SA405 - AMP Rader §3.1

Lesson 5: Fixed-Charge Facility Location

1 Gotit Grocery

Gotit Grocery Company is considering 3 locations for new distribution centers to serve its customers in Maryland. The following table shows the fixed cost (in millions of dollars) of opening each potential center, the number (in thousands) of truckloads forecasted to be demanded at each city over the next 5 years, and the transporation cost (in millions of dollars) per thousand truckloads moved from each center location to each city.

	Fixed	Transport Costs			
	Cost	Annapolis	Ocean City	Laurel	Baltimore
Distribution Center 1	200	6	5	9	3
Distribution Center 2	400	4	3	5	6
Distribution Center 3	225	5	8	2	4
Demand		11	18	15	25

According to management, if Gotit does open a new distribution center, that center must send at least 10 thousand truckloads in order to be a worthwhile investment. Gotit seeks a minimum cost distribution system assuming any distribution center can meet any or all demands.

2	Concrete Model
	$\mathbf{x_{i,j}}$ be the flow along edge (i,j) . Ignoring the facility opening costs/variables write a concrete del for this transportation problem.
3	Binary Decision Variables to Represent Decisions
a b	e use of binary $\{0,1\}$ variables to model yes/no decisions is very common. In this model, we use inary decision variable for each potential distribution center that indicates whether or not it is ened:
a v	alue of indicates that the facility is used, and we must pay the "fixed-cost" to open it;
a v	alue of indicates that the facility is not used, and therefore we don't have to pay for it.
Wh	nenever we use binary decision variables, we must include that enforce the
	rect behavior of the variable in the context of the model. This can require some thought, reful logic, and even creativity.

1. Define three new decision variables, z_1, z_2, z_3 , which encapsulate the facility opening logic.
2. Using these new decision variables, modify the objective function of your formulation to incorporate the fixed costs of opening the distribution centers.
4 Fixed-Charge Forcing Constraints Explicitly, using the binary variables above, if $z_1 = 1$ then we are opening distribution center 1. However, implicitly, we must force the logic that if $z_1 = 0$ then:
Constraints that enforce this logic are called forcing constraints . There are two options for this, single variable OR multiple variable.
3. Write a constraint that enforces the logic that if $z_1 = 0$ then $x_{1,1}$ must also be zero.
This type of constraint is often referred to as a strong forcing constraint . 4. Write all of the strong forcing constraints needed for this model.
4. Willow an of the strong forcing constraints needed for this model.

The next type of constraint is generally referred to as **weak forcing constraints**.

5. Write an inequality that enforces the logic that, if $z_1 = 0$ then $x_{1,1} = x_{1,2} = x_{1,3} = x_{1,4} = 0$.

6. Write all of the weak forcing constraints for this model.

5 Lower Bound Constraints

The last type of constraint in this model also often comes up in fixed charge models. It forces a minimum amount of production to occur in order to use a facility. Recall that Gotit will only open a distribution center if it sends at least 10 thousand truck loads.

7. Write an inequality that enforces the logic that, if $z_1 = 0$ then at least 10 thousand truck loads must come from DC 1.

8. Write all of the lower bound constraints for this model.

6 Parameterized Model: Fixed-Charge Facility Location

maximize	$\sum_{i \in I} \sum_{j \in J} c_{ij} x_{ij} + $
subject to	$\sum_{i \in I} x_{ij} \ge d_j, \text{ for } j \in J$
	weak forcing constraints:
	OR
	strong forcing constraints:
	lower bound constraints:
	$x_{ij} \ge 0$, integer, $\forall i \in I, j \in J$