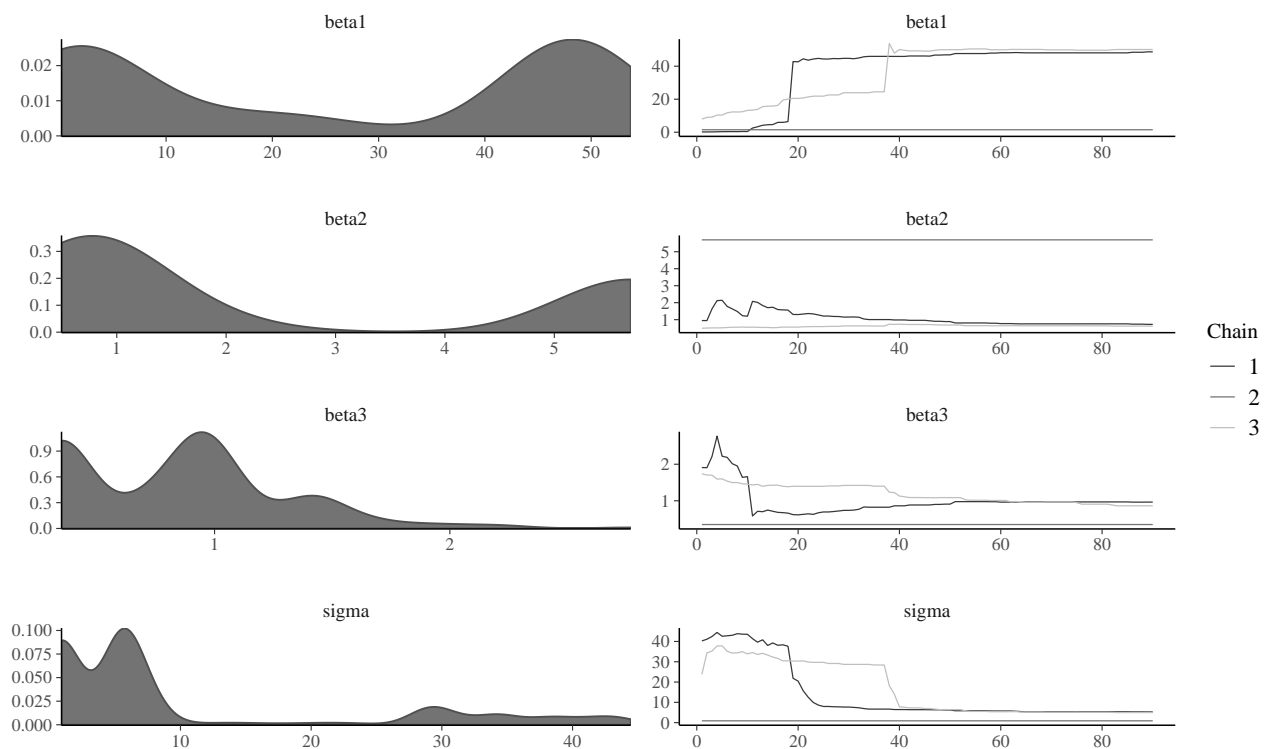
```
mcmc_cadeia <- as.array(ajuste_Von_Bertanlanffy)

traceplot(ajuste_Von_Bertanlanffy, pars = parametros, inc_warmup = TRUE)
```

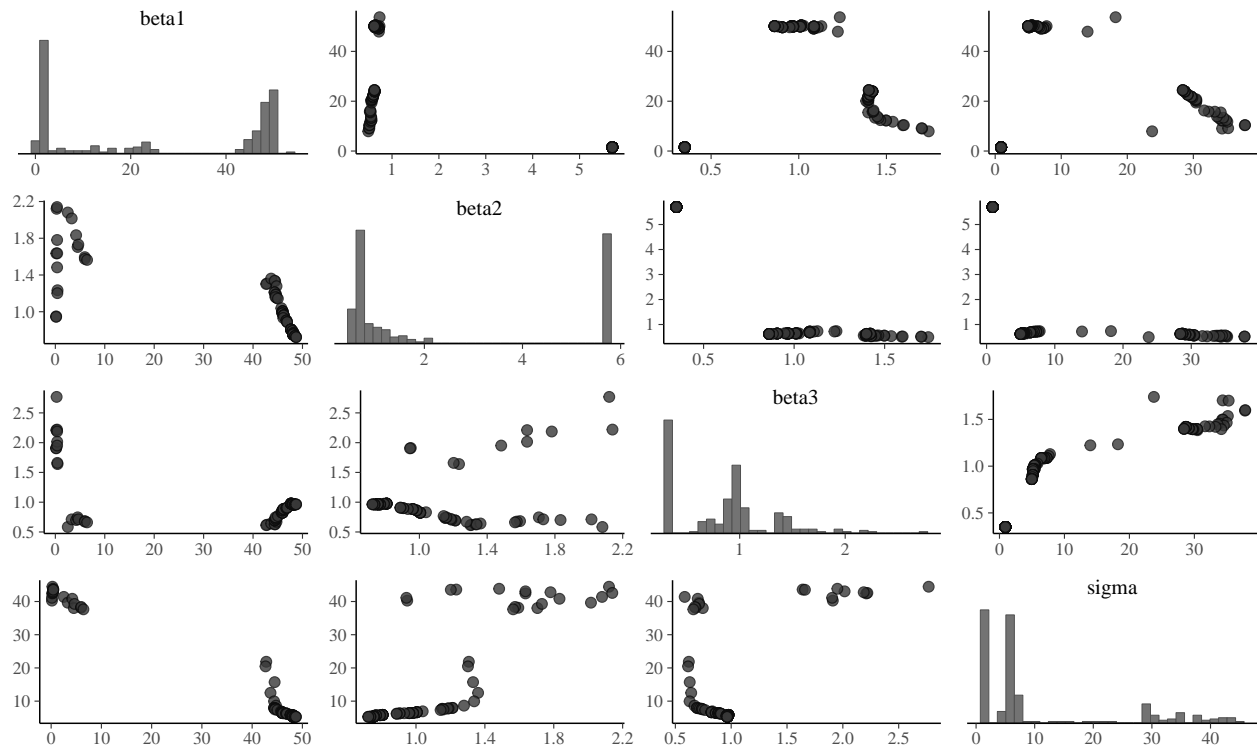




```
color_scheme_set("darkgray")
mcmc_combo(mcmc_cadeia, pars = parametros, n_warmup=0)
```



```
mcmc_pairs(mcmc_cadeia, pars = parametros)
```



## 5.8 Normal distribution without covariates in Stan

$Y \sim N(\mu, \sigma^2)$ . Therefore,  $\theta = (\mu, \sigma^2)^\top$ . Here, we specify the prior distribution for each parameter.

## 5.9 Classic inference: MLE for $\mu$ and $\sigma$

```
c(mu=coef(ajuste), sigma=sigma(ajuste))
```

```
## mu.(Intercept)      sigma
##      17.52381      10.17162
```

## 5.10 Bayesian Inference: Stan code (specific prior)

```
normal_dist_example<- '
data {
  int<lower=0> N;
  vector[N] y;
}
parameters {
  real mu;
  real<lower=0> sigma;
}
model {
  y ~ normal(mu, sigma);
  mu ~ normal(0,1e6);
  sigma ~ student_t(3,0,1);
}
```

```

}
'

normal_dist_fit <- stan(model_code = normal_dist_example,
data = list(N = dim(stackloss)[1],
  y = stackloss$stack.loss),
  chain = 3,
  iter = 11000,
  warmup = 1000,
  thin = 10,
  refresh = 0)

```

## 5.11 MCMC diagnostics using the bayesplot package

```

parametros<- c("mu", "sigma")

CI_theta <- summary(normal_dist_fit,
  pars = parametros,
  probs = c(0.025, 0.975))$summary
print(round(CI_theta),10)

```

```

##      mean se_mean sd 2.5% 97.5% n_eff Rhat
## mu      18      0  2   13    22  2970   1
## sigma   10      0  2    7    13  2974   1

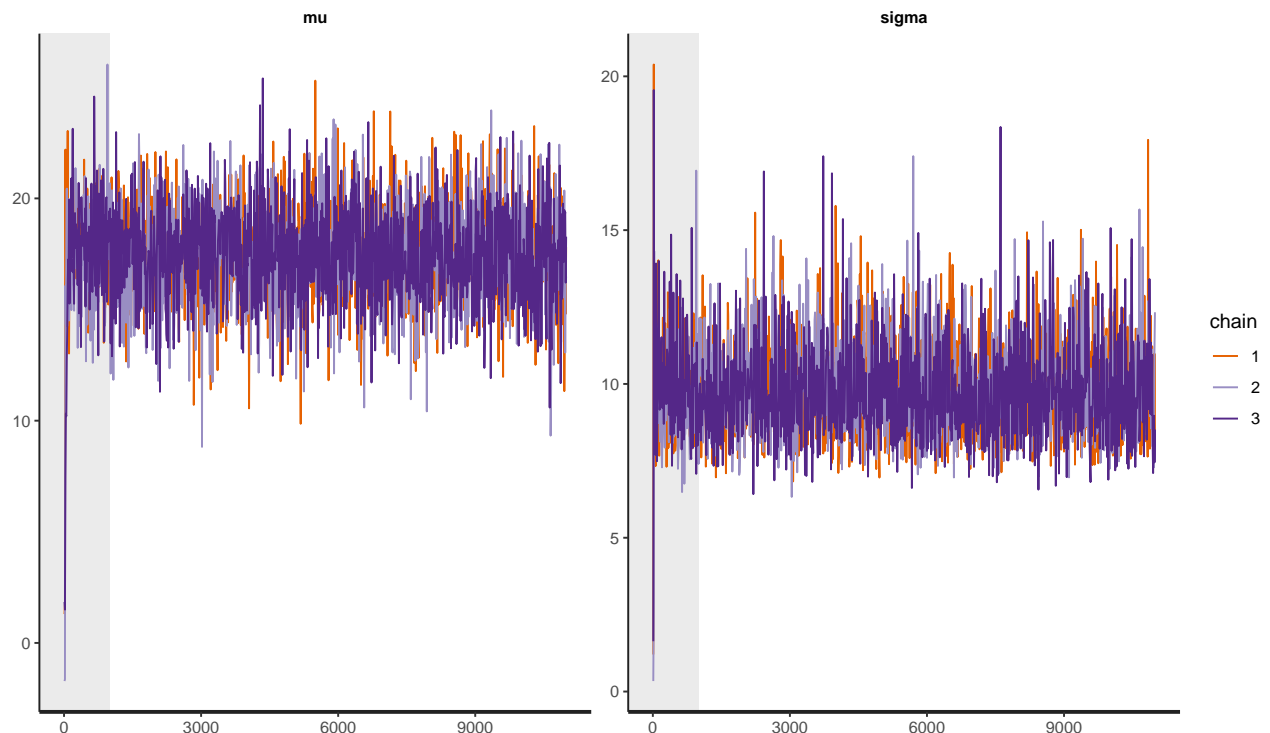
```

## 5.12 MCMC diagnostics using the bayesplot package

```

traceplot(normal_dist_fit, pars = parametros, inc_warmup = TRUE)

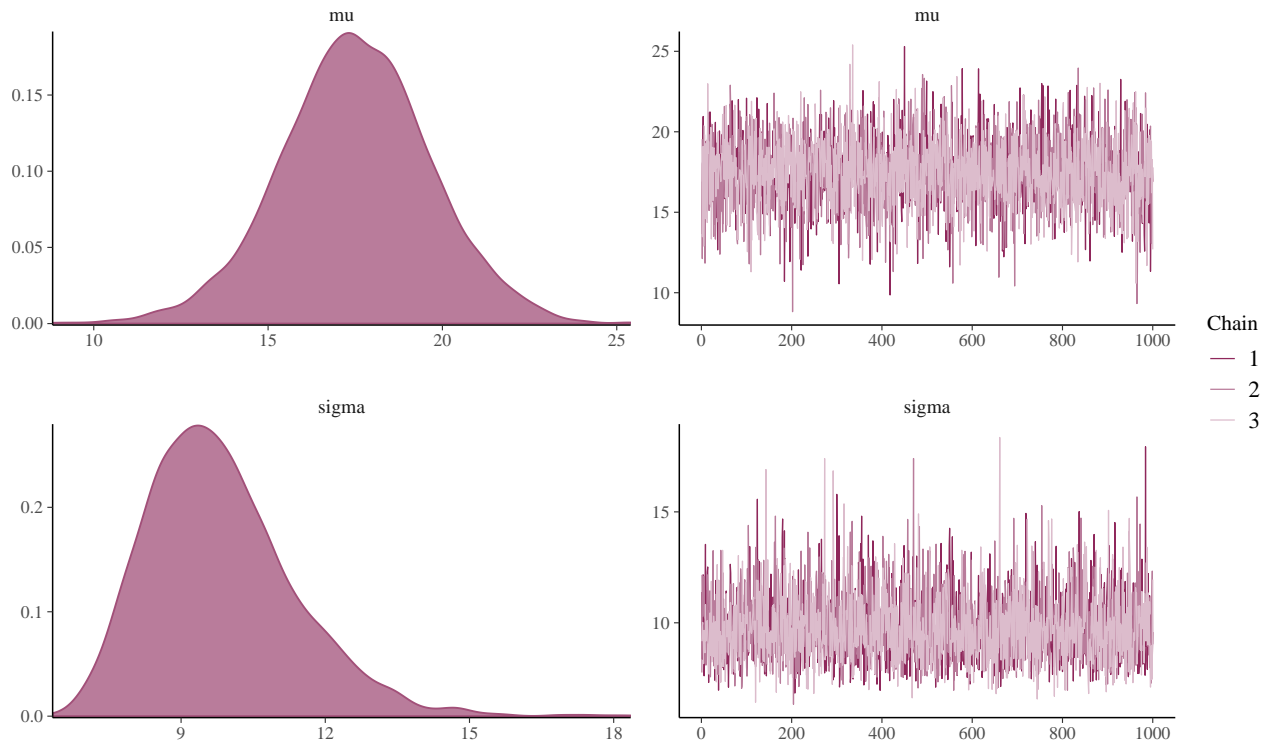
```



```
color_scheme_set("pink")
```

### 5.13 MCMC diagnostics using the bayesplot package

```
mcmc_combo(mcmc_cadeia, pars = parametros, n_warmup=0)
```



### 5.14 MCMC diagnostics using the bayesplot package

```
mcmc_pairs(mcmc_cadeia, pars = parametros)
```

