

# Flash Cards for Quantum/Nuclear Monte Carlo

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## Parameters in the Code

**hspot(???)** ???

**sxzupdate(sxznew(out),detrat(out),sxzold,i,opi,sp)**

**vnpsi2(w,dopot)** This subroutine ...???

**d15(kop)** = di(i) =  $\sum_k S_{ik}^{-1} \langle k | \mathcal{O}_i | \mathbf{r}, s_i \rangle = (S'/S)_{ii}$  for a specific kop (1 of 15)

**d2b(s'',s''',ij)** =  $\frac{\langle \Phi | R, s_1, \dots, s_{i-1}, s'', s_{i+1}, \dots, s_{j-1}, s''', s_{j+1}, \dots, s_A \rangle}{\langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_{j-1}, s', s_{j+1}, \dots, s_A \rangle}$  OR

**d2b(s,s',ij)** =  $\frac{\langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_{j-1}, s', s_{j+1}, \dots, s_A \rangle}{\langle \Phi | RS \rangle}$

**di(m)** =  $\sum_k S_{mk}^{-1} \langle k | \mathcal{O}_i | \mathbf{r}_i, s_i \rangle = \sum_s \text{opi}(s, m) \langle s | s_i \rangle$

**f2b(s,s',ij)** =  $\sum_{kop=1}^{15} f_{ij}^{kop} \langle s s' | \mathcal{O}_{ij}^{kop} | s_i s_j \rangle$

**fst(3,3,ij)** =  $f$  in front of specific operator

**opi(s,m)** =  $\sum_k S_{mk}^{-1} \langle k | \mathcal{O}_i | \mathbf{r}_i, s \rangle = \sum_{s'} \text{sxz}(s', i, m) \langle s' | \mathcal{O}_i | s \rangle$

**ph(i,4,j,idet)** =  $\sum_k S_{ik} \langle k | \mathcal{O}_j | s_j \rangle$

**sp(s,i)** =  $\langle s | s_i \rangle$

**spx(s,15,i)** =  $\langle s | \mathcal{O}_i^p | s_i \rangle$ , where  $p$  goes over the 15 cartesian coordinates.

**sx15(s,15,i,j)** =  $\sum_k S_{jk}^{-1} \langle k | \sum_{kop=1}^{15} \mathcal{O}_{kop} | \mathbf{r}, s \rangle = \text{opmult}(\text{sxz0})$ , where  $\text{sx15}(:, \text{kop}, :, k) = \text{opi}(s, k)$

**sxz(s,i,j)** =  $\sum_k S_{jk}^{-1} \langle k | \mathbf{r}_i, s \rangle$

# Variational Monte Carlo

## Steps for Metropolis Algorithm:

1. Start with some random walker configuration  $\mathbf{R}$
2. Propose a move to a new walker  $\mathbf{R}'$  from the distribution  $T(\mathbf{R}' \leftarrow \mathbf{R})$
3. The probability of accepting the move is given by

$$A(\mathbf{R}' \leftarrow \mathbf{R}) = \min \left( 1, \frac{T(\mathbf{R}' \leftarrow \mathbf{R})P(\mathbf{R}')}{T(\mathbf{R} \leftarrow \mathbf{R}')P(\mathbf{R})} \right).$$

The move is accepted if  $U[0, 1] < A(\mathbf{R}' \leftarrow \mathbf{R})$ .

4. Repeat from step 2.

## Variational Energy (In terms of $E_L(\mathbf{R})$ and $P(\mathbf{R})$ ), $E_V$ and $P$ :

$$E_V = \frac{\int \Psi^*(\mathbf{R}) \hat{H} \Psi(\mathbf{R}) d\mathbf{R}}{\int \Psi^*(\mathbf{R}) \Psi(\mathbf{R}) d\mathbf{R}} = \int P(\mathbf{R}) E_L(\mathbf{R}) d\mathbf{R}$$

$$P(\mathbf{R}) = |\Psi_T(\mathbf{R})|^2 / \int |\Psi_T(\mathbf{R})|^2 d\mathbf{R}$$

$$E_L(\mathbf{R}) = \Psi_T^{-1}(\mathbf{R}) \hat{H} \Psi_T(\mathbf{R})$$

## Sampled Variational Energy:

$$E_V \approx \frac{1}{N} \sum_{n=1}^N E_L(\mathbf{R}_n)$$

where  $\mathbf{R}_n$  are drawn from  $P(\mathbf{R})$ .