${\rm HW}~1~{\rm STATS}~402$

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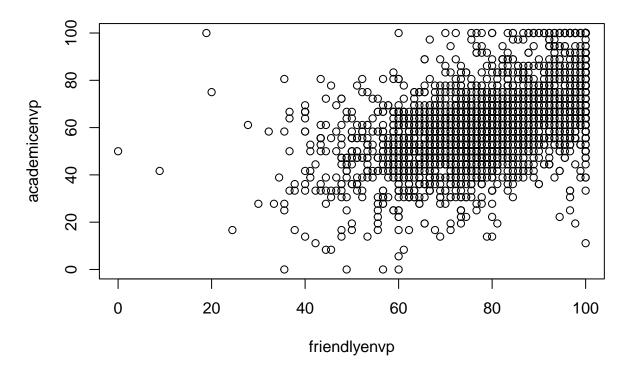
2024 - 10 - 13

1a.

Before we start our analysis, we see that some of the rows have NA values so in order to clean our data, we will drop all the NA rows.

##		friendlyenvp	academicenvp
##	1	100.00000	100.00000
##	2	88.88889	75.00000
##	3	75.55556	NA
##	4	51.11111	NA
##	5	95.55556	69.44444
##	6	100.00000	100.00000

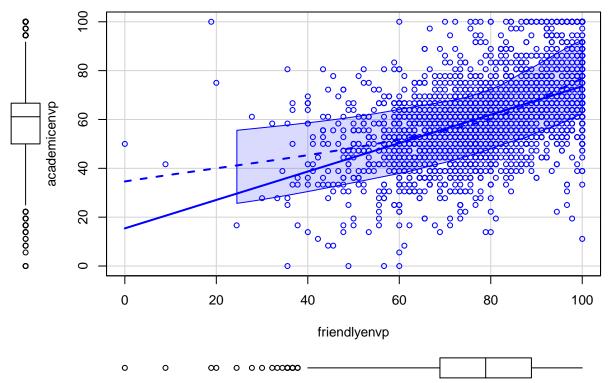
Scatterplot of friendlyenvp vs academicenvp



b.

Loading required package: carData

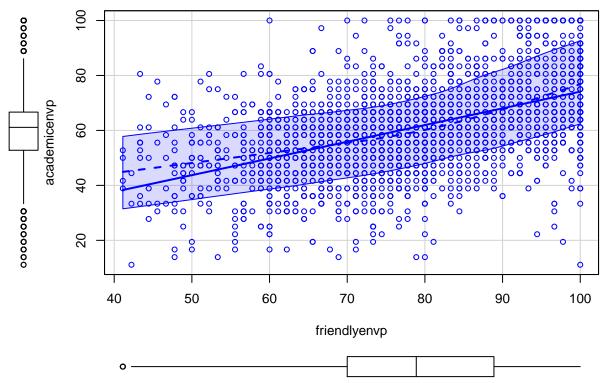
Scatterplot of friendlyenvp vs academicenvp



From this plot, we can see the solid straight line is the line of best fit from fitting a regression. Meanwhile, the dotted line is the lowess line that is non-parametric and is fitted through the averages of Y and is accompanied by some thin lines that indicate the confidence band. The Boxplot of friendliness has a longer whisker for the left side and a lot of lower outliers suggesting a left skew. Similarly, the boxplot for academic satisfaction is asymetric on the left side indicating a left skew but also notice that there are a couple upper outliers.

c.





Some noticeable changes start with how the regression line's fit has changed and seems to fit the data better and looks closer to the points. The regression line is also a lot closer to the lowess line. There's also a lot less outliers for friendliness.

d.

```
##
## Call:
  lm(formula = academicenvp ~ friendlyenvp, data = clean)
##
##
## Residuals:
##
       Min
                                3Q
                1Q
                    Median
                                        Max
                                    73.589
   -62.491
           -8.524
                    -0.400
                             7.671
##
##
   Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
##
   (Intercept)
                15.42112
                            1.42961
                                       10.79
                                               <2e-16 ***
                                               <2e-16 ***
                                       32.40
##
   friendlyenvp 0.58181
                            0.01796
## Signif. codes:
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 13.96 on 2980 degrees of freedom
## Multiple R-squared: 0.2605, Adjusted R-squared: 0.2603
## F-statistic: 1050 on 1 and 2980 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = academicenvp ~ friendlyenvp, data = subs)
##
## Residuals:
##
       Min
                1Q
                    Median
                                3Q
                                       Max
   -63.001
           -8.427
                    -0.246
                             7.565
                                    50.200
##
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
##
  (Intercept)
                 13.3301
                             1.4965
                                       8.908
                                               <2e-16 ***
                  0.6078
                             0.0187
                                      32.504
                                               <2e-16 ***
##
  friendlyenvp
##
                  0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 13.62 on 2940 degrees of freedom
## Multiple R-squared: 0.2644, Adjusted R-squared: 0.2641
## F-statistic: 1057 on 1 and 2940 DF, p-value: < 2.2e-16
```

The slope on the model using the subset data is .6078 while it's .5818 for the original data meaning the average rate of change in the academicenvp score is slightly higher for the 2nd model per unit increase in the friendly envp score. The \mathbb{R}^2 for the subset model .2644 is slightly higher than the model for the original data .2603 indicating a slightly better fit and more variance in academic envp is explained by friendly envp. Also, the intercept and standard error for the residuals is smaller for the model using the subset data compared to the model using the original data.

e.

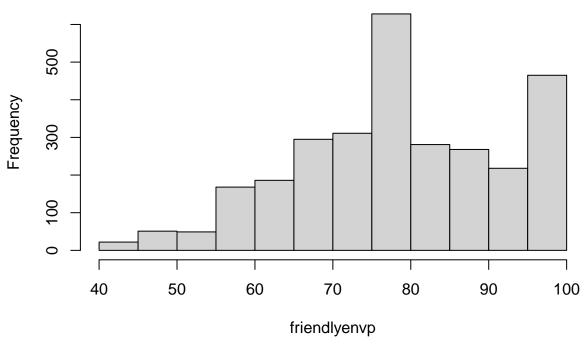
From the results of fitting a regression onto the subset data,

 $\hat{\beta}_1$ For a one unit increase in the friendly envp score, the acamdeicenvp score increases on average by .6078. $\hat{\beta}_0$ When the friendly envp score is 0, the average academic envp score is 13.33.

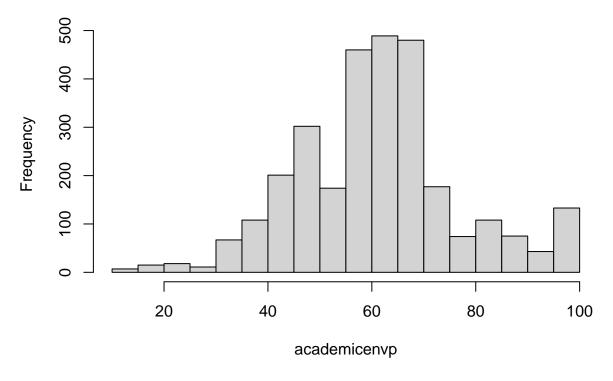
 R^2 26.44% of the variance in academicenvp can be explained by friendly envp.

f.

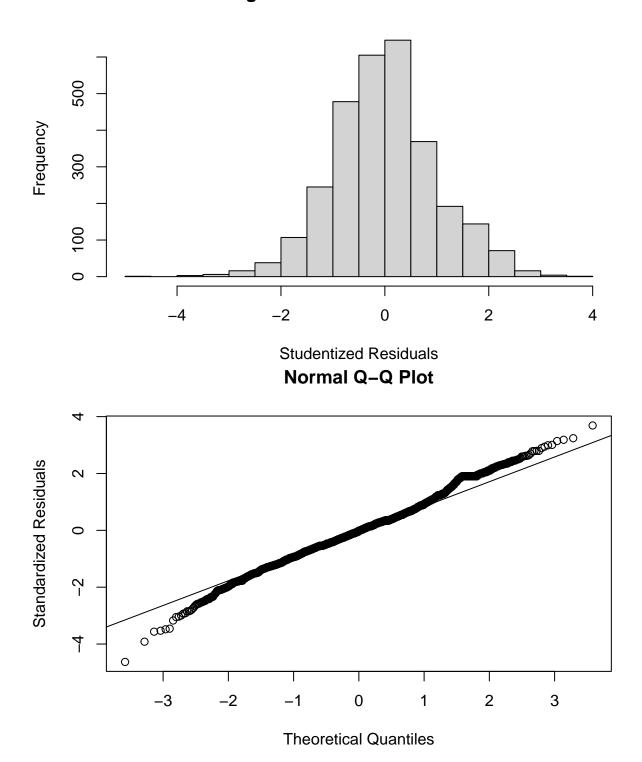
Histogram of Friendlyenvp



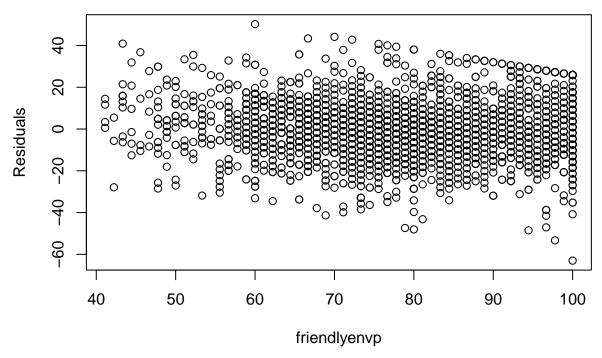
Histogram of Academicenvp



Histogram of Studentized Residuals

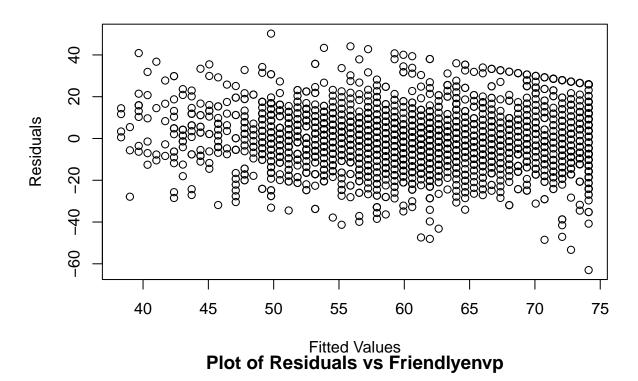


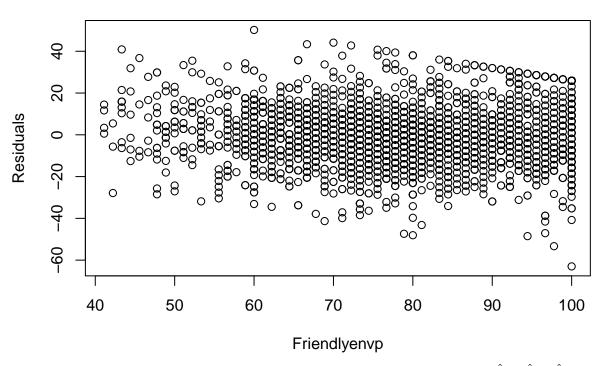
Plot of Residuals vs friendlyenvp



As stated earlier, friendly envp has a noticeable left skew while academicenvp has a more moderate left skew and almost looks symmetric. Meanwhile, we can see that the studentized residiuals seem to follow a normal distribution fairly well. Furthermore the qqplot gives better evidence of this and shows that our data roughly follows a normal distribution due to that nearly straight line pattern with the exception of the tiny bump around 1.5 and some points above/below 3 standard deviations. The Residual plot also indicates linearity due to the lack of pattern and the scatter across all x values are roughly equivalent (although there seems to be less spread past 80 that's not drastically different) implying roughly equal variance.

Plot of Residuals vs Fitted Values





They look almost identical and it's not exactly a surprise considering the fact that $\hat{Y} = \hat{\beta_0} + \hat{\beta_1} X$ the fitted value is simply a linear transformation of the predictor which does not affect the plot.

h.

Utilizing the model fitted on the subset data, H_0 :Homoscedascity is present, H_a :Heteroscedascity is present and Let $\alpha = .05$

```
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 30.21301, Df = 1, p = 3.871e-08
```

Since our p-value is extremely low and < .05, we reject the null hypothesis that homoscedacity is present. However, our residual plots look alright to conclude equal variance as the spread seems roughly equal across all the predictor values. As stated earlier, the spread past 80 seems to be a little bit less which our test may have picked up on but it isn't a drastic violation to conclude unequal variance. Also, this may be due to our large sample size that makes the test more powerful leading to statistical significance which may not always imply practical significance.

```
## Non-constant Variance Score Test
## Variance formula: ~ fitted.values
## Chisquare = 0.003011394, Df = 1, p = 0.95624
```

Interestingly, if we don't remove the outliers, we fail to reject the null hypothesis and conclude that there is homoscedascity since the p-value is very large and greater than our significance level 0.9562 > 0.05. This is consistent with what we're seeing in the residual plots of roughly equal variance.

2.1.

What we mean when we say equality of error variance is that the errors/residuals should be spread out the same across all values of the predictor variable. In other words we should not have scatterplots where we see things like a funnel shape.

2.2.

The principle of least squares is where we fit a regression/line of best fit based on selecting the coefficients of the line that minimize (the least part) the sum of squared residuals (the squares part). i.e. $argmin_{\beta_0,\beta_1}$ $\sum_{i=1}^{n} (Y_i - \beta_0 - \beta_1 X_i)^2$

2.3.

As started in 1g, $\hat{Y} = \hat{\beta}_0 + \hat{\beta}_1 X$ which means that \hat{Y} is really similar to X already which is no surprise they would have almost an identical performance when it comes to evaluating equal error variance. Mathematically speaking, \hat{Y} is a linear transformation of X which will not alter the shape/look of the plot.

2.4.

$$TSS = \sum_{i=1}^{n} (Y_i - \bar{Y})^2 = \sum_{i=1}^{n} (Y_i - \hat{Y}_i + \hat{Y}_i - \bar{Y})^2 =$$

$$\begin{split} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 + 2 \sum_{i=1}^{n} (Y_i - \hat{Y}_i) (\hat{Y}_i - \bar{Y}) + \sum_{i=1}^{n} (\hat{Y}_i - \bar{Y})^2 = \\ \sum_{i=1}^{n} (Y_i - \hat{Y}_i) (\hat{Y}_i - \bar{Y}) = \\ \sum_{i=1}^{n} \hat{\epsilon}_i (\hat{Y}_i - \bar{Y}) = \\ \sum_{i=1}^{n} \hat{\epsilon}_i \hat{Y}_i - \sum_{i=1}^{n} \hat{\epsilon}_i \bar{Y} = \\ \sum_{i=1}^{n} \hat{\epsilon}_i \hat{Y}_i - \bar{Y}_i \sum_{i=1}^{n} \hat{\epsilon}_i \\ \sum_{i=1}^{n} \hat{\epsilon}_i \hat{Y}_i - \bar{Y}_i \sum_{i=1}^{n} \hat{\epsilon}_i \\ = 0 \text{ so we are left with } \sum_{i=1}^{n} \hat{\epsilon}_i \hat{Y}_i = \sum_{i=1}^{n} \hat{\epsilon}_i (\hat{\beta}_0 + \beta_1 \hat{X}_i) = \\ \hat{\beta}_0 \sum_{i=1}^{n} \hat{\epsilon}_i + \hat{\beta}_1 \sum_{i=1}^{n} \hat{\epsilon}_i X_i = \\ 0 + \hat{\beta}_1 \sum_{i=1}^{n} \hat{\epsilon}_i X_i = \sum_{i=1}^{n} (Y_i - \hat{Y}_i) X_i = \sum_{i=1}^{n} (Y_i - \hat{\beta}_0 - \hat{\beta}_1 X_i) X_i = \\ \sum_{i=1}^{n} X_i Y_i - \hat{\beta}_0 \sum_{i=1}^{n} X_i - \hat{\beta}_1 \sum_{i=1}^{n} X_i^2 = \\ \sum_{i=1}^{n} X_i Y_i - (\bar{Y} - \hat{\beta}_1 \bar{X}) \sum_{i=1}^{n} X_i - \hat{\beta}_1 \sum_{i=1}^{n} X_i^2 = \\ \sum_{i=1}^{n} X_i Y_i - (\bar{Y} - \hat{\beta}_1 \bar{X}) n \bar{X} - \hat{\beta}_1 \sum_{i=1}^{n} X_i^2 = \\ \sum_{i=1}^{n} X_i Y_i - (\bar{Y} - \hat{\beta}_1 \bar{X}) n \bar{X} - \hat{\beta}_1 \sum_{i=1}^{n} X_i^2 = \\ \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \hat{\beta}_1 n \bar{X}^2 - \hat{\beta}_1 \sum_{i=1}^{n} X_i^2 = \\ \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} - \hat{\beta}_1 (\sum_{i=1}^{n} X_i^2 - n \bar{X}^2) \\ \text{By algebra we get } \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} - \hat{\beta}_1 (\sum_{i=1}^{n} X_i^2 - n \bar{X}^2) = 0 \\ \text{Hence we can conclude } 2 \sum_{i=1}^{n} (Y_i - \hat{Y}_i) (\hat{Y}_i - \bar{Y}) = 0 \\ \text{and } TSS = \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 + \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 \text{ and notice how the formulas on the right is simply RSS and } \\ \text{ESS where } RSS = \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 \text{ and } ESS = \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 \text{ and notice how the formulas on the right is simply RSS and } \\ \text{ESS} \text{ where } RSS = \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 \text{ and } ESS = \sum_{i=1}^{n} (\hat{Y}_i - \hat{Y}_i)^2 \text{ and notice how the formulas on the right is simply RSS and } \\ \text{ESS} \text{ where } RSS = \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2 \text{ and notice how the formulas on the right is } \\ \text{The substitute of the properties of the properties$$

Therefore TSS = RSS + ESS

2.5

We are interested in deriving $\hat{\beta}_0$ & $\hat{\beta}_1$ or the coefficients of the line of best fit. The line of best fit is derived from minimizing the sum of squared residuals/loss function i.e. $L = \sum_{i=1}^{n} (Y_i - \beta_0 - \beta_1 X_i)^2$. In order to minimize such a function, we can take the partial derivatives and set them equal to 0.

First i)
$$\frac{\partial L}{\partial \beta_0} = -2\sum_{i=1}^n (Y_i - \beta_0 - \beta_1 X_i) = 0$$
 and then ii) $\frac{\partial L}{\partial \beta_1} = -2\sum_{i=1}^n X_i (Y_i - \beta_0 - \beta_1 X_i) = 0$

From i, divide both sides by -2 and we get $\sum_{i=1}^{n} (Y_i - \beta_0 - \beta_1 X_i) = \sum_{i=1}^{n} Y_i - \sum_{i=1}^{n} \beta_0 - \beta_1 \sum_{i=1}^{n} X_i = n\bar{Y} - n\beta_0 - \beta_1 n\bar{X}$ Since this is set to 0 solve for β_0 and we get $n\beta_0 = n\bar{Y} - \beta_1 n\bar{X}$ $\hat{\beta_0} = \bar{Y} - \hat{\beta_1} \bar{X}$

From ii, divide both sides by -2 and we get $\sum_{i=1}^{n} X_i Y_i - X_i \beta_0 - \beta_1 X_i^2$. Recall $\beta_0 = \bar{Y} - \beta_1 \bar{X}$ so $\sum_{i=1}^{n} X_i Y_i - X_i (\bar{Y} - \beta_1 \bar{X}) - \beta_1 X_i^2 = \sum_{i=1}^{n} X_i Y_i - X_i \bar{Y} + \beta_1 X_i \bar{X} - \beta_1 X_i^2 = \sum_{i=1}^{n} X_i Y_i - \sum_{i=1}^{n} X_i \bar{Y} + \beta_1 \sum_{i=1}^{n} X_i \bar{X} - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i^2 = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} + \beta_1 n \bar{X}^2 - \beta_1 \sum_{i=1}^{n} X_i \bar{Y} - n \bar{X}$

Set equal to 0 and we get $\sum_{i=1}^{n} X_i Y_i - n\bar{X}\bar{Y} = \beta_1 \left(\sum_{i=1}^{n} X_i^2 - n\bar{X}^2\right)$ Solving for $\hat{\beta}_1$ we get $\hat{\beta}_1 = \frac{\sum_{i=1}^{n} X_i Y_i - n\bar{X}\bar{Y}}{\sum_{i=1}^{n} X_i^2 - n\bar{X}^2}$

Notice
$$\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y}) = \sum_{i=1}^{n} X_i Y_i - X_i \bar{Y} - \bar{X} Y_i + \bar{X} \bar{Y} = \sum_{i=1}^{n} X_i Y_i - \sum_{i=1}^{n} X_i \bar{Y} - \sum_{i=1}^{n} \bar{X} \bar{Y} + \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y} - n \bar{X} \bar{Y} + n \bar{X} \bar{Y} = \sum_{i=1}^{n} X_i Y_i - n \bar{X} \bar{Y}$$

Using the above results, if we replace $Y_i - \bar{Y}$ with another $X_i - \bar{X}$, we get $\sum_{i=1}^n (X_i - \bar{X})^2 = \sum_{i=1}^n X_i^2 - n\bar{X}^2$

so we can conclude
$$\hat{\beta_1} = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sum_{i=1}^n (X_i - \bar{X})^2}$$

Hence we have derived the coefficients $\hat{\beta}_0, \hat{\beta}_1$ using partial derivatives.

3a.

No because covariance does not tell us about the strength of the relationship directly but rather how two variables vary around their two means. Furthermore regarding the math, there is a lack of standardization to truly be able to compare the strength of the relationships between researchers A and B. To make a meaningful comparison, we would need to calculate the correlations which we would do by dividing each covariance by their respective standard deviations for the predictor and response variable. $r = \frac{S_{xy}}{S_x S_x}$

b.

We call correlation standardized covariance because if we look at the formulas, $r = \frac{\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y})}{S_x S_y * (n-1)}$ and $S_{xy} = \frac{1}{n-1} \sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y}), \text{ we can rewrite r such that it looks similar to the covariance where the x and y variables are standardized.}$ $r = \frac{\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y})}{S_x S_y * (n-1)} = \frac{1}{n-1} \frac{\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y})}{S_x S_y} = \frac{1}{n-1} \sum_{i=1}^{n} (\frac{X_i - \bar{X}}{S_x})(\frac{Y_i - \bar{Y}}{S_y})$

$$r = \frac{\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y})}{S_x S_y * (n-1)} = \frac{1}{n-1} \frac{\sum_{i=1}^{n} (X_i - \bar{X})(Y_i - \bar{Y})}{S_x S_y} = \frac{1}{n-1} \sum_{i=1}^{n} \left(\frac{X_i - \bar{X}}{S_x}\right) \left(\frac{Y_i - \bar{Y}}{S_y}\right)$$

 $\frac{1}{n-1}\sum_{i=1}^{n}Z_{X_{i}}Z_{Y_{i}}$ Note $Z_{X_{i}}=\frac{X_{i}-\bar{X}}{S_{x}},Z_{Y_{i}}=\frac{Y_{i}-\bar{Y}}{S_{y}}$ notice how the correlation now looks like the covariance formula with the only difference being that the x and y variables have been standardized since we are subtracting each variable by its mean and dividing by its standard deviation. Hence, this is why correlation is called standardized covariance.

4a.

```
xbar <- mean(friendlyenvp)</pre>
sx2 <- var(friendlyenvp)</pre>
sx <- sd(friendlyenvp)</pre>
ybar <- mean(academicenvp)</pre>
sy2 <- var(academicenvp)</pre>
sy <- sd(academicenvp)</pre>
xbar
## [1] 78.89115
```

[1] 180.3267

[1] 13.42858 ybar

[1] 61.28201

```
sy2
## [1] 252.0083
## [1] 15.87477
\begin{split} \bar{X} &= 78.8912, S_x^2 = 180.3267, S_x = 13.4286 \\ \bar{Y} &= 61.282, S_y^2 = 252.0083, S_y = 15.8748 \end{split}
b.
sxy <- cov(friendlyenvp,academicenvp)</pre>
rxy <- cor(friendlyenvp,academicenvp)</pre>
## [1] 109.6069
rxy
## [1] 0.5141625
S_{xy} = 109.6069, r_{xy} = .5142
c.
TSS <- (nrow(subs)-1)*sy2
TSS
## [1] 741156.4
SSX <- (nrow(subs)-1)*sx2
SSX
## [1] 530340.7
RSS <- TSS*(1-rxy^2)
RSS
## [1] 545222
```

```
Se2 <- RSS/(nrow(subs)-2)
Seb <- sqrt(Se2/SSX)
Seb
## [1] 0.01869974
beta1 <- sxy/sx2
tstat <- beta1/Seb
tstat
## [1] 32.50441
Fstat <- (TSS-RSS)/Se2
Fstat
## [1] 1056.537
\begin{array}{l} \mathrm{i})TSS = S_y^2*(n-1) = 252.0083*(2942-1) = 741156.4 \\ \mathrm{ii})SSX = S_x^2*(n-1) = 180.3267*(2942-1) = 530340.7 \\ \mathrm{iii})1 - R^2 = 1 - r^2 = \frac{RSS}{TSS} \text{ thus } RSS = TSS*(1-r^2) = 741156.4*(1-.5142^2) = 545222 \end{array}
iv)S(e)_{\hat{\beta_1}} = \frac{S_e}{\sqrt{SSX}} = \frac{\sqrt{\frac{RSS}{n-2}}}{\sqrt{SSX}} = \frac{\sqrt{\frac{545222}{2942-2}}}{\sqrt{530340.7}} = 0.0187
\mathbf{v})\hat{\beta}_{1} = \frac{S_{xy}}{S_{x}^{2}} = \frac{109.6069}{180.3267} = 0.6078
t = \frac{\hat{\beta}_{1} - 0}{S(e)_{\hat{\beta}_{1}}} = \frac{.6078}{.0187} = 32.5044
vi)F = \frac{\frac{ESS}{k}}{\frac{RSS}{n-k-1}} = \frac{\frac{741156.4 - 545222}{545222}}{\frac{545222}{2942 - 1 - 1}} = 1056.537
vii)Notice how t^2 = 32.5044^2 = 1056.537 = F Hence we can conclude t^2 = F
```

Appendix

```
knitr::opts_chunk$set(echo = FALSE)
df <- read.csv('campusclimate.csv')</pre>
head(df[,c('friendlyenvp','academicenvp')])
clean <- df[,c('friendlyenvp', 'academicenvp')]</pre>
clean <- clean[complete.cases(clean),] #Drop NA Rows</pre>
plot(x = clean$friendlyenvp, y = clean$academicenvp,
     xlab = 'friendlyenvp',ylab = 'academicenvp',
     main = 'Scatterplot of friendlyenvp vs academicenvp')
library(car)
scatterplot(academicenvp ~ friendlyenvp, span=0.6, lwd=3,
id.n=4, data=clean,
main = "Scatterplot of friendly envp vs academic envp",
xlab = 'friendlyenvp',ylab = 'academicenvp')
subs <- clean[clean$friendlyenvp > 40 & clean$academicenvp > 10,]
#Select rows where friendly envp is greater than 40
#AND academicenup is greater than 10
```

```
attach(subs)
scatterplot(academicenvp ~ friendlyenvp, span=0.6, lwd=3,
id.n=4, data=subs, main ="Scatterplot of friendlyenvp vs academicenvp"
 ,xlab = 'friendlyenvp',ylab = 'academicenvp')
model1 <- lm(academicenvp ~ friendlyenvp, data = clean)</pre>
model2 <- lm(academicenvp ~ friendlyenvp, data = subs)</pre>
summary(model1)
summary(model2)
hist(friendlyenvp,main = "Histogram of Friendlyenvp")
hist(academicenvp,main = "Histogram of Academicenvp")
hist(rstudent(model2), main = "Histogram of Studentized Residuals", xlab="Studentized Residuals")
qqnorm(rstandard(model2), ylab = 'Standardized Residuals')
qqline(rstandard(model2))
plot(x = friendlyenvp, y = model2$residuals, xlab = "friendlyenvp",
     ylab = 'Residuals',main ='Plot of Residuals vs friendlyenvp')
plot(x = model2$fitted.values, y = model2$residuals,
     xlab = "Fitted Values", ylab = 'Residuals',
     main ='Plot of Residuals vs Fitted Values')
plot(x = friendlyenvp, y = model2$residuals,
     xlab = "Friendlyenvp", ylab = 'Residuals',
     main ='Plot of Residuals vs Friendlyenvp')
ncvTest(model2)
ncvTest(model1)
xbar <- mean(friendlyenvp)</pre>
sx2 <- var(friendlyenvp)</pre>
sx <- sd(friendlyenvp)</pre>
ybar <- mean(academicenvp)</pre>
sy2 <- var(academicenvp)</pre>
sy <- sd(academicenvp)</pre>
xbar
sx2
sx
ybar
sy2
sxy <- cov(friendlyenvp,academicenvp)</pre>
rxy <- cor(friendlyenvp,academicenvp)</pre>
sxy
rxy
TSS \leftarrow (nrow(subs)-1)*sy2
TSS
SSX \leftarrow (nrow(subs)-1)*sx2
SSX
RSS \leftarrow TSS*(1-rxy^2)
RSS
Se2 <- RSS/(nrow(subs)-2)
Seb <- sqrt(Se2/SSX)
Seb
beta1 <- sxy/sx2
tstat <- beta1/Seb
tstat
```

Fstat <- (TSS-RSS)/Se2 Fstat