

Work Done by Variable Forces

PA 111

$$W = \int_{x_i}^{x_f} F(x) dx$$

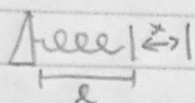
Area under the curve is the work done by the force

Springs: $\vec{F} = -k\vec{x}$

$$W_{\text{spring}} = \int_{x_i}^{x_f} -kx dx$$

$$= -\frac{1}{2}k(x_f^2 - x_i^2)$$

In Hooke's Law, x is not the length of the spring



x is the change in position of the spring from equilibrium

$$PE_e = \frac{1}{2}kx^2$$

$$m = 4 \text{ kg} \quad k = 700 \text{ N/m} \quad v = 1 \text{ m/s}$$

Find max compression in spring

$$KE_i + PE_{g_i} + PE_{e_i} = KE_f + PE_{g_f} + PE_{e_f}$$

$$\frac{1}{2}mv_i^2 + 0 + 0 = 0 + 0 + \frac{1}{2}kx^2$$

$$\frac{1}{2}(4)(1^2) = \frac{1}{2}(700)x^2$$

$$x = 7.6 \text{ cm}$$

$x_2 = 10 \text{ cm}$, Find v_{max}

$$\frac{1}{2}kx_0^2 = \frac{1}{2}mv^2$$

$$\frac{1}{2}(700)(.1)^2 = \frac{1}{2}(4)v^2$$

$$v = 1.3 \text{ m/s}$$

With friction

$$E_i = E_f + W_{nc}$$

$$-W_{nc} = E_i - E_f$$

$$-W_{nc} = fkd = \mu_k mgd$$

Find v after rough patch

Roller μ_k

$$d = 5 \text{ cm}$$

$$\mu_k = .415$$

$$\frac{1}{2}kx_i^2 = \frac{1}{2}mv^2 + \mu_k mgd$$

$$\frac{1}{2}(700)(.1)^2 = \frac{1}{2}(4)v^2 + .415(4)(9.8)(.05)$$

$$v = 1.2 \text{ m/s}$$

Find P_{avg}

$$3 \text{ } \frac{1}{2} 44 \quad t = 15$$

$$W = 44(9.8)(3) = 1293.6 \text{ J}$$

$$P = 1293.6 / 15 = 86.2 \text{ W}$$