

Free-fall objects

PH 111

2-36: A ball is thrown vertically upward with a speed of 25 m/s

a. How high does it rise?

Assume height relative to release level

$$\vec{v}_{0y} = +25 \text{ m/s} \quad \vec{a}_y = -9.8 \text{ m/s}^2 \quad \vec{v}_y = 0 \text{ m/s}$$

Looking for \vec{y}_{max}

$$0 = 25^2 + 2(-9.8)\vec{y} \quad \vec{y}_{\text{max}} = 32 \text{ m}$$

b. How long does it take to reach its highest point?

$$0 = 25 - 9.8t \quad t = 2.6 \text{ s}$$

c. How long does it take the ball to hit the ground from its highest point?

Assume launched from ground

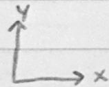
$$t = 2(2.6) = 5.2 \text{ s}$$

d. What is its velocity when it returns to the same level from which it started?

$$\vec{v}_y = -25 \text{ m/s}$$

Ways to indicate direction for vector quantities

1. Use +/- with number



2. Use a labeled arrow

$$\vec{v} \quad v = 2.3 \text{ m/s}$$

3. Use words

Vectors in 3 dimensions

$$\text{position: } \vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$$

$$\text{displacement} = \Delta \vec{r} = \vec{r} - \vec{r}_0 = (x - x_0)\hat{i} + (y - y_0)\hat{j} + (z - z_0)\hat{k}$$

$$\vec{v}_{\text{avg}} = \Delta \vec{r} / \Delta t \quad \vec{v}_{\text{inst}} = \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{r}}{\Delta t} = \frac{dx}{dt}\hat{i} + \frac{dy}{dt}\hat{j} + \frac{dz}{dt}\hat{k}$$

$$\vec{a}_{\text{avg}} = \Delta \vec{v} / \Delta t \quad \vec{a}_{\text{inst}} = \frac{d\vec{v}}{dt}$$

Horizontal

Vertical

$$a_x = 0$$

$$a_y = -g$$

$$v^2 = v_0^2 + 2ax$$

$$x = v_0 t$$

(range)

Same as \Rightarrow

$$v = v_0 + at$$

$$x = v_0 t + \frac{1}{2}at^2$$