```
Linear Regression - Colab
pip install ucimlrepo
     Collecting ucimlrepo
       Downloading ucimlrepo-0.0.6-py3-none-any.whl (8.0 kB)
     Installing collected packages: ucimlrepo
     Successfully installed ucimlrepo-0.0.6
!pip install hvplot
     Collecting hyplot
       Downloading hyplot-0.9.2-py2.py3-none-any.whl (1.8 MB)
                                                  - 1.8/1.8 MB 17.4 MB/s eta 0:00:00
     Requirement already satisfied: bokeh>=1.0.0 in /usr/local/lib/python3.10/dist-packages (
     Requirement already satisfied: colorcet>=2 in /usr/local/lib/python3.10/dist-packages (f
     Requirement already satisfied: holoviews>=1.11.0 in /usr/local/lib/python3.10/dist-packa
     Requirement already satisfied: pandas in /usr/local/lib/python3.10/dist-packages (from h
     Requirement already satisfied: numpy>=1.15 in /usr/local/lib/python3.10/dist-packages (f
```

Requirement already satisfied: packaging in /usr/local/lib/python3.10/dist-packages (fro Requirement already satisfied: panel>=0.11.0 in /usr/local/lib/python3.10/dist-packages Requirement already satisfied: param<3.0,>=1.12.0 in /usr/local/lib/python3.10/dist-pack Requirement already satisfied: Jinja2>=2.9 in /usr/local/lib/python3.10/dist-packages (f Requirement already satisfied: contourpy>=1 in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: pillow>=7.1.0 in /usr/local/lib/python3.10/dist-packages Requirement already satisfied: PyYAML>=3.10 in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: tornado>=5.1 in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: xyzservices>=2021.09.1 in /usr/local/lib/python3.10/dist-Requirement already satisfied: pyviz-comms>=0.7.4 in /usr/local/lib/python3.10/dist-pack Requirement already satisfied: python-dateutil>=2.8.2 in /usr/local/lib/python3.10/dist-Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: tzdata>=2022.1 in /usr/local/lib/python3.10/dist-packages Requirement already satisfied: markdown in /usr/local/lib/python3.10/dist-packages (from Requirement already satisfied: markdown-it-py in /usr/local/lib/python3.10/dist-packages Requirement already satisfied: linkify-it-py in /usr/local/lib/python3.10/dist-packages Requirement already satisfied: mdit-py-plugins in /usr/local/lib/python3.10/dist-package Requirement already satisfied: requests in /usr/local/lib/python3.10/dist-packages (from Requirement already satisfied: tqdm>=4.48.0 in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: bleach in /usr/local/lib/python3.10/dist-packages (from r Requirement already satisfied: typing-extensions in /usr/local/lib/python3.10/dist-packa Requirement already satisfied: MarkupSafe>=2.0 in /usr/local/lib/python3.10/dist-package Requirement already satisfied: six>=1.5 in /usr/local/lib/python3.10/dist-packages (from Requirement already satisfied: webencodings in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: uc-micro-py in /usr/local/lib/python3.10/dist-packages (f Requirement already satisfied: mdurl~=0.1 in /usr/local/lib/python3.10/dist-packages (fr Requirement already satisfied: charset-normalizer<4,>=2 in /usr/local/lib/python3.10/dis Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.10/dist-packages (Requirement already satisfied: urllib3<3,>=1.21.1 in /usr/local/lib/python3.10/dist-pack Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/python3.10/dist-pack Installing collected packages: hvplot Successfully installed hvplot-0.9.2

df

```
from ucimlrepo import fetch_ucirepo
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
import hvplot.pandas
from sklearn.model_selection import train_test_split
from sklearn import metrics
from sklearn.linear_model import LinearRegression
%matplotlib inline
# fetch dataset
automobile = fetch_ucirepo(id=10)
# data (as pandas dataframes)
X = automobile.data.features
y = automobile.data.targets
# metadata
#print(automobile.metadata)
# variable information
#print(automobile.variables)
df = pd.concat([X,y], axis=1)
```

	price	highway- mpg	city- mpg	peak- rpm	horsepower	compression- ratio	stroke	bore	fuel- system	en
0	13495.0	27	21	5000.0	111.0	9.0	2.68	3.47	mpfi	
1	16500.0	27	21	5000.0	111.0	9.0	2.68	3.47	mpfi	
2	16500.0	26	19	5000.0	154.0	9.0	3.47	2.68	mpfi	
3	13950.0	30	24	5500.0	102.0	10.0	3.40	3.19	mpfi	
4	17450.0	22	18	5500.0	115.0	8.0	3.40	3.19	mpfi	
200	16845.0	28	23	5400.0	114.0	9.5	3.15	3.78	mpfi	
201	19045.0	25	19	5300.0	160.0	8.7	3.15	3.78	mpfi	
202	21485.0	23	18	5500.0	134.0	8.8	2.87	3.58	mpfi	
203	22470.0	27	26	4800.0	106.0	23.0	3.40	3.01	idi	
204	22625.0	25	19	5400.0	114.0	9.5	3.15	3.78	mpfi	
205 rd	ows × 26 co	olumns								

Data Cleaning

peak-rpm horsepower

stroke bore

fuel-system

engine-size

engine-type

0

0

0

0

0

https://colab.research.google.com/drive/1IXUGKsY39nOhNykPkvcA53Rz4Qoe63cl#scrollTo=L6P5FYs4nInm&printMode=true

num-of-cylinders

compression-ratio

```
height
width
                     0
length
                     0
wheel-base
                     0
engine-location
                     0
drive-wheels
                     0
body-style
                     0
num-of-doors
                     0
aspiration
                     0
fuel-type
                     0
make
                     0
normalized-losses
symboling
                     0
dtype: int64
```

Coverting categorical types into a numerical type
from sklearn.preprocessing import LabelEncoder

categorical_columns = ['fuel-system','engine-type','engine-location','drive-wheels','body-st

label_encoder = LabelEncoder()
for column in categorical_columns:
 encoded_column_name = column + '_encoded'

df[encoded_column_name] = label_encoder.fit_transform(df[column])

df

	price	highway- mpg	city- mpg	peak- rpm	horsepower	compression- ratio	stroke	bore	fuel- system	en
0	13495.0	27	21	5000.0	111.0	9.0	2.68	3.47	mpfi	
1	16500.0	27	21	5000.0	111.0	9.0	2.68	3.47	mpfi	
2	16500.0	26	19	5000.0	154.0	9.0	3.47	2.68	mpfi	
3	13950.0	30	24	5500.0	102.0	10.0	3.40	3.19	mpfi	
4	17450.0	22	18	5500.0	115.0	8.0	3.40	3.19	mpfi	
						•••				
200	16845.0	28	23	5400.0	114.0	9.5	3.15	3.78	mpfi	
201	19045.0	25	19	5300.0	160.0	8.7	3.15	3.78	mpfi	
202	21485.0	23	18	5500.0	134.0	8.8	2.87	3.58	mpfi	
203	22470.0	27	26	4800.0	106.0	23.0	3.40	3.01	idi	
204	22625.0	25	19	5400.0	114.0	9.5	3.15	3.78	mpfi	

205 rows × 34 columns

Dropping the categorical type in the dataframe for accurat linear regression analysis
categorical_columns = ['fuel-system','engine-type','engine-location','drive-wheels','body-st
df = df.drop(columns=categorical_columns,axis=1)
df

	price	highway- mpg	city- mpg	peak- rpm	horsepower	compression- ratio	stroke	bore	engine- size	C,
0	13495.0	27	21	5000.0	111.0	9.0	2.68	3.47	130	
1	16500.0	27	21	5000.0	111.0	9.0	2.68	3.47	130	
2	16500.0	26	19	5000.0	154.0	9.0	3.47	2.68	152	
3	13950.0	30	24	5500.0	102.0	10.0	3.40	3.19	109	
4	17450.0	22	18	5500.0	115.0	8.0	3.40	3.19	136	
						•••				
200	16845.0	28	23	5400.0	114.0	9.5	3.15	3.78	141	
201	19045.0	25	19	5300.0	160.0	8.7	3.15	3.78	141	
202	21485.0	23	18	5500.0	134.0	8.8	2.87	3.58	173	
203	22470.0	27	26	4800.0	106.0	23.0	3.40	3.01	145	
204	22625.0	25	19	5400.0	114.0	9.5	3.15	3.78	141	

205 rows × 26 columns

df.dtypes

price	float64
	int64
highway-mpg	
city-mpg	int64
peak-rpm	float64
horsepower	float64
compression-ratio	float64
stroke	float64
bore	float64
engine-size	int64
num-of-cylinders	int64
curb-weight	int64
height	float64
width	float64
length	float64
wheel-base	float64
num-of-doors	float64
normalized-losses	float64
symboling	int64
fuel-system_encoded	int64
engine-type_encoded	int64

```
engine-location_encoded int64
drive-wheels_encoded int64
body-style_encoded int64
aspiration_encoded int64
fuel-type_encoded int64
make_encoded int64
dtype: object
```

df.shape

(205, 26)

df.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 205 entries, 0 to 204
Data columns (total 26 columns):

#	Column (Cotal 26 Column)	*	-Null Count	Dtype
0	price	205	non-null	float64
1	highway-mpg		non-null	int64
2	city-mpg		non-null	int64
3	peak-rpm	205	non-null	float64
4	horsepower	205	non-null	float64
5	compression-ratio	205	non-null	float64
6	stroke	205	non-null	float64
7	bore	205	non-null	float64
8	engine-size	205	non-null	int64
9	num-of-cylinders	205	non-null	int64
10	curb-weight	205	non-null	int64
11	height	205	non-null	float64
12	width	205	non-null	float64
13	length	205	non-null	float64
14	wheel-base	205	non-null	float64
15	num-of-doors	205	non-null	float64
16	normalized-losses	205	non-null	float64
17	symboling	205	non-null	int64
18	fuel-system_encoded	205	non-null	int64
19	engine-type_encoded	205	non-null	int64
20	<pre>engine-location_encoded</pre>	205	non-null	int64
21	drive-wheels_encoded	205	non-null	int64
22	body-style_encoded	205	non-null	int64
23	aspiration_encoded	205	non-null	int64
24	fuel-type_encoded	205	non-null	int64
25	make_encoded	205	non-null	int64
dtvne	es: float64(12), int64(14)		

dtypes: float64(12), int64(14)

memory usage: 41.8 KB

df.corr()

	price	price highway- price mpg city-mpg peak-rp		peak-rpm	horsepower	compression- ratio	
price	1.000000	-0.690526	-0.667449	-0.100854	0.757917	0.070990	0.
highway-mpg	-0.690526	1.000000	0.971337	-0.054257	-0.770903	0.265201	-0.
city-mpg	-0.667449	0.971337	1.000000	-0.113723	-0.803162	0.324701	-0.
peak-rpm	-0.100854	-0.054257	-0.113723	1.000000	0.130971	-0.435936	-0.
horsepower	0.757917	-0.770903	-0.803162	0.130971	1.000000	-0.205740	0.
compression-ratio	0.070990	0.265201	0.324701	-0.435936	-0.205740	1.000000	0.
stroke	0.082095	-0.043961	-0.042179	-0.066844	0.088264	0.186105	1.
bore	0.532300	-0.586992	-0.584508	-0.254761	0.575737	0.005201	-0.
engine-size	0.861752	-0.677470	-0.653658	-0.244599	0.810713	0.028971	0.
num-of-cylinders	0.687770	-0.466666	-0.445837	-0.124358	0.691208	-0.020002	0.
curb-weight	0.820825	-0.797465	-0.757414	-0.266283	0.750968	0.151362	0.
height	0.134388	-0.107358	-0.048640	-0.320602	-0.110137	0.261214	-0.
width	0.728699	-0.677218	-0.642704	-0.219859	0.642195	0.181129	0.
length	0.682986	-0.704662	-0.670909	-0.287031	0.554434	0.158414	0.
wheel-base	0.583168	-0.544082	-0.470414	-0.360704	0.351957	0.249786	0.
num-of-doors	0.046001	-0.044213	-0.020671	-0.240295	-0.124001	0.161502	-0.
normalized-losses	0.133999	-0.178221	-0.218749	0.237748	0.203434	-0.114525	0.
symboling	-0.082201	0.034606	-0.035823	0.273679	0.071389	-0.178515	-0.
fuel- system_encoded	0.516533	-0.645659	-0.671581	0.014714	0.659120	-0.100786	0.
engine- type_encoded	0.071535	-0.078456	-0.085004	0.005592	0.010258	-0.071873	-0.
engine- location_encoded	0.331013	-0.102026	-0.153487	0.198400	0.317610	-0.019762	-0.
drive- wheels_encoded	0.576866	-0.452220	-0.449581	-0.039724	0.516936	0.127479	0.
body- style_encoded	-0.072677	-0.007170	0.031697	-0.109410	-0.152438	0.136243	-0.

aspiration_encoded	0.177285	-0.254416	-0.202362	-0.183629	0.240182	0.295541	0.
fuel-type_encoded	-0.110207	-0.191392	-0.255963	0.477060	0.165190	-0.984356	-0.
make_encoded	-0.161471	0.050022	0.053642	-0.218342	-0.053654	0.138828	-0.
26 rows × 26 columns							

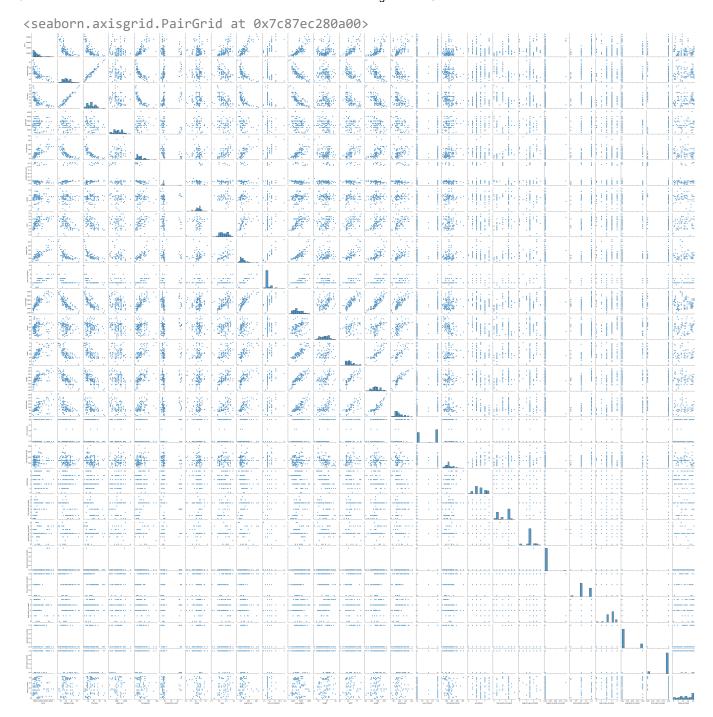
```
fig, ax = plt.subplots(figsize = (25, 10))
sns.heatmap(df.corr(), annot=True, cmap='Reds')
```

<Axes: >

VAXCS. /																										
price -	1	-0.69	-0.67	-0.1	0.76	0.071	0.082	0.53	0.86	0.69	0.82	0.13	0.73	0.68	0.58	0.046	0.13	-0.082	0.52	0.072	0.33	0.58	-0.073	0.18	-0.11	-0.16
highway-mpg -	-0.69		0.97	-0.054	-0.77	0.27		-0.59	-0.68	-0.47	-0.8	-0.11	-0.68	-0.7	-0.54	-0.044			-0.65	-0.078		-0.45		-0.25		
city-mpg -	-0.67	0.97	1	-0.11	-0.8	0.32		-0.58	-0.65	-0.45	-0.76	-0.049	-0.64	-0.67	-0.47	-0.021	-0.22		-0.67	-0.085		-0.45			-0.26	0.054
peak-rpm -	-0.1	-0.054	-0.11	1	0.13	-0.44		-0.25	-0.24	-0.12	-0.27	-0.32	-0.22	-0.29	-0.36	-0.24			0.015	0.0056		-0.04	-0.11		0.48	-0.22
horsepower -	0.76	-0.77	-0.8	0.13	1	-0.21	0.088	0.58	0.81	0.69	0.75	-0.11	0.64	0.55	0.35	-0.12	0.2	0.071	0.66	0.01	0.32	0.52			0.17	-0.054
compression-ratio -		0.27	0.32	-0.44		1	0.19	0.0052				0.26													-0.98	0.14
stroke -	0.082				0.088		1	-0.056		0.0082	0.17	-0.055	0.18	0.13	0.16				0.088	-0.14		0.072	-0.015		-0.24	-0.2
bore -	0.53	-0.59	-0.58	-0.25	0.58	0.0052		1		0.23	0.65	0.17		0.61	0.49	0.11			0.48	0.029		0.48				0.25
engine-size -		-0.68	-0.65	-0.24	0.81	0.029		0.58		0.85	0.85	0.067	0.74	0.68	0.57	0.017			0.51	0.041		0.52	-0.073			
num-of-cylinders -		-0.47	-0.45	-0.12	0.69	-			0.85	1	0.61	-0.014			0.34	-0.017			0.33	0.077			-	-0.048		
curb-weight -		-0.8	-0.76	-0.27	0.75	0.15		0.65	0.85	0.61	1	0.3	0.87	0.88	0.78	0.2	0.098		0.61	-0.055		0.58	0.13	0.32	-0.22	0.024
height -		-0.11	-0.049	-0.32	-0.11			0.17	0.067	-0.014	0.3	1	0.28	0.49	0.59	0.54	-0.37	-0.54	0.017	-0.13		-0.02	0.57		-0.28	0.24
width -		-0.68	-0.64	-0.22	0.64			0.56	0.74	0.55	0.87	0.28		0.84	0.8	0.2		-0.23	0.52	0.012		0.47			-0.23	
length -		-0.7	-0.67	-0.29	0.55			0.61	0.68	0.43	0.88	0.49	0.84		0.87	0.39		-0.36	0.56	-0.11		0.49			-0.21	
wheel-base -		-0.54	-0.47	-0.36	0.35			0.49	0.57	0.34	0.78	0.59	8.0	0.87	1	0.44		-0.53	0.38	-0.14		0.46	0.4	0.26	-0.31	0.079
num-of-doors -					-0.12	0.16						0.54		0.39	0.44	1	-0.36	-0.66	-0.01	-0.063		-0.1	0.68			0.16
normalized-losses -			-0.22	0.24							0.098		0.084	0.019	-0.057	-0.36	1	0.47	0.23				-0.25			-0.25
symboling -		0.035	-0.036	_	0.071				-0.11	-0.11	-0.23	-0.54	-0.23	-0.36	-0.53	-0.66	0.47	1	0.091	0.05		-0.042	-0.6	-0.06		
fuel-system_encoded		-0.65	-0.67	0.015	0.66		0.088		0.51	0.33	0.61	0.017	0.52	0.56	0.38	-0.01			1	-0.092		0.42	-0.065	0.29		
engine-type_encoded				0.0056																1		-0.12	-0.037			
engine-location_encoded - drive-wheels encoded -		-0.1 -0.45	-0.15 -0.45	-0.04	0.32 0.52	-0.02 0.13	-0.14	0.19	0.2		0.05	-0.11		-0.051 0.49	-0.19 0.46		-2.9e-17		0.11	0.11	0.15	0.15	-0.28			
body-style encoded		-0.45			-0.15			0.48	_	-0.042	0.58	-0.02 0.57	0.47	0.49	0.46	-0.1 0.68	_	-0.042 -0.6	0.42 -0.065	-0.12 -0.037	_	-0.16	-0.16 1			
aspiration encoded		-0.0072	-0.2		0.24	0.14	0.22	0.011				0.087	0.13	0.33	0.4		-0.25		0.29	-0.037	-0.28	0.066	0.063	0.063	-0.15	0.054
fuel-type encoded		-0.19	-0.26	0.48	0.24	-0.98	-0.24	-0.054			-0.22	-0.28	-0.23	-0.21	-0.31	-0.18		0.19	0.042	0.083		-0.13	-0.15	-0.4	1	-0.11
make encoded		0.05		-0.22	-0.054	_	-0.24	-			0.024		0.0038		0.079	0.16	-0.25	-0.12						0.054	-0.11	1
make_encoded		-	-			-		-		-			-		-			-	-	-	-	-		-	-	
	price	highway-mpg	city-mpg	peak-rpm	horsepower	compression-ratio	stroke	bore	engine-size	num-of-cylinders	curb-weight	height	width	length	wheel-base	num-of-doors	normalized-losses	symboling	fuel-system_encoded	engine-type_encoded	engine-location_encoded	drive-wheels_encoded	body-style_encoded	aspiration_encoded	fuel-type_encoded	make_encoded

Exploratory Data Analysis

sns.pairplot(df)



Training a Linear Regression Model

X and y arrays

Train Test Split

```
X_test.shape (62, 25)
```

Linear Regression

```
model = LinearRegression()
model.fit(X_train, y_train)

v LinearRegression
LinearRegression()
```

Model Evaluation

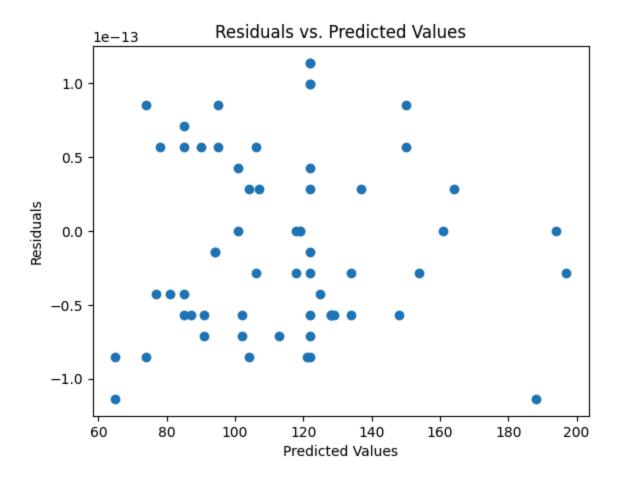
```
model.coef_
     array([-2.78263758e-15, 1.47624968e-15, -1.09236736e-16, 2.71685639e-16,
            -1.31928379e-15, -8.49612120e-15, 3.35728726e-14, 4.75795023e-16,
            1.95259003e-15, -1.54871236e-16, 1.38015749e-15, -5.92406309e-16,
            -4.87730338e-16, -6.98331142e-16, 1.11063094e-14, 1.00000000e+00,
            1.32510326e-15, -5.11506256e-16, -3.98484956e-16, -3.35745331e-16,
            2.43758464e-15, 1.28467343e-15, 1.33107585e-15, -2.04532711e-14,
            1.31877948e-16])
model.fit(X_train, y_train)
     LinearRegression
     LinearRegression()
model.coef_
     array([-2.78263758e-15, 1.47624968e-15, -1.09236736e-16, 2.71685639e-16,
            -1.31928379e-15, -8.49612120e-15, 3.35728726e-14, 4.75795023e-16,
            1.95259003e-15, -1.54871236e-16, 1.38015749e-15, -5.92406309e-16,
            -4.87730338e-16, -6.98331142e-16, 1.11063094e-14, 1.00000000e+00,
            1.32510326e-15, -5.11506256e-16, -3.98484956e-16, -3.35745331e-16,
            2.43758464e-15, 1.28467343e-15, 1.33107585e-15, -2.04532711e-14,
            1.31877948e-16])
pd.DataFrame(model.coef_, X.columns, columns=['Coeffiecients'])
```

	Coeffiecients
highway-mpg	-2.782638e-15
city-mpg	1.476250e-15
peak-rpm	-1.092367e-16
horsepower	2.716856e-16
compression-ratio	-1.319284e-15
stroke	-8.496121e-15
bore	3.357287e-14
engine-size	4.757950e-16
num-of-cylinders	1.952590e-15
curb-weight	-1.548712e-16
height	1.380157e-15
width	-5.924063e-16
length	-4.877303e-16
wheel-base	-6.983311e-16
num-of-doors	1.110631e-14
normalized-losses	1.000000e+00
symboling	1.325103e-15
fuel-system_encoded	-5.115063e-16
engine-type_encoded	-3.984850e-16
engine-location_encoded	-3.357453e-16
drive-wheels_encoded	2.437585e-15
body-style_encoded	1.284673e-15
aspiration_encoded	1.331076e-15
fuel-type_encoded	-2.045327e-14
make_encoded	1.318779e-16

Prediction from our Model

```
y_pred = model.predict(X_test)
residuals = y_test - y_pred

plt.scatter(y_pred, residuals)
plt.xlabel('Predicted Values')
plt.ylabel('Residuals')
plt.title('Residuals vs. Predicted Values')
plt.show()
```



Regression Evaluation Metrics

```
MAE = metrics.mean_absolute_error(y_test, y_pred)
MSE = metrics.mean_squared_error(y_test,y_pred)
RMSE = np.sqrt(MSE)

MAE
5.271768684671711e-14
```

MSE

3.713244622253227e-27

```
RMSE
6.093639817262937e-14

df['normalized-losses'].mean()
122.0
```

Residual Analysis

<seaborn.axisgrid.FacetGrid at 0x7c87c2a74310>