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In[1398]:= λh = 0.01;
λs = 0.01;
λhs = √(4 * λh * λs);
θθ = ArcTan[(4 * λh - λhs) / (λs - λhs)];
vtree = λh * (ϕ * Cos[θθ])4 + (λhs / 2) * (Sin[θθ] * Cos[θθ])2 * ϕ4 + (λs / 4) * (ϕ * Sin[θθ])4;

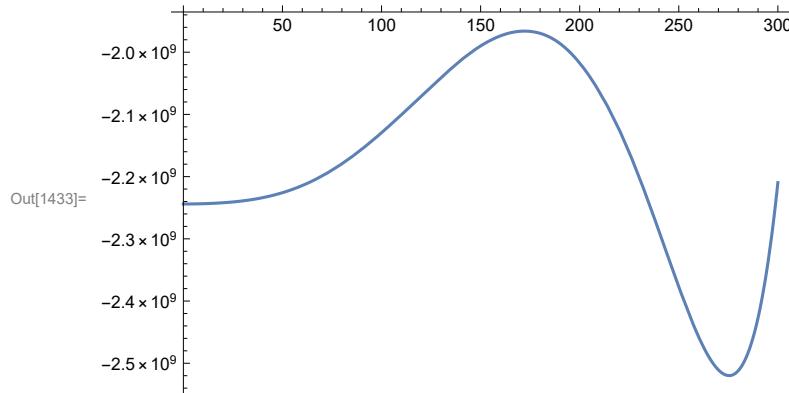
g1 = 0.648;
gy = 0.358;
yt = 0.936;
Mhiggs = 3 * λh * (ϕ * Cos[θθ])2 + (λhs / 2) * (ϕ * Sin[θθ])2;
Msinglet = (λhs / 2) * (ϕ * Cos[θθ])2 + (3 * λs) * (ϕ * Sin[θθ])2;
Mgoldstone = λh * (ϕ * Cos[θθ])2 + (λhs / 2) * (ϕ * Sin[θθ])2;
B = ((Mhiggs / ϕ)4 + 3 * (Mgoldstone / ϕ)4 + λhs2 + (3 / 16) * (Cos[θθ])4 * (g12 + gy2)2 +
      (3 / 8) * (Cos[θθ])4 * g14 - 3 * (Cos[θθ])4 * yt4) / (32 * π2);
vϕ = 246;
vloop = B * ϕ4 * (Log[ϕ / vϕ] - 1 / 4);

γE = 0.5772;
b1 = Mhiggs2 / T2;
b2 = Msinglet2 / T2;
b3 = Mgoldstone2 / T2;
MW+ = 1/2 * g1 * ϕ;
MW- = 1/2 * g1 * ϕ;
aw = (MW+)2 / T2;
Mz = 1/2 * (g12 + gy2)1/2 * ϕ;
az = (Mz)2 / T2;
Mtop = 1/√2 * yt * ϕ;
atop = (Mtop)2 / T2;
CB = 3 / 2 - 2 * γE + 2 * Log[4 * π];
CF = 3 / 2 - 2 * γE + 2 * Log[π];
iBhiggs = (1 - Exp[-(b1 / 6.3)4]) *
          (-Sqrt[π/2] * b13/4 * Exp[-Sqrt[b1]] * (1 + (15/8) * b1-1/2 + (105/128) * b1-1)) +
          (Exp[-(b1 / 6.3)4]) * (-π4 / 45 + (π2 / 12) * b1 - (π / 6) * b13/2 - (b12 / 32) (Log[b1] - CB));
iBsinglet = (1 - Exp[-(b2 / 6.3)4]) *
             (-Sqrt[π/2] * b23/4 * Exp[-Sqrt[b2]] * (1 + (15/8) * b2-1/2 + (105/128) * b2-1)) +
             (Exp[-(b2 / 6.3)4]) * (-π4 / 45 + (π2 / 12) * b2 - (π / 6) * b23/2 - (b22 / 32) (Log[b2] - CB));
iBgold = (1 - Exp[-(b3 / 6.3)4]) *
          (-Sqrt[π/2] * b33/4 * Exp[-Sqrt[b3]] * (1 + (15/8) * b3-1/2 + (105/128) * b3-1)) +
          (Exp[-(b3 / 6.3)4]) * (-π4 / 45 + (π2 / 12) * b3 - (π / 6) * b33/2 - (b32 / 32) (Log[b3] - CB));

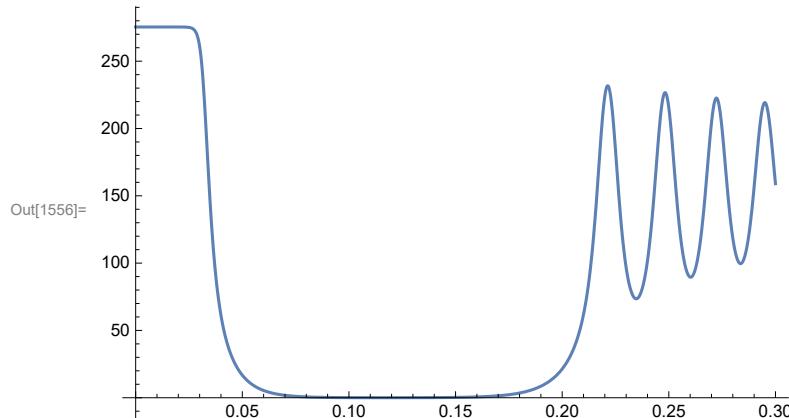
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$$\begin{aligned}
iBW &= \left(1 - \text{Exp}\left[-(a_w / 6.3)^4\right]\right) * \left(-\sqrt{\pi/2} * a_w^{3/4} * \text{Exp}\left[-\sqrt{a_w}\right] * \right. \\
&\quad \left.\left(1 + (15/8) * a_w^{-1/2} + (105/128) * a_w^{-1}\right)\right) + \\
&\quad \left(\text{Exp}\left[-(a_w / 6.3)^4\right]\right) * \left(-\pi^4/45 + (\pi^2/12) * a_w - (\pi/6) * a_w^{3/2} - (a_w^2/32) * (\text{Log}[a_w] - C_B)\right); \\
iBz &= \left(1 - \text{Exp}\left[-(a_z / 6.3)^4\right]\right) * \left(-\sqrt{\pi/2} * a_z^{3/4} * \text{Exp}\left[-\sqrt{a_z}\right] * \right. \\
&\quad \left.\left(1 + (15/8) * a_z^{-1/2} + (105/128) * a_z^{-1}\right)\right) + \\
&\quad \left(\text{Exp}\left[-(a_z / 6.3)^4\right]\right) * \left(-\pi^4/45 + (\pi^2/12) * a_z - (\pi/6) * a_z^{3/2} - (a_z^2/32) * (\text{Log}[a_z] - C_B)\right); \\
iF &= \left(1 - \text{Exp}\left[-(a_{top} / 3.25)^4\right]\right) * \left(-\sqrt{\pi/2} * a_{top}^{3/4} * \text{Exp}\left[-\sqrt{a_{top}}\right] * \right. \\
&\quad \left.\left(1 + (15/8) * a_{top}^{-1/2} + (105/128) * a_{top}^{-1}\right)\right) + \\
&\quad \left(\text{Exp}\left[-(a_{top} / 3.25)^4\right]\right) * \left(-\left(7/360\right) * \pi^4 + (\pi^2/24) * a_{top} + (a_{top}^2/32) * (\text{Log}[a_{top}] - C_F)\right); \\
v_{FT} &= \left(T^4 / (2 * \pi^2)\right) * (iBhiggs + iBsinglet + 3 * iBgold + (3+3) * iBW + 3 * iBz + (3*4) * iF);
\end{aligned}$$

```
v = vtree + vloop + vFT;
Plot[v /. T → 170, {ϕ, 0, 300}]
```



```
In[1554]:= DV := D[v, ϕ] /. ϕ → ϕ[r]
Sol1 = NDSolve[{ϕ''[r] + 2/r * ϕ'[r] - DV == 0,
ϕ'[0.1 * 10^-16] == 0.1 * 10^-16, ϕ[0.1 * 10^-16] == 275.40156614835765} /.
T → 170, ϕ[r], {r, 0.1 * 10^-16, 10}];
Plot[ϕ[r] /. Sol1, {r, 0.1 * 10^-16, 0.3}, PlotRange → Full]
```



```
Plot[{ϕ[r] /. Sol1}, {r, 0.001, 5}, ImageSize → 400,
Epilog → Inset[Plot[{ϕ[r] /. Sol1}, {r, 0.1*10-16, 2.5},
Frame → True, Axes → False, ImageSize → 400/2], {1.5, -1*1084}]]
```