

## ASYMMETRIC CRYPTO

- Diffie - hellman key exchange (DHKE) - 1967 by Diffie and Hellman
  - Method of securely exchanging keys over a public channel with no prior knowledge of each other
  - Key can be used to encrypt subsequent communications using symmetric key cipher
- RSA (Rivest Shamir Adleman)
  - Generates two large random prime numbers, uses them to generate public + private key pairs for encryption, decryption, digital signature generation and digital signature verification

### Task 1 - Deffie-hellman key exchange

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Dirty Diffie-Hellman  
(Like dirty Santa, but geekier)

Crappy PHP script for a simple Diffie-Hellman key exchange calculator. I guess I could have used Javascript instead of PHP, but I had rounding errors.

Set these two for everyone

g:  p:

	Alice	Bob
a:	<input type="text" value="5"/>	<input type="text" value="7"/>

a = 5  
A =  $g^a \bmod p = 59^5 \bmod 251 = 246$   
b = 7  
B =  $g^b \bmod p = 59^7 \bmod 251 = 165$   
Alice and Bob exchange A and B in view of Carl  
key<sub>a</sub> =  $B^a \bmod p = 165^5 \bmod 251 = 187$   
key<sub>b</sub> =  $A^b \bmod p = 246^7 \bmod 251 = 187$

## Task 2 - Manual RSA encryption and decryption

### a. Deriving the private key

```
crypto@crypto: ~/Downloads/Sophia/lab5
File Edit Tabs Help
crypto@crypto:~$ cd Downloads/
crypto@crypto:~/Downloads$ mkdir Sophia
crypto@crypto:~/Downloads$ cd Sophia
crypto@crypto:~/Downloads/Sophia$ mkdir lab5
crypto@crypto:~/Downloads/Sophia$ cd lab5
crypto@crypto:~/Downloads/Sophia/lab5$ Python3 RSA.py

Command 'Python3' not found, did you mean:

  command 'cython3' from deb cython3
  command 'python3' from deb python3-minimal

Try: sudo apt install <deb name>

crypto@crypto:~/Downloads/Sophia/lab5$ python3 RSA.py
public key (33, 53671)
private key (12897, 53671)
encrypt [31644]
decrypt [200]
crypto@crypto:~/Downloads/Sophia/lab5$
```

Q: What are the numerical values of the private key and the public key?

public key (33, 53671)

private key (12897, 53671)

### b. Encrypting a message

Q: What is the cipher-text of "100"?

encrypt [31644]

### c. Decrypting a message

Q: What is the plain-text of C?

decrypt [200]

Q: Try to encrypt a big number, e.g., 100000, and then decrypt the cipher-text. Describe your finding and justify it. What is the biggest number that can be correctly encrypted and then decrypted?

- Maximum depends on product between the two prime numbers -  $191 \times 281 = 53671$ 
  - 53671 is the limit for correctly encrypting and decrypting

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crypto@crypto: ~/Downloads/Sophia/lab5

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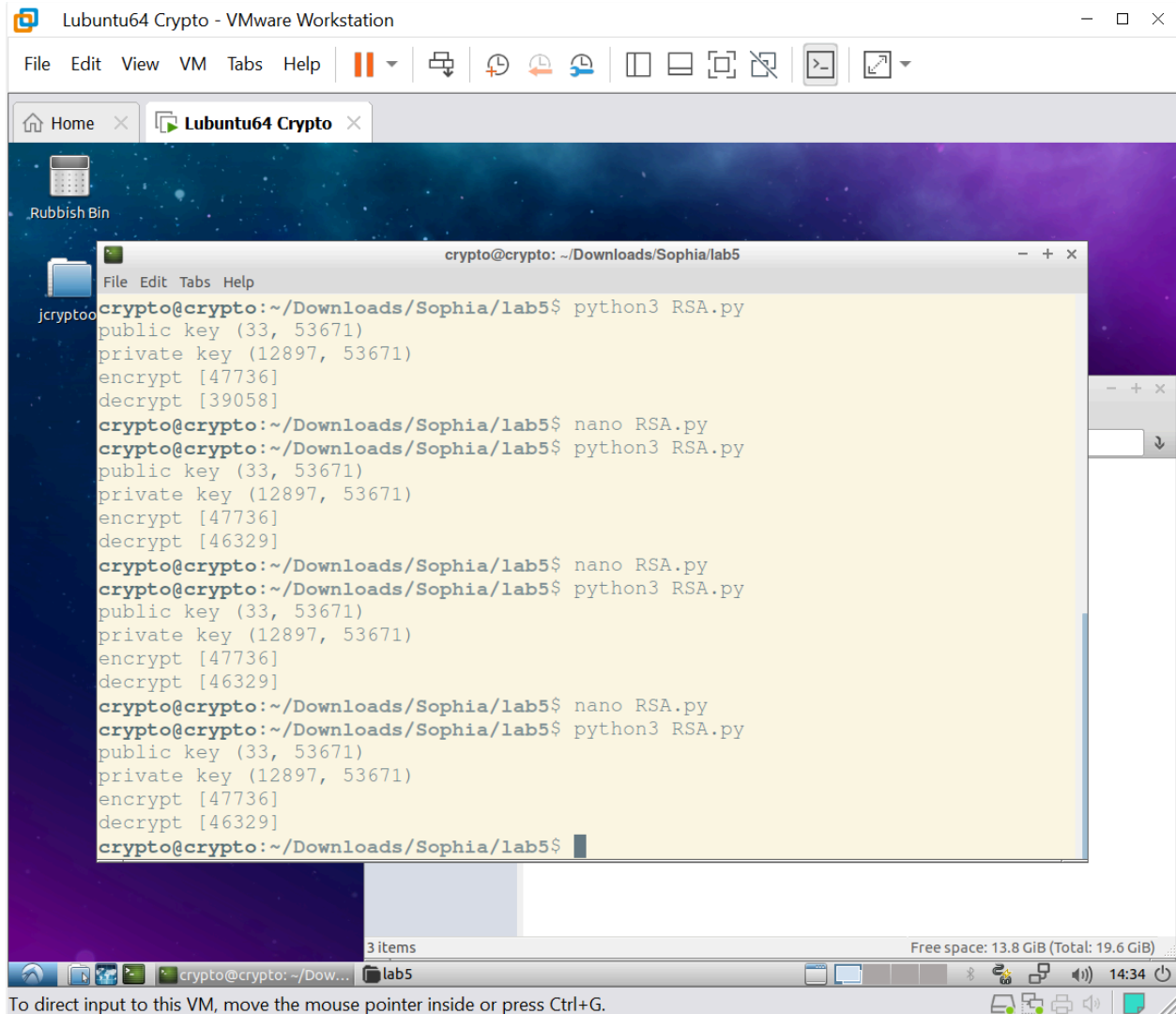
GNU nano 2.9.3 RSA.py

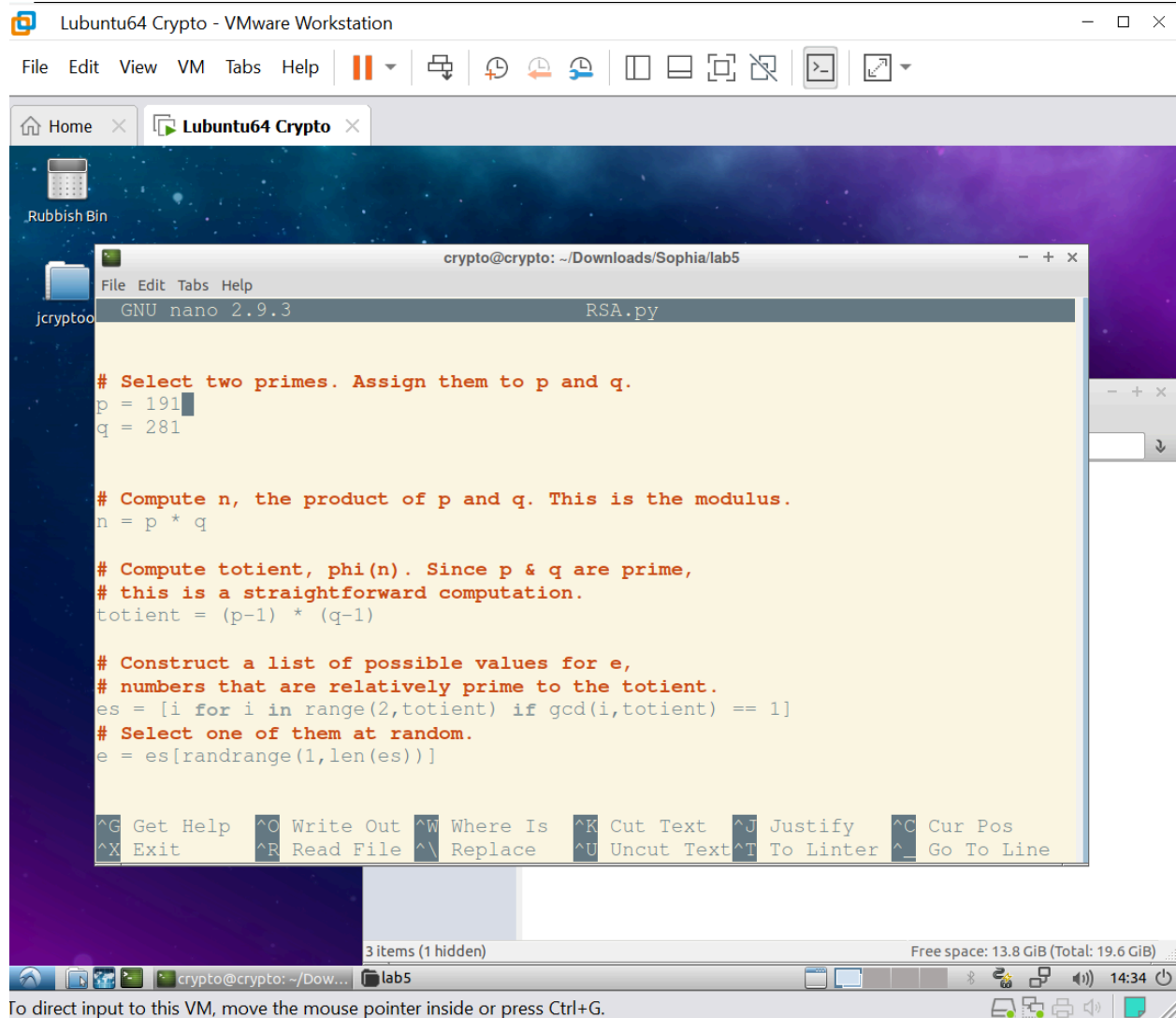
```
"Not everything that can be counted counts, and not everything that counts can$
"Make everything as simple as possible, but not simpler." - Albert Einstein
"There are only two ways to live your life. One is as though nothing is a mira$

# Decrypt. Takes a key and an array of numbers.
# Runs RSA on each of the values. Returns a byte string.
def decrypt(key, arr):
    return [rsa(key,a) for a in arr]

print ("public key",pub)
print ("private key",pri)
print ("encrypt",encrypt(pub,[100000]))
print ("decrypt",decrypt(pri,[47736]))
```

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^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Linter ^\_ Go To Line





#### d. RSA key generation and encryption with an online tool

##### Step 1: Set prime numbers

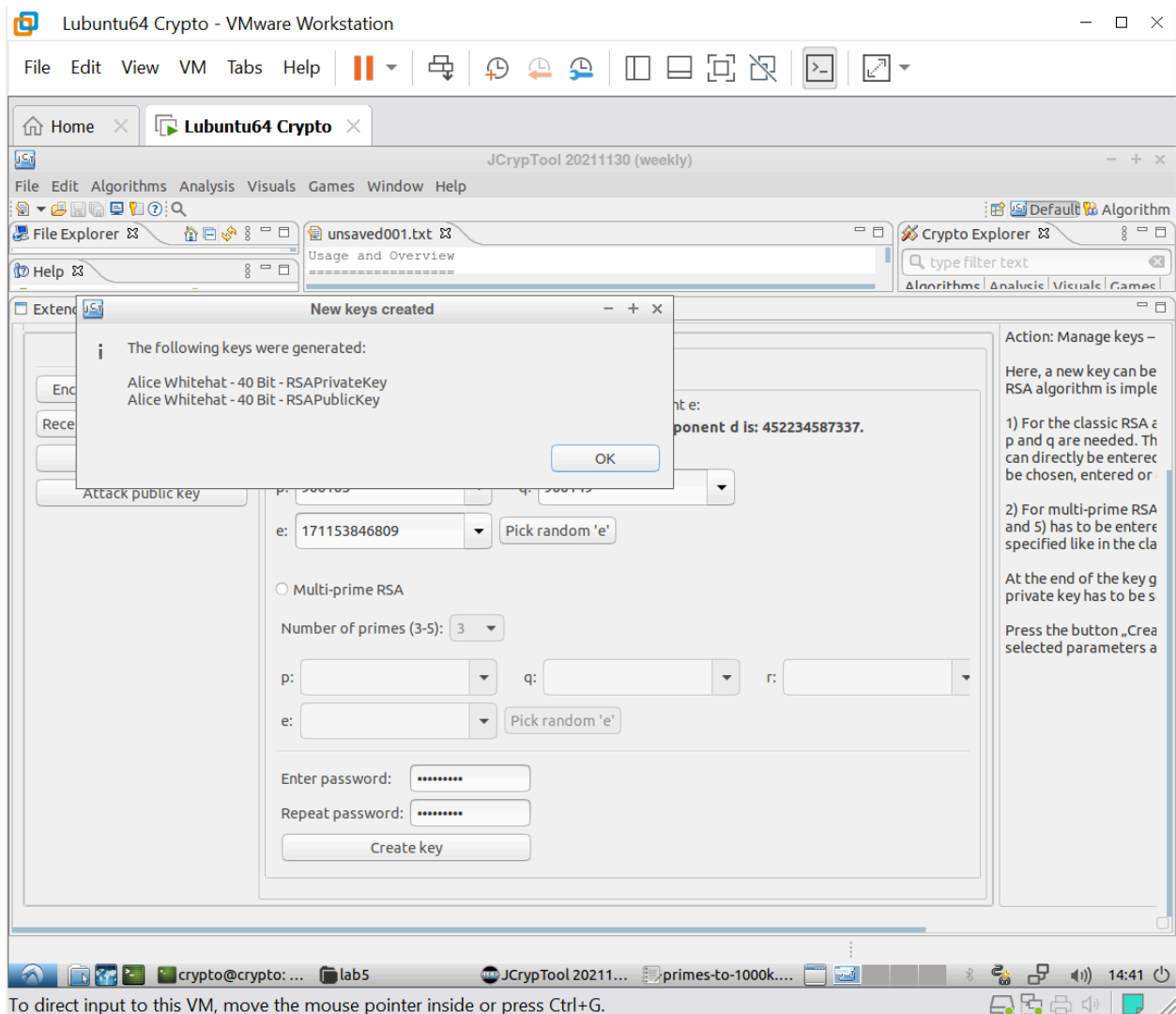
As a starting point for RSA, choose two prime numbers  $p$  and  $q$ :

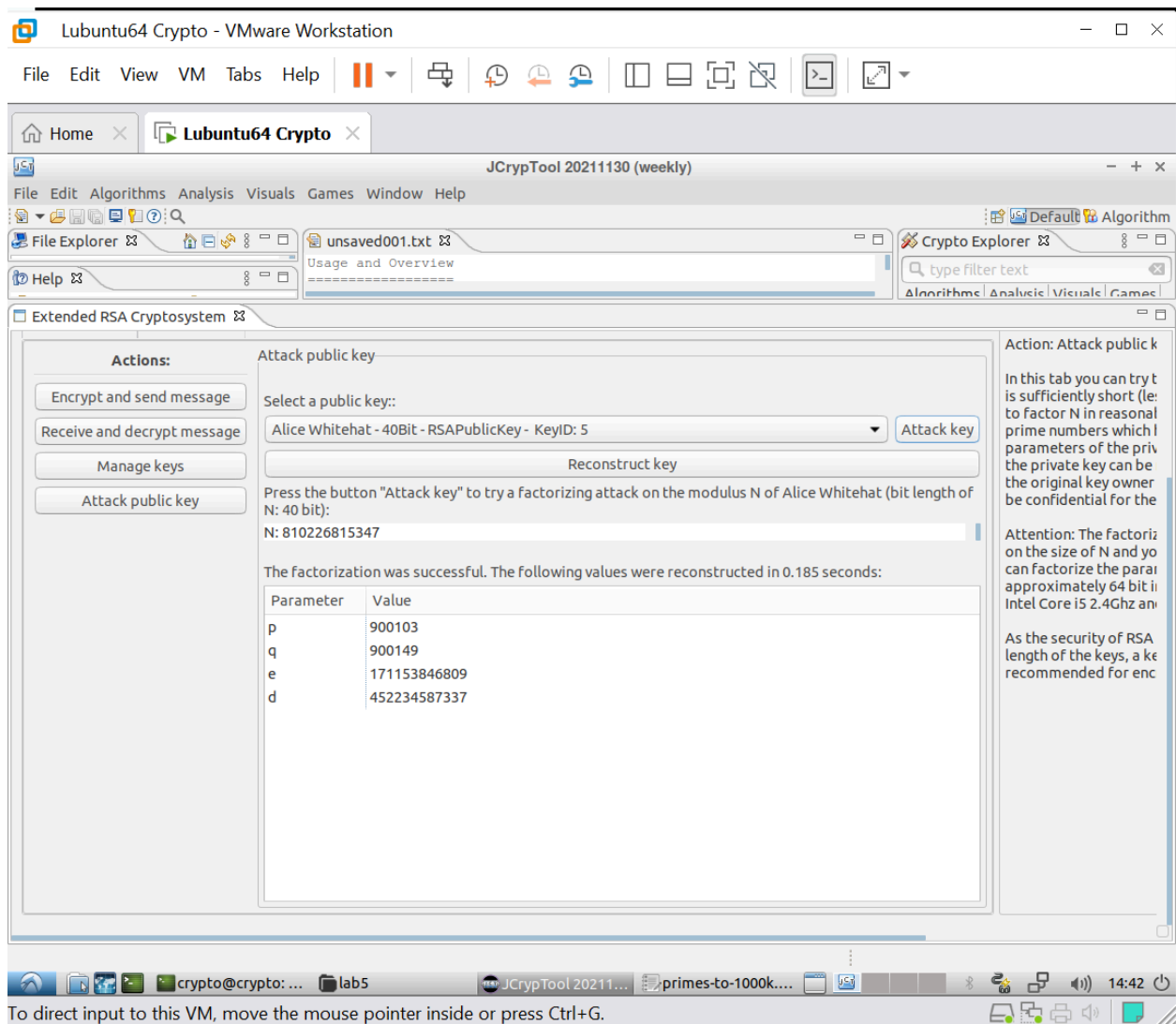
$p =$  191

$q =$  281

### Task 3 - Attack RSA keys

- Security of RSA based on how hard the Integer Factorisation Problem (IFP) is
  - Integer factorisation - the decomposition of a composite number into a product of smaller integers
  - RSA can be cracked through the exhaustive-search method when the number is large





Q: To factor a number N using exhaustive-search, i.e., try factors in 1, 2, 3.....N, how many numbers at most should be tried?

Maximum numbers to check is  $N - 1$ , ensures it doesn't leave a remainder: finds factors



## Task 4 - RsA encryption and decryption

### a. Generate RSA private and public key pair

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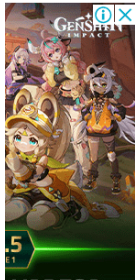
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certificate.fyicenter.com/2145\_FYIcenter\_Public\_Private\_Key\_Decoder\_and\_Viewer.html#Result

need to do is to paste your Public or Private key in PEM format into the input box and click the "Go" button below. Decoded key details will be displayed in the result area.

**Key in PEM Format:**


```
-----BEGIN RSA PRIVATE KEY-----
MIIEpAIBAAKCAQEAQpC9LL0uZV/IFVnRAfUdMz7cOW4s51gsu1IntTFOJsO3Zhg
WCR9c96bz3IbhkkB6gg287Lq7T7Ws1QQZ+CVvW15980E9E/0WZwE368j6axsq+71
L16lHa17FgK+IWUx8qJGPOZrDcFW/VUhhfv0708Y/UakGAe867eTrj7qHboFEVGE
C6bi4fvvWqmbWp11ISGC6VqPBd/6giw+h161mXFQe38cKvF6MFidUKRrzUib0oF
LPNLE2gsmSW9mwiHLwPM7w5a8s+TcZ0s6WGq72ld5G1zKW8PoQ8fPhYo0k2We1LK
4PcgT+47V4R+8MW1NDhpp09Ykq6amIyL6fqMEwIDAQABAOIBACgm/pdd55YqlpLC
c1XSXoSbKa3fZTMZ1R7wEG97WNRizlG0omaP1VgxsGktvqi8tL2+0gA7pmRWqIKC
```


**Name your key:**

(All fields are required.)

Or select [RSA Public Key](#), [DSA Public Key](#), [DH Public Key](#) or [EC Public Key](#) to try sample public keys.

Or select [RSA Private Key](#), [DSA Private Key](#), [DH Private Key](#) or [EC Private Key](#) to try sample private keys.

 FYIcenter.com

 **FYIcenter.com Decoded Result:**

Specified Key: **Valid** ✓

**Private Key Detailed Information:**

Key Details:

- Type: RSA
- Size (bits): 2048
- Modulus (n):  
a8f711f4b2f4b9957f2055674407d474ccfb7285b8b39d60b2ed489d34c53  
0edd986058247d73de9bcf721b864901ea0836f3b2eae3ed6b2541067e09  
6979f7cd04f44ff4599c04daf23e9ac6cabee5f2f5ea51da97b1602be216  
f2a2463ce66b0dc156fd552185fbceef4f18fd46a41807bcebb793ae3eea1  
051151840ba6e2e1fbf0bc0aa66d6a759654860ba56a3c177fea08b0fa197  
65c541edfc70abc5e8c162754291af35226f4a052cf34b13682c9ac5bd9b0  
2f03ccf0e5af2cf937193ace961aaef695de46d73296f0fa10f1f3e1628d  
967b52cae0f7204fee3b57847ef0c5b5343869a74f5892ae9a988c8be9fa8
- Public Exponent (e): 65537 (0x010001)
- Private Exponent (d):

# PEM Parser

Sample files:

Decode Pem Format Enter the text of your Certificate

```
GT/t/zaP1tMVjKF8BIXYWEP3NgELTP/3DKgCnDKECgYEAoFJ9nIVIZDSS/n5WIBWL
82Y3R9HPclrcrKHkvalyjPf6GziZ0+p8ARYh9bpjITW0i+lv3gZA9duANKVs7OSu
iX+9lAC2p/O1FFuoWZeQjjscFRouy/6rpK33bD/NF/P4T/aojh0G6kYgEK7R0RXC
6ZERMg3dmZskvWOnmHrdWYMCgYBn8HNNMhDIG1yGL3hLL0v3sJs61+vMAFI3EITn
mCfxD6WfMgTL+/43mFijHWEO7yclT5xFTZEE5ZDh1KWmZXMpoR1n6Zmq2vPhO2/
bYbRdlgyOa/KgGTEEU2EiYebXWoF88zoqIH5BwMXvwj8hd9cBs/EmmHnD2AcWhCB
FsmsoQKBgQCJenGOmKXMTM++nvBRsDDv2tlvnfr2sglvf+8n1zoL6cA3I7YUFHvU
VgXcmrOd4kIRjQvJVLt16jgaCA9i0MVLz8mLEAK2pfnoztZm1LklZSf6Ft+VnH3I
lbCXuqK9Q1vZpP6y1MQsmxKOGImDWF3knsxlGRjHD5P8o6dv4M6WUw==
-----END RSA PRIVATE KEY-----
```

Cert Password (if any)

Submit

Private-Key:

Algo

Format

Fingerprint

Modulus

Q: Try the following tools and confirm that you can recover RSA components.

Yes i can recover the RSA components

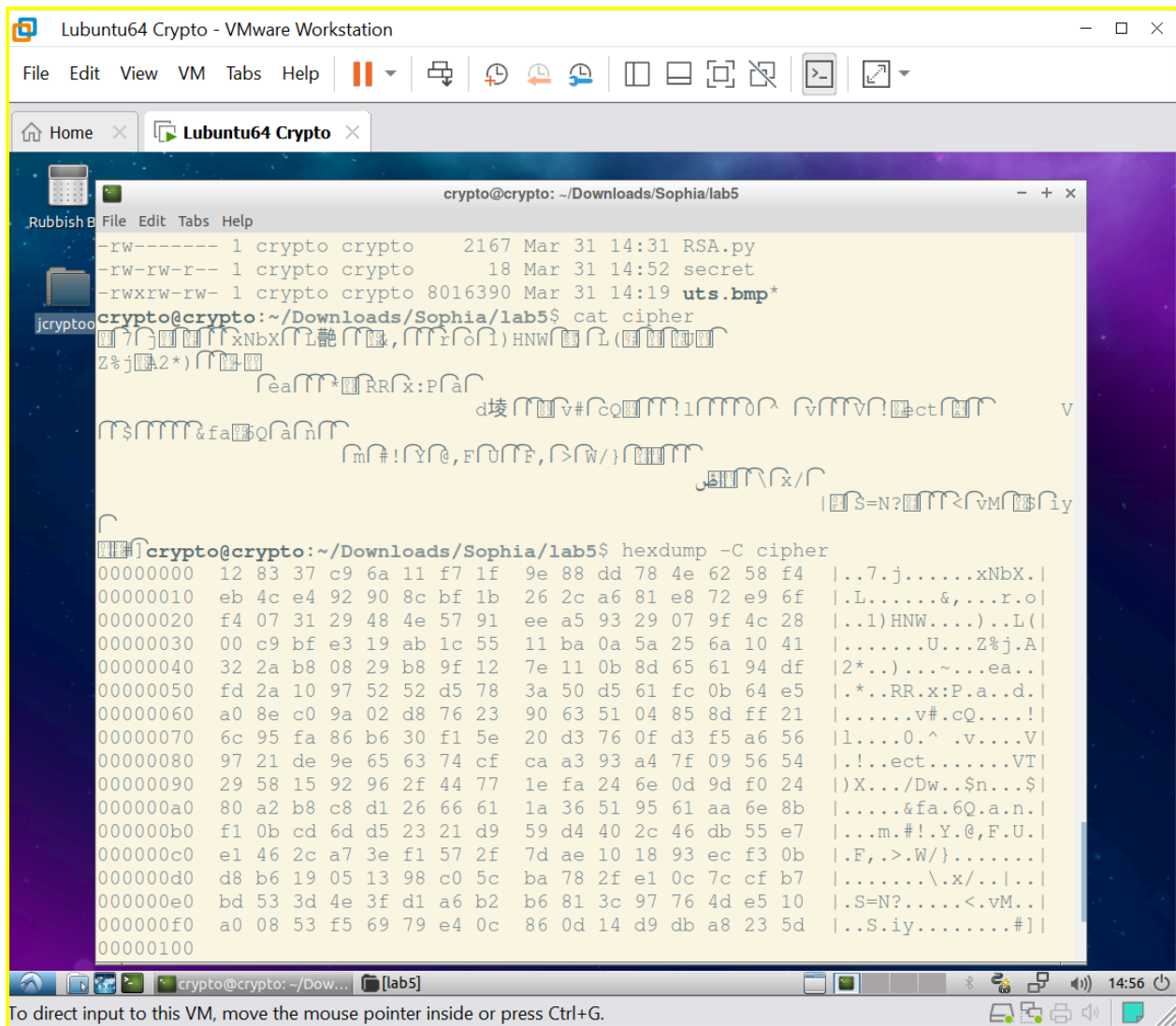
```
crypto@crypto:~/Downloads/Sophia/lab5$ openssl rsa -in private.pem -outform PEM
-pubout -out public.pem
writing RSA key
crypto@crypto:~/Downloads/Sophia/lab5$ ls
primes-to-1000k.txt  private.pem  public.pem  RSA.py  uts.bmp
crypto@crypto:~/Downloads/Sophia/lab5$ cat public.pem
-----BEGIN PUBLIC KEY-----
MIIBIjANBgkqhkiG9w0BAQEFAAOCAQ8AMIIBCgKCAQEAgPcR9LL0uZV/IFVnRAfU
dMz7coW4s51gsulInTTFOJsO3ZhgWCR9c96bz3IbhkkB6gg287Lq7T7WslQQZ+CV
vWl5980E9E/OWZwE368j6axsq+71L16lHal7FgK+IWUx8qJGPOZrDcFW/VUhhfvO
708Y/UakGAe867eTrj7qHboFEVGEC6bi4fvwvAqmbWp1llSGC6VqPBd/6giw+hl6
lmXFQe38cKvF6MFidUKRrzUib0oFLPNLE2gsmsW9mwiHLwPM7w5a8s+TcZOs6WGq
72ld5G1zKW8PoQ8fPhYo0k2We1LK4PcgT+47V4R+8MW1NDhpp09Ykq6amIyL6fqM
EwIDAQAB
-----END PUBLIC KEY-----
crypto@crypto:~/Downloads/Sophia/lab5$
```

**b. Encrypt a small file with the public key and decrypt with the private key**

```
crypto@crypto: ~/Downloads/Sophia/lab5
-h, --help          output a brief help message.

crypto@crypto:~/Downloads/Sophia/lab5$ openssl rsa -in private.pem -outform PEM
-pubout -out public.pem
writing RSA key
crypto@crypto:~/Downloads/Sophia/lab5$ ls
primes-to-1000k.txt  private.pem  public.pem  RSA.py  uts.bmp
crypto@crypto:~/Downloads/Sophia/lab5$ cat public.pem
-----BEGIN PUBLIC KEY-----
MIIBIjANBgkqhkiG9w0BAQEFAAOCAQ8AMIIBCgKCAQEApCpR9LL0uZV/IFVnRAfU
dMz7coW4s5lgsulInTTFOJsO3ZhgWCR9c96bz3IbhkKB6gg287Lq7T7WslQQZ+CV
vWl5980E9E/0WZwE368j6axsq+71L161Hal7FgK+IWUx8qJGPOZrDcFW/VUhhfvO
708Y/UakGAe867eTrj7gHboFEVGEc6bi4fvwvAqmbWp111SGC6VgPBd/6giw+hl6
lmXFQe38cKvF6MFidUKRrzUib0oFLPNLE2gsmsW9mwiHLwPM7w5a8s+TcZO6WGq
72ld5G1zKW8PoQ8fPhYo0k2We1LK4PcgT+47V4R+8MW1NDhpp09Ykq6amIyL6fqM
EwIDAQAB
-----END PUBLIC KEY-----
crypto@crypto:~/Downloads/Sophia/lab5$ echo "I owe you AUD2000" > secret
crypto@crypto:~/Downloads/Sophia/lab5$ ls
primes-to-1000k.txt  private.pem  public.pem  RSA.py  secret  uts.bmp
crypto@crypto:~/Downloads/Sophia/lab5$ openssl rsautl -encrypt -inkey public.pem
-pubin -in secret -out cipher
crypto@crypto:~/Downloads/Sophia/lab5$ ll -a
ll: command not found
crypto@crypto:~/Downloads/Sophia/lab5$ ll -a
total 7920
drwxrwxr-x 2 crypto crypto    4096 Mar 31 14:53 ./
drwxrwxr-x 3 crypto crypto    4096 Mar 31 14:12 ../
-rw-rw-r-- 1 crypto crypto     256 Mar 31 14:53 cipher
-rw----- 1 crypto crypto   57784 Mar 31 14:08 primes-to-1000k.txt
-rw----- 1 crypto crypto    1679 Mar 31 14:47 private.pem
```

To direct input to this VM, move the mouse pointer inside or press Ctrl+G.



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crypto@crypto: ~/Downloads/Sophia/lab5

```
crypto@crypto:~/Downloads/Sophia/lab5$ hexdump -C cipher
00000000  12 83 37 c9 6a 11 f7 1f 9e 88 dd 78 4e 62 58 f4 |..7.j.....xNbX.|
00000010  eb 4c e4 92 90 8c bf 1b 26 2c a6 81 e8 72 e9 6f |.L.....&,...r.o|
00000020  f4 07 31 29 48 4e 57 91 ee a5 93 29 07 9f 4c 28 |..1)HNW....).L(|
00000030  00 c9 bf e3 19 ab 1c 55 11 ba 0a 5a 25 6a 10 41 |.....U...Z%j.A|
00000040  32 2a b8 08 29 b8 9f 12 7e 11 0b 8d 65 61 94 df |2*...)...~...ea..|
00000050  fd 2a 10 97 52 52 d5 78 3a 50 d5 61 fc 0b 64 e5 |.*..RR.x:P.a..d.|
00000060  a0 8e c0 9a 02 d8 76 23 90 63 51 04 85 8d ff 21 |.....v#.cQ....!|
00000070  6c 95 fa 86 b6 30 f1 5e 20 d3 76 0f d3 f5 a6 56 |l....0.^ .v....V|
00000080  97 21 de 9e 65 63 74 cf ca a3 93 a4 7f 09 56 54 |.!...ect.....VT|
00000090  29 58 15 92 96 2f 44 77 1e fa 24 6e 0d 9d f0 24 |)X.../Dw..$n...$|
000000a0  80 a2 b8 c8 d1 26 66 61 1a 36 51 95 61 aa 6e 8b |.....&fa.6Q.a.n.|
000000b0  f1 0b cd 6d d5 23 21 d9 59 d4 40 2c 46 db 55 e7 |...m.#!.Y.@,F.U.|
000000c0  e1 46 2c a7 3e f1 57 2f 7d ae 10 18 93 ec f3 0b |.F,..>.W/}.....|
000000d0  d8 b6 19 05 13 98 c0 5c ba 78 2f e1 0c 7c cf b7 |.....\x/..|..|
000000e0  bd 53 3d 4e 3f d1 a6 b2 b6 81 3c 97 76 4d e5 10 |.S=N?.....<.vM..|
000000f0  a0 08 53 f5 69 79 e4 0c 86 0d 14 d9 db a8 23 5d |..S.iy.....#]|
00000100

crypto@crypto:~/Downloads/Sophia/lab5$ openssl rsautl -decrypt -inkey private.pem -in cipher -out plain.txt
crypto@crypto:~/Downloads/Sophia/lab5$ ls
cipher      primes-to-1000k.txt  public.pem  secret
plain.txt   private.pem          RSA.py      uts.bmp
crypto@crypto:~/Downloads/Sophia/lab5$ cat plain.txt
cat: plain.txt: No such file or directory
crypto@crypto:~/Downloads/Sophia/lab5$ cat plain.txt
I owe you AUD2000
crypto@crypto:~/Downloads/Sophia/lab5$ cat secret
I owe you AUD2000
crypto@crypto:~/Downloads/Sophia/lab5$
```

crypto@crypto: ~/Downloads/Sophia/lab5

14:56

To direct input to this VM, move the mouse pointer inside or press Ctrl+G.

### c. Size limitation of RSA encryption

```
crypto@crypto: ~/Downloads/Sophia/lab5
File Edit Tabs Help
plain.txt  private.pem          RSA.py          uts.bmp
crypto@crypto:~/Downloads/Sophia/lab5$ cat plain.text
cat: plain.text: No such file or directory
crypto@crypto:~/Downloads/Sophia/lab5$ cat plain.txt
I owe you AUD2000
crypto@crypto:~/Downloads/Sophia/lab5$ cat secret
I owe you AUD2000
crypto@crypto:~/Downloads/Sophia/lab5$ head -c 1024 /dev/urandom > random1024
crypto@crypto:~/Downloads/Sophia/lab5$ ll -a
total 7928
drwxrwxr-x 2 crypto crypto 4096 Mar 31 14:59 ./
drwxrwxr-x 3 crypto crypto 4096 Mar 31 14:12 ../
-rw-rw-r-- 1 crypto crypto 256 Mar 31 14:53 cipher
-rw-rw-r-- 1 crypto crypto 18 Mar 31 14:54 plain.txt
-rw----- 1 crypto crypto 57784 Mar 31 14:08 primes-to-1000k.txt
-rw----- 1 crypto crypto 1679 Mar 31 14:47 private.pem
-rw-rw-r-- 1 crypto crypto 451 Mar 31 14:50 public.pem
-rw-rw-r-- 1 crypto crypto 1024 Mar 31 14:59 random1024
-rw----- 1 crypto crypto 2167 Mar 31 14:31 RSA.py
-rw-rw-r-- 1 crypto crypto 18 Mar 31 14:52 secret
-rwxrw-rw- 1 crypto crypto 8016390 Mar 31 14:19 uts.bmp*
crypto@crypto:~/Downloads/Sophia/lab5$ openssl rsautl -encrypt -inkey public.pem
-pubin -in random100 -out randomCipher100
rsautl: Cannot open input file random100, No such file or directory
rsautl: Use -help for summary.
crypto@crypto:~/Downloads/Sophia/lab5$ openssl rsautl -encrypt -inkey public.pem
-pubin -in random1024 -out randomCipher1024
RSA operation error
140391828128192:error:0406D06E:rsa routines:RSA_padding_add_PKCS1_type_2:data to
o large for key size:../crypto/rsa/rsa_pk1.c:125:
crypto@crypto:~/Downloads/Sophia/lab5$
```

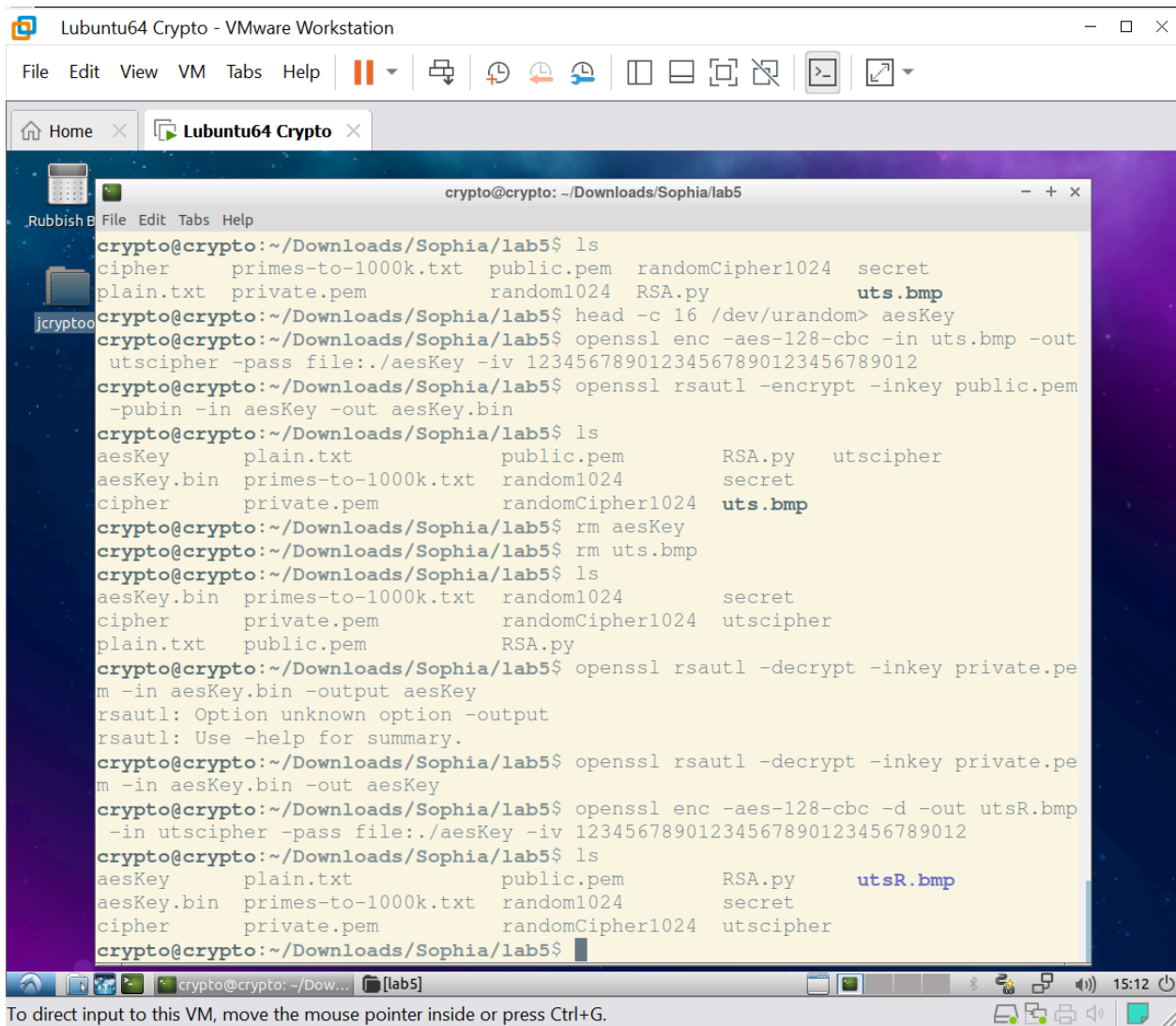
Q: How many bytes at maximum can be encrypted with 2048-bit key RSA? Why?

245 bytes

- RSA encrypts data in blocks and is based on the size of the key
- An RSA key can handle data blocks that are 2048 bits - 8 bits in a byte
  - $2048 \text{ bits} / 8 \text{ bits} = 256 \text{ bytes} - 10 \text{ bytes (for padding)} = 245 \text{ bytes}$



#### d. Protect big files



```
crypto@crypto: ~/Downloads/Sophia/lab5$ ls
cipher      primes-to-1000k.txt  public.pem  randomCipher1024  secret
plain.txt   private.pem          random1024  RSA.py            uts.bmp
crypto@crypto: ~/Downloads/Sophia/lab5$ head -c 16 /dev/urandom> aesKey
crypto@crypto: ~/Downloads/Sophia/lab5$ openssl enc -aes-128-cbc -in uts.bmp -out
utscipher -pass file:./aesKey -iv 12345678901234567890123456789012
crypto@crypto: ~/Downloads/Sophia/lab5$ openssl rsautl -encrypt -inkey public.pem
-pubin -in aesKey -out aesKey.bin
crypto@crypto: ~/Downloads/Sophia/lab5$ ls
aesKey      plain.txt            public.pem      RSA.py         utscipher
aesKey.bin  primes-to-1000k.txt  random1024     secret
cipher      private.pem          randomCipher1024  uts.bmp
crypto@crypto: ~/Downloads/Sophia/lab5$ rm aesKey
crypto@crypto: ~/Downloads/Sophia/lab5$ rm uts.bmp
crypto@crypto: ~/Downloads/Sophia/lab5$ ls
aesKey.bin  primes-to-1000k.txt  random1024     secret
cipher      private.pem          randomCipher1024  utscipher
plain.txt   public.pem           RSA.py
crypto@crypto: ~/Downloads/Sophia/lab5$ openssl rsautl -decrypt -inkey private.pe
m -in aesKey.bin -output aesKey
rsautl: Option unknown option -output
rsautl: Use -help for summary.
crypto@crypto: ~/Downloads/Sophia/lab5$ openssl rsautl -decrypt -inkey private.pe
m -in aesKey.bin -out aesKey
crypto@crypto: ~/Downloads/Sophia/lab5$ openssl enc -aes-128-cbc -d -out utsR.bmp
-in utscipher -pass file:./aesKey -iv 12345678901234567890123456789012
crypto@crypto: ~/Downloads/Sophia/lab5$ ls
aesKey      plain.txt            public.pem      RSA.py         utsR.bmp
aesKey.bin  primes-to-1000k.txt  random1024     secret
cipher      private.pem          randomCipher1024  utscipher
crypto@crypto: ~/Downloads/Sophia/lab5$
```

Q: Why are the private keys in asymmetric ciphers often generated rather than specified?

- Randomness + uniqueness - unpredictable for security = increases key strength
- Prevents key from getting leaked