

Calculating the Trial Wave Function for AFDMC

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1 Trial Wave Function

The trial wave function for AFDMC must be simple to evaluate. In the past the simple Slater determinant with pair-wise correlations has been used as shown in [1],

$$\langle RS|\Psi_T\rangle = \langle RS|\left[\prod_{i<j} f_c(r_{ij})\right]\left[1 + \sum_{i<j} \sum_p f_p(r_{ij})\mathcal{O}_{ij}^p\right]|\Phi\rangle, \quad (1)$$

where the \mathcal{O}_{ij}^p 's are $\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j$, $\boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j$, and $t_{ij}\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j$, where $t_{ij} = 3\boldsymbol{\sigma}_i \cdot \hat{\mathbf{r}}_{ij}\boldsymbol{\sigma}_j \cdot \hat{\mathbf{r}}_{ij} - \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j$. The $\boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j$ and t_{ij} terms were not included in this paper because in this original paper they looked at the terms that included the most important physics.

My goal is to add the additional independent pair correlations.

$$\langle RS|\Psi_T\rangle = \langle RS|\left[\prod_{i<j} f_c(r_{ij})\right]\left[1 + \sum_{i<j} \sum_p f_p(r_{ij})\mathcal{O}_{ij}^p + \sum_{i<j} \sum_{k<l} \sum_p f_p(r_{ij})\mathcal{O}_{ij}^p f_p(r_{kl})\mathcal{O}_{kl}^p\right]|\Phi\rangle \quad (2)$$

The triple sum is called the independent pair correlation term because the sum over $k < l$ does not include any pairs that include i or j . For example, if $i = 1$ and $j = 2$ then we could include the kl pairs of 34, 45, etc., but would not include the pairs 13, 25, etc.

2 Evaluation of the Trial Wave Function

To understand how to do this I'm going to just assume that \mathcal{O}_{ij}^p only contains the term $\boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j$ and I'll start by looking at the trial wave function, equation 1, with only the linear term. So now

$$\langle RS|\Psi_T\rangle = \langle RS|\left[\prod_{i<j} f_c(r_{ij})\right]\left[1 + \sum_{i<j} f_1(r_{ij})\boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j\right]|\Phi\rangle. \quad (3)$$

Also since the central correlations don't change the states by any more than a multiplicative factor I am going to ignore that term as well. I will also just look at one term in the sum (a particular i and j value). So we are just looking at

$$\langle RS|[1 + f_1(r_{ij})\boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j]|\Phi\rangle. \quad (4)$$

Now we also know that the Slater determinant is defined as

$$\langle RS|\Phi\rangle = \det(S) = \frac{1}{\sqrt{N!}} \begin{vmatrix} \phi_1(R_1 S_1) & \phi_2(R_1 S_1) & \cdots & \phi_N(R_1 S_1) \\ \phi_1(R_2 S_2) & \phi_2(R_2 S_2) & \cdots & \phi_N(R_2 S_2) \\ \vdots & \vdots & \ddots & \vdots \\ \phi_1(R_N S_N) & \phi_2(R_N S_N) & \cdots & \phi_N(R_N S_N) \end{vmatrix}, \quad (5)$$

where $\phi_i(R_j S_j) = \phi_i^r(R_j) \phi_i^s(S_j)$ and S is called the Slated Matrix.

Now lets look at equation 4 again for an example.

$$\langle RS| [1 + f_1(r_{ij}) \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j] |\Phi\rangle \quad (6)$$

$$= \det(S) + f_1(r_{ij}) \langle RS| \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j |\Phi\rangle \quad (7)$$

$$= \det(S) + f_1(r_{ij}) \det(S'') \quad (8)$$

Here S'' is the updated matrix. It only has two columns different than S and so we can get it's determinant of S'' easily once we have the determinant of S by using the fact that

$$\det(S_{ij}^{-1} S''_{jk}) = \frac{\det(S''_{jk})}{\det(S_{ij})}, \quad (9)$$

where there are two primes simply because there were two columns changed. When we solve for $\det(S)$ we finish solving for the inverse, S^{-1} and the product $S_{ij}^{-1} S''_{jk}$ is 1 on the diagonal and 0 everywhere else except the two columns i and j . This makes the $\det(S_{ij}^{-1} S''_{jk})$ easy to solve for since it is simply the determinant of the submatrix. Thus once we have $\det(S)$ it is easier to solve for $\det(S'')$. All that is left is to do this over the pair loops and over each operator.

3 Implimentation in the code

Now how is this implimented into the code. The element of the Slater martix that corresponds to the k^{th} orbital and the i^{th} particle is given by

$$S_{ki} = \langle k|r_i, s_i\rangle = \sum_{s=1}^4 \langle k|r_i, s\rangle \langle s|s_i\rangle. \quad (10)$$

From this you can see that a general Slater matrix can be written as a linear combination of matrix elements $\langle k|r_i, s\rangle$ and coefficients $\langle s|s_i\rangle$.

Therefore it's convenient to precompute

$$\text{sxz}(s, i, j) = \text{sxmallz}(j, s, i) = \sum_k S_{jk}^{-1} \langle k|r_i, s\rangle. \quad (11)$$

For example if we were computing the determinant of $S''_{ij} = \langle k|r_i, s'_i\rangle$ where the s'_i was changed is different from s_i on the changed columns, then the product matrix could be computed as

$$S_{jk}^{-1} S''_{ki} = \sum_{s=1}^4 \left(\sum_k S_{jk}^{-1} \langle k|r_i, s\rangle \right) (\langle s|s_i\rangle) = \sum_{s=1}^4 \text{sxz}(s, i, j) \langle s|s_i\rangle. \quad (12)$$

Question 2: Is this how we use sxz?

I have looked at how to calculate the trial wave function with a correlation operator in the middle now lets look at how to do it with 1 and 2-body spin-isospin operators in the middle. Here I am mostly filling in gaps in my understanding of Kevin Schmidt's writeup.

3.1 1-body spin-isospin operators

Here the idea is we want to calculate expectation values like

$$\left\langle \sum_i \mathcal{O}_i \right\rangle = \frac{\langle \Phi | \sum_i \mathcal{O}_i | R, S \rangle}{\langle \Phi | R, S \rangle}. \quad (13)$$

Now let's expand this the numerator term

$$\langle \Phi | \sum_i \mathcal{O}_i | R, S \rangle = \langle \Phi | \sum_i \mathcal{O}_i | R, s_1, \dots, s_A \rangle \quad (14)$$

$$= \langle \Phi | \sum_i \sum_{s=1}^4 |s\rangle \langle s| \mathcal{O}_i | R, s_1, \dots, s_A \rangle \quad (15)$$

$$= \langle \Phi | \sum_i \sum_{s=1}^4 \langle s | \mathcal{O}_i | s_i \rangle | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_A \rangle \quad (16)$$

$$= \langle \Phi | \sum_i \sum_{s=1}^4 \alpha_{is} | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_A \rangle \quad (17)$$

$$= \sum_i \sum_{s=1}^4 \alpha_{is} \langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_A \rangle \quad (18)$$

$$= \sum_i \sum_{s=1}^4 \alpha_{is} \text{d1b}(s, i) \langle \Phi | R, S \rangle, \quad (19)$$

where $\alpha_{is} = \langle s | \mathcal{O}_i | s_i \rangle$ and $\text{d1b}(s, i) = \langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_A \rangle / \langle \Phi | R, s_1, \dots, s_A \rangle$. Rearranging this we can get the expectation value

$$\left\langle \sum_i \mathcal{O}_i \right\rangle = \sum_i \sum_{s=1}^4 \alpha_{is} \text{d1b}(s, i). \quad (20)$$

Notice that when you match the notation we have

$$\text{d1b}(s, i) = \langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_A \rangle \langle \Phi | R, s_1, \dots, s_A \rangle \quad (21)$$

$$= \sum_k \langle k | r_i, s \rangle \langle k | r_i, s_i \rangle \quad (22)$$

$$= \sum_k S_{ik}^{-1} \langle k | r_i, s \rangle \quad (23)$$

$$= \text{sxz}(s, i, i). \quad (24)$$

3.2 2-body spin-isospin operators

Here the idea is we want to calculate expectation values like

$$\left\langle \sum_{i<j} \mathcal{O}_{ij} \right\rangle = \frac{\langle \Phi | \sum_{i<j} \mathcal{O}_{ij} | R, S \rangle}{\langle \Phi | R, S \rangle}. \quad (25)$$

Now let's expand this the numerator term

$$\langle \Phi | \sum_{i<j} \mathcal{O}_{ij} | R, S \rangle = \langle \Phi | \sum_{i<j} \mathcal{O}_{ij} | R, s_1, \dots, s_A \rangle \quad (26)$$

$$= \langle \Phi | \sum_{i<j} \sum_{s=1}^4 \sum_{s'=1}^4 |s\rangle \langle s|s'\rangle \langle s' | \mathcal{O}_{ij} | R, s_1, \dots, s_A \rangle \quad (27)$$

$$= \langle \Phi | \sum_{i<j} \sum_{s=1}^4 \sum_{s'=1}^4 \langle s, s' | \mathcal{O}_{ij} | s_i, s_j \rangle | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_{j-1}, s', s_{j+1}, \dots, s_A \rangle \quad (28)$$

$$= \langle \Phi | \sum_{i<j} \sum_{s=1}^4 \sum_{s'=1}^4 \alpha_{ijs} | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_{j-1}, s', s_{j+1}, \dots, s_A \rangle \quad (29)$$

$$= \sum_{i<j} \sum_{s=1}^4 \sum_{s'=1}^4 \alpha_{ijs} \langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_{j-1}, s', s_{j+1}, \dots, s_A \rangle \quad (30)$$

$$= \sum_{i<j} \sum_{s=1}^4 \sum_{s'=1}^4 \alpha_{ijs} \text{d2b}(s, s', ij) \langle \Phi | R, S \rangle, \quad (31)$$

where $\alpha_{ijs} = \langle s, s' | \mathcal{O}_{ij} | s_i, s_j \rangle$ and

$$\text{d2b}(s, s', ij) = \langle \Phi | R, s_1, \dots, s_{i-1}, s, s_{i+1}, \dots, s_{j-1}, s', s_{j+1}, \dots, s_A \rangle / \langle \Phi | R, s_1, \dots, s_A \rangle. \quad (32)$$

Rearranging this we can get the expectation value

$$\left\langle \sum_{ij} \mathcal{O}_{ij} \right\rangle = \sum_{ij=1}^{((A-1)A)/2} \sum_{s=1}^4 \sum_{s'=1}^4 \alpha_{ijs} \text{d2b}(s, s', ij), \quad (33)$$

and where the sum, $\sum_{ij}^{((A-1)A)/2}$ is essentially doing the same thing as $\sum_{i=1}^{A-1} \sum_{j=i+1}^A$ or $\sum_{i<j}$. Notice again that we have

$$\text{d2b}(s, s', ij) = \det \begin{pmatrix} \text{sxz}(s, i, i) & \text{sxz}(s, i, j) \\ \text{sxz}(s', j, i) & \text{sxz}(s', j, j) \end{pmatrix} = \text{sxz}(s, i, i) \text{sxz}(s', j, j) - \text{sxz}(s, i, j) \text{sxz}(s', j, i). \quad (34)$$

You can see this if you notice that

$$\text{d2b}(s, s', ij) = \frac{\det(S''(s))}{\det(S)} = \det(S''(s)S^{-1}). \quad (35)$$

Now comparing this to equation 12 and noting that since the two matrices only differ by columns i and j , you can see that the determinant of the product, $\text{d2b}(s, s', ij)$, is just the determinant of the submatrix.

3.3 Inverse Update

Now in cases where we have two set's of operators like for example when we need to calculate the expectation value of the potential, there is the correlation operator and the potential operators. One of the operators is handled in the inner loop while the other is handled in a more outer loop. We can include the second operator (set of operators) in the same way that the operators were included above except that we will now need the inverse of the new Slater Matrix, S'^{-1} . To do this we need to update $\text{sxz}(s, i, j)$. The new sxz will be called sxzi and is shown here

$$\text{sxzi}(s, n, m) = \sum_k S'^{-1}_{mk} S'_{kn}(s), \quad (36)$$

where

$$S'_{kn}(s) = \begin{cases} \langle k | r_m, s \rangle & n \neq i \\ \langle k | \mathcal{O}_i | r_i, s \rangle & n = i. \end{cases} \quad (37)$$

For example assume we needed to get something like

$$\langle R, S | \left(\sum_{i < j} v_{ij} \right) \left(1 + \sum_{i < j} \sum_p \mathcal{O}_{ij}^p \right) | \Phi \rangle, \quad (38)$$

where the first operator is part of the potential and the second is the correlation operator. I have left off any operators that don't depend on the spin. Now let's look at a single set of pairs for only one of the p operators. This would look like

$$\langle R, S | v_{ij} (1 + \mathcal{O}_{kl}) | \Phi \rangle = \det(S'') + \det(S'''), \quad (39)$$

where the number of primes is the number of changed columns (unless i or j was equal to k or l).

4 Breakup of correlation operator in Cartesian

Here I am going to show how we have broken up the correlation operator in Cartesian coordinates. The correlation operator is

$$\sum_{p=1}^6 f^p(r_{ij}) \mathcal{O}_{ij}^p \quad (40)$$

where here I'm going to drop the subscripts ij and the argument (r_{ij}) . Here I am going to break these up into Cartesian components. The first three are simple.

$$\mathcal{O}^1 = f^1 \quad (41)$$

$$\mathcal{O}^2 = f^2 \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j = f^2 \tau_{i\gamma} \tau_{j\gamma} \quad (42)$$

So the first piece of the breakup comes from the $\tau_{i\gamma} \tau_{j\gamma}$ term. The next two come from sums and terms so I will try to show those here.

$$\mathcal{O}^3 = f^3 \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j = f^3 \sigma_{i\alpha} \sigma_{j\alpha} \quad (43)$$

$$\mathcal{O}^5 = f^5 (3 \boldsymbol{\sigma}_i \cdot \hat{r}_{ij} \boldsymbol{\sigma}_j \cdot \hat{r}_{ij} - \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j) = f^5 3 \sigma_{i\alpha} r_\alpha \sigma_{j\beta} r_\beta - f^5 \sigma_{i\alpha} \sigma_{j\alpha} \quad (44)$$

$$\mathcal{O}^3 + \mathcal{O}^5 = f^3 \sigma_{i\alpha} \sigma_{j\alpha} + f^5 3 \sigma_{i\alpha} r_\alpha \sigma_{j\beta} r_\beta - f^5 \sigma_{i\alpha} \sigma_{j\alpha} \quad (45)$$

$$= \sigma_{i\alpha} \sigma_{j\beta} [(f^3 - f^5) \delta_{\alpha\beta} + f^5 3 r_\alpha r_\beta] \quad (46)$$

This is the $\sigma_{i\alpha} \sigma_{j\beta}$ breakup term. The last term is

$$\mathcal{O}^4 = f^4 \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j = f^4 \sigma_{i\alpha} \sigma_{j\alpha} \tau_{i\gamma} \tau_{j\gamma} \quad (47)$$

$$\mathcal{O}^6 = f^6 (3 \boldsymbol{\sigma}_i \cdot \hat{r}_{ij} \boldsymbol{\sigma}_j \cdot \hat{r}_{ij} - \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j) (\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j) = f^6 3 \sigma_{i\alpha} r_\alpha \sigma_{j\beta} r_\beta \tau_{i\gamma} \tau_{j\gamma} - f^6 \sigma_{i\alpha} \sigma_{j\alpha} \tau_{i\gamma} \tau_{j\gamma} \quad (48)$$

$$\mathcal{O}^4 + \mathcal{O}^6 = f^4 \sigma_{i\alpha} \sigma_{j\alpha} \tau_{i\gamma} \tau_{j\gamma} + f^6 3 \sigma_{i\alpha} r_\alpha \sigma_{j\beta} r_\beta \tau_{i\gamma} \tau_{j\gamma} - f^6 \sigma_{i\alpha} \sigma_{j\alpha} \tau_{i\gamma} \tau_{j\gamma} \quad (49)$$

$$= \sigma_{i\alpha} \sigma_{j\beta} \tau_{i\gamma} \tau_{j\gamma} [(f^4 - f^6) \delta_{\alpha\beta} + f^6 3 r_\alpha r_\beta] . \quad (50)$$

The $\sigma_{i\alpha} \sigma_{j\beta} \tau_{i\gamma} \tau_{j\gamma}$ term is the third term in the breakup. These three terms together require 39 operations. $\tau_{i\gamma} \tau_{j\gamma}$ requires 3, $\sigma_{i\alpha} \sigma_{j\beta}$ 9, and $\sigma_{i\alpha} \sigma_{j\beta} \tau_{i\gamma} \tau_{j\gamma}$ 27, where the α, β and γ are summer over the three Cartesian coordinates and i and j refer to particles.

5 V6 Potential

Now let's look at the v6 potential, which is

$$V = \sum_{i < j} \sum_p v_p(r_{ij}) \mathcal{O}_{ij}^p, \quad (51)$$

where the \mathcal{O}_{ij}^p are given by the same six operators discussed in the trial wave function correlations above. Now let's look at equations 41, 42, 46, and 50. Using these but changing the f 's to v 's we can write

$$V = V_c + \frac{1}{2} \sum_{ij} \sum_{\alpha} \tau_{i\alpha} A_{ij}^{\tau} \tau_{j\alpha} + \frac{1}{2} \sum_{ij} \sum_{\alpha\beta} \sigma_{i\alpha} A_{ij\alpha\beta}^{\sigma} \sigma_{j\beta} + \frac{1}{2} \sum_{ij} \sum_{\alpha\beta} \sigma_{i\alpha} \tau_{i\alpha} A_{ij\alpha\beta}^{\sigma\tau} \tau_{j\alpha} \sigma_{j\beta}, \quad (52)$$

where

$$V_c = \sum_{i < j} u_{ij}^1 \quad (53)$$

$$A_{ij}^\tau = u_{ij}^2 \quad (54)$$

$$A_{ij\alpha\beta}^\sigma = (u_{ij}^3 - u_{ij}^5)\delta_{\alpha\beta} + u_{ij}^5 3r_{ij}^\alpha r_{ij}^\beta \quad (55)$$

$$A_{ij\alpha\beta}^{\sigma\tau} = (u_{ij}^4 - u_{ij}^6)\delta_{\alpha\beta} + u_{ij}^6 3r_{ij}^\alpha r_{ij}^\beta, \quad (56)$$

and the $1/2$'s come from the fact that we are not summing over all i and j , not just $i < j$. Now we can diagonalize these matrices (find their eigenvalues and eigenvectors). and rewrite V in terms of those.

$$\sum_j A_{ij}^\tau \psi_j^{\tau n} = \lambda_n^\tau \psi_i^{\tau n} \quad (57)$$

$$\sum_{j\beta} A_{ij\alpha\beta}^\sigma \psi_j^{\sigma n} = \lambda_n^\sigma \psi_i^{\sigma n} \quad (58)$$

$$\sum_{j\beta} A_{ij\alpha\beta}^{\sigma\tau} \psi_j^{\sigma\tau n} = \lambda_n^{\sigma\tau} \psi_i^{\sigma\tau n}. \quad (59)$$

And since we know that the eigenvectors are orthogonal we know that

$$\sum_j \psi_j^n \psi_j^m = \delta_{nm}, \quad (60)$$

we can rewrite the A matrices as

$$\sum_j A_{ij}^\tau \psi_j^{\tau n} \psi_j^{\tau m} = \lambda_n^\tau \psi_i^{\tau n} \psi_j^{\tau m} \quad (61)$$

$$A_{ij}^\tau \delta_{nm} = \lambda_n^\tau \psi_i^{\tau n} \psi_j^{\tau m} \quad (62)$$

$$A_{ij}^\tau = \sum_n \psi_i^{\tau n} \lambda_n^\tau \psi_j^{\tau n}, \quad (63)$$

and similarely

$$A_{ij}^\sigma = \sum_{n\alpha} \psi_{i\alpha}^{\sigma n} \lambda_n^\sigma \psi_{j\alpha}^{\sigma n} \quad (64)$$

$$A_{ij}^{\sigma\tau} = \sum_{n\alpha} \psi_{i\alpha}^{\sigma\tau n} \lambda_n^{\sigma\tau} \psi_{j\alpha}^{\sigma\tau n}. \quad (65)$$

This allows us to rewrite the potential as

$$\begin{aligned} V &= V_c \\ &+ \frac{1}{2} \sum_{ij} \sum_{\alpha} \sum_n \tau_{i\alpha} \psi_i^{\tau n} \lambda_n^\tau \psi_j^{\tau n} \tau_{j\alpha} \\ &+ \frac{1}{2} \sum_{ij} \sum_{\alpha\beta} \sum_n \sigma_{i\alpha} \psi_{i\alpha}^{\sigma n} \lambda_n^\sigma \psi_{j\beta}^{\sigma n} \sigma_{j\beta} \\ &+ \frac{1}{2} \sum_{ij} \sum_{\alpha\beta} \sum_n \sigma_{i\alpha} \tau_{i\alpha} \psi_{i\alpha}^{\sigma\tau n} \lambda_n^{\sigma\tau} \psi_{j\beta}^{\sigma\tau n} \tau_{j\alpha} \sigma_{j\beta}. \end{aligned} \quad (66)$$

Now if you write

$$\mathcal{O}_{n\alpha}^\tau = \sum_i \psi_i^{\tau n} \tau_{i\alpha} \quad (67)$$

$$\mathcal{O}_n^\sigma = \sum_{i\alpha} \psi_{i\alpha}^{\sigma n} \sigma_{i\alpha} \quad (68)$$

$$\mathcal{O}_{n\alpha}^{\sigma\tau} = \sum_{i\alpha} \psi_{i\alpha}^{\sigma\tau n} \sigma_{i\alpha} \tau_{i\alpha}, \quad (69)$$

we can then write the potential as

$$V = V_c + \frac{1}{2} \sum_{\alpha=1}^3 \sum_{n=1}^A \lambda_n^\tau (\mathcal{O}_{n\alpha}^\tau)^2 + \frac{1}{2} \sum_{n=1}^{3A} \lambda_n^\sigma (\mathcal{O}_n^\sigma)^2 + \frac{1}{2} \sum_{\alpha=1}^3 \sum_{n=1}^{3A} \lambda_n^{\sigma\tau} (\mathcal{O}_{n\alpha}^{\sigma\tau})^2. \quad (70)$$

Now once we are here with the v6 potential we can then use the Hubbard-Stratanovich transformation to linearise these quadratic operators once they are in the exponential for the propogators. The Hubbard-Stratanovich transformation is

$$e^{\frac{\mathcal{O}^2}{2}} = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{\infty} dx e^{-\frac{x^2}{2} + x\mathcal{O}} \quad (71)$$

References

- [1] S. Gandolfi, A. Lovato, J. Carlson, and Kevin E. Schmidt. From the lightest nuclei to the equation of state of asymmetric nuclear matter with realistic nuclear interactions. 2014. arXiv:1406.3388v1 [nucl-th].