

ECE 250 Algorithms and Data Structures

Lab 1: Linked Lists

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Outline

- List and Node Classes
- The Constructor
- Simple Function Definitions
- Push Front Definition
- Pop Front Definition
- Stepping through Linked Lists
- The Destructor
- Assignment and Copy Constructor
- Summary

List and Node Classes

- A linked list is a container where each object is stored in separate node
- Each node must, in addition to storing an object, must also include a reference/pointer to the next node
 - In C++, this is the address of the next node

Lab 1: Linked Lists

List and Node Classes

- We must dynamically create the nodes in a linked list
- Thus, because new returns a pointer, the logical manner in which to track a linked lists is through a pointer
- A Node class must store the data object and a reference to the next node (also a pointer)

The Node Class

- The node must store an object and a pointer:
 - In this case, the object is an integer

```
class Node {
   private:
        int
              element;
        Node *next_node;
   public:
        Node( int = 0, Node * = 0 );
        int retrieve() const;
        Node *next() const;
};
    In Project 1, the type is given by the template:
        Object element;
```

Lab 1: Linked Lists

The Node Class

 The constructor assigns the two member variables based on the arguments

```
Node::Node( int e, Node *n ):element( e ), next_node( n ) {
    // empty constructor
}
```

The default values for both arguments are both 0

The Node Class

 The two member functions are accessors which simply return the element and the next_node member variables, respectively

```
int Node::retrieve() const {
    return element;
}

Node *Node::next() const {
    return next_node;
}
```

Project 1 – Creating your VS Project

- Create a VS project name P1(type is c++, General)
- Add source code provided for P1, in course web page.
 - Start by solving part a) Single List
 - Files needed in the VS project :
 - Ece250.h
 Exception.h
 Tester.h
 From Common
 Source Files
 - Single_list.h
 - Single_node.h
 - Single_node_tester.h
 - Single_list_tester.h
 - Single_list_driver.cpp

Project 1 – Creating your VS Project

- Compile your VS Project as given. It should compile without errors.
- Complete class Single_node.h
- Questions about C++ syntax so far?
 - Template classes
 - Friend classes
 - Constructor, initializing values

The List Class

- Because each node in a linked list refers to the next, the linked list class needs to store the address of the first node
 - This requires one member variable: a pointer to a node

```
class List {
    private:
        Node *list_head;
    // ...
};
```

The List Class

This is the class definition:

```
class List {
    private:
        Node *list head;
    public:
        List();
        // Accessors
        bool empty() const;
        int front() const;
        Node * head() const;
        int count( int ) const;
        // Mutators
        void push_front( int );
        int pop_front();
        int erase( int );
};
```

Lab 1: Linked Lists

The List Class

 This is the class in your project 1 – very similar but not the same:

```
template <typename Object>
class Single_list {
private:
   Single_node<Object> *list_head;
   Single_node<Object> *list_tail; I
   int node_count;
```

- To begin, let us look at the internal representation of a linked list
- Suppose we want a linked list to store the values

```
42 95 70 81
```

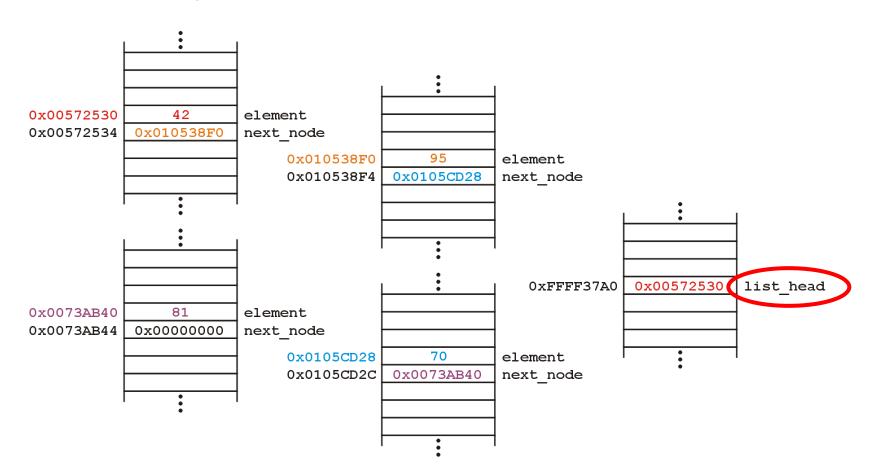
in this order

This could be the result of:

```
int main() {
    List ls;
    ls.push_front( 81 );
    ls.push_front( 70 );
    ls.push_front( 95 );
    ls.push_front( 42 );
    return 0;
}
```

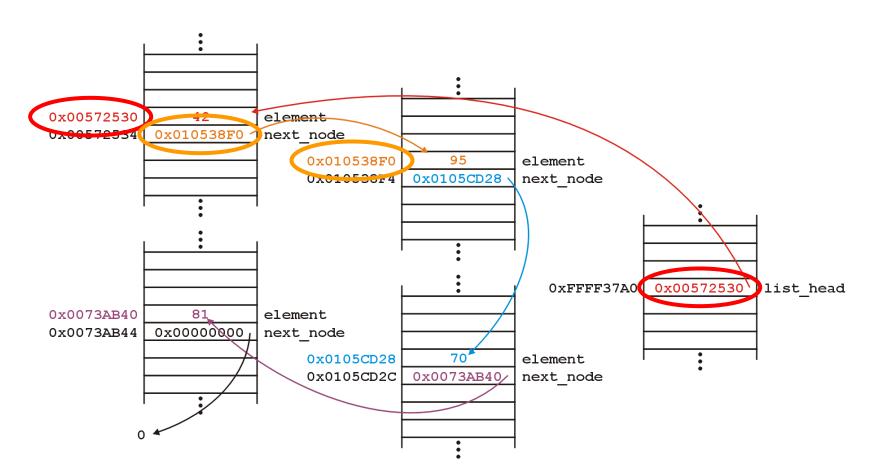
Lab 1: Linked Lists

- These nodes could be stored anywhere in memory:
 - For example,



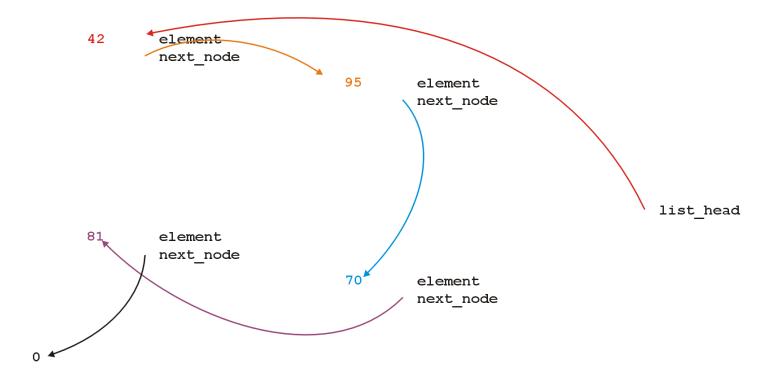
Lab 1: Linked Lists

 Notice how each next_node address points to the next node in the list?



Lab 1: Linked Lists

 Because the addresses are arbitrary, we can remove that information:



We will clean up the representation as follows:



- We do not specify the addresses because they are arbitrary and:
 - The contents of the circle is the stored object
 - The next_node pointer is represented by an arrow

Operations on Linked Lists

- First, we want to create a linked list
- We also want to be able to:

Operations on the entire linked list may include:

```
Membership int count(int) const;Erase an object int erase(int);
```

 Additionally, we may wish to check the state: is the linked list empty?

```
bool empty() const;
```

Lab 1: Linked Lists

The Constructor

- The constructor initializes the linked list
- We do not count how may objects are in this list, thus:
 - We must rely on the last pointer in the linked list to point to a special value
 - In C++, we use 0 (the zero address)

The Constructor

Thus, in the constructor, we assign 0 to list_head:

```
List::List():list_head( 0 ) {
    // empty constructor
}
```

 We will always ensure that when a linked list is empty, the list head is assigned @

Starting with the easier member functions:

```
bool List::empty() const {
    if ( list_head == 0 ) {
        return true;
    } else {
        return false;
or better yet:
bool List::empty() const {
    return ( list_head == 0 );
```

 The member function Node *head() const is easy enough to implement:

```
Node *List::head() const {
    return list_head;
}
```

This will always work: if the list is empty, it will return 0

- To get the first element in the linked list, we must access the node to which the list_head is pointing
- Because we have a pointer, we must use the -> operator to call the member function:

```
int List::front() const {
    return head()->retrieve();
}
```

- The member function int front() const requires some additional consideration, however:
 - What if the list is empty?
- If we tried to access a member function of a pointer set to 0, we would access restricted memory
- The operating system would terminate the running program

- Instead, we can use an exception handling mechanism where we throw an exception
- We define a class

```
class underflow {
    // emtpy
};

and then we throw an instance of this class:
    throw underflow();
```

Thus, the full function is

```
int List::front() const {
    if ( empty() ) {
        throw underflow();
    }

    return head()->retrieve();
}
```

Why is emtpy() better than

```
int List::front() const {
    if ( list_head == 0 ) {
        throw underflow();
    }

    return head()->retrieve();
}
```

- Two benefits:
 - more readable
 - if the implementation changes we do nothing

- Next, let us add an element to the list
- If it is empty, we start with:

and, if we try to add 81, we should end up with:

Lab 1: Linked Lists

Push Front Definition

- To visualize what we must do:
 - We must create a new node which stores:
 - The value 81, and
 - The address (pointer) 0
 - We must then assign its address to list_head
- We can do this as follows:

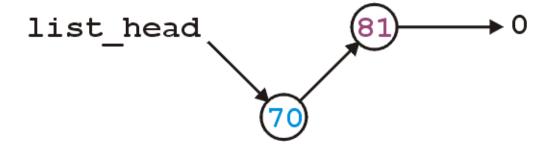
```
list head = new Node( 81, 0 );
```

We could also use the default value...

Lab 1: Linked Lists

Suppose however, we already have a non-empty list

Adding 70, we want:



Lab 1: Linked Lists

Push Front Definition

- To achieve this, we must we must create a new node which stores:
 - The value 70, and
 - The address of the current list head
 - We must then assign its address to list_head
- We can do this as follows:

```
list_head = new Node( 70, list_head );
```

Thus, our implementation could be:

```
void List::push_front( int n ) {
    if ( empty() ) {
        list_head = new Node( n, 0 );
    } else {
        list_head = new Node( n, list_head );
    }
}
```

We could, however, note that when the list is empty,
 list_head == 0, thus we could shorten this to:

```
void List::push_front( int n ) {
    list_head = new Node( n, list_head );
}
```

Are we allowed to do this?

```
void List::push_front( int n ) {
    list_head = new Node( n, list_head );
}
```

- Yes: the right-hand side of an assignment statement is evaluated first
- The original value of list_head is accessed first before the function call is made

Lab 1: Linked Lists

Pop Front Definition

- Removing from the linked list may appear easier:
 - We simply assign the list head to the next pointer of the first node
- Graphically, given:



we want:



Pop Front Definition

Easy enough:

```
int List::pop_front() {
    list_head = list_head->next();
}
```

- Unfortunately, we have some problems:
 - We want to return the item stored
 - The list may be empty
 - We still have the memory allocated for the node containing 70

Pop Front Definition

We could try:

```
int List::pop_front() {
    if ( empty() ) {
        throw underflow();
    }

int e = front();
    delete list_head;
    list_head = list_head -> next();
    return e;
}
```

Let's examine this...

```
int List::pop_front() {
   if ( empty() ) {
        throw underflow();
                          list head
    int e = front();
                          e = 70
    delete list_head;
    list_head = list_head->next();
    return e;
```

```
int List::pop_front() {
    if ( empty() ) {
        throw underflow();
    int e = front();
                           list head
    delete list_head;
                          e = 70
    list_head = list_head->next();
    return e;
```

```
int List::pop_front() {
   if ( empty() ) {
        throw underflow();
    int e = front();
    delete list_head;
    list_head = list_head->next();
                          list head
    return e;
                          e = 70
```

- The problem is, we are accessing a node which we have just deleted
- Unfortunately, this will work more than 99% of the time:
 - the running program (process) may still own the memory
- Once in a while it will fail ...
 - ... and it will be almost impossible to debug

Pop Front Definition

 The correct implementation assigns a temporary pointer to point to the node being deleted:

```
int List::pop front() {
    if ( empty() ) {
          throw underflow();
    int e = front();
    Node *ptr = list head;
    list_head = list_head->next();
    delete ptr;
    return e;
```

```
int List::pop_front() {
    if ( empty() ) {
          throw underflow();
                            list head -
   int e = front();
                            e = 70
                            ptr
   Node *ptr = list_head;
   list_head = list_head->next();
   delete ptr;
   return e;
```

```
int List::pop_front() {
    if ( empty() ) {
          throw underflow();
    int e = front();
                            list head -
    Node *ptr = list_head;
                            e = 70
                            ptr
    list_head = list_head->next();
    delete ptr;
    return e;
```

```
int List::pop_front() {
    if ( empty() ) {
          throw underflow();
    int e = front();
    Node *ptr = list head;
    list_head = list_head->next();
                            list head
    delete ptr;
                            e = 70
                            ptr
    return e;
```

```
int List::pop_front() {
    if ( empty() ) {
          throw underflow();
    int e = front();
    Node *ptr = list head;
    list_head = list_head->next();
                            list head
   delete ptr;
                            e = 70
                            ptr
    return e;
```

Project 1: Linked List – Accessors and push_front

- Notice that the constructor is given to you
- Complete accessors in class Single_list.h (except count)

```
int size() const;
bool empty() const;
Object front() const;
Object back() const;
Single_node<Object> *head() const;
Single_node<Object> *tail() const;
```

- Complete the mutator push_front
- Test these functions using commands listed in Single_list_tester.h.

Testing

Test file with functions implemented so far, ie.

```
new
push_front 3
push_front 7
front 7
back 3
head
retrieve 7
next
retrieve 3
next0
exit
size 2
empty 0
Exit
```

- Try command "cout" to list the content of your list
- Notice file int.in. If your code passes this test you have 50 % of the total mark.

 The next step is to look at member functions which potentially require us to step through the entire list:

```
int count( int ) const;
int erase( int );
```

- For count, we will return 1 if the object was found and 0 otherwise
- For erase, we return 1 if the object was found and 0 otherwise and we will delete the node.

- The process of stepping through a linked list can be thought of as being analogous to a for loop:
 - We initialize a temporary pointer with the list head
 - We continue iterating until the pointer equals 0
 - With each step, we set the pointer to point to the next object

Thus, we have:

```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // Do something
    // - use ptr->fn() to call member functions
    // - use ptr->var to assign/access member variables
}
```

Analogously:

```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // do something
    // use ptr->fn() to call member functions
    // use ptr->var to assign/access member variables
}

for ( int i = 0; i < N; ++i ) {
    // do something
}</pre>
```

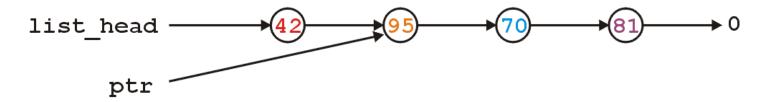
 With the initialization and first iteration of the loop, we have:



 ptr != 0 and thus we evaluate the body of the loop and then set ptr to the next node: ptr = ptr->next()

```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // Do something
}
```

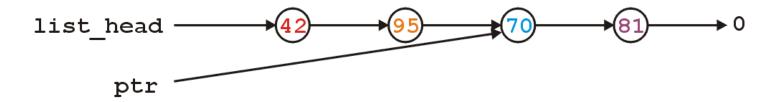
 ptr != 0 and thus we evaluate the loop and increment the pointer



In the loop, we can access 95 by using ptr->retrieve()

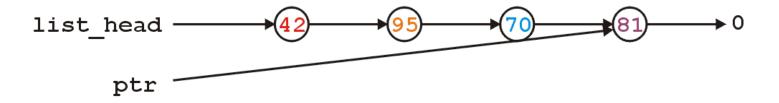
```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // Do something
}
```

 ptr != 0 and thus we evaluate the loop and increment the pointer



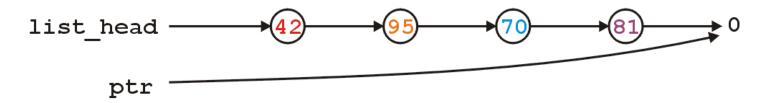
```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // Do something
}
```

 ptr != 0 and thus we evaluate the loop and increment the pointer



```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // Do something
}
```

 Here, we check and find ptr != 0 is false, and thus we exit the loop



 Because the variable ptr was declared inside the loop, we can no longer access it

```
for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
    // Do something
}
```

- To implement bool count(int) const;, we check if the argument matches the retrieved element with each step
 - If we find the argument, we return true
 - If we finish the loop, this indicates we did not find the argument:
 return false

The implementation:

```
int List::count( int n ) const {
    for ( Node *ptr = head(); ptr != 0; ptr = ptr->next() ) {
        if ( ptr->retrieve() == n ) {
            return 1;
        }
    }
    return 0;
}
```

- To erase an arbitrary element, i.e., to implement interase (int), we must update the previous node
- For example, given



if we delete 70, we want to end up with



Stepping through Linked Lists

- Notice that the erase function must modify the member variables of the node prior to the node being removed
- Thus, it must have access to the private instance variable next_node
- We could supply the member function

```
void set_next( Node * );
```

however, this would be globally accessible

- In Java/C#, you could define the Node class to be an inner class
 - this is an elegant OO solution
- In C++, you explicitly break encapsulation by declaring the class List to be a *friend* of the class Node:

```
class Node {
Node * next() const;
    // ... declaration ...
    friend class List;
};
```

- Now, inside erase (a member function of List), you can modify all the member variables of any instance of the Node class
 - Challenge for erase: you will need an additional temporary pointer when removing a node—once you update the linked list, you must delete the removed node

The Destructor

- We dynamically allocated memory each time we added a new Node into this list
- Suppose we delete a list before it is empty
 - By default, this does not clean up any of those remaining nodes
- Thus, we need to define a destructor:

```
class List {
    private:
        Node *list_head;
    public:
        List();
        ~List();
        // ...etc...
};
```

The Destructor

- The destructor has to delete any memory which was allocated with new but not yet deallocated
- This is straight-forward enough:

```
while ( !empty() ) {
    pop_front();
}
```

 The overhead of pop_front is negligible when compared to calling delete

Project 1: count, erase and destructor

- Complete count
- Test
- Complete pop_front
- Complete erase, and destructor
- Test

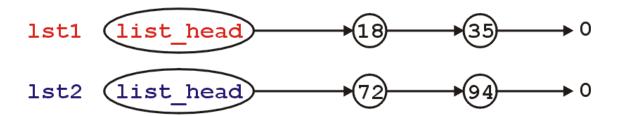
- We now have the functionality of the linked list class
- However, there are other functional operations required for linked lists to interact with C++
- Recall two common C++ operations:
 - Assignment
 - Passing by value (the copy constructor)

 Suppose you have two objects, be they linked lists or otherwise, for example:

```
List lst1;
List lst2;

lst1.push_front( 35 );
lst1.push_front( 18 );
lst2.push_front( 94 );
lst2.push_front( 72 );
```

This is the current state:



If we assign

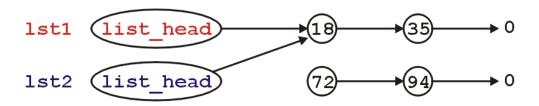
```
lst2 = lst1;
```

by default, all that occurs is that the member variables from lst1 are copied to the member variables of lst2

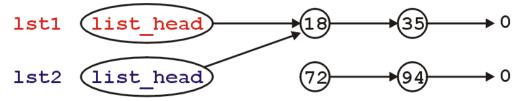
- Because the only member variable of this class is list_head, the value it is storing (the address of the first node) is copied over
- It is equivalent to writing:

```
lst2.list_head = lst1.list_head;
```

Graphically:



- What's wrong with this picture?
 - We no longer have links to either of the nodes storing 72 or 94
 - Also, suppose we call the member function lst1.pop_front();
 - This only affects the member variable from the object lst1
 - Thus, we go from

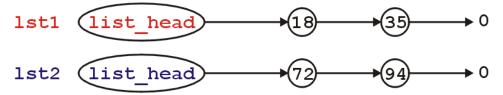


- Now, the second list 1st2 is pointing to memory which has been deallocated...
- What is the behavior is we call

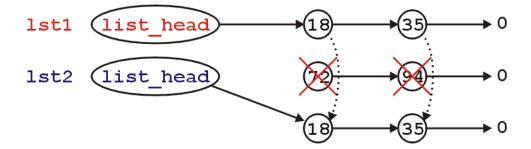
```
lst2.pop_front();
```

 The behaviour is undefined, however, soon this will probably lead to an access violation

- We need to properly implement assignment
- The logical solution would be to:
 - Delete all the nodes in 1st2
 - Copy all of the nodes in 1st1 to 1st2
 - Thus, we go from



to



- To define assignment, we must overload the function named operator=
 - This is a how you indicate to the compiler that you are overloading the = operator
- Its signature is:

```
List & operator = ( List const & );
```

 To avoid copies, the argument and return value are passed by reference

```
List &operator=( const List &rhs );
```

Because it is a reference, that means that you must referuse, for example, rhs.head() Or rhs.push front()

Because we are overwriting the current object, we must:

```
List &operator=( List const &rhs ) {
    // clean up this object
    // make a complete copy of rhs
    return *this;
}
```

 Here, the name of the argument rhs refers to the righthand side of the assignment

 To clean up the current linked list, we need to remove all nodes in this linked list:

```
List &operator=( List const &rhs ) {
    while ( !empty() ) {
        pop_front();
    }
    // Make a complete copy of rhs
    return *this;
}
```

However, we have a problem: consider

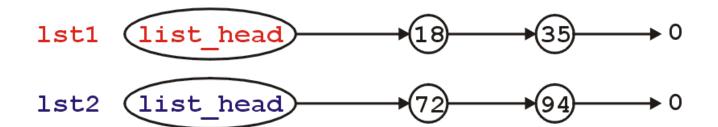
```
List a;
a.push front( 3 );
a = a;
List &operator= ( const List &rhs ) {
    while ( !empty() ) {
        pop front();
    }
    // Both rhs and *this refer to the same
    // linked list which is now empty
    // Make a complete copy of rhs
    return *this;
```

 To avoid this problem, we must always make the following check:

- To make a copy of the right hand side is a little more difficult...
- We must step through the second linked list and create a new node for each object in the rhs list

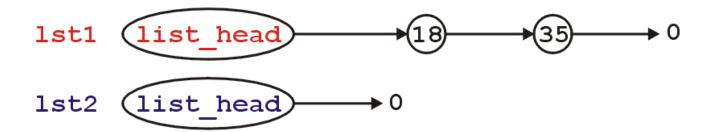
```
List &List::operator= ( const List &rhs ) {
    while ( !empty() ) {
        pop front();
    }
    if ( rhs.empty() ) {
        return * this;
    }
    list head = new Node( rhs.front() ); // copy the front element
    for ( Node * lhptr = head(), * rhptr = rhs.head();
        rhptr -> next() != 0;
        rhptr = rhptr -> next(), lhptr = lhptr -> next()
    ) {
        lhptr -> next node = new Node( rhptr -> next() -> retrieve() );
    }
    return * this;
```

- Visually, we are doing the following:
- In assigning 1st2 = 1st1;



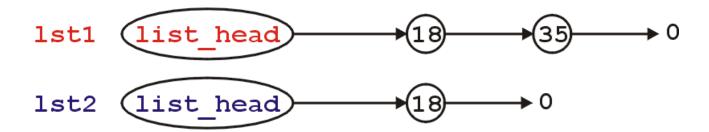
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Empty the second list:

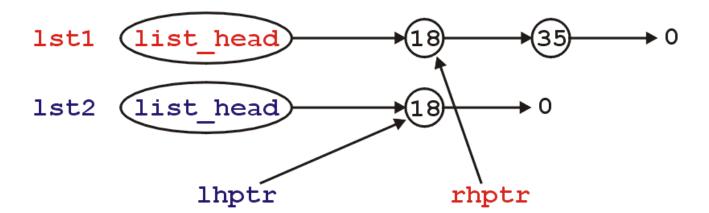


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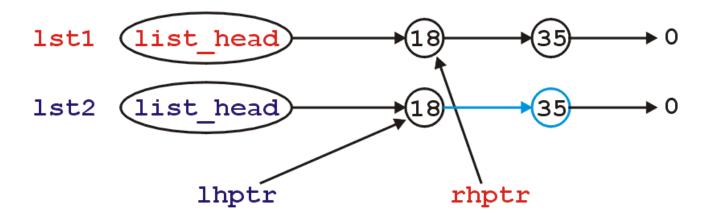
• If the 1st list is not empty, push the front element of the 1st list onto the 2nd list:



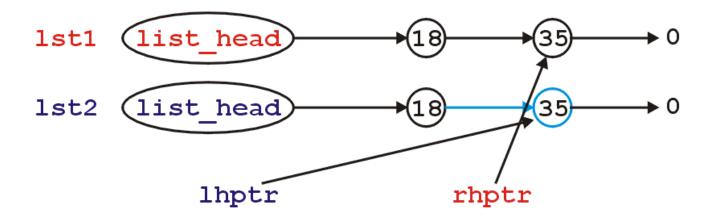
Get two pointers pointing to the first nodes in each of the lists



 While there is a node following the node pointed to by <u>rhptr</u>, add that node to the 2nd list:



 Then, increment each of the pointers and continue repeating this procedure until there are no more nodes to add



- Because in Project 1, you have a tail pointer, you can actually do this a lot more easily
- Like the member function, step through the first linked list, however, just call push_back(ptr -> retrieve()) with node in the list

- Why do we return *this?
- Suppose you have the assignment:

```
1st3 = 1st2 = 1st1;
```

- The assignment operator is right associative: it first evaluates 1st2 = 1st1;
- After this, it must assign 1st3 = ?;
- ? is whatever is returned by the assignment operation of lst2 = lst1;

- We have discussed assignment
- We must now look at a similar problem:
 - Making a copy of an already-existing object (Ex1 and Ex2 below)
 - Passing or returning by value
- These are the same problem: an object is being constructed and initialized with the value of another.

```
Ex1.
List ls1;
Ls1.push_front(57);
List ls2( ls1 );
Ex2.
List ls1;
List ls1;
Ls1.push_front(57);
List ls2 = ls1;
```

- Consider this example where a linked list is passed to a function:
 - Four values are stored in the list

```
List my_marks;
my_marks.push_front( 81 );
my_marks.push_front( 70 );
my_marks.push_front( 95 );
my_marks.push_front( 42 );

my_marks.list_head

cout << average( my_marks );

42 +95 +70 +81 +66
```

```
int average( List ls ) {
   int n = 0, sum = 0;
   while ( !ls.empty() ) {
      sum += ls.pop_front();
      ++n;
   }
   return sum/n;
}
```

By default, pass by value copies values

```
List my_marks;
my_marks.push_front( 81 );
my_marks.push_front( 70 );
my_marks.push_front( 95 );
my_marks.push_front( 42 );
```

This includes all member wy_marks.list_head variables are copied cout << average(my_marks);
 down including pointers which are just addresses

Passed by value
- all member variables passed by value

int average(List ls) {

```
int n = 0, sum = 0;
while ( !ls.empty() ) {
    sum += ls.pop_front();
    ++n;
}
return sum/n;
```

Assignment and Copy Constructor

Now we have two my_marks.push_front(70); my_marks.push_front(95); objects which store my_marks.push_front(42); the same address in my_marks.list_heathe member variablecout << average(my_marks); list head

```
List my marks;
my marks.push front(81);
my marks.push front( 70 );
my marks.push front(95);
my marks.push front( 42 );
          my marks.list head
    int average( List ls
                  ls.list head
        int n = 0, sum = 0;
        while ( !ls.empty() ) {
            sum += ls.pop front();
            ++n;
        return sum/n;
```

Assignment and Copy Constructor

After one iteration
 of the loop, the
 pop_front function
 is called which
 deletes the first node

```
List my marks;
my marks.push front(81);
my marks.push front( 70 );
my marks.push front(95);
my marks.push_front( 42 );
           my marks.list head
cout << average( my_marks );</pre>
    int average( List ls ) {
        int n = 0, sum = 0;
        while ( !ls.empty() ) {
            sum += ls.pop_front();
            ++n;
                                 ls.list head
        return sum/n;
```

Assignment and Copy Constructor

 At the end of the function, all nodes have been deleted

```
List my marks;
my marks.push front( 81 );
my marks.push front( 70 );
my marks.push front( 95 );
my marks.push front( 42 );
           my marks.list head
cout << average( my marks );</pre>
    int average( List ls ) {
        int n = 0, sum = 0;
        while ( !ls.empty() ) {
             sum += ls.pop front();
            ++n;
                                  ls.list head
        return sum/n;
```

Assignment and Copy Constructor

 If, in the original function we now attempt to access a node, it no longer exists

```
List my_marks;
my_marks.push_front( 81 );
my_marks.push_front( 70 );
my_marks.push_front( 95 );
my_marks.push_front( 42 );

my_marks.list_head

cout << average( my_marks );
```

- We can, however, define a copy constructor
 - This function is count called whenever a copy of the object is being made

```
List my marks;
my marks.push front(81);
my_marks.push_front( 70 );
my marks.push front( 95 );
my marks.push front(42);
           my marks.list head
cout << average( my marks );</pre>
                     If a copy constructor exists, it is called
                      List::List( List const & );
    int average( List ls ) {
         int n = 0, sum = 0;
         while ( !ls.empty() ) {
             sum += ls.pop front();
             ++n;
         return sum/n;
```

Assignment and Copy Constructor

 In this case, the copy constructor should make a copy of all four nodes

```
List my_marks;
my_marks.push_front( 81 );
my_marks.push_front( 70 );
my_marks.push_front( 95 );
my_marks.push_front( 42 );

my_marks.list_head

cout << average( my_marks );

42 95 70 81 0
```

Assignment and Copy Constructor

 Any changes made to this copy do not affect the original linked list

```
int average( List ls ) {
    int n = 0, sum = 0;
    while ( !ls.empty() ) {
        sum += ls.pop_front();
        ++n;
    }
        ls.list_head
    return sum/n;
}
```

- Thus, we require a copy constructor
- This is a method called when an object is being copied, either as a result of being passed-by-value to a function or being returned-by-value from a function
- Like a constructor, you should assume the variables are not initialized
- Unlike a constructor, you are not passed arguments to the constructor, rather, you are passed a reference to the object which should be copied

 The signature of a copy constructor has a constant reference to the same class as an argument:

```
List( const List & );
```

 The implementation of the copy constructor is almost identical to that of the operator =, except you are starting with a fresh object

One simple implementation of a copy constructor is:

```
List::List( const List & lst ):list_head(0) {
    *this = lst;
}
```

- Here, all we do is:
 - initialize the array (set list_head to 0), and
 - let operator = do all the work

Summary

- First, things to remember:
 - In C++, a member function and a member variable cannot have the same name
 - Common mistakes:

```
ptr->retrieve;
list->head;
```

 Today, we looked at an example of a linked list implementation.

Summary

- The Linked List example included
 - An overview of the list and node classes
 - Operations on linked lists
 - The default constructor
 - Getting started by coding simple functions
 - Implementing push front and pop front functions
 - Functions that require stepping through linked lists
 - The required behavior of the list destructor
 - The default and required behavior of operator=
 - The need for a copy constructor

Summary

The complete class is:

```
class List {
        private:
                Node * list head;
        public:
                List();
                List( const List & );
                ~List();
                List & operator = ( const List & );
                bool empty() const;
                int front() const;
                Node * head() const;
                int count( int ) const;
                void push front( int );
                int pop front();
                int remove( int );
};
```

Project 1: assignment operator and copy constructor

- Complete = operator
- Complete copy constructor
- Test



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 - that you inform me that you are using the slides,
 - that you acknowledge my work, and
 - that you alert me of any mistakes which I made or changes which you make, and allow me the option of incorporating such changes (with an acknowledgment) in my set of slides

Sincerely,
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