

# Algorithms & Data Structures I:

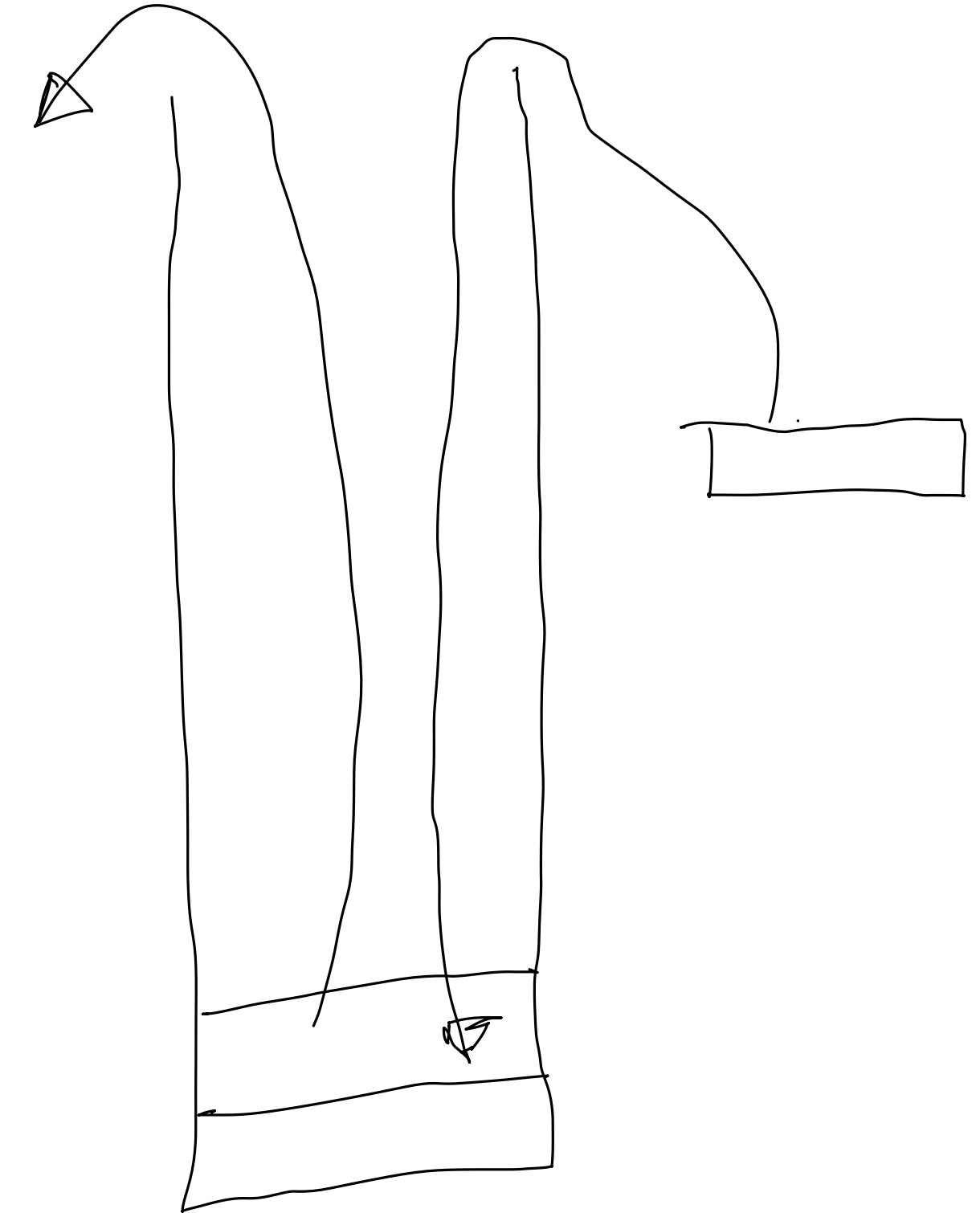
## 2\_Stack

# Today's Topics

- What a stack is
- Stack applications
- Implementation
  - Using an array
  - Using a linked list
- Keeping minimum in Stack
- Correct brackets sequence

# What a stack is

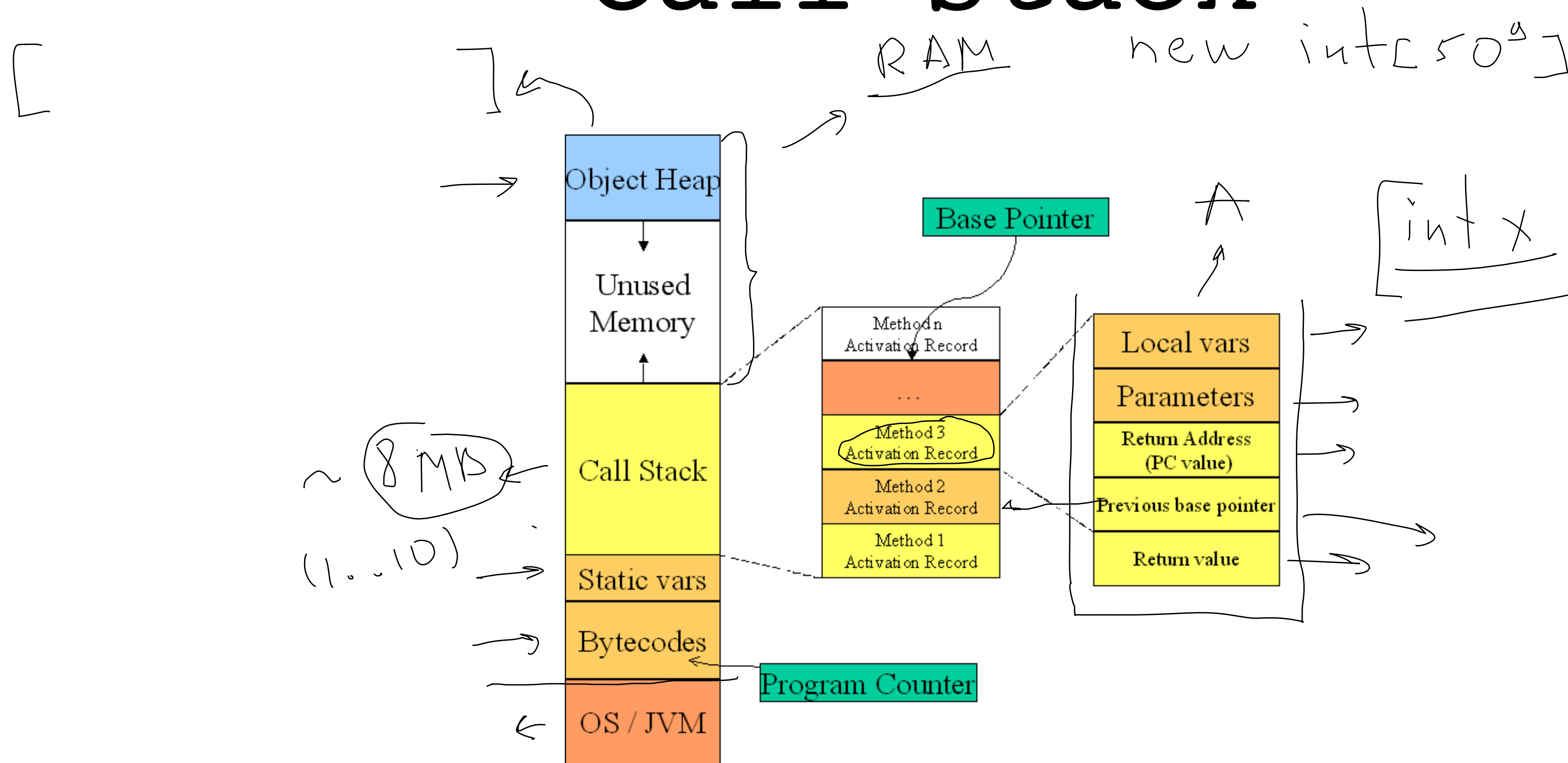
- Push(x)
  - add an element to the top
- Pop()
  - remove last added element from stack and return it
- LIFO
  - **Last In First Out**



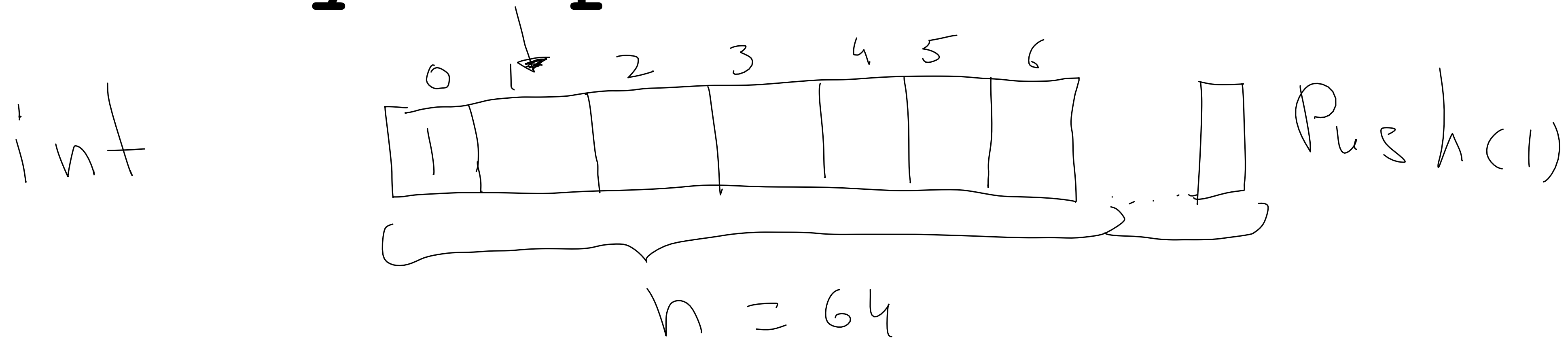
# Applications

- Operation Systems
  - Memory management
  - Function Call Stack
- Calculators
  - Expression evaluation
  - Parenthesis matching

# Call Stack



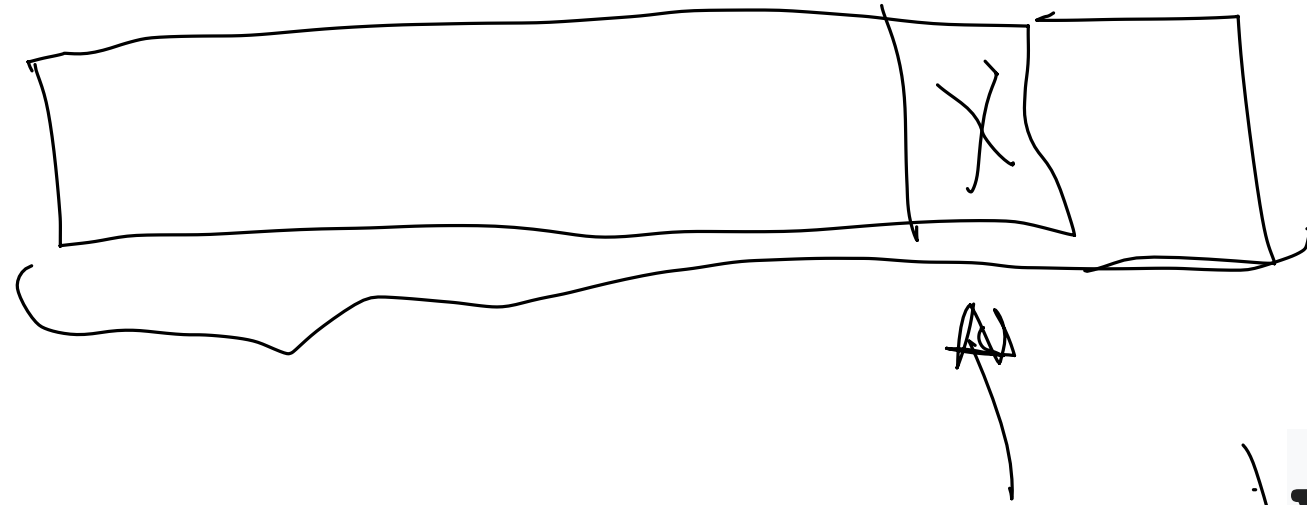
# Array Implementation Idea



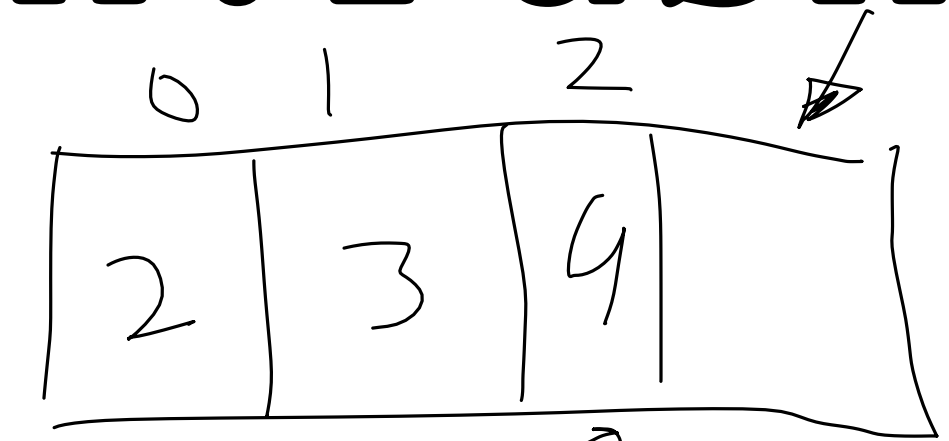
• capacity = 64

• head = 0

# Array Implementation.Push



```
void Push(x):  
    if head == capacity:  
        ExtendStack()  
    else:  
    array[head] = x  
    head = head + 1
```

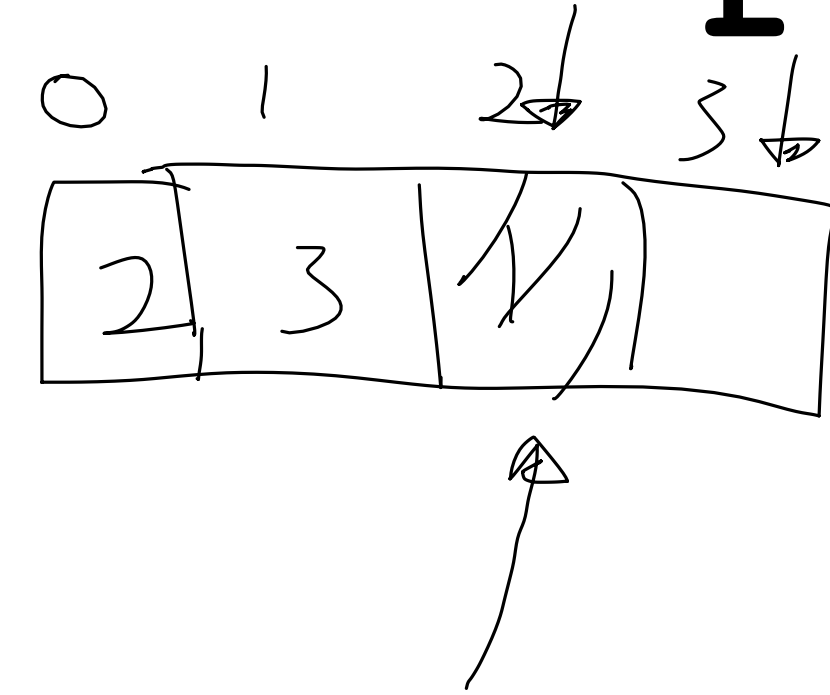


head = 2

Push(4):

head = 3

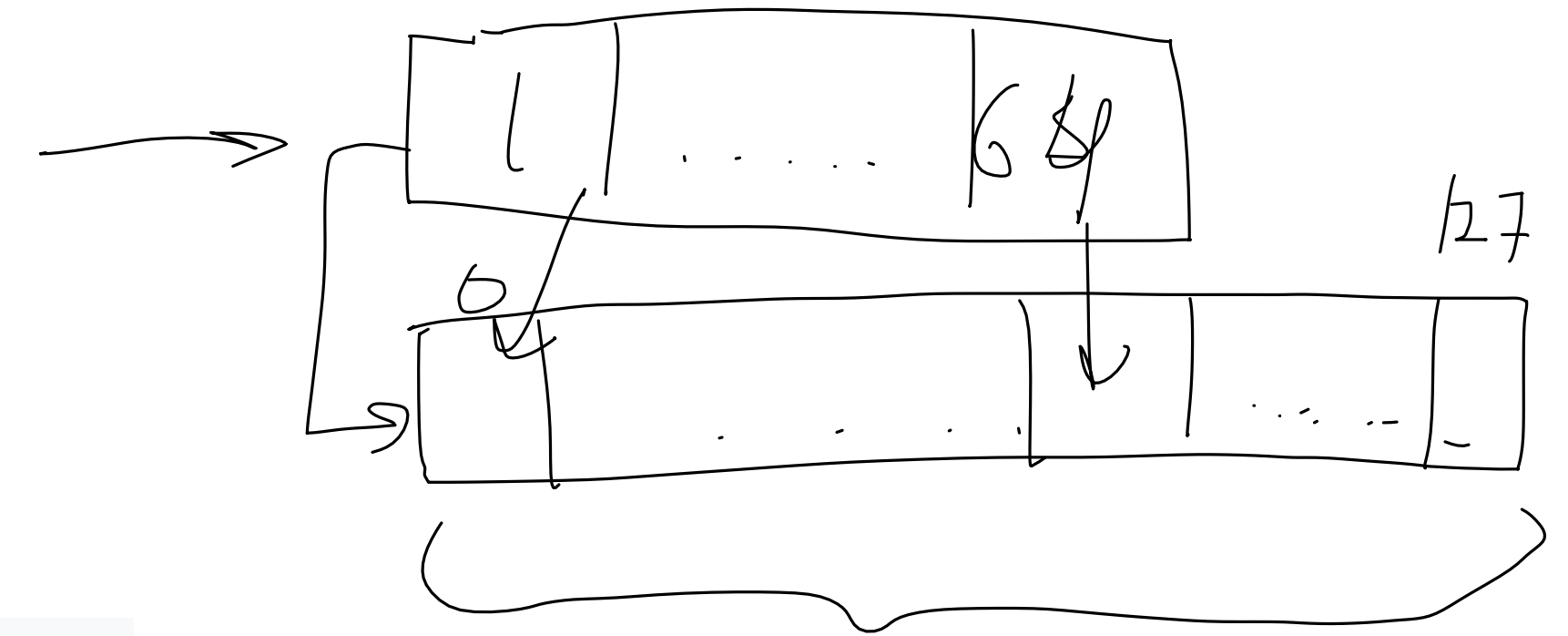
# Array Implementation.Pop



```
type Pop(x):  
    if head == 0:  
        error "underflow"  
    else:  
        head = head - 1  
        return array[head]
```



# Array Implementation.Extend



```
void ExtendStack(x):
```

```
    capacity = capacity * 2
```

```
    allocate new_array(capacity)
```

```
    copy array into new_array
```

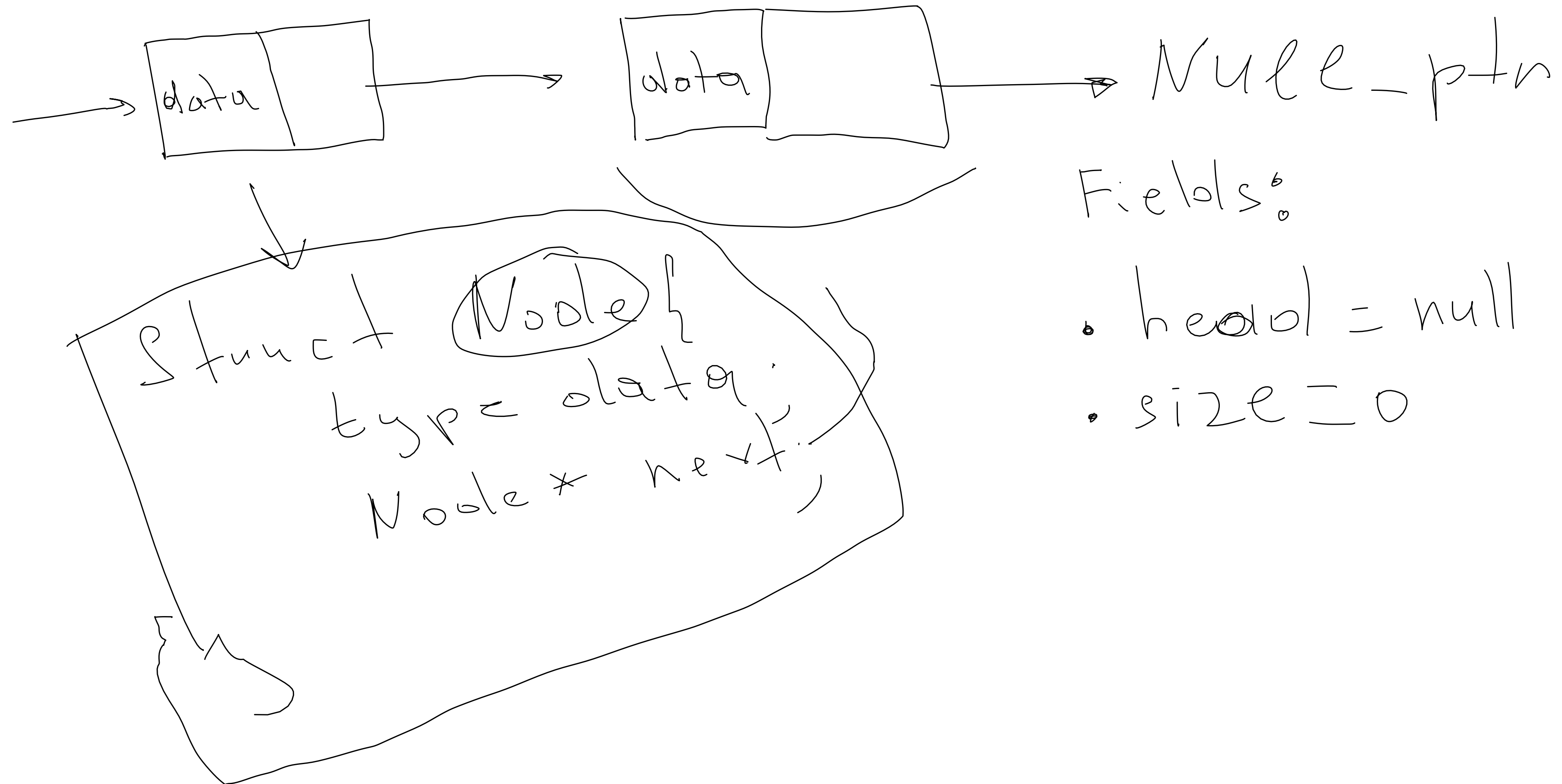
```
    free(array)
```

array = new\_array

$O(1) \rightarrow O(1) \cdot 2$   
one pointer on.

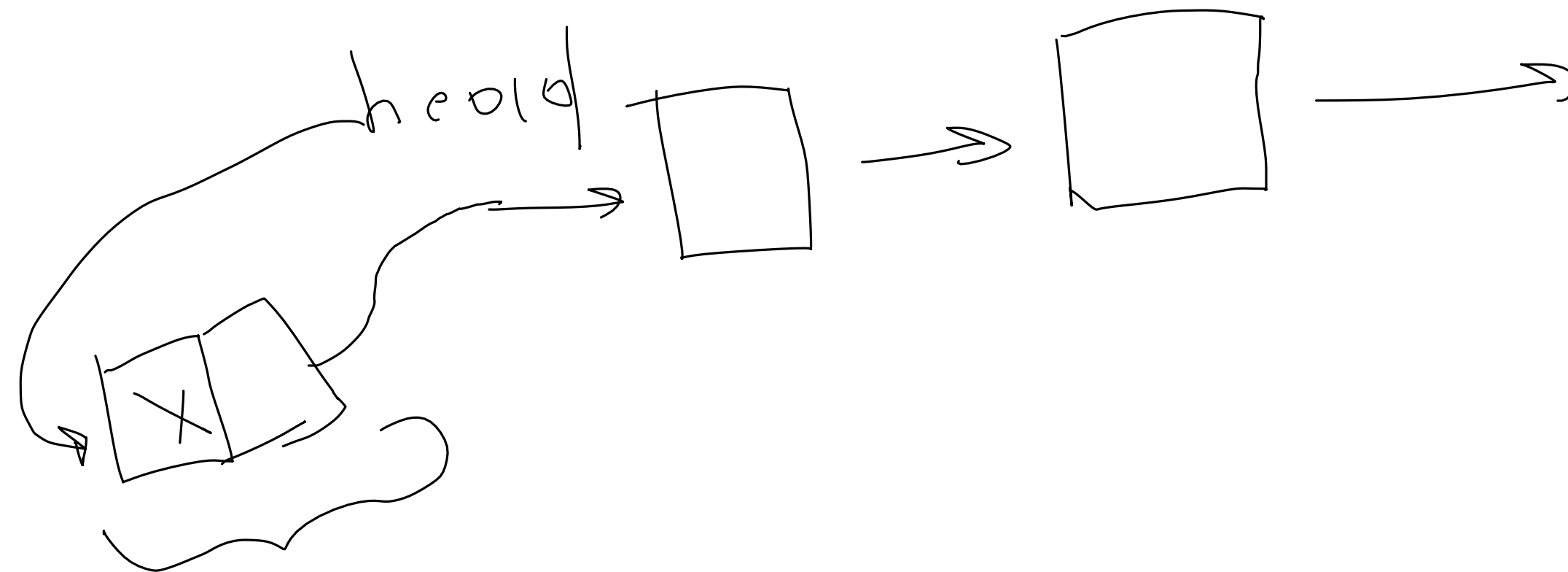
$O(n) + O(n) = O(n)$

# Linked List Implementation Idea



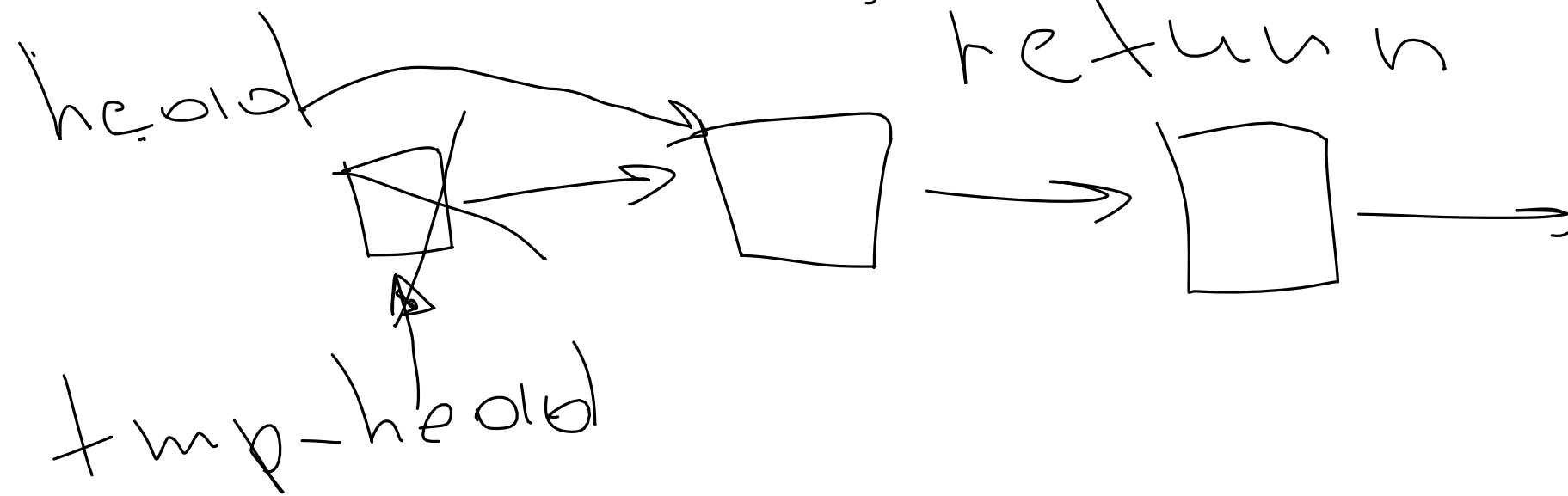
# Linked List Implementation.Push

```
void Push(x):  
    allocate new_head  
    new_head.value = head.value ✕  
    new_head.next = head  
    head = new_head  
    size += 1
```



# Linked List Implementation.Pop

```
type Pop(x):  
    if head == null_ptr:  
        error "underflow"  
    else:  
        return_value = head.value  
        tmp_head = head  
        head = head.next  
        free(tmp_head)  
    return return_value
```



# Pros & Cons

• Array

Time Complexity

Push:  $O(n)$

Pop:  $O(1)$

Space Complexity:  
 $O(n)$

• Linked List

Time complexity

Push:  $O(1)$

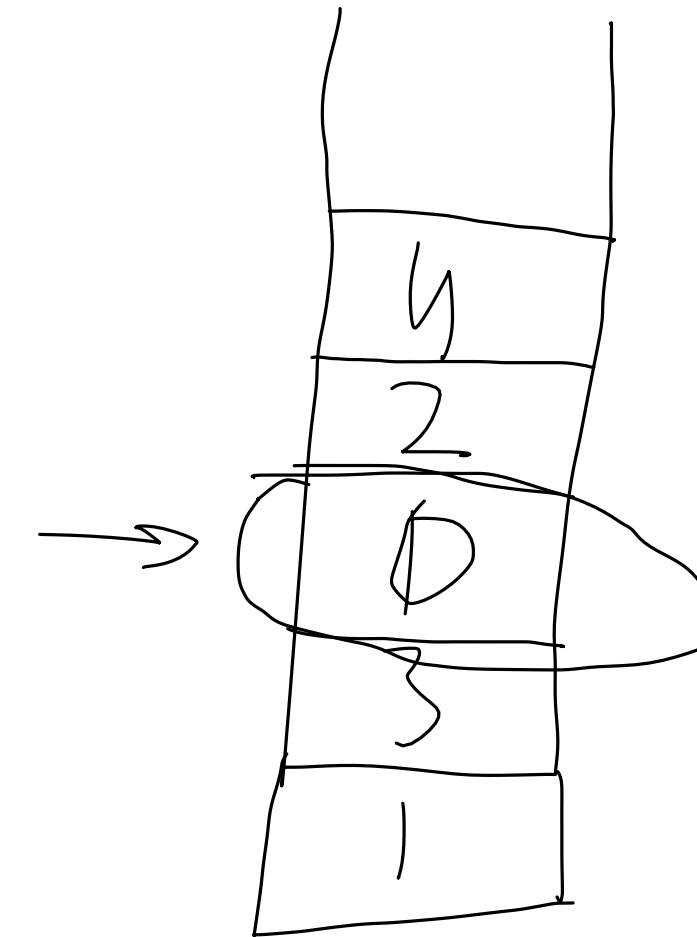
Pop:  $O(1)$

Space Complexity:  
 $O(n)$

# Keeping minimum in Stack

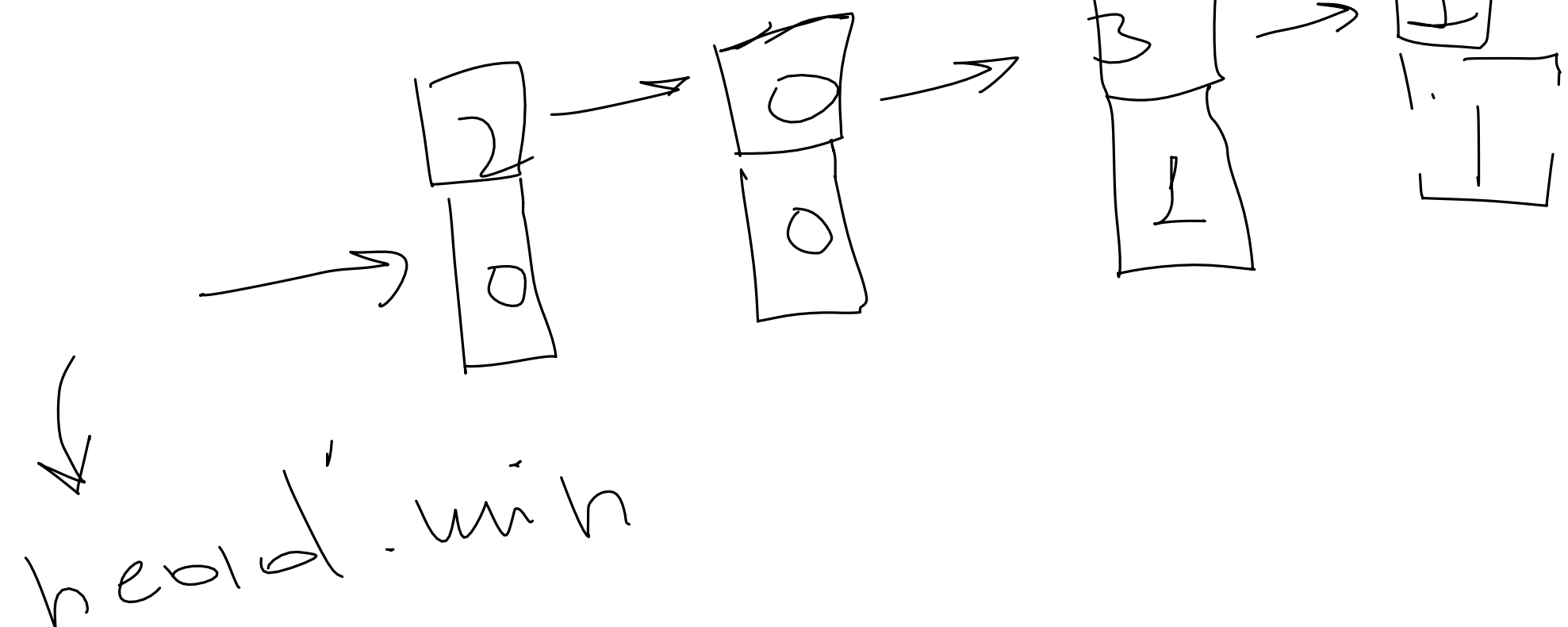
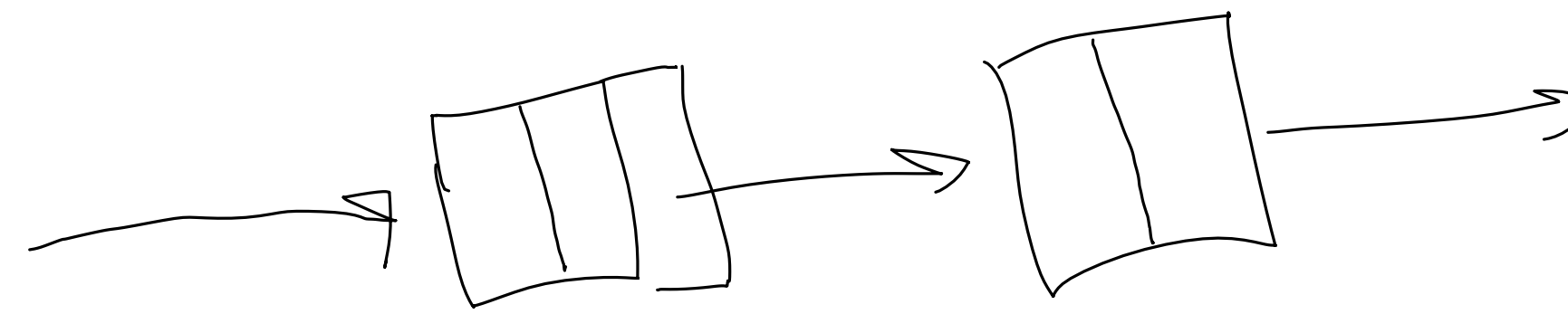
type GetMin()

min



minimum = 0

Node {  
data  
next  
minimum



minimum:

1  
1  
0  
0  
?

# Correct brackets sequence. Definition

Alphabet =  $\{ '(', '[', \{', '}', ']', ')' \}$

Sequence  $S$  is correct if:

- empty sequence is correct:  $S = \epsilon$

- $S \rightarrow (S)$

$$[S]$$
$$\{S\}$$

- $S \rightarrow S_1 S_2$

# Correct brackets sequence. Example

a      ( ) [ ]

b      [ ( ( ) ) ]

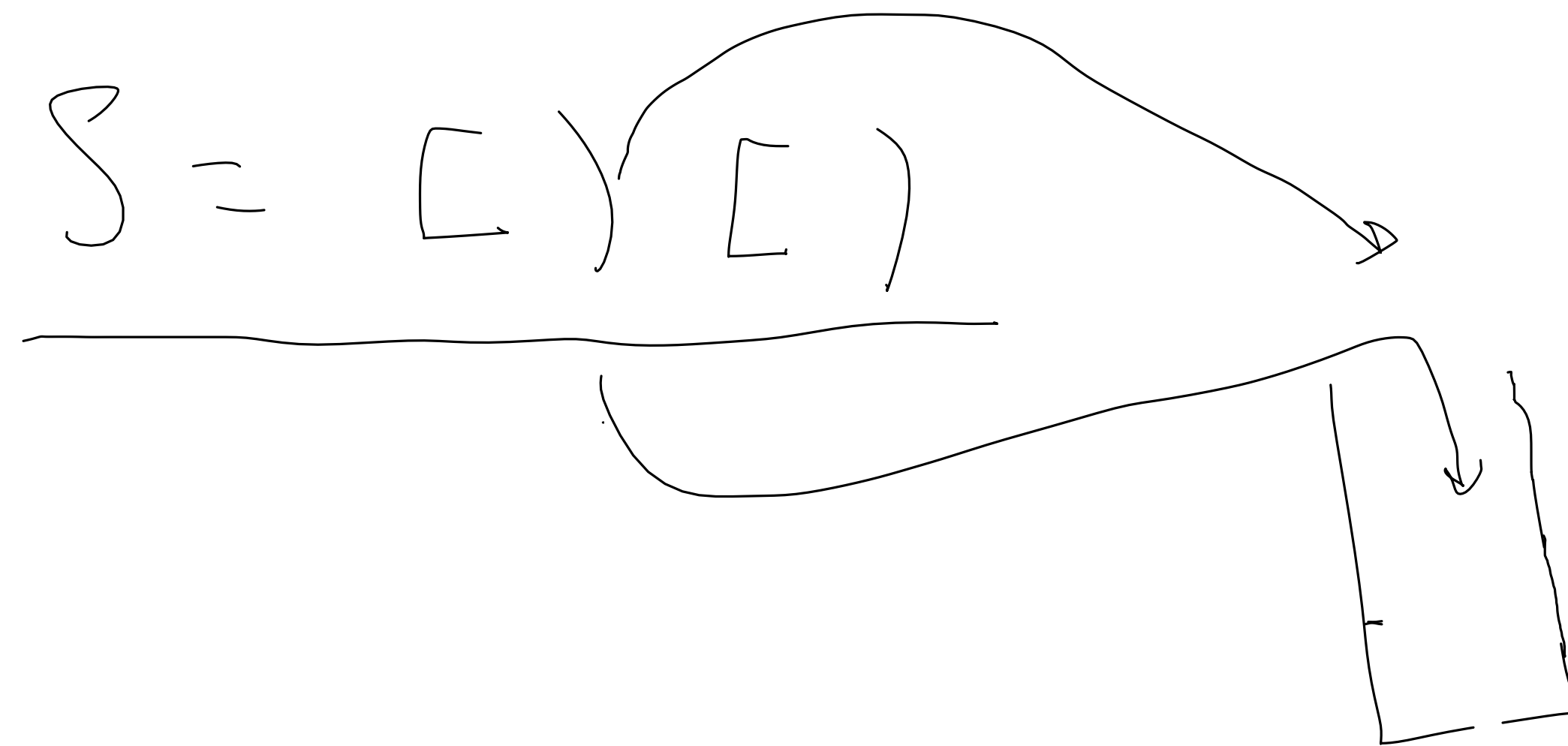
c      [ ) [ )  
         ↗



# Correct brackets sequence. Problem

Problem: Check if Sequence  $S$   
is correct

$\left[ \begin{array}{l} '(' \leftrightarrow ')' \\ '[' \leftrightarrow ']' \end{array} \right]$



# Correct brackets sequence. Algorithm

brackets = { '()', '[]', '{ }' }

# Correct brackets sequence. Pseudocode

```
for symbol in S:  
    if (isClosedBracket(symbol)) {  
        if (stack.empty()) {  
            return NO
```

```
        } else {
```

```
            last_element = stack.pop()  
            if (ClassOf(last_element) != ClassOf(symbol))  
                return false
```

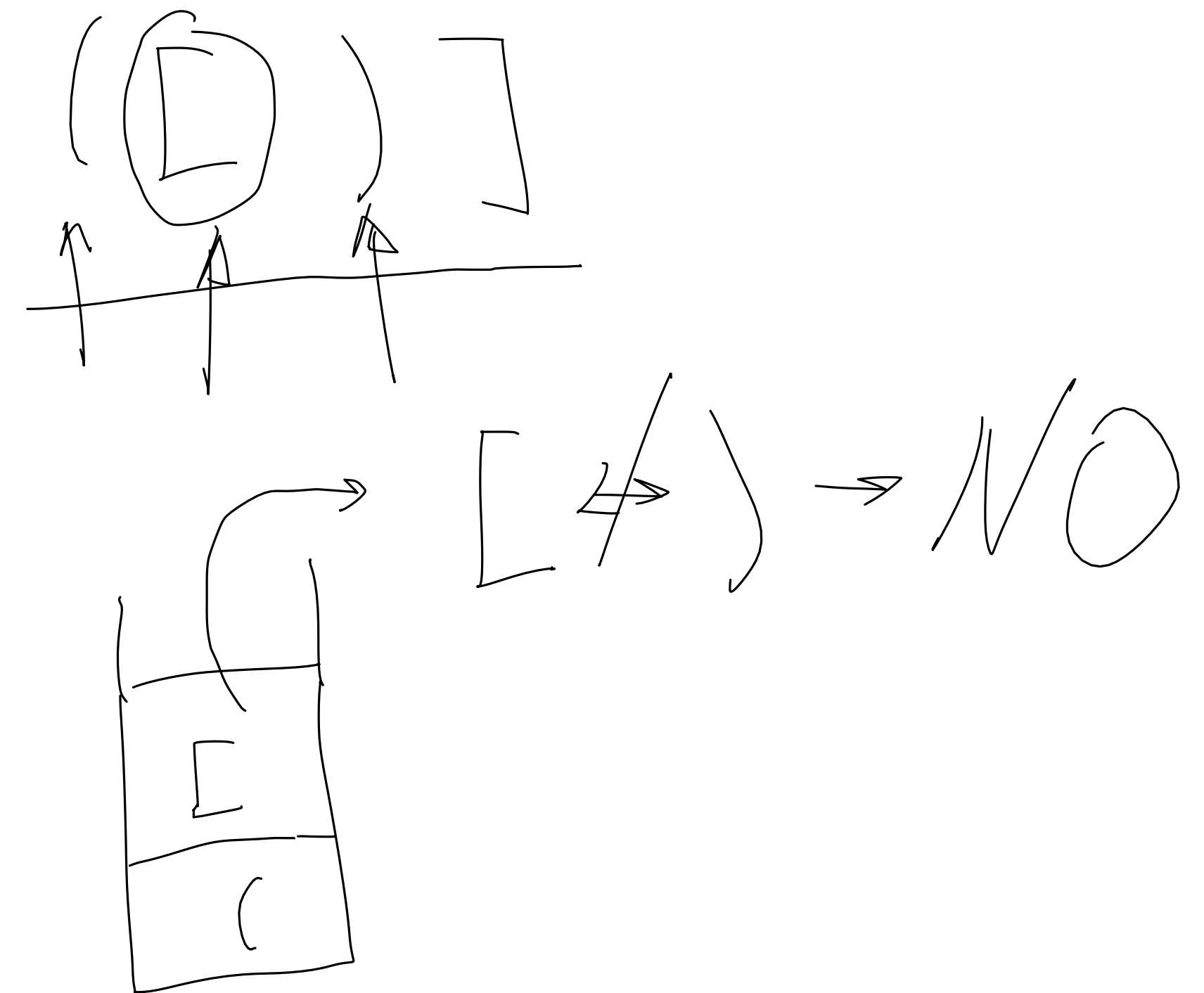
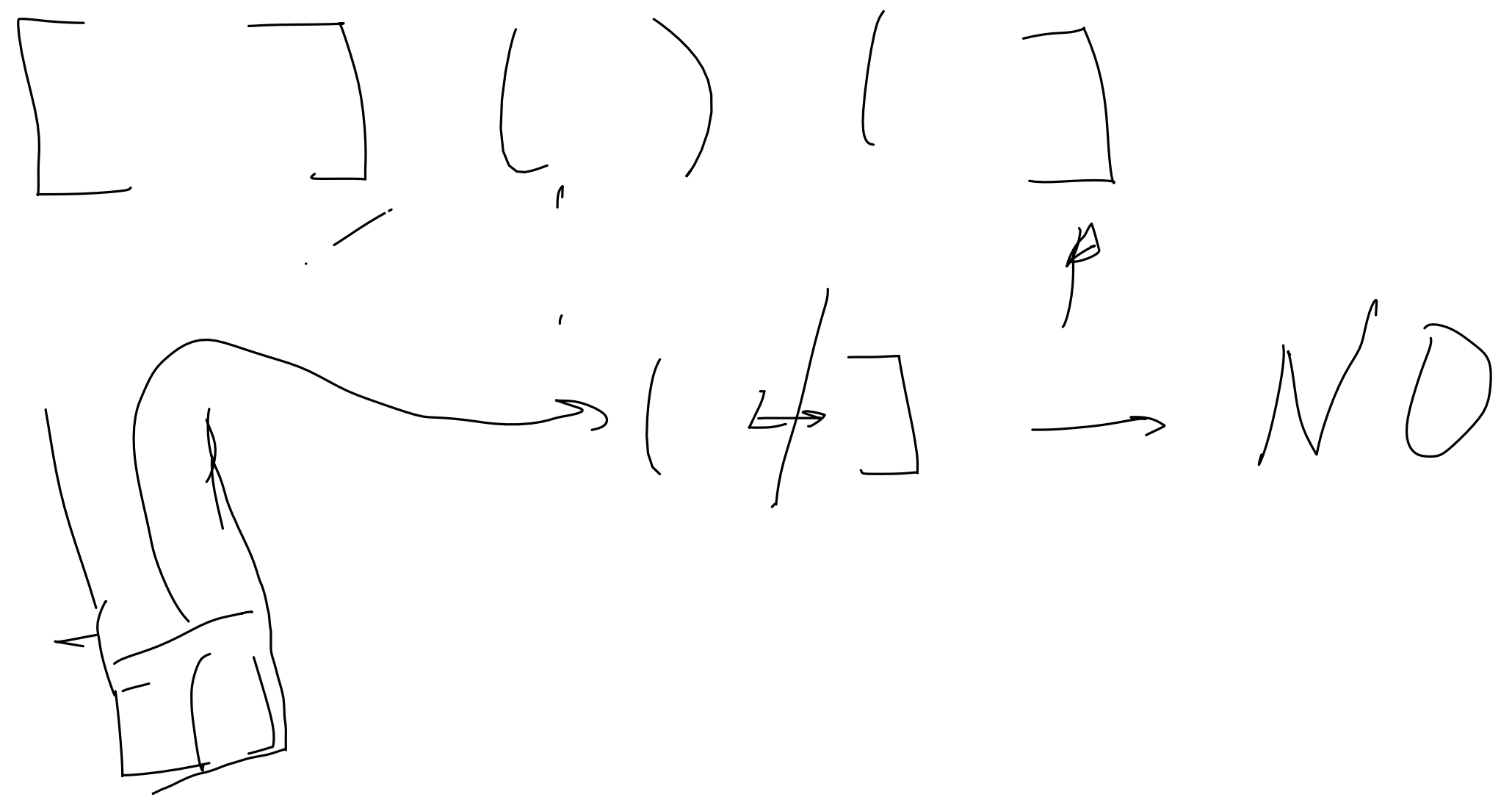
```
}  
else {
```

```
    stack.push(symbol);
```

```
}
```

```
}
```

```
return stack.empty();
```



Your questions!