# The Consumption Origins of Business Cycles: Lessons from Sectoral Dynamics

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#### Abstract

We measure the impact of household consumption shocks on aggregate fluctuations. These shocks affect household consumption directly, and production and prices indirectly through their impact on aggregate consumption. We show how to identify such shocks using prior knowledge of their differential impact across sectoral variables. Shocks independently affecting household consumption demand have accounted for almost 40% of business cycle fluctuations since the mid-1970s, playing a central role in recessions within the period. The inferred household consumption shock series correlates well with measures of changes in consumer confidence and household wealth.

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# 1 Introduction

Household consumption accounts for more than two-thirds of GDP. Accordingly, cash transfers to households are often used to mitigate recessions. Nevertheless, in canonical business cycle models, household consumption decisions play a role mainly as a propagation channel for shocks generated elsewhere, and little to no role as an independent source of fluctuations. We use cross-sectoral information to show that this is an important omission. We define a consumption shock as one that affects aggregate consumption directly, and then propagates to the rest of the economy, for example because firms may want to reduce their output and hire fewer workers in response to lower consumption demand. An example of such a shock is a deterioration in household expectations or "sentiments", another would be a sudden and exogenous reduction in household wealth. Other sources of a consumption shock with similar effects would include a shock to consumer credit or employment uncertainty. We find that, in combination, such shocks have accounted for close to 40% of output fluctuations since the mid-1970s.

Our findings are made possible by a novel identification strategy that allows us, with minimal structural assumptions, to use cross-sectional information to infer aggregate responses to shocks. We show that, given a large enough panel dataset, one can identify the time-path of an aggregate shock based on information of its differential impact on cross-sectional observations. To efficiently use this identification strategy, we devise a new time series model that can handle large cross-sections of data while allowing for substantial heterogeneity across sectors.

We find that the identified household consumption demand shock generates not only a significant impact on aggregate consumption but, more interestingly, also on GDP. The response of other aggregate variables is further consistent with the conventional characterization of "aggregate demand" shocks with an increase in inflation and the interest rate. At the same time, the impact on corporate credit spreads and measured TFP is small, so that the shock is distinct from a productivity or credit shock. Overall, we find that shocks to household consumption have accounted for close to 40% of output fluctuations at business cycle frequencies since 1973, and an increasing fraction of output declines in recessions within that period. Those shocks had a maximal impact in the 2008 recession, where it accounts for an output drop of 4.7%, accounting for close to 70% of the shortfall relative to projected output.

We show how we can identify the consumption shock based off information on its marginal effect on a large enough panel of economic variables. Specifically, we propose to capture its effect on sectoral prices and quantities by their degree of specialization in the production of goods and services consumed by households. For example, apparel manufacturing, which mostly caters to households will, all else equal, react more to a household demand shock than software, which also caters to firms and government. Such a relationship is present in most equilibrium models.

Our methodology explicitly acknowledges that our identification assumption can only hold as an approximation. The sectoral impact of a shock also depends on inter-sectoral linkages, the differing intensity of various frictions, and other factors. We formally account for this lack of precision by casting our assumptions in terms of uncertain prior distributions within a Bayesian setting. Given this uncertainty, the use of cross-sectoral data plays a crucial role in allowing us to obtain reasonably precise estimates in spite of the uncertainty in the identification assumption.

In order to be able to make best use of detailed cross-sectoral data, we need a tractable econometric methodology which allows us to estimate aggregate and idiosyncratic dynamics jointly and efficiently. We accomplish that with the use of a novel time series model called a Hierarchical Vector Autoregression (Hi-VAR). Given that framework, we can then use established time-series techniques to identify the dynamic response of the economy to the identified shocks, their relevance in explaining the variance of aggregate variables, and their role in particular historical episodes.

How should we interpret the estimated household consumption shocks? To provide additional interpretation, we compare the consumption shock that we infer to time series not used in estimation. Specifically, we show that fluctuations in our inferred shock line up well with fluctuations in household wealth and with a survey-based measure of consumer sentiment. The correlation with household wealth is especially salient around the Great Recession, as one might expect, and the correlation with consumer sentiment appears to hold more consistently over time. Together those exercises suggest a role for both shocks to household wealth and to household sentiment as central driving forces in business cycles.

More generally, we verify that the consumption shock that we identify can be interpreted as a shock to an aggregated Euler Equation. We make this case both theoretically and through a calibrated multi-sector DSGE model. We verify that, in such a model, a discount factor shock has a larger impact on sectors with high consumption shares. We use the same model to inspect the effects of a TFP news shock, and find that those do not generate the same type of pattern. This distinction implies that, to the extent that we are identifying expectational shocks, those are specific to household expectation formation.

We extend our methodology to identify several types of shocks simultaneously. While not strictly necessary for identification, in doing this, we can lever additional information to make up for the uncertainty in our identification hypothesis. For our baseline analysis, we identify six structural shocks. Apart from the shock to household consumption, we identify shocks to energy cost, technological progress, government consumption, monetary policy, and corporate finance. To identify the first three shocks, we rely on input or demand intensity shares that can be read directly from input-output tables. Furthermore, we identify corporate credit shocks by exploiting heterogeneity in external financial dependence measures as in Rajan and Zingales (1998), and monetary shocks using sectoral price stickiness data from Nakamura and Steinsson (2008). As a test of the validity of our procedure, we verify that the impulse response functions for monetary shocks implied by our method largely conform to theoretical predictions as well as findings by previous studies. Together, we find that those six shocks can account for most of the output fluctuations at business cycle frequencies. Consumption (38%) accounts for the largest share. Credit (18%), government consumption (14%), and energy (11%) play a significant if secondary, role. Lastly, monetary and technology shocks play a relatively minor role (5.6% and 7.5%, respectively).

Since at least the 1990s, consumption shocks have been recognized as playing a potentially important roles in business cycles (Blanchard (1993), Hall (1993), Cochrane (1994)). Most notably, in the Great Recession, consumption fluctuations in response to the housing bust have been identified as a primary driving force Mian and Sufi (2015). We provide credible evidence that consumption shocks have been an important contributor to business cycles at least since the 1970s.

The shock that we identify can be alternatively interpreted as a shock to an aggregate consumption Euler equation. Those can emerge from fluctuations in aggregate disaster risk (Gourio, 2012) and idiosyncratic risk (Werning, 2015), among others, so long as the structure of the economy is such that those same shocks only affect production decisions through their effects on consumption. Such discount rate shocks have also been incorporated as an element in structurally estimated DSGE models (Smets and Wouters, 2003). Relative to those economic-model-based approaches, we identify consumption shocks with minimal structure on the statistical model.

The importance of consumption decisions is reflected in the usefulness of consumer sentiment indices for forecasting (Matsusaka and Sbordone, 1995). The recognition of this fact has given rise to explorations of consumer sentiment index as a proxy for news about future shocks (see Barsky and Sims (2012) and Bhandari, Borovička, and Ho (2019)). Our results highlight a potentially special role for household expectations relative to expectations of business owners.

In recent years the interconnections between household wealth, consumption, and employment have become the object of a rapidly expanding literature on quantitative models with heterogeneous agents, summarized in Krueger, Mitman, and Perri (2016). Some of

those approaches build in feedbacks from consumption decisions to employment through the use of new Keynesian frictions (Kaplan, Moll, and Violante, 2018). Our results suggest that further work may do well to concentrate in shocks that emerge within the detailed consumption block implied by those models.

At different points in time, economists have been interested in evaluating the relative importance of "demand" vs. "supply shocks". Classic approaches include a priori long-run restrictions (Blanchard and Quah (1989) and Gali (1999)). More recently, Angeletos, Collard, and Dellas (2020) and Bachmann and Zorn (2013) have argued that demand shocks are the dominant driver of output growth fluctuations in the US and Germany, respectively. Apart from relying on an altogether different source of identification, our methodology singles out household consumption as a particularly relevant source of demand shocks.

From a methodological standpoint, in not imposing "hard" identifying restrictions, our approach connects to the use of sign restrictions, pioneered by Uhlig (2005), Faust (1998), Canova and Nicolo (2002), and Rubio-Ramirez, Waggoner, and Zha (2010). We also build on papers that propose using Bayesian priors instead of hard identification restrictions (Kociecki (2010) and Baumeister and Hamilton (2015)). Relatively speaking, our paper is closest to Amir-Ahmadi and Drautzburg (2020), who add sign and magnitude restrictions on selected sectoral responses to identify aggregate shocks in a standard VAR framework, and ingeniously show that this can lead to substantially improved identification. Our contribution to that literature is to provide a method to add a large number of restrictions on many observables with maximal tractability. As a result, we can add a large number of fairly "soft" identification restrictions that add up to precise estimates. In contrast, Wolf (2020) shows that using a standard number of sign restrictions in a VAR with common aggregate variables can lead to identification problems.<sup>2</sup>

The Hierarchical VAR that we use adds to the existing suite of time series models designed to incorporate large panels, including dynamic factor models (Stock and Watson (2005a)), factor augmented VARs (Bernanke et al. (2005), Boivin et al. (2009)), and global VARs (Chudik and Pesaran (2016), Holly and Petrella (2012)).

Importantly, our approach adds to efforts to find a "general-purpose" methodology for identification that researchers can apply in a broad range of contexts. For example, recently

<sup>&</sup>lt;sup>1</sup>Also, Schwartzman (2014) and Fulford and Schwartzman (2015) use cross-sectional information to identify shocks. Whereas the first paper uses a structural small open economy model, the second paper leverages the cross-sectional impact of a shock identified from a historical narrative. De Graeve and Karas (2014) also make a case for using the information on the relative magnitude of the responses to shocks to help identify shocks.

<sup>&</sup>lt;sup>2</sup>While we use sectoral data to gain more information for identification, another approach to add identification restrictions on aggregate data alone is to use zero restrictions and sign restrictions jointly along the lines of Arias et al. (2018) and Arias et al. (2019).

Gabaix and Koijen (2020) proposed to use weighted averages of idiosyncratic shocks as instruments in various settings.<sup>3</sup> It is also related to the extensive literature on Bartik instruments (Bartik (1991)) in applied microeconomics. We share with this approach the insight that differential exposure to aggregate shocks can be a powerful tool for identification (Goldsmith-Pinkham et al. (2018)).

More broadly, the paper also contributes to the general trend within macroeconomics of using cross-sectional data to inform inference on questions of relevance to macroeconomists (Holly and Petrella (2012), Beraja et al. (2016), Sarto (2018), Chen et al. (2018), and Guren et al. (2019), for example). In the terms laid out by Nakamura and Steinsson (2018), it highlights that the impact elasticities of cross-sectional units to particular aggregate shocks are especially relevant "portable" moments. The use of rich cross-sectional data allows for the use of minimal structural assumptions, which are, furthermore, allowed to be uncertain.

The paper proceeds as follows: In Section 2, we define the consumption shock, provide the basic propositions that establish our identification method, and discuss the specifics of how we implement it using the information on sectoral consumption and output. Section 3 provides the details of the Hi-VAR econometric model used to infer aggregate dynamics from the cross-sectional data. Section 4 provides the results, Section 5 interprets the inferred consumption shock in light of information not used in the estimation. Section 6 cross-validates our methodology against the use of external instruments and provides a more detailed analysis of the role of priors and model fit.

# 2 The Consumption Shock: Definition and Identification

We start our discussion by defining the shock to household consumption and showing how it can be backed out from data given knowledge of the impact that a change in consumption has on a cross section of economic variables. Later we relax this assumption and show how economic theory in combination with a large cross section of sectoral variables can guide the estimation of these impact effects. The discussion clarifies that the shock is, in fact, a composite of various sources of fluctuations that emerge first in the household sector and propagate from there to the rest of the economy through consumption expenditures. Those might include shocks to household credit, to the expectations of households, or to household income risk, so long as those are not the reflection of broader economic shocks. To keep the notation transparent, we start with a simple case where those shocks only affect aggregate

<sup>&</sup>lt;sup>3</sup>The underlying idea is that shocks specific to 'large' idiosyncratic units can have sizeable aggregate effects. In our setting we would call these shocks aggregate shocks (one example is the energy price shock that we model) even if they emanate from one sector.

consumption. We later extend it to a more general case where they affect an equation defining the "household demand" block as in Werning (2015).

Consider a log-linearized economic system, in which innovations to different variables can be expressed as:<sup>4</sup>

$$c_{t} - E_{t-1}c_{t} = \sum_{s \in \mathcal{C}} \frac{\partial c}{\partial \varepsilon_{s}} \varepsilon_{s,t} + \sum_{s \notin \mathcal{C}} \frac{\partial c}{\partial \varepsilon_{s}} \varepsilon_{s,t}$$
$$\mathbf{x}_{t} - E_{t-1}\mathbf{x}_{t} = \frac{\partial \mathbf{x}}{\partial \mathbf{c}} \left( c_{t} - E_{t-1}c_{t} \right) + \sum_{s \notin \mathcal{C}} \frac{\partial \mathbf{x}}{\partial \varepsilon_{s}} \varepsilon_{s,t} + \mathbf{w}_{t}$$

where  $c_t$  is the log deviation of aggregate consumption at time t from its steady-state,  $\mathbf{x}$  is a vector including log deviations of other variables in the economy, including sectoral prices and quantities,  $\varepsilon_{s,t}$  is a vector of macroeconomic shocks<sup>5</sup>,  $\mathcal{C}$  is the set of consumption shocks,  $\mathbf{w}_t$  is a set of shocks specific to each variable in  $\mathbf{x}_t$ . As usual, we assume that aggregate shocks are drawn independently over time and from each other.

The key assumption is that innovations to consumption depends on a set of shocks,  $s \in \mathcal{C}$  that do not affect any other variables directly. In this context, the consumption shock is the linear combination of those innovations,  $\varepsilon_t^C \equiv \sum_{s \in \mathcal{C}} \frac{\partial c}{\partial \varepsilon_{s,t}} \varepsilon_{s,t}$ . A straightforward substitution allows us to express innovations to  $\mathbf{x}_t$  as a function of exogenous shocks only:

$$\mathbf{x}_{t} - E_{t-1}\mathbf{x}_{t} = \frac{\partial \mathbf{x}}{\partial \mathbf{c}} \varepsilon_{t}^{C} + \sum_{s \in \mathcal{C}} \theta_{s}^{x} \varepsilon_{s,t} + \mathbf{w}_{t}$$

where now  $\theta_s^x \equiv \frac{\partial \mathbf{x}}{\partial \varepsilon_{\mathbf{s},\mathbf{t}}} + \frac{\partial \mathbf{x}}{\partial \mathbf{c}} \frac{\partial \mathbf{c}}{\partial \varepsilon_{\mathbf{s},\mathbf{t}}}$ . It follows that the vector of loadings of the consumption shock on the variables  $\mathbf{x_t}$  is given by  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}}$ , which is the key object in our analysis since it encodes the effects of changes in consumption.

We now state a result that allows us to use the information on  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}}$  to infer the time path of  $\varepsilon_t^C$  as well as its contribution to the variance of various economic variables using the Kalman filter. The result is useful because the Kalman filter estimate is the maximum likelihood estimate if the shocks are Gaussian and, more generally, minimizes the mean-squared error of the estimates. It is also part of our more general Bayesian approach.

**Proposition 1** The Kalman filter estimate of  $\varepsilon_t^C$  only depends on  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}}$  and the covariance matrix of  $\mathbf{x}_t - E_{t-1}\mathbf{x}_t$ .

<sup>&</sup>lt;sup>4</sup>In Section 3 we show how a system of this form maps into the time series model what we use for inference.

<sup>&</sup>lt;sup>5</sup>Each shock is independent of the others as well as identically and independently distributed over time with mean 0.

The proposition states that one can infer the shock based on two pieces of information: The loadings of a set of observed variables on that shock and the covariance of those variables. Importantly, the estimate *does not* depend on the loadings of innovations on other shocks.

Our result holds because, by design, the Kalman filter separates the effect on a measured variable of an unobserved state variable (in our case, the consumption shock) from a "noise" term. The latter is typically identified with measurement error and defined to be orthogonal to the state variable. In the current context, this noise term includes the effect of other macroeconomic shocks. Those shocks can be treated as noise because, by a standard assumption in macroeconomics, they are orthogonal to the consumption shock.<sup>6</sup>

To fix ideas further, suppose there were two macroeconomic shocks of interest, the consumption shock, defined as above, and a shock to the financial system. This example is relevant since, as it turns out, the subsequent analysis implies that these are the two most relevant shocks to explain output fluctuations in the period under analysis. A shock to the financial system would affect the non-consumption variables in the economy directly by reducing the supply of credit to non-financial firms. It could also have a substantial impact on consumption through a reduction in the supply of consumer credit or its impact on household wealth and employment prospects. This consumption impact would, in turn, feed back into the rest of the economy through the dependence of different variables on consumption. Suppose the part of the financial shock that propagates through consumption was erroneously attributed to the consumption shock, while the part that affects production directly through the credit supplied to non-financial firms remained attributed to a financial shock. Then, the two misidentified shocks would be correlated. It follows that the Kalman filter estimate would not make this erroneous attribution and would identify the shocks correctly. We give a detailed proof in the appendix. As one might expect, increasing the dimension of the  $\mathbf{x}_t$ vector included in the estimation will improve the precision of our estimates.

**Proposition 2** The variance of the estimation error of  $\varepsilon_t^C$  declines (weakly) as the dimension of  $\mathbf{x}_t$  increases. The estimation error disappears as the dimensionality of  $\mathbf{x}_t$  goes to infinity.

The proof of this proposition proceeds in two steps. First, under standard regularity conditions on the dependence structure of  $\mathbf{w}_t$  (satisfied in our econometric model) the space spanned by all factors (the  $\varepsilon$  shocks) can be identified as the number of sectors grows towards infinity (see Bai and Ng (2008) and Stock and Watson (2016)). The impact of  $\varepsilon_t^C$  on  $\mathbf{x}_t$  –

<sup>&</sup>lt;sup>6</sup>This is a significant difference with the approach in Fulford and Schwartzman (2015), that requires restrictions on factor loadings associated with other shocks. The reason such restrictions are not necessary is that the Kalman filter exploits the information in the covariance matrix of  $\mathbf{x}_t$ , in combination with the definition of macroeconomic shocks as being independent of each other.

 $E_{t-1}\mathbf{x}_t$ ,  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}}$  encodes our identification assumptions and is thus known.<sup>7</sup> With these impact coefficients in hand, we can think of regressing for each time period  $t \mathbf{x}_t - E_{t-1}\mathbf{x}_t$  on the regression coefficients. This regression will then uncover  $\varepsilon_t^C$  exactly in the limit as the number of sectors grows towards infinity.

The results above make clear that the identification of the consumption shock only requires the effects of various economic variables and the covariance matrix between innovations to different cross-sectional units. It is straightforward to see that the propositions apply more broadly to any shock. In the language of Nakamura and Steinsson (2018), the marginal effects of a shock on a large panel of economic variables, possibly including several sectors or regions, would be the "portable" statistic useful to identify the time-path of the shock and its aggregate effects.

## 2.1 Extension: Shocks to the aggregate consumption block

One may legitimately ask whether meaningful economic systems of the form expressed above exist. Aggregate consumption may also depend on other variables in complicated ways, so that isolating a consumption shock may not be realistic. Fortunately, as shown in Werning (2015), in a large class of economic systems, including many with heterogeneous consumers and incomplete markets, the set of variables determined jointly with aggregate consumption is small. In fact, Werning shows that for those models one can write a "generalized" Euler equation which, in innovation form, would be expressed as:

$$c_t - E_{t-1}c_t = -\phi \left( r_t - E_{t-1}r_t \right) + E_t c_{t+1} - E_{t-1}c_{t+1} + \varepsilon_t^C + \sum_{s \notin \mathcal{C}} \frac{\partial c}{\partial \varepsilon_s} \varepsilon_{s,t}$$

where  $r_t$  is the interest rate faced by households. Now, the consumption shock effectively acts like a shock to the household's discount factor. This implies that not only innovations to consumption, but also to interest rate faced by households and revisions to future consumption will depend on the consumption shock  $\varepsilon_t^C$ . In this more general setting,  $\mathbf{x}_t$  becomes:

<sup>&</sup>lt;sup>7</sup>In our empirical implementation we do consider uncertainty about these identification assumptions.

$$\mathbf{x}_{t} - E_{t-1}\mathbf{x}_{t} = \frac{\partial \mathbf{x}}{\partial \mathbf{c}} \left( c_{t} - E_{t-1}c_{t} \right)$$

$$+ \frac{\partial \mathbf{x}}{\partial \mathbf{E}\mathbf{c}} \left( E_{t}c_{t+1} - E_{t-1}c_{t+1} \right)$$

$$+ \frac{\partial \mathbf{x}}{\partial \mathbf{r}} \left( r_{t} - E_{t-1}r_{t} \right)$$

$$+ \sum_{s \notin \mathcal{C}} \frac{\partial \mathbf{x}}{\partial \varepsilon_{\mathbf{s}}} \varepsilon_{s,t} + \mathbf{w}_{t}$$

so that the loading of the consumption shock  $\varepsilon_t^C$  on  $\mathbf{x}_t$  becomes  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}} \frac{\partial c_t}{\partial \varepsilon_t^C} + \frac{\partial \mathbf{x}}{\partial \mathbf{E} \mathbf{c}} \frac{\partial E c_{t+1}}{\partial \varepsilon_t^C} + \frac{\partial \mathbf{x}}{\partial \mathbf{r}} \frac{\partial r_t}{\partial \varepsilon_t^C}$ .

The exercise raises the possibility that consumption shocks may affect non-consumption variables through the effect of those shocks on interest rates and expected future consumption. To highlight that our identification strategy accounts for that possibility, in Section 2.2, we show that our identification assumptions align well with the sectoral impact of a discount rate shock in a quantitative DSGE model with sectoral linkages and nominal frictions.

## 2.2 Identification of the consumption shock through priors

The theoretical discussion above makes clear how one can recover the time-path of the consumption shock given knowledge about the impact of that shock on a panel of economic variables. In order to implement those procedures we need two objects: (i) A panel of innovations to a large number of variables  $(\mathbf{x}_t - E_{t-1}[\mathbf{x}_t])$  and (ii) the "loading" of those innovations on the aggregate shock,  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}}$  (or  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}} \frac{\partial c_t}{\partial \varepsilon_t^C} + \frac{\partial \mathbf{x}}{\partial \mathbf{E} \mathbf{c}} \frac{\partial E_{t+1}}{\partial \varepsilon_t^C} + \frac{\partial \mathbf{x}}{\partial \mathbf{r}} \frac{\partial r_t}{\partial \varepsilon_t^C}$  in the case of a shock to the Euler equation).

The problem of obtaining the innovations to different variables is an econometric problem that we tackle in Section 3 below.<sup>8</sup> To do that, we construct a time series model that builds on (and extends) existing techniques such as dynamic factor models and factor augmented VARs. For now, we assume that we can measure those innovations, and focus instead on the identification of the marginal effects.

Precise estimates of the required loadings are hard to obtain. For example, it could require obtaining an instrument for the consumption shock, for which there is currently no clear candidate. Otherwise, one could try to derive those loadings from a structural model, but this would beg the question as to whether the model is correctly specified. To make progress, we use the fact that, in a wide range of models, the marginal effect of a consumption shock on sectoral variables depends on the share of sectoral output that is sold

<sup>&</sup>lt;sup>8</sup>In practice, the parameters of the model that allows us to filter out innovations are estimated jointly with the shocks.

to households. This is our key identification assumption. As an illustration, we prove that this assumption holds for a prototypical multi-sector equilibrium model in Appendix C.

At the same time, this dependence is admittedly imprecise. For that reason, we use Bayesian methods to make this lack of precision explicit and allow it to affect our estimates and statements about our uncertainty surrounding those estimates. In formal terms, we postulate prior distributions for the marginal effects of shocks. The prior means depend on cross-sectional information that we describe below, and the prior variances denote our degree of uncertainty around our assumptions. This use of "soft" prior restrictions for identification was proposed by Baumeister and Hamilton (2015), and contrasts with traditional approaches, which achieve identification by setting hard constraints on the shock process. Relative to that previous work, we can estimate a large scale model tractably by setting a Gaussian priors directly on the marginal impact of the structural shocks.

We now discuss in more detail how we set those priors for the marginal effect of consumption on sectoral variables. We denote the marginal effect on impact of a shock s to a variable k in sector i by  $D_{k,s}^i$ . To set the prior mean for  $D_{k,s}^i$ , we assume that it can be decomposed as follows:

$$(E\left[D_{k,s}^{i}\right])^{2} = \gamma_{k}^{i}\beta_{k,s}\alpha_{k,s}^{i} \quad , \tag{1}$$

$$(E\left[D_k^i\right])^2 = \sum_{s=1}^S (E\left[D_{k,s}^i\right])^2 \quad . \tag{2}$$

where

- 1.  $\alpha_{k,s}^i$  is a measure of the relative impact of shock s on variable k for sector i as compared to other sectors. We encode in this component the notion that, the more a sector sells of its output directly to households, the more sensitive it is to household consumption shocks. This measure, which we derive from cross-sectoral data, is not comparable across shocks.<sup>10</sup>
- 2.  $\beta_{k,s}$  is a measure of the *overall* impact of shock s on variable k across all sectors. We use an 'ignorance prior,' and set this variable to 1/S, where S is the number of

<sup>&</sup>lt;sup>9</sup>We work with the squared prior mean here (i) to focus on pinning down the magnitudes of the prior mean in this step (economic theory will then help us pin down the sign of the prior mean) and (ii) because we find it easier to work at the level of contributions to the overall variance since equation (2) gives us information about those contributions.

<sup>&</sup>lt;sup>10</sup>To keep units consistent, we normalize our indicator variable to be between 0 and 1. If there are missing values for the indicator variables for some sectors, we assume that the indicators for those sectors take on the average value of the relevant indicator.

structural shocks that we will allow for in our implementation.

3.  $\gamma_k^i$ : a measure of the overall sectoral sensitivity of variable k in sector s to all shocks. For example, this variable encodes the notion that consumption of durable goods is overall more sensitive to all shocks than the consumption of nondurables. Given  $\alpha_{k,s}^i$  and  $\beta_{k,s}$ , we can back out this variable if we have values for  $\sum_{s=1}^{S} (E\left[D_{k,s}^i\right])^2$ . We estimate those by estimating the model described in Section 3 below in a training sample with agnostic priors. We do not need to impose any identifying restrictions on the structural shocks for that training sample step because we are only interested in estimating how relevant those shocks are for fluctuations of different variables together, and the factor structure of the shocks allows us to do that even if we cannot disentangle the role of individual shocks. 12

Given information on  $\alpha_{k,s}^i$ ,  $\beta_{k,s}$ , and  $\sum_{s=1}^S (E\left[D_{k,s}^i\right])^2$  we can solve the system of linear equations above for  $(E\left[D_{k,s}^i\right])^2$  and  $\gamma_k^i$ . The procedure above thus allows us to set a magnitude for the prior mean  $E\left[D_{k,s}^i\right]$ . We use a priori information on the sectoral impact of shocks to set the sign.

As an example of what this procedure achieves, consider a scenario where we only have two shocks (named shock 1 and 2), and one observable per sector. Also, to cut down on notation define  $\tilde{D}_{k,s}^i \equiv [E(D_{k,s}^i)]^2$  and  $\tilde{\alpha}_{k,s}^i \equiv \beta_{k,s}\alpha_{k,s}^i$ . Let's focus on one specific sector, sector a. There are three equations in three unknowns for that sector. We also drop the subscript k since there is only one variable.

$$\tilde{D}_1^a = \gamma^a \tilde{\alpha}_1^a \tag{3}$$

$$\tilde{D}_2^a = \gamma^a \tilde{\alpha}_2^a \tag{4}$$

$$\tilde{D}^a = \tilde{D}_1^a + \tilde{D}_2^a \tag{5}$$

Adding the first two equations gives

$$\tilde{D}^a = \gamma^a \tilde{\alpha}_1^a + \gamma^a \tilde{\alpha}_2^a$$

and thus

$$\gamma^a = \frac{\tilde{D}^a}{\tilde{\alpha}_1^a + \tilde{\alpha}_2^a}$$

<sup>&</sup>lt;sup>11</sup>The prior we use for the agnostic estimation is the same as for our actual estimation except that we impose priors with large variances on the impact of the structural shocks and the residual covariances. For the choice of the training sample, our default is the full sample - our approach can, therefore, be interpreted as an empirical Bayes approach.

<sup>&</sup>lt;sup>12</sup>When doing this we also only impose a very loose prior on the covariance matrix of the non-structural shocks.

which in turns allows us to solve for the squared shock loadings:

$$\tilde{D}_1^a = \frac{\tilde{D}^a}{\tilde{\alpha}_1^a + \tilde{\alpha}_2^a} \tilde{\alpha}_1^a$$

Our procedure thus produces (squared) prior means that weight different shocks according to both the relevant indicator  $\alpha$  and the overall impact of a shock on a variable,  $\beta$ .

By choosing normal priors, we do not necessarily force the sign restrictions to hold with certainty. Because of the normality assumption, the posterior mean might have a different sign from the prior mean. This probability depends on the prior variance. In our baseline estimates, we set it such that the prior standard deviation to be  $1/2 \times abs$  ( $E\left[D_{k,s}^{i}\right]$ ), ensuring a wide band of uncertainty around our prior assumptions.

Table 1 depicts the sectors with the largest and smallest fraction of their output sold to households. The top sector is Men's and boys' clothing. It has a ratio of consumption to gross output that is larger than one since a sizeable fraction is imported. Sectors at the top include education (such as elementary and daycare schools), and at the bottom include equipment and machinery (such as cookware and tableware light trucks), and business services (such as employment agency services).

Rank (out of 187 sectors)	Sector name	C/Y value
Top 1	Men's and boys' clothing	1.30
Top 10	Elementary and secondary schools	1.00
Top 20	Day care and nursery schools	0.98
Top 40	Other video equipment	0.81
Top 60	New domestic autos	0.66
Median (top 94)	Cereals	0.55
Bottom 60	Photographic equipment	0.43
Bottom 40	Other fuels	0.28
Bottom 20	Nonelectric cookware and tableware	0.16
Bottom 10	Employment agency services	0.01
Bottom 1	Used light trucks	0.00

Table 1: Top and bottom sectors, by the ratio of consumption to gross output

To obtain a rough sense of the relevance of those sectoral differences in predicting business cycles, we calculate the difference in 12 months output and consumption growth, and inflation in the top 40 sectors by consumption orientation as compared to the bottom 40. Figure 1 shows the correlation between those differences with and year on year output growth at different lags and leads. We also include the correlation between aggregate consumption growth and aggregate output growth and of output with itself for further reference. The

figure shows that consumption tends to lead output by a little, but that the difference between sectors in different points in the cross-section leads output by more. While only a rough test of predictive value, this picture suggests that this particular way of looking at the cross-section of sectors has value as a lens through which to understand output fluctuations.

We can further verify that our prior assumption is sensible in the context of a fully specified multi-sector extension of the medium-scale New-Keynesian model of Justiniano et al. (2010) (described in detail in Appendix E).<sup>13</sup> We examine the impacts of a discount factor shock (which affects household consumption directly through the Euler equation). The top panel of figure 2 shows the relationship between the consumption / gross output ratio implied by the model calibration for each sector and the immediate impact of a shock to the Euler equation on output in each sector. It confirms that in the context of this canonical business cycle framework, the impact of the discount shock on output does increase with the Consumption / Gross Output ratio, albeit imperfectly.

The Euler equation can be equally affected by news shocks (see, for example, Schmitt-Grohé and Uribe (2012)). However, those shocks affect current production through other channels, for example by boosting investment and production in upstream sectors. In the end, those other effects lead to a very different pattern of impact, as shown in the bottom panel of Figure 2.<sup>14</sup> Sectors that have a lower ratio of consumption to gross output react more. When news hits, the most significant responses are in sectors that are deeper inside the production chain by producing intermediate inputs or investment goods. Our identification assumption thus does generally not mistake news shocks for consumption shocks.

Lastly, we also need to set the prior mean for the impact of shocks on aggregate variables. For the consumption shock, we use the minimal assumption that it tends to increase consumption while remaining agnostic on its impact on other aggregate variables. To be precise, we set the prior mean impact of the consumption shock on consumption innovations to be consistent with the overall variance of those innovations driven by aggregate shocks (which we obtain from our identification-agnostic estimation on a training sample). We further set the prior impact of the consumption shock on other aggregate variables to have mean zero, and a standard deviation of 0.25 (we use the same prior for the impact of the other structural shocks in our model on consumption). When implementing our empirical strategy, we will further constrain our approach by simultaneously identifying various shocks. The identification approach for those other shocks follows a similar structure as the identification of the

<sup>&</sup>lt;sup>13</sup>When quantifying the equilibrium model, we allow for close to 50 sectors calibrated to match US intersectoral linkages. This is just for numerical efficiency. In our empirical application we use the full 187 sectors mentioned earlier.

<sup>&</sup>lt;sup>14</sup>We model a news shock in the evolution of Total Factor Productivity. Details can be found in Appendix E.

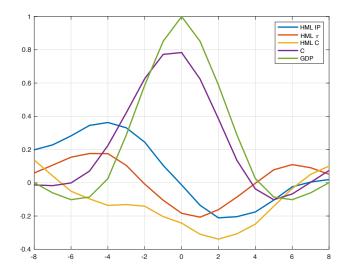


Figure 1: Correlation with lags of GDP

The horizontal axis refers to the lag of GDP, with negative numbers corresponding to leads. HML IP is the difference between the FRB Industrial Production index with high and low consumption share sectors. HML  $\pi$  and HML C refer to the same difference for inflation and consumption growth among BEA personal consumption expenditure categories.

consumption shock, and we will discuss it in more detail in section 3.

# 3 Estimation: The Hierarchical VAR model

We now describe in detail the full econometric framework used to obtain the results in the paper. The framework allows us to jointly measure innovations to aggregate and sectoral variables, identify aggregate shocks, and estimate impulse response functions, variance, and historical decompositions of the impact of those shocks on different variables. Specifically, we combine a VAR-type time series model (Sims (1980)) for a vector of aggregate variables  $Y_t$  with autoregressive models for vectors of sectoral data  $X_t^i$ , where t indicates the time and i indicates the sector. Aggregate and sectoral data interact in two ways: (i) via structural shocks that affect both types of data and (ii) via direct feedback from (lagged) aggregate data to sectoral data. We describe each of these blocks in turn. We follow up with an in-depth discussion of how the model ought to be interpreted and describe in detail how the model is estimated. We conclude the section with a comparison with other approaches.

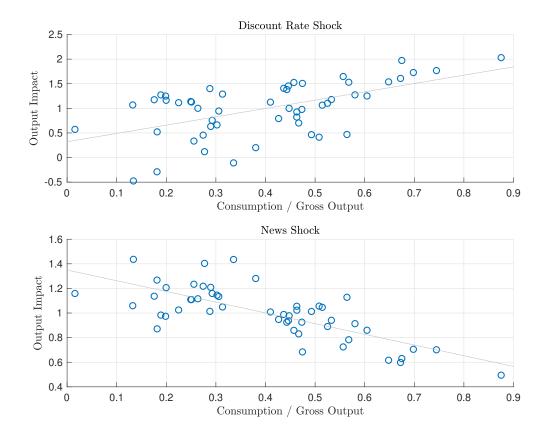


Figure 2: Response to shock vs. consumption / output data in calibrated structural model.

# 3.1 Modeling aggregate variables

We model aggregate variables as following a linear vector autoregressive process. A key difference from traditional VARs is that we break the link between forecast errors and structural shocks, thus allowing sectoral data to help identify structural shocks. The aggregate variable vector  $Y_t$  (of dimension N by 1) is a function of its past values, structural shocks  $\varepsilon_t$ , and other shocks  $w_t$ :

$$Y_t = \mu + \sum_{l=1}^{L} A_l Y_{t-l} + D\varepsilon_t + w_t \tag{6}$$

where  $\varepsilon_t$  is of dimension  $S \times 1$ , and D is an  $N \times S$  matrix encoding the impact of the Gaussian structural shocks  $\varepsilon$  on the aggregate variables, and  $w_t$  is a independently and identically distributed  $N \times 1$  vector of mean 0, non-structural Gaussian shocks with covariance matrix  $\Omega$ . We further assume that  $\varepsilon_t \sim_{iid} N(0, I)$ . As will be clear later, we can allow for S < N, S = N, or S > N, whereas standard VAR analyses require  $S \le N$ .

 $<sup>^{15}</sup>$ The distributional assumptions are necessary because we ultimately want to carry out Bayesian inference, for which we need to build a likelihood function.

For later discussion, it is useful to note that the one-step ahead forecast error for the aggregate level is given by  $D\varepsilon_t + w_t$ , whereas a standard VAR model for the aggregate variables would assume that any estimate of the structural shock is a linear combination of the aggregate one-step-ahead forecast error.<sup>16</sup>

## 3.2 Modeling idiosyncratic variables

There are observations for I idiosyncratic units (such as industries, regions, or, in our specific application, sectors) with K variables (such as prices and quantities) each. The law of motion for the data from unit i, summarized in the K-dimensional vector  $X_t^i$ , is given by:

$$X_t^i = \mu^i + \sum_{l=1}^{L^X} B_l^i X_{t-l}^i + \sum_{l=1}^{L^Y} C_h^i Y_{t-l} + D^i \varepsilon_t + w_t^i$$
 (7)

where  $D^i$  is a  $K \times S$  matrix encoding the impact of shocks  $\varepsilon$  on the idiosyncratic variables (i.e. it collects the variables  $D^i_{k,s}$  described in section 2.2) and the mean zero Gaussian vector  $w^i_t$  incorporates the impact of idiosyncratic (or non-structural) shocks on individual units. We denote the covariance matrix of  $w^i_t$  by  $\Omega^i$ . We assume that  $w^i_t$  is independent across i and independent from  $w_t$ . Our assumptions on the correlation structure of  $w^i_t$  allow for correlation in the innovations to different variables within a sector, although not across sectors.

# 3.3 Interpretation and comparison with other approaches

We now present a more detailed discussion of how to interpret the model and of the relevant identification issues. This interpretation will also allow us to compare the model with other existing approaches.

To interpret the econometric model, it is be useful to rewrite our model as follows: first, define the vector of all observables

$$Z_t = [Y_t' \ X_t^{1'} \ X_t^{2'} \ \dots \ X_t^{I'}]'$$

We can then recast our model in the following way:

$$Z_{t} = \mu^{Z} + \sum_{l=1}^{\max(L^{X}, L^{Y}, L)} B_{l}^{Z} Z_{t-l} + \underbrace{D^{Z} \varepsilon_{t} + w_{t}^{Z}}_{u_{t}^{Z}}$$
(8)

 $<sup>^{16}</sup>$ This is true even if fewer than N shocks are identified, as is common in the literature on sign restrictions in VARs.

where  $w_t^Z$  is a vector that stacks the non-structural shocks according to the ordering of observables in  $Z_t$ . Our model imposes restrictions on the matrices  $B_l$  by assuming that one sector's variables cannot directly respond to any other sector's lagged variables. Furthermore, we impose that the residuals  $u_t^Z$  are orthogonal to all variables in  $Z_{t-1}$ . This model can be mapped back into the system described in Section 2 - the conditional mean of the variables is given by  $\mu^Z + \sum_{l=1}^{max(L^X, L^Y, L)} B_l^Z Z_{t-l}$ , and the impact of the consumption shock and other structural shocks is determined by  $D^Z \varepsilon_t$ , where the elements of  $D^Z$  corresponding to a consumption shock map into  $\frac{\partial \mathbf{x}}{\partial \mathbf{c}}$ .

We now characterize the identification of model parameters and aggregate shocks. Because of the structure of the one-step-ahead forecast error, we can identify  $\mu^Z$  as well as the coefficient matrices  $B_l^Z$ , as is usually the case in VAR analyses.

Focusing on  $u_t^Z$ , we can see that it follows a factor structure, where the common factors are the iid structural shocks  $\varepsilon_t$ , so that standard results on identification in factor models apply (Bai and Ng (2008)). While we cannot identify the effects of individual structural shocks without additional assumption, we can identify the overall effect of *all* structural shocks.

To identify  $\varepsilon_t$ , we need identification restrictions akin to those used in the structural VAR literature. To see this, define

$$u_t = D\varepsilon_t + w_t, \tag{9}$$

$$u_t^i = D^i \varepsilon_t + w_t^i \ \forall i. \tag{10}$$

For any conformable orthogonal matrix Q, we can construct alternative models that feature the same first and second moments and thus the same Gaussian likelihood:

$$u_t = \underbrace{DQ^{-1}}_{\tilde{D}} \underbrace{Q\varepsilon_t}_{\tilde{\varepsilon}_t} + w_t \tag{11}$$

$$u_t^i = \underbrace{D^i Q^{-1}}_{\tilde{D}^i} \underbrace{Q \varepsilon_t}_{\tilde{\varepsilon}_t} + w_t^i \ \forall i.$$
 (12)

It follows that, even though the overall impacts  $D\varepsilon_t$  and  $D^i\varepsilon_t$   $\forall i$  are identified, the impact of each shock is not, so that additional restrictions are necessary to pin those down. The priors on D and  $D^i$  described in section 2 above further constrain Q but, unless they are degenerate, do not pin it down entirely. However, as shown by recent work, even such "set" identification can be very informative if applied to enough variables (Amir-Ahmadi and Drautzburg, 2020). This insight is especially relevant for our setting, where we have many sectors on which we impose restrictions.

It is also important to point out that this identification discussion does not mean that all prior distributions of D and  $D^i$  are equally consistent with the data. What is true is that for any given value of D and  $D^i$ , there is a set of other values that have the same likelihood, but some sets are more likely than others. Prior distributions will put different weights on D and  $D^i$ 's belonging to different sets. They can, therefore, be assessed via their marginal likelihoods obtained by integrating across all their possible values. The outcome is that, while the priors are essential for identification, the data constrains posterior estimates for D and  $D^i$ .

Our econometric model breaks the close link between one-step-ahead forecast errors and structural shocks implied by standard VARs. This distinction is useful for two distinct reasons: (i) this allows sectoral data and aggregate data to jointly identify structural shocks and (ii) it does not necessarily force structural shocks to explain large fractions of the variances of our observables if the data do not call for structural shocks to be important.<sup>17</sup> To safeguard ourselves against overestimating the contribution of  $w_t$  to aggregate variation, we suggest adding shocks to the vector of structural innovations  $\varepsilon_t$  with no loose "identification" priors. The additional 'structural' shocks will soak up any explanatory power that the model would otherwise falsely attribute to  $w_t$ . In our application, we add three of those shocks. We should note that others have imposed a factor structure on residuals of time series models. Altonji and Ham (1990), Clark and Shin (1998), Stock and Watson (2005b), and Gorodnichenko (2005) follow the same route to estimate common shocks in time series models with many observables. <sup>18</sup> In particular, we share with Stock and Watson (2005b) the assumption that non-structural shocks cannot contemporaneously affect variables in other blocks of the model. Gorodnichenko (2005) interprets  $w_t$  as shocks that can arise in equilibrium models due to "expectations errors, measurement errors, heterogeneous information sets (e.g., consumers and the central banker can have different information sets), myopia and other forms of irrational behavior." Gorodnichenko (2005) also describes an equilibrium model with imperfect information that has such a factor structure in residuals.

Our model differs from other approaches that model large panels of time series by explicitly modeling a distinction between time series at the aggregate and idiosyncratic levels and by explicitly modeling the dynamics in each idiosyncratic unit. For example, FAVARs (Bernanke et al. (2005)) do not explicitly model dynamics at the level of each individual sector. Furthermore, identifying structural shocks in both factor models and FAVARs requires

 $<sup>^{17}</sup>$ Our model does not preclude structural shocks from being the main drivers of business cycles a priori: the estimated variances of the non-structural shocks could be minimal.

<sup>&</sup>lt;sup>18</sup>Cesa-Bianchi and Ferrero (2020) use this assumption in the context of a panel VAR for sectors of the US economy. Their work focuses on identifying shocks via restrictions on aggregate variables after exploiting this factor structure.

imposing identifying assumptions for both the unobserved factors and the structural shocks. While our model does have a factor structure, we only require identifying assumptions for the structural shocks since all other factors are observable. Another modeling approach that touches on issues similar to ours is Global VAR (Chudik and Pesaran (2016)). Those do not break the link between aggregate shocks and one-step-ahead forecast errors at the aggregate level and require a priori restrictions on how shocks propagate between idiosyncratic variables.

What sets our approach apart from the previous literature on structural VARs is that (i) because of our model structure, we can use substantially larger datasets than standard VAR applications can, (ii) we can identify several shocks simultaneously, rather than one or two.<sup>19</sup> Our approach is close to the Dynamic Factor Model framework in Stock and Watson (2005a), with aggregate variables as "observed" factors. One way in which we extend on that approach is by allowing explicitly for correlation across the variables within each idiosyncratic block.<sup>20</sup> Those models often select a small number of factors, which follow persistent VAR processes. In contrast, we use a larger number of *iid* structural shocks as factors in our empirical application. Those descriptions of the data are mutually consistent, since multiple *iid* shocks can drive each of the "VAR factors". Typically, however, in dynamic factor models, the number of *iid* shocks driving the 'VAR factors' is imposed to be the same as the number of 'VAR factors.'<sup>21</sup>

Finally, as can be seen from equation 8, our model is a restricted VAR using many variables. As such, there is a natural connection to the literature that uses shrinkage priors for such VARs (Banbura et al. (2010)). Instead of using shrinkage priors (such as the Minnesota prior) in a VAR for all of our variables, we instead impose restrictions implied by the grouping of variables into sectoral and aggregate variables.<sup>22</sup>. One key innovation relative to many prior studies is that, as discussed above we apply a Gaussian prior directly to the effects of the structural shocks on aggregate and sectoral data.<sup>23</sup> This procedure allows us to

<sup>&</sup>lt;sup>19</sup>By estimating the responses to structural shocks directly, we do not need to post-process reduced-form VAR estimates to obtain the structural representation that allows us to compute the effects of structural shocks. Eliminating this additional step is useful because the algorithms used to deliver the impulse responses after estimating a reduced-form model can be numerically time-consuming because not all proposed candidate parameter vectors of the structural VAR satisfy the identification restrictions as in Rubio-Ramirez et al. (2010) or because the imposed restrictions are overidentifying as in Amir-Ahmadi and Drautzburg (2020).

<sup>&</sup>lt;sup>20</sup>As Stock and Watson (2016) discuss, likelihood-based approaches to factor model estimation typically assume that idiosyncratic shocks are uncorrelated across series. The primary approach that allows for such correlation are non-parametric approximate factor models estimated with frequentist methods.

<sup>&</sup>lt;sup>21</sup>Notice that, for applications where no structural shocks are identified, one can assume as many iid shocks as 'VAR factors' without loss of generality under Gaussianity and linearity.

<sup>&</sup>lt;sup>22</sup>We do still use a Minnesota-type prior for the aggregate variables in our VAR.

<sup>&</sup>lt;sup>23</sup>We can do this because we directly estimate the impact of structural shocks rather than first estimate a reduced-form model and then infer the structural model afterward, as is common in the VAR literature. By

impose more prior information on the magnitudes of these effects compared to what would be feasible in the standard sign restriction approach.<sup>24</sup> By exploiting our specific model structure, we can efficiently estimate very large scale models. Also, because we directly estimate a structural VAR, our approach can handle set-identified, exactly identified, and over-identified environments. The difference between those alternatives depends on the priors on the parameters governing the contemporaneous impact of structural shocks.

Importantly, our approach is computationally very efficient because, as we will show below, it relies solely on standard steps in Gibbs samplers (drawing from Normal and inverse-Wishart priors as described in Koop and Korobilis (2010) as well as using Gibbs sampling for linear and Gaussian state-space models as in Carter and Kohn (1994)). The hierarchical structure of our model implies that those procedures are amenable to parallelization.<sup>25</sup> This implies that our approach can be very efficient even in applications that have a much larger scale than our application in this paper.<sup>26</sup>

## 3.4 Implementing the estimation: Priors and Sampling algorithm

#### **3.4.1** Priors on $D^i$ and D

We describe the prior distributions for the impact coefficients D and  $D^i$  for the consumption shock in detail in Section 2 above. We use a similar procedure to add priors to the other five shocks: technology, credit supply, government consumption, monetary, and energy cost. Table 2 describes the aggregate and sectoral indicators used to construct the prior means for the impact matrices. We describe the direction of impact on sectoral variables and the ranking for which variables are most affected in table 3. Those follow basic economic theory: the household consumption shock has a larger output and price impact on sectors with higher consumption to gross-output ratio and a smaller consumption impact. The technology shock has a more positive quantity impact and more negative in sectors with high R&D expenditures. Credit shocks reduce quantities and increase prices in sectors with high exter-

directly estimating a structural representation, we follow in the footsteps of, for example, Baumeister and Hamilton (2015) and Sims and Zha (1998), who estimate structural VARs. Baumeister and Hamilton (2018) and Baumeister and Hamilton (2019) are closest to our approach because they also use the information on the contemporaneous impact of the structural shocks to inform their priors.

<sup>&</sup>lt;sup>24</sup>In the standard approach to impose sign restrictions, as outlined in Rubio-Ramirez et al. (2010), inequality restrictions are imposed on impulse responses in conjunction with a uniform (Haar) prior on the rotation matrices that map reduced form parameters to initial impulse responses. We could incorporate strict inequality restrictions in our framework by incorporating a Metropolis step into our algorithm.

<sup>&</sup>lt;sup>25</sup>This parallelization argument does not hold, for example, in large scale VARs. And while certain aspects of Gibbs samplers for factor models might also be amenable to parallelization, these models do not directly emphasize the dynamics of all variables in the sector transparently.

 $<sup>^{26}</sup>$ As a final note on the model, it might be helpful to note that one could interpret the lagged aggregate variables  $Y_{t-l}$  as additional, but observable, factors.

nal dependence. Government shocks increase prices and output (and reduce consumption) in sectors with high government consumption. Monetary shocks increase prices by less and increase output and consumption by more in sectors where prices are stickier. Energy shocks increase prices and reduce quantities by more in sectors that are more intensive in energy inputs. Appendix B.2 describes the data used to set those priors in detail. In Appendix C, we develop a tractable two-period model that allows us to derive those relationships. We also introduce three additional structural shocks (elements of  $\varepsilon$ ) to allow for the possibility that we do not explicitly model some important source of fluctuation.<sup>27</sup> We do not impose any restriction on those elements. As we will see later, when we present a variance decomposition, these three additional shocks are not important drivers of the aggregate variables in our model.

	Positive aggregate impact	Index for sector-specific $\alpha^i_{k,s}$ in $E[D^i_{k,s}]$
Household	Household consumption	Household consumption / Gross output
Technology	TFP (Fernald, 2014)	R&D expenditures / Gross output
Credit	Baa-Treasury credit spread	External finance dependence
Government	Government consumption	Government consumption / Gross output
Monetary	Fed funds rate	Average price duration
Energy	Energy price index	Cost of energy inputs / Gross output

Table 2: Assumptions used for prior means for impact coefficients for different shocks. See Appendix C for detailed motivation

	PCE price	PCE quantity	Industrial Production	
Household	$+\uparrow$	$+\downarrow$	+ ↑	
Technology	- ↓	+ ↑	$+\uparrow$	
Credit	$+\uparrow$	- \downarrow	- 🗼	
Government	$+\uparrow$	- \downarrow	$+\uparrow$	
Monetary	$+\downarrow$	+ ↑	$+\uparrow$	
Energy	$+\uparrow$	- \downarrow	- ↓	

Table 3: Signs and ranking of impact  $\alpha_{k,s}^i$ :  $\uparrow$  implies that impact increases with sector-specific index for  $\alpha_k^i$  in table 2 and  $\downarrow$  that it decreases.

# **3.4.2** Priors on $\mu^Z$ and $B_l^Z$

For the intercepts at the sectoral and aggregate level, we use Gaussian priors with mean zero and large variances. For the  $A_l$  matrices (the VAR coefficients at the aggregate level),

<sup>&</sup>lt;sup>27</sup>We use loose Gaussian priors centered at 0 for the corresponding elements of D and  $D^i$ .

we use a Minnesota-type prior (Koop and Korobilis (2010)). We do this because we have a relatively large number of observables at the aggregate level, so some prior shrinkage is useful. At the sectoral level, we have fewer variables (per sector), so we simply use priors for  $B_l^i$  and  $C_h^i$  centered at 0 with relatively large variances.

#### 3.4.3 Setting priors for $\Omega$ and $\Omega^i$

To use the Gibbs sampler, we use inverse-Wishart priors for the covariance matrices of the reduced form shocks at the aggregate and sectoral levels. As is well known, this imposes some restrictions on what prior beliefs we can impose on our model. One is that the variances are bounded away from 0 (really not much of a problem in our case), while the main problem is that there is no genuinely uninformative prior (as we increase the variance, we also have to at some point increase the prior mean since variances are bounded below by 0). To set this prior, we will use the results from the of the estimation with the training sample and an agnostic prior, as also outlined in Table 4.

**Prior on**  $\Omega$  To set the prior for  $\Omega$ , we use results from our agnostic prior estimation. We set the prior mean to the estimated posterior mean of  $\Omega$  and use as degrees of freedom the size of our overall sample. Table 4 below summarizes the priors on the different parameters.

**Prior on**  $\Omega^i$  For  $\Omega^i$ , we follow the same strategy as for its aggregate counterpart  $\Omega$ , except that we use a smaller number of degrees of freedom (there is less need for shrinkage as the number of variables per sector is smaller than the number of aggregate variables).

#### 3.4.4 Drawing $\varepsilon_t$ given all other parameters

As mentioned before, we exploit the Gibbs sampler throughout by imposing independent Normal-inverse Wishart priors.

We assume Gaussian innovations for tractability. If we use a variant of equations (6) and (7), it is straightforward to see that, conditional on  $A_l$ ,  $B_l$ ,  $C_l$ ,  $\Sigma$ , D, and  $D^i$ ,  $\varepsilon_t$  can be drawn via exploiting the Kalman filter (simply put all known quantities on the left-hand-side: all that remains on the right-hand side are the  $\varepsilon$  terms,  $w^i$  and w), based on Carter and Kohn (1994). To make this step more numerically efficient, we follow Durbin and Koopman (2012) and collapse the large vector of observables in a vector with the same dimension as the structural shocks. As discussed by Durbin and Koopman (2012), this can be done without loss of information.

#### 3.4.5 Drawing other parameters given $\varepsilon$

Since we condition on  $\varepsilon$  at this stage, drawing all other parameters amounts to drawing from Gaussian and inverse Wishart posteriors. For the aggregate equations, we use a Minnesotatype prior following Koop and Korobilis (2010). Such a prior is useful because it avoids overfitting. Since there are only two or three variables per sector (depending on whether or not industrial production data is available), overfitting is less of an issue, so we use priors centered at 0 with a standard deviation of .5 there. One helpful insight here is that, conditional on  $\varepsilon$ , all other blocks can be run in parallel. This means that our approach can be scaled up easily. This is especially useful for extensions where the researcher might want to depart from the Normal-inverse Wishart prior used here.

## 4 Estimation Results

We now describe the main results. To obtain those, we used eight aggregate US time series (in year-over-year growth rates where applicable): (i) real GDP growth, (ii) CPI inflation, (iii) the effective Federal Funds rate, (iv) growth rate in real government spending, (v) real PCE consumption growth, (vi) Moody's Seasoned Baa Corporate Bond Yield Relative to Yield on 10-Year Treasury Constant Maturity, (vii) Fernald's utility adjusted TFP (Fernald (2014)), (viii) and energy inflation based on the relevant producer price index. We use data from the first quarter of 1961 to the last quarter of 2017. The data is described in detail in Appendix B.1.

For the sectoral data, we use three variables for each sector, where available: (i) the year on year growth rate of sectoral PCE (ii) the year on year sectoral inflation as measured by the associated price index and (iii) the year on year growth in Industrial Production as made available by the Federal Reserve Board. The latter is not available for all sectors, so we only use it where available. The sectoral data is described in Appendix B.2

In terms of specification, we use six lags throughout, except for the lagged aggregate variables in the sectoral equations, where we only use two lags. We also allow for six aggregate shocks: monetary policy, government spending, financial, energy, technology, and household demand. The identification for the household demand shock is discussed in Section 2. We identify the other shocks analogously, but using different sources of cross-sectional variation to pin down the component  $\alpha_{k,s}^i$  encoding the relative impact of the shock s on variable k for sector i and assigning a positive aggregate impact to a different aggregate variable. We also allow for three unidentified sources of sectoral variation, which we include to allow for the possibility that we missed some relevant aggregate structural shocks.

Table 4: Summary of prior distributions

Parameters	Prior Density	Prior Parameters			
$\mu, A_l$ $\Omega$	Normal Inverse Wishart	Minnesota prior as in Koop & Korobilis  Mean: training sample  Degrees of freedom: sample size			
$D,$ constrained elements $D,$ unconstrained elements $\mu^i, B_l^i, C_h^i$ $\Omega_i$ $D^i$	Normal Normal Normal Inverse Wishart Normal	Mean and standard deviation: system of equations Mean 0, standard deviation 0.25 Mean 0, standard deviation 0.5 (each element)			
0.2	1 0 0	Spread  0.1  0.1  0.2  4 6 8 10	Government Spending  0.8  0.6  0.4  0.2  0  0.2  0.4  2  4  6  8  1		
Nominal Interest Rate	Consumption	TFP 0.6 0.7 0.7 0.7 0.7 0.7 0.7 0.7 0.7 0.7 0.7	Energy Prices  5  4  3  2		

Figure 3: Responses to Household Demand Shock. Dashed lines are 16th and 84th Posterior Percentile Bands, Dots are 5th and 95th Posterior Percentiles. The x-axis Shows Time in Quarters.

# 4.1 Impulse Response Functions

We now show the impulse response functions obtained from the model estimation. Figure 3 shows the median and various percentiles of the impulse responses to a one-standard-deviation shock for the household consumption shock.<sup>28</sup> The results conform to the expected response to a generic aggregate demand shock. There is an increase in inflation, output, and nominal interest rates. Energy costs also increase, which again is consistent with an increase in demand for energy. At the same time, 90 percent posterior bands of the responses of TFP and credit spreads contain 0, implying that the consumption shock is not, first and foremost, a response to technology changes or financing conditions.

We also examine how incorporating the sectoral data helps with identification. Specifi-

<sup>&</sup>lt;sup>28</sup>The impulse responses to other shocks are in Appendix I. These other responses are broadly in line with previous responses obtained for these shocks in the literature.

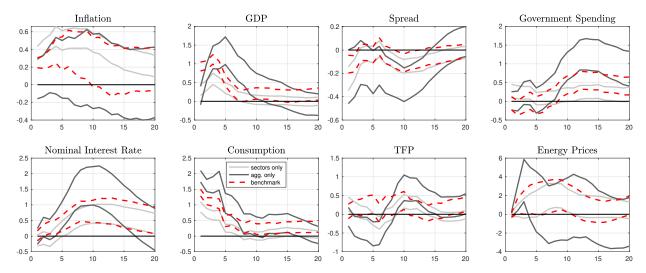


Figure 4: Responses to Household Demand Shocks: Comparison of Identification Schemes. Error Bands are 16th and 84th Percentile Posterior Bands.

cally, figure 4 shows that, relative to a specification where the shock is identified only from its impact on aggregate consumption, the impulse response functions for the household demand shock becomes much more tightly estimated once we incorporate priors on the sectoral responses. It is those tighter posteriors that make clear the impact of those shocks on inflation and interest rates.<sup>29</sup>

# 4.2 The sources of business cycles

In this section, we examine how the different identified structural shocks explain business cycles. We do this in two ways: through a variance decomposition, describing the fraction of business cycle variance explained by the various shocks, and through a historical decomposition, which shows the contribution of each shock to various cyclical downturns.

The results for the variance decomposition are presented in table 5 below. To obtain the numbers in the table, we decompose for each variable the fraction of the overall forecast error variance at business cycle frequencies into different components.<sup>30</sup> The numbers refer to average variances for forecast errors 6 to 32 quarters ahead. The six identified shocks account for about 80% or more of overall variance, with the remaining explained by the three unnamed shocks and the residuals  $w_t$ . The table shows that household consumption shocks play a prominent role not only in explaining nominal interest rates and inflation (as one would expect), but also GDP, consumption, and energy prices. The other shock with a

 $<sup>^{29}</sup>$ To obtain the impulse responses based only on sectoral or aggregate information, we choose very loose priors for D and  $D^i$ , respectively, and re-estimate our model.

 $<sup>^{30}</sup>$ We focus here on the posterior mean. The 5th and 95th percentiles for the household consumption shock can be found in Appendix J.

prominent role is to corporate credit, accounting for a large part of the variance of GDP and consumption. If we count household consumption, government consumption, and monetary policy shocks as "demand" shocks and energy and technology as "supply" shocks, we find that demand shocks account for substantially more of GDP variation at business cycle frequencies than supply shocks.

	tech	credit	household	gov	energy	monetary
$\pi$	4.7	7.6	16.1	37.0	18.7	8.6
$\operatorname{gdp}$	7.5	18.2	35.2	14.3	10.7	5.6
i	5.3	7.7	27.9	35.4	7.9	8.7
$\mathbf{c}$	5.7	11.6	42.8	17.7	10.3	5.2
spread	16.4	38.6	9.1	15.1	7.4	5.1
g	5.0	8.8	28.4	29.0	9.8	9.0
$\operatorname{tfp}$	21.3	5.7	10.3	24.6	8.7	7.0
energy	4.9	5.2	9.3	9.4	61.2	4.9

Table 5: Mean of variance decomposition across business cycle frequencies and posterior draws

The variance decomposition provides a view of the average importance of different shocks in driving different variables. Alternatively, one might ask how relevant the various shocks were in particular recession episodes. This question allows for the possibility that recessions are qualitatively different from expansions, and that they may have been caused by different shocks. To answer this question, we use a historical decomposition.

Table 6 provides the results of such a decomposition for the recession episodes fully included in the sample. The first column shows the peak-to-trough changes in the *level* of (log) real GDP for the various recessions, and the second column shows the expected change in GDP in the absence of any shocks after the recession peak. It is typically positive, reflecting, among other, things, that the estimated growth rate of real GDP is positive. The subsequent columns show the difference between this baseline behavior and the one that would result if the economy was only hit by each inferred sequence of shocks (we provide point estimates based on posterior means). Thus, for example, in the 1980 recession, output dropped by 2.2% when it was expected to grow by 0.7%. Out of that 2.9% short-fall, the shock to household consumption accounted for 0.9%, or about a third, with the credit shock accounting for a slightly smaller part. Both shocks appear to have large impacts in most subsequent recessions, with household consumption having an increasingly large role. By the 2007-09 recession, household consumption accounts for more than two-thirds of the difference between projected and realized output growth and the credit shock for half as much.

One striking result is how unimportant the monetary shock was, even following the

Volcker disinflation. A possible interpretation is that this shock propagated into the economy primarily by depressing household consumption and by changing credit conditions, with nominal frictions leading to infrequent price changes playing a minor role.

	data	no shocks	tech	credit	household	gov	energy	monetary
80	-2.2	0.7	-0.1	-0.7	-0.9	-0.1	-0.1	-0.0
81-82	-2.5	3.5	0.6	-2.3	-3.2	-0.1	0.3	-0.1
90-91	-1.4	1.5	0.3	-0.8	-1.6	-0.1	-0.1	-0.0
2001	0.4	2.4	-0.5	-0.1	-1.3	-0.0	0.2	0.0
2007-2009	-4.1	4.5	-0.2	-3.8	-6.3	-0.2	0.3	-0.1

Table 6: Counterfactual Recessions. Contributions of various shocks to peak to trough change in the level of GDP relative to No Shock Forecast.

# 5 Interpretation: sentiments, news and wealth

How should we interpret the consumption shock? As the derivation in section 2 makes clear, the shock may be a combination of various shocks that affect households first, and sectoral output and prices in response to household spending decisions.

We provide some insight into the interpretation of our estimated shock by examining the behavior of the inferred consumption shock series in comparison to data not used in its estimation. This exercise provides external validation for our findings since those series were not used in the estimation at all.

One potential source of consumption shocks are fluctuations in housing wealth. This was strongly highlighted in empirical, theoretical and quantitative work by Mian et al. (2013), Kaplan et al. (2016) and Berger et al. (2018). Figure 5a compares the time-series for the household consumption shock inferred using our methodology to the growth rate of average wealth of households in the bottom 90% of the wealth distribution, obtained from Saez and Zucman (2016). We aggregate our shock to an annual frequency since the wealth measure is only available at that frequency. The two series correlate well, especially from the late 1990s onward, and very prominently so around the 2007-09 recession.

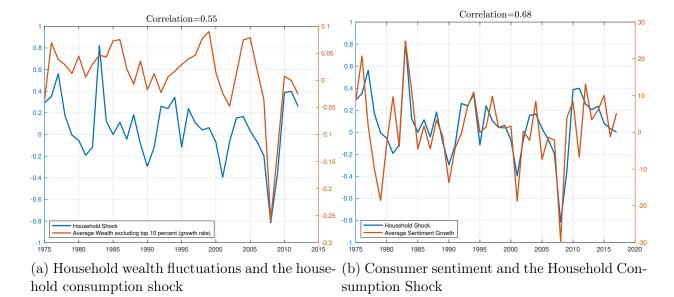


Figure 5: Comparison of Household Consumption shock with Wealth and Sentiment Changes.

At the same time, the correlation is smaller earlier in the sample, indicating that the source of household consumption fluctuations may have been different over that period. Figure 5b compares the shock to a measure of changes in consumer sentiment derived from the Michigan Survey. While the consumer sentiment data exhibits more substantial high-frequency fluctuation, the two series track each other very closely for the entire sample, including the early part. This tracking becomes apparent in the figure, which plots annual averages.<sup>31</sup>

# 6 Further Validation and Analysis

In this section, we conduct some further analysis to validate our approach in various ways. We start with an external validation of our approach, by comparing estimated impulse-response functions for the monetary policy shock, estimated using our method, to IRFs measured with the use of external instruments established in the literature. Next, we evaluate the importance of prior information on the impact of shocks, and the extent to which it is modified by data. Finally, we perform an analysis of the model fit, by assessing the extent to which the structural restrictions in the Hi-VAR constrain the interplay between sectoral and aggregate variables.

<sup>&</sup>lt;sup>31</sup>The correlation for the original quarterly series is not much lower at 0.57.

## 6.1 External Validation: Comparison with IV based identification

Our approach uses sectoral data to provide additional information about the various shocks of interest. Another source of information that has been used repeatedly in empirical macroe-conomics are instruments for aggregate shocks (see, for example, Mertens and Ravn (2013) and Stock and Watson (2018)). We use the Romer & Romer monetary shock (Romer and Romer (2004)) as updated by Wieland and Yang (2019). We drop sectoral information and instead incorporate information coming from the instrument along the lines of Caldara and Herbst (2019). We denote the monetary shock by  $\varepsilon_t^m$ , the observed Romer & Romer shock by  $m_t$ , and add the following equation to our aggregate block (which we do not change otherwise):

$$m_t = \mu^m + \beta^m \varepsilon_t^m + u_t^m \tag{13}$$

where  $u_t^m$  is a mean zero Gaussian shock. We use loose priors on all parameters in this equation. The priors on  $\mu^m$  and  $\beta^m$  are centered on 0 and 1, respectively. In Figure 6, we compare the median estimated response of all aggregate variables obtained from using the instrument to the estimated response using the sector-based identification approach. The impact response of the nominal interest rate is very similar under the two identification approaches. The responses were the approaches differ the most (inflation and GDP) are those were our approach arguably yields more credible responses (a decline in inflation and no significant increase in GDP growth on impact). It is by now well known that analyses based on Romer & Romer-type shocks can lead to such incredible responses (see Bu et al. (2020)). For the other variable, the instrument-based responses are mostly within our 90 percent posterior bands.

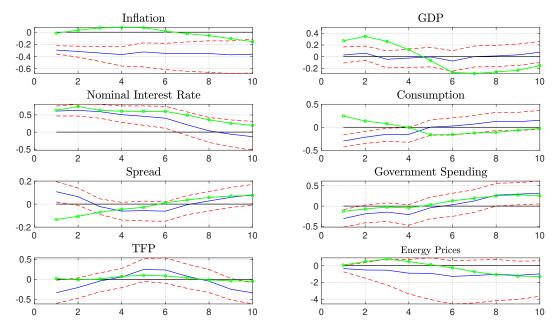


Figure 6: Benchmark Responses (Median, 5th and 95th Percentiles) to a One-Standard Deviation Monetary Shock and Median Response based on Romer & Romer Shock (green).

## 6.2 The importance of prior information

While standard asymptotic results imply that most parameters in our analysis, such as VAR coefficients and the variance of innovations, are well identified by the data, this is not the case for the impact matrix  $D^Z$ . In particular, the posterior distribution of  $D^Z$  is influenced by the priors even asymptotically. This influence confirms that the priors are necessary for the identification of the structural shocks.

There is no amount of data that can be completely informative about the impact of each individual shock,  $D^Z$ . However, standard results from factor analysis imply that one can identify the part of the covariance of innovations that is accounted for by aggregate shocks.<sup>32</sup> That part is equal to  $D^ZD^{Z'}$ , since the covariance of macroeconomic shocks  $\varepsilon_t$  is itself equal to the identity matrix.<sup>33</sup>, and in general converges in large samples to a known matrix,  $\phi$ . In Appendix F we show that, given  $\lim_{T\to\infty} D^ZD^{Z'} = \phi$  the asymptotic posterior distribution of  $D^Z$  satisfies

$$P(D^Z|D^ZD^{Z'} = \phi) \propto \mathbb{1}\left(D^ZD^{Z'} = \phi\right)p(D^Z) \tag{14}$$

where 1 is the indicator function. That is, asymptotically, only the parts of the prior

 $<sup>^{32}</sup>$ We check this result numerically in a Monte Carlo exercise described in Appendix G

<sup>&</sup>lt;sup>33</sup>Specifically, the vector of aggregate shocks at any time t is given by  $\varepsilon_t$  and the part of innovations accounted for those shocks is given by  $D^Z \varepsilon_t$ , so that  $E\left[D^Z \varepsilon_t \varepsilon_t' D^{Z'}\right] = D^Z E\left[\varepsilon_t \varepsilon_t'\right] D^{Z'} = D^Z D^{Z'}$ 

distribution that are consistent with  $\phi$  are retained. Since there are multiple values of  $D^Z$  for which  $D^ZD^{Z'} = \phi$ , the posterior distribution for  $D^Z$  remains non-degenerate in large samples. At the same time, it is constrained by the data. In particular, note that expression 14 describes the joint distribution of  $D^Z$ , which is itself a matrix. The dependence of the distribution on  $D^ZD^{Z'}$  induces dependence between the elements of this matrix: We may take the a priori stance that a certain level of impact for the consumption shock on a certain variable is probable, but it will only remain so if it is compatible with the level of impact for other shocks that are themselves also probable.

To assess the relative role of restrictions imposed by the data on our prior distributions, we plot the prior median of the impact of a given shock on the variables in a sector against the posterior median (i.e., the prior and posterior medians of the relevant entries of  $D^Z$ ). We do this to (i) check that our prior information is not completely overruled by the data (in which case we should go back to the drawing board) and (ii) that our analysis indeed adds information relative to the prior so that the data is indeed helpful to identify the effects of shocks. We focus here on the consumption shock - the figures for the other shocks look similar. Figure 7 shows a scatter plot of the prior vs. the posterior medians across sectors for our three sectoral variables as well as the identity function (all dots would be on this line if the data were not informative at all).<sup>34</sup> The data is informative in that it shifts the median impact of the shock across sectors.

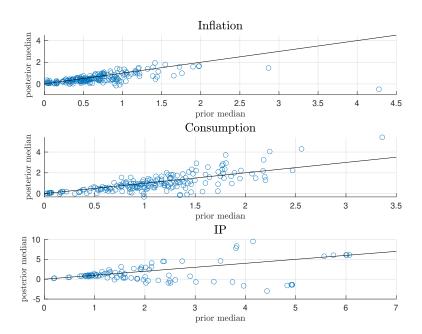


Figure 7: Prior vs Posterior Impact of Household Shock Across Sectors.

<sup>&</sup>lt;sup>34</sup>Note that IP data is not available for all sectors.

Given the uncertainty about the marginal effect of the consumption shock on different prices and quantities, our estimate is more credible if the marginal effect of other shocks does not look too similar to that of the consumption shock. The two prime candidates for shocks that could have similar estimated effects as the household shock are the credit shock and the monetary shock. Therefore we produce a scatter plot of the posterior medians for the (impact) consumption shock response across sectors against the posterior median of the (impact) monetary and credit shock responses across sectors. Figures 8a and 8b shows these scatter plots. As can be seen from those scatter plots, the impacts of shocks across sectors are not strongly correlated, highlighting that we are identifying a shock that is very different from monetary and credit disturbances.

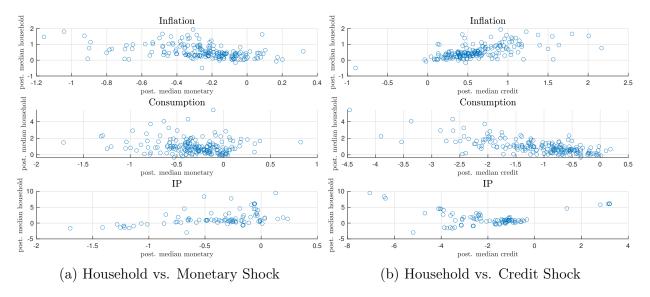


Figure 8: Comparison of Impact Responses Across Sectors.

# 6.3 Model fit and the interplay between sectoral and aggregate data

Our model is restrictive because correlations between sectors or between sectors and aggregate variables have to come through either the structural shocks  $\varepsilon_t$  or lagged aggregate variables. These restrictions could lead to misspecification, casting doubt on our identification strategy. To address this possible concern, we first compute the correlations between aggregate consumption growth and consumption growth at the sectoral level that appear in our dataset as well as the corresponding correlations for aggregate and sectoral inflation. We then draw 1000 parameter values from the posterior, simulate data of the same length as our dataset for each set of parameters (after discarding 1000 burn-in observations), and compute the same correlations for our simulated data. This exercise gives us the posterior distribution of the correlations we are interested in. We are thus carrying out a posterior predictive

check as advocated for by Rubin (1984) and further discussed by Gelman et al. (2013) and Geweke (2005), for example. The top two panels in Figure 9 plot the correlations from the data (black) as well as the median (red), and the 5th and 95th percentiles (blue) of the posterior distribution. We sort the correlations from the actual data by size (starting with the largest correlation) to make the figure easier to interpret. We order the sectors in the same order for the simulated data. As can be seen from figure 9, our model can replicate the correlation patterns between aggregate and sectoral data. An inquisitive reader might ask for a more stringent test, namely a check of the correlation of variables across sectors rather than between any sector and the corresponding aggregate variable. We show the results for this posterior predictive check in the bottom two panels of Figure 9. The figure looks noisier just because there are many more data points (pairwise correlations between the 187 sectors in our sample), but the main pattern remains, our model can replicate the broad correlation patterns. Our model misses at the very tail ends of the spectrum of correlations (more so for inflation than for consumption growth), but given that our model is tightly parametrized and parsimonious, we think of these results as very encouraging.

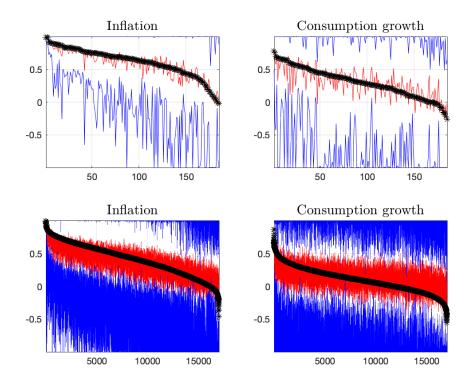


Figure 9: Posterior Predictive Check, Model-Implied Correlations vs Data. Top Two Panels: Correlation with Aggregate Inflation and Consumption Growth, sector on x-axis. Bottom Two Panels: Correlation Across Sectors, sector pairs on x-axis. Red line: Posterior Median, Blue Lines: 5th and 9th Posterior Percentiles. Data in Black.

## 6.4 Other Extended Analysis

In the Appendix, we give further results for our model. In particular, we show analytically in Appendix H why a researcher would generally want to use the most disaggregated data possible (like we do), and we characterize in detail the asymptotic behavior of the impact of economic shocks on aggregate and sectoral variables in Appendix F. We also show a small Monte Carlo exercise in Appendix G. Finally, in Appendix J we show that the role of the household consumption shock is robust to various changes in the specification, from having a larger prior variance on the aggregate impact of this shock to dropping the Great Recession from the sample as well as using fewer lags in our model.

## 7 Conclusion

We propose a novel approach to use cross-sectional data in order to measure business cycle shocks and their aggregate impacts. The approach relies on using a priori information on the differential impact of the shock on different sectors, casting that information as a Bayesian prior to properly account for any uncertainty surrounding it, and relying on a rich set of cross-sectional data to "average out" identification errors at the level of individual sectors.

We use this method to measure shocks to aggregate consumption, defined as shocks that affect sectoral output and prices through their impact on aggregate consumption but not otherwise. We find that such shocks account for approximately 40% of output fluctuations at business cycle frequencies, and a large part of output losses during recessions.

The results highlight the value of detailed work in understanding the sources of aggregate consumption dynamics, and suggests that policies that stabilize consumption can have a significant business cycle stabilization effect.

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# A Proof of Proposition 1

Here we give a proof of Proposition 1. We cast this proof in terms of the time series model we use for our application, but translating it into the nomenclature used in section 2 is straightforward. Consider a version of our model without dynamics (to focus our attention on the identification of shocks)<sup>35</sup>:

$$u_t = D\varepsilon_t + w_t \tag{15}$$

$$\varepsilon_t = \varepsilon_t \tag{16}$$

 $u_t$  are the stacked forecast errors at the aggregate level and sectoral level stacked into one vector. The second equation/identity is added to turn our model into a state space model. Because all shocks are Gaussian, we can apply the Kalman filter to calculate filtered estimates of our structural shocks  $\varepsilon_t$ . Note that because our state  $\varepsilon_t$  does not feature any dynamics, filtered estimates will generally equal smoothed estimates, so there is no need to have a separate treatment for smoothed estimates below. We assume the equations above are the true data-generating process. Without loss of generality, we assume that the shock whose responses are not misspecified is the first element of  $\varepsilon_t$ . The Kalman filter returns a least squares estimate of  $E_t\varepsilon_t = \varepsilon_{t|t}$ :

$$\varepsilon_{t|t} = \beta u_t$$

The matrix of coefficients  $\beta$  is given by the standard formula linking the covariance matrix of the right hand side variable  $u_t$  with the covariance of the right-hand-side variable with the left-hand side variable, the vector of structural shocks  $\varepsilon_t$ :

$$\beta = E(\varepsilon_t u_t') [E(u_t u_t')]^{-1}$$

The second term on the right hand side,  $E(u_t u_t')$ , can be identified from the data as the second moment matrix of the observables. As such, it does not depend on whether or not D is correctly specified as long as our choice of D is consistent with the overall variability of the data. Where identification matter is in the first term on the right-hand side:

$$E(\varepsilon_t u_t') = D'$$

Let's now assume that we have a misspecified version of the model where, instead of using the true impact matrix D, we use a matrix  $\tilde{D}$  such that the first column of D and  $\tilde{D}$  coincide. Therefore, the response to the first element of  $\varepsilon$  is correctly specified, whereas the others are

<sup>35</sup>All VAR-type parameters are identified in our setting, so this is without loss of generality.

not. This means that the first row of D' and  $\tilde{D}'$  coincide. This in turn, means that the first row of  $D'[E(u_tu_t')]^{-1}$  equals the first row of  $\tilde{D}'[E(u_tu_t')]^{-1}$  and thus that the first element of the estimated shock series is independent of whether D or  $\hat{D}$  is used to form the estimate.

### B Data

### B.1 Aggregate Data

See figure 6 for a depiction of the aggregate time-series. The sources and definitions are given below. Growth refers to year on year month changes.

- Real GDP growth: Real Gross Domestic Product, Billions of Chained 2012 Dollars Series (GDPC1) Quarterly, Seasonally Adjusted Annual Rate
- CPI inflation: FRED Series CPIAUCSL, Consumer Price Index for All Urban Consumers: All Items. Quarterly, seasonally adjusted, Index 1982- 1984 = 100 1947Q1-2018Q1.
- The effective Federal Funds rate: FRED Series FEDFUNDS, Quarterly, not seasonally adjusted, Percent, 1954Q3-2018Q1.
- Growth rate in real government spending: FRED Series GCEC1, Quartlery, seasonally adjusted, Billions of chained 2009 Dollars. 1947Q1-2018Q1.
- Real PCE consumption growth:FRED Series PCECC96, Quarterly, sea- sonally adjusted, Billions of chained 2009 Dollars. 1947Q1-2018Q1.
- Moody's Seasoned BAA Corporate Bond Yield Relative to Yield on 10-Year Treasury Constant Maturity: FRED Series BAA10YM, Quarterly, not seasonally adjusted, Percent. 1953Q2-2018Q1.
- Fernald's utility adjusted TFP (Fernald (2014)): Percent Change (natural log difference); All variables are percent change at an annual rate (=400 \* change in natural log).
- Inflation based on the relevant producer price index: Producer Prices Index: Economic Activities: Total Energy for the United States, FRED Series (PIEAEN01USQ661N), Quarterly, not seasonally adjusted, Index 2010=1. 1955Q2-2018Q1.

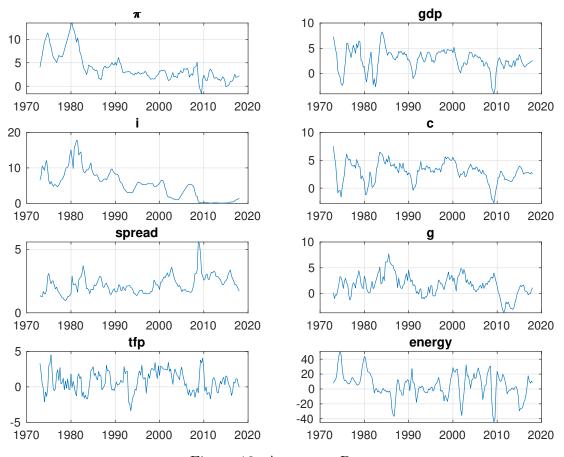


Figure 10: Aggregate Data

#### B.2 Sectoral Level Data

Unless otherwise noted, the data originally was classifed by 4-digit 2007 NAICS and was converted to PCE using the 2007 PCE Bridge Table published by the BEA.

- PCE Price Index (PCEPI): BEA Table 2.4.4U. Price Indexes for Personal Consumption Ex- penditures by Type of Product [Index numbers, 2009=100; quarters and months are seasonally adjusted]. Data is available from 1959Q1-2018Q1. See figure 11 upper panel for a depiction of the data series.
- PCE Quantity Index (PCEQI): BEA Table 2.4.3U. Real Personal Consumption Expenditures by Type of Product, Quantity Indexes [Index numbers, 2009=100; quarters and months are seasonally adjusted]. Data is available from 1959Q1-2018Q1. See figure 11 middle panel for a depiction of the data series.
- Industrial production index: This is the Fed Board of Governor's IP data. One can access the IP data release here: https://www.federalreserve.gov/releases/G17/. See

figure 11 lower panel for a depiction of the data series.

- RD intensity: The ratio of RD expenditure to total revenue (sales). Provided by the NSF. All source data can be found in Data/PCEmeasures/Tech/NSF RD/NSF Tables. The most recent data from the NSF, 2014, is used when available for that industry.
- External financing: Using capital expenditure and cash flow by firm and year from Compustat for 1979 to 2015, we can construct the external financing ratio as in Rajan and Zingales (1998), as one minus the ratio between cash flow to capital expenditure. Then matching each firm to its industry, we take the median capital expenditure value across firms for each industry and year. Then, we take the median again across years to obtain a single value for each industry.
- Household Consumption Share: We calculate the Household share as the proportion of output that goes to Personal Consumption Expenditures from the BEA IO Use Table.
- Government Consumption Share: We calculate the government share as the total output sold to all federal, state, and local government categories listed in the Use Table, divided by total industry output.
- Energy exposure: We take the ratio of intermediate inputs from energy sectors to total intermediate inputs using the BEA Use Table. Energy sectors are defined as electrical power generation, oil and gas extraction, natu- ral gas distribution, and petroleum and coal manufacturing.
- Price stickiness: The median price adjustment duration from Nakumura Steinsson (2008) across PCE categories. To capture the frequency of price changes within in industry, we take the price adjustment durations estimated by Nakamura and Steinsson (2008). The estimates are provided at the Entry Line Item (ELI) level. By using the ELI/PCE crosswalk provided by the BLS, we can transfer these ELI level duration values to the PCE classification. For each PCE category, we assign the average of the duration values for the set of ELIs with which the PCE category is matched.

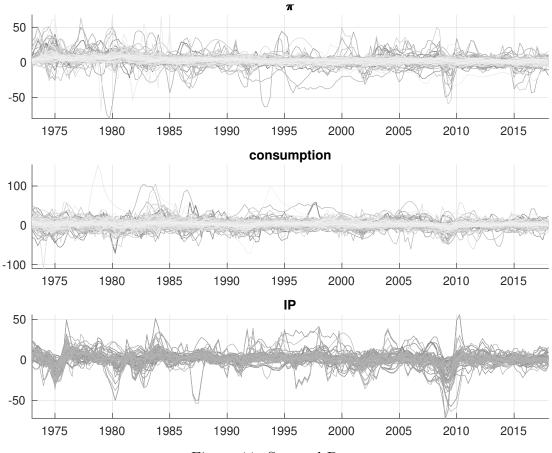


Figure 11: Sectoral Data

# C A Tractable Multi-Sector Model with Nominal Rigidites

We now lay out a tractable, multi-sector model with nominal rigidities to motivate the shock identification scheme. Nominal rigidities allow for a non-trivial "aggregate demand" channel. Since our main focus is in the cross-sectional differences between industries, rather than their individual dynamics, we lay out a static multi-sector economy. This is appropriate for our empirical analysis since we impose identifying restrictions on the impact of shocks rather than on the dynamic responses to those. The model shares many elements with the framework developed in Pasten et al. (2018), while also allowing for nominal wage stickiness and for several aggregate shocks.

#### C.1 Households

There are I sectors, indexed  $i \in \{1, ..., I\}$ . There is a representative household with Cobb-Douglas preferences over the various goods, with share-parameter  $\alpha_i$  for a good of industry i.

$$U = \prod_{i} C_i^{\alpha_i},$$

where  $\sum_{i} \alpha_{i} = 1$ . The household chooses its the amount it consumes of good i,  $C_{i}$ , to maximize its utility subject to the budget constraint

$$\sum_{i} P_i C_i + T = WL + \Pi + \sum_{i} r_i \bar{K}_i,$$

where T is a lump-sum tax levied by the government to finance its consumption, W is the wage rate,  $\Pi$  are profits rebated from firms,  $\bar{K}_i$  is the stock of capital specific to sector i owned by the household, with  $r_i$  the corresponding rental rate, and L < 1 is employment to be determined in equilibrium.

Finally, households supply one unit of labor inelastically, but nominal wages are rigid so that labor is rationed.

Given those constraints, optimal household consumption choice satisfies:

$$P_iC_i = \alpha_i^C PC$$

for 
$$P^C \equiv \prod_i \left(\frac{P_i}{\alpha_i}\right)^{\alpha_i}$$
 and  $C \equiv \prod_i (C_i)^{\alpha_i}$ .

## C.2 Fiscal Authority

The fiscal authority minimizes the cost of consuming an exogenously given aggregate government consumption G,

$$\min \sum_{i} P_{i}G_{i}$$

$$s.t. : \prod_{i} (G_{i})^{\alpha_{i}^{G}} = G,$$

where G is exogenously determined and  $\alpha_i^G$  are expenditure shares. The optimality condition for the government is:

$$G_i = \alpha_i^G \frac{P_G}{P_i} G$$

where

$$P_G = \prod_i \left(\frac{G_i}{\alpha_i^G}\right)^{\alpha_i^G}.$$

#### C.3 Firms

Within each sector there is a continuum of varieties of intermediate products indexed  $v \in [0, 1]$ . Those varieties are purchased by final goods producers that bundle them into the I goods according to a CES aggregator:

$$Y_{i} = \left[ \int_{0}^{1} Y_{i}(v)^{\frac{\theta-1}{\theta}} dv \right]^{\frac{\theta}{\theta-1}}$$

The demand for final good producer in sector i for intermediate input of variety v is

$$Y_i(v) = \left(\frac{P_i(v)}{P_i}\right)^{-\theta} Y_i$$

where

$$P_i = \left[ \int P_i(v)^{1-\theta} dv \right]^{\frac{1}{1-\theta}}$$

For each variety, production takes place with a Cobb-Douglas production function:

$$Y_i(v) = e^{\epsilon_i} \prod_j (X_{ji}(v))^{\gamma_{ji}} \times (L_i(v))^{\lambda_i} (K_i(v))^{\chi},$$

where  $X_{ji}(v)$  is the quantity of final goods materials produced in sector j used as materials in sector i for variety v,  $L_i(v)$  is labor,  $K_i(v)$  is sector-specific capital, and  $\epsilon_i$  is a sector-specific exogenous productivity shock. The share parameter for good j used in sector i is  $\gamma_{ji}$ . We assume that  $\sum_{j} \gamma_{ji} + \lambda_i + \chi = 1$ , so that firms in the industry face constant returns to scale.

Producers of varieties are monopolists. Firms differ on the information set available to them regarding prices and the demand for their intermediate input. Letting **s** denote the state of the economy, they take the wage rate, final goods prices, and household demand as

given and choose their inputs to maximize expected profits.

$$\max_{M_{ji}} E\left[P_{i}(v)Y_{i}(v,\mathbf{s}) - \sum_{j} P_{j}(\mathbf{s})X_{ji}(v,\mathbf{s}) - w(\mathbf{s})L_{i}(v,\mathbf{s}) - r_{i}(\mathbf{s})K_{i}(v,\mathbf{s})|\mathcal{I}_{i}(v)\right]$$

$$s.t. : Y_{i}(v,\mathbf{s}) = \left(\frac{P_{i}(v)}{P_{i}(\mathbf{s})}\right)^{-\theta} Y_{i}(\mathbf{s})$$

$$Y_{i}(v,\mathbf{s}) = e^{\epsilon_{i}} \prod_{j} \left(X_{ji}(v,\mathbf{s})\right)^{\gamma_{ji}} \left(L_{i}(v,\mathbf{s})\right)^{\lambda_{i}} \left(K_{i}(v,\mathbf{s})\right)^{\chi}$$

where  $\mathcal{I}_i(v)$  is the information set for variety v in sector i. For a fraction  $\phi_i$  of variety producers in sector i ( $v \in [0, \phi_i]$ ) the information set does not includes the realized vector of shocks  $\mathbf{s}$ . For the remainder, the information set does includes it. Yet, firms commit to producing as much as necessary to satisfy demand at the prices that they choose.

Given cost-minimization, marginal cost is

$$\operatorname{mc}_{i}(\mathbf{s}) = e^{-\epsilon_{i}} \prod_{j} \left( \frac{P_{j}(\mathbf{s})}{\gamma_{ji}} \right)^{\gamma_{ji}} \left( \frac{w(\mathbf{s})}{\lambda_{i}} \right)^{\lambda_{i}} \left( \frac{\mathbf{r}(\mathbf{s})}{\chi} \right)^{\chi}$$

Firms with full information set prices to

$$P_i(v, \mathbf{s}) = \frac{\theta}{\theta - 1} \mathrm{mc}_i(s)$$

Firms without full information set prices to

$$P_i(v) = \frac{\theta}{\theta - 1} E\left[ \frac{P_i(\mathbf{s})^{\theta} Y_i(\mathbf{s})}{E\left[P_i(\mathbf{s})^{\theta} Y_i(\mathbf{s})\right]} mc_i(\mathbf{s}) \right]$$

We thus have that the price index for sector i is

$$P_i(\mathbf{s}) = \left[ \phi_i \left( \frac{\theta}{\theta - 1} E \left[ \frac{P_i(\mathbf{s})^{\theta} Y_i(\mathbf{s})}{E \left[ P_i(\mathbf{s})^{\theta} Y_i(\mathbf{s}) \right]} m c_i(\mathbf{s}) \right] \right)^{1 - \theta} + (1 - \phi_i) \left( \frac{\theta}{\theta - 1} m c_i(\mathbf{s}) \right)^{1 - \theta} \right]^{\frac{1}{1 - \theta}}$$

Given that all firms in a sector have the same marginal cost, we can write the average markup as

$$\mu_i = \frac{P_i(\mathbf{s})}{mc_i(\mathbf{s})} = \left[\phi_i \frac{\theta}{\theta - 1} E\left[\frac{P_i(\mathbf{s})^{\theta} Y_i(\mathbf{s})}{E\left[P_i(\mathbf{s})^{\theta} Y_i(\mathbf{s})\right]} mc_i(\mathbf{s})\right]^{1 - \theta} \left(\frac{1}{mc_i(\mathbf{s})}\right)^{1 - \theta} + (1 - \phi_i) \left(\frac{\theta}{\theta - 1}\right)^{1 - \theta}\right]^{\frac{1}{1 - \theta}}$$

### C.4 Market Clearing

Market clearing for each sector i, requires that all output is used either as materials, for household consumption or for government consumption:

$$Y_i = \sum_{j} X_{ij} + C_i + G_i$$

Also, there is a fixed stock of capital  $\bar{K}_i$  for each sector. Market clearing in capital markets thus requires that the demand for capital in sector i equals supply:

$$K_i = \bar{K}_i$$

The resource constraint in the labor market is

$$\sum_{i} L_i \le 1$$

With sticky wages the inequality need not hold. We assume that wages are stuck at a level high enough that it doesn't bind. Labor rationing thus implies that

$$L = \sum_{i} L_{i}$$

#### C.5 Shocks

As in Woodford (2003), we assume exogenous processes for nominal aggregates. In particular, we assume that nominal private consumption and nominal government consumption are set exogenously. Specifically, we assume that

$$P^{C}C = M^{C}M^{Y}$$
$$P^{G}G = M^{G}M^{Y}$$

so that nominal private and government consumptions can be affected either by an exogenous component which is specific to each type of final expenditure  $M^C$  or  $M^G$ , or by a common

component  $M^Y$ .

Finally, we also allow for industry level productivity shocks  $\epsilon_i$ . We assume that  $\epsilon_i = \sum_{r=1}^{R} \lambda_{ir} \epsilon_r + \hat{\epsilon}_i$ , where  $\epsilon_r$  are aggregate shocks,  $F_i$  captures the sensitivity of various sectors to that shock, and  $\hat{\epsilon}_i$  is a sector-specific shock. In our application, we will allow  $\epsilon_r$  to incorporate shocks to technology and financial shocks.

### C.6 Reduced log-linearized system

# D Log-linearized system

Up to a first-order approximation the economy is described by the following system of equations (small letters indicate log deviations from steady-state):

$$p^{C} + c = m^{C} + m^{Y}$$

$$p^{G} + g = m^{G} + m^{Y}$$
(17)

$$w = 0 (18)$$

$$g_i - g = p^G - p_i \ \forall i \tag{19}$$

$$c_i - c = p^C - p_i \ \forall i \tag{20}$$

$$y_i = \epsilon_i + \sum_j \gamma_{ji} x_{ji} + \lambda_i l_i + \chi k_i \ \forall i$$
 (21)

$$w + l_i = p_i + y_i - \mu_i \ \forall i \tag{22}$$

$$p_j + x_{ji} = p_i + y_i - \mu_i \ \forall i, j$$
 (23)

$$r_i + k_i = p_i + y_i - \mu_i \ \forall i \tag{24}$$

$$k_i = \bar{k}_i \tag{25}$$

$$\mu_i = -\phi_i \left( \sum_j \gamma_{ji} p_j + \lambda_i w + \chi r_i - \epsilon_i \right) \tag{26}$$

$$y_{i} = \sum_{j} \frac{X_{ij}}{Y_{i}} x_{ij} + \frac{C_{j}}{Y_{i}} c_{j} + \frac{G_{j}}{Y_{i}} g_{j}$$
(27)

The system can be reduced to:

$$p_{i} - (1 - \chi)\mu_{i} = -\epsilon_{i} + \sum_{j} \gamma_{ji}p_{j} + \chi \left(p_{i} + y_{i} - \bar{k}_{i}\right)$$

$$p_{i} + y_{i} = \sum_{j} \gamma_{ij} \frac{Y_{j}}{Y_{i}} (y_{j} + p_{j} - \mu_{j}) + \frac{C_{i}}{Y_{i}} (m^{C} + m^{Y}) + \frac{G_{i}}{Y_{i}} (m^{G} + m^{Y})$$

$$\mu_{i} = -\frac{\phi_{i}}{1 - \phi_{i}\chi} \left(-\epsilon_{i} + \sum_{j} \gamma_{ji}p_{j} + \chi \left(p_{i} + y_{i} - \bar{k}_{i}\right)\right)$$

Or, eliminating  $\mu_i$ ,

$$p_{i} = \frac{1 - \phi_{i}}{1 - \chi} \left( -\epsilon_{i} + \sum_{j} \gamma_{ji} p_{j} + \chi \left( y_{i} - \bar{k}_{i} \right) \right)$$

$$p_{i} + y_{i} = \sum_{j} \gamma_{ij} \frac{Y_{j}}{Y_{i}} (y_{j} + \frac{1}{1 - \phi_{j}} p_{j}) + \frac{C_{i}}{Y_{i}} (m^{C} + m^{Y}) + \frac{G_{i}}{Y_{i}} (m^{G} + m^{Y})$$

The system can be rewritten as

$$p_{i} = \frac{1 - \phi_{i}}{1 - \chi} \chi \left[ (1 - \chi \Phi_{i}) \left[ \sum_{j} f_{ij} (y_{j} + \frac{1}{1 - \phi_{j}} p_{j}) + \frac{C_{i}}{Y_{i}} (m^{C} + m^{Y}) + \frac{G_{i}}{Y_{i}} (m^{G} + m^{Y}) \right] + \Phi_{i} \left( \epsilon_{i} + \chi \bar{k}_{i} \right) \right] - \Phi_{i} \left( \epsilon_{i} + \chi \bar{k}_{i} \right) + \Phi_{i} \sum_{j} b_{ji} p_{j}$$

$$y_{i} = (1 - \chi \Phi_{i}) \left[ \sum_{j} f_{ij} (y_{j} + \frac{1}{1 - \phi_{j}} p_{j}) + \frac{C_{i}}{Y_{i}} (m^{C} + m^{Y}) + \frac{G_{i}}{Y_{i}} (m^{G} + m^{Y}) \right] + \Phi_{i} \left( \epsilon_{i} + \chi \bar{k}_{i} \right) - \Phi_{i} \sum_{j} b_{ji} p_{j}$$

with  $f_{ij} = \gamma_{ij} \frac{Y_j}{Y_i}$  capturing forward links and  $b_{ji} = \gamma_{ji}$  capturing backward links

After log-linearizing and rearranging, the model can be reduced to:

$$p_{i} = \frac{1 - \phi_{i}}{1 - \chi} \left( -\epsilon_{i} + \sum_{j} \gamma_{ji} p_{j} + \chi \left( y_{i} - \bar{k}_{i} \right) \right)$$

$$p_{i} + y_{i} = \sum_{j} \gamma_{ij} \frac{Y_{j}}{Y_{i}} \left( y_{j} + \frac{1}{1 - \phi_{j}} p_{j} \right) + \frac{C_{i}}{Y_{i}} (m^{C} + m^{Y}) + \frac{G_{i}}{Y_{i}} (m^{G} + m^{Y})$$

where small caps letters denote log deviations from a reference level. The first set of equations are "sectoral supply" equations, relating marginal production cost to prices. The second set of equations are "sectoral demand" equations, relating nominal expenditures to sectoral prices. The last set of equations link nominal consumption expenditures and exogenous demand shocks.

The system has the form

$$Z = AZ + b = A^{N}Z + \sum_{n=0}^{N-1} A^{n}b$$

with Z including prices and quantities in all sectors, b including the direct impact of all exogenous shocks, and A including the indirect impact of shocks through linkages.

Lemma 1 characterizes the direct and indirect impacts of the shocks on prices, output and consumption:

**Lemma 1** The direct impact of shocks is given by  $b = [\mathbf{p}^{Direct}, \mathbf{y}^{Direct}, \mathbf{c}^{Direct}]^T$ , where

$$p_i^{Direct} = \Phi_i \chi \left[ \frac{C_i}{Y_i} m^C + \frac{G_i}{Y_i} m^G + m^Y \right] - \Phi_i \left( \epsilon_i + \chi \bar{k}_i \right)$$
 (28)

$$y_i^{Direct} = (1 - \Phi_i \chi) \left[ \frac{C_i}{Y_i} m^C + \frac{G_i}{Y_i} m^G + m^Y \right] + \Phi_i \left( \epsilon_i + \chi \bar{k}_i \right)$$
 (29)

$$c_i^{Direct} = \left(1 - \Phi_i \chi \frac{C_i}{Y_i}\right) m^C + (1 - \Phi_i \chi) m^Y - \Phi_i \chi \frac{G_i}{Y_i} m^G + \Phi_i \left(\epsilon_i + \chi \bar{k}_i\right)$$
(30)

and

$$\Phi_i \equiv \frac{1 - \phi_i}{\chi (1 - \phi_i) + 1 - \chi}$$

is inversely related to  $\phi_i$ . Indirect effects are  $AZ = \left[\mathbf{p}^{Inirect}, \mathbf{y}^{Inirect}, \mathbf{c}^{Inirect}\right]^T$ , where

$$p_i^{Indirect} = \Phi_i \sum_j \left( \chi \frac{f_{ij}}{1 - \phi_j} + b_{ji} \right) p_j + \chi \Phi_i \sum_j f_{ij} y_j \tag{31}$$

$$y_i^{Indirect} = (1 - \chi \Phi_i) \sum_j f_{ij} y_j + \sum_j \left[ \frac{1 - \chi \Phi_i}{1 - \phi_j} f_{ij} - \Phi_i b_{ji} \right] p_j$$
 (32)

$$c_i^{Indirect} = -p_i^{Indirect} \tag{33}$$

where  $f_{ij} = \gamma_{ij} \frac{Y_j}{Y_i}$  capture forward linkages and  $b_{ji} = \gamma_{ji}$  captures backward linkages.

Lemma 1 implies that the direct impact of a consumption shock  $m^C$  on prices increases in  $\Phi_i \chi_{i}^{C_i}$ 

# E Dynamic Model

In what follows we present a dynamic model with multiple sectors, sticky nominal prices and sticky nominal wages. The exposition largely follows Justiniano et al. (2010), with some simplifications (we omit markup shocks) and extensions where needed.

### E.1 Final good producers

There are J sectors (indexed  $j \in [1, ..., J]$ ). In each of these sectors there are perfectly competitive firms producing final goods  $Y_t^j$  combining a continuum of intermediate goods  $\{Y_t(i)\}_r$ ,  $i \in [0, 1]$ , according to the technology

$$Y_t^j = \left[ \int_0^1 Y_t^j(i)^{\frac{\epsilon_p - 1}{\epsilon_p}} di \right]^{\frac{\epsilon_p}{\epsilon_p - 1}}$$

From profit maximization and zero profit conditions we have that

$$Y_t(i) = \left(\frac{P_t(i)}{P_t}\right)^{-\epsilon_p} Y_t^j$$

where  $P_t$  is the price of final good j and satisfies

$$P_t = \left[ \int_0^1 P_t(i)^{\frac{1}{1 - \epsilon_p}} di \right]^{1 - \epsilon_p}$$

### E.2 Intermediate good producers

A monopolist produces the intermediate good i in sector j according to the production function

$$Y_t^j(i) = \max \left\{ \left( \frac{K_t^j(i)}{(1-\gamma^j)\alpha^j} \right)^{(1-\gamma^j)\alpha^j} \left( \frac{A_t^j L_t^j(i)}{(1-\gamma^j)\left(1-\alpha^j\right)} \right)^{(1-\gamma^j)\left(1-\alpha^j\right)} \prod_{j'} \left( \frac{M_t^{j'j}(i)}{\gamma^{j'j}} \right)^{\gamma^{j'j}} - A_t F^j, 0 \right\}$$

where  $K_t^j(i)$ ,  $L_t^j(i)$  denote the amounts of capital and labor employed by firm i in sector j,  $M_t^{j'j}(i)$  is the amount of materials produced in sector j' used by firm i in sector j and  $F^j$  is a fixed cost of production, chosen so that profits are zero in stead state.  $A_t^j$  respresents exogenous technological progress in sector j. We assume that it consists of a combination of aggregate and sector specific components:

$$A_t^j = A_t U_t B_t^j$$

where

$$A_t = A_{t-1}Z_t$$

with

$$\ln Z_t = (1 - \rho^Z)\gamma + \rho^Z \ln Z_{t-1} + \epsilon_t^Z + \epsilon_{t-4} \hat{n}ews$$

where  $\epsilon_{t-4}$  news captures news received in t-4 about productivity in t. Furthermore,

$$\ln U_t = \rho^U \ln U_{t-1} + \epsilon_t^U$$

and

$$\ln B_t^j = (1 - \rho^B) \ln B^j + \rho^B \ln B_{t-1}^j + \epsilon_t^j$$

Every period in each sector j, a fraction  $\xi_p^j$  of intermediate firms cannot choose its price optimally, and as in Smets and Wouters (2003), they reset it according to the indexation rule

$$P_t(i) = P_{t-1}(i) \left( \prod_{t=1}^j \right)^{\iota_p} \prod^{1-\iota_p},$$

where  $\pi_t^j = \frac{P_t^j}{P_{t-1}^j}$  is gross sector j inflation and  $\pi$  is its steady state. The remaining fraction of

firms chooses its price  $P_t(i)$  optimally, by maximizing the present discounted value of future profits

$$E_{t} \left\{ \sum_{s=0}^{\infty} \left( \xi_{p}^{j} \right)^{s} \frac{\beta^{s} \Lambda_{t+s}}{\Lambda_{t}} \left[ P_{t}(i) \left( \Pi_{t,t+s}^{j} \right) Y_{t+s}(i) - W_{t+s}^{j} L_{t+s}(i) - R_{t+s}^{k,j} K_{t+s}(i) - \sum_{j'} P_{t+s}^{j'}(i) M_{t+s}^{j'}(i) \right] \right\}$$

where

$$\Pi_{t,s}^{j} \equiv \prod_{k=1}^{s} \left( \Pi_{t+k-1}^{j} \right)^{\iota_p} \Pi^{(1-\iota_p)k} \text{ for } s \ge 1$$

$$\Pi_{t,t}^{j} = 1$$

and

$$Y_{t+s}(i) = \left(\frac{P_{t+s}(i)}{P_{t+s}}\right)^{-\epsilon_p} Y_{t+s}^j$$

subject to the demand function and to cost minimization. In this objective,  $\Lambda_t$  is the marginal utility of nominal income for the representative household that owns the firm, while  $W_t$  and  $r_t^{k,j}$  are the nominal wage and the rental rate of capital specific to sector j.

Cost minimization by firms implies that

$$\frac{K_t^j(i)}{L_t^j(i)} = \frac{W_t^j}{R_t^{k,j}} \frac{\alpha^j}{1 - \alpha^j}$$

and

$$\frac{M_t^{j'j}(i)}{L_t^j(i)} = \frac{W_t^j}{P_t^{j'}} \frac{\gamma^{j'j}}{(1 - \gamma^j)(1 - \alpha^j)},$$

so that nominal marginal cost in sector j is common to all firms and given by

$$MC_t^j = \left(R_t^{k,j}\right)^{(1-\gamma^j)\alpha^j} \left(\frac{W_t^j}{A_t^j}\right)^{(1-\gamma^j)\left(1-\alpha^j\right)} \prod_{j'} \left(P_t^{j'}\right)^{\gamma^{j'j}}.$$

Substituting back input choices, and ignoring the fixed costs, yields employment in each variety as a function of sectoral output and the price of the variety,

$$L_t^j(i) = (1 - \gamma^j)(1 - \alpha^j) \frac{MC_t^j}{W_t^j} \left(\frac{P_t(i)}{P_t}\right)^{-\epsilon_p} Y_t^j.$$

Integrating both sides yields sectoral employment:

$$L_{t}^{j} = (1 - \gamma^{j})(1 - \alpha^{j}) \frac{MC_{t}^{j}}{W_{t}^{j}} P_{t}^{\epsilon_{p}} Y_{t}^{j} \int P_{t}(i)^{-\epsilon_{p}} di.$$

From the intermediate input demand function,

$$Y_t(i) = \left(\frac{P_t(i)}{P_t}\right)^{-\epsilon_p} Y_t^j.$$

Given that, with our production function, average variable costs and marginal costs coincide, the objective function for firms setting prices optimally can be rewritten as

$$\max_{P_t(i)} E_t \left[ \sum_{s=0}^{\infty} \left( \xi_p^j \right)^s \frac{\beta^s \Lambda_{t+s}}{\Lambda_t} \left[ \left( P_t^j(i) \Pi_{t,t+s}^j - M C_t \right) Y_{t+s}(i) \right] \right]$$

$$s.t. : Y_{t+s}^j(i) = \left( \frac{P_t(i) \Pi_{t,t+s}^j}{P_{t+s}} \right)^{-\epsilon_p} Y_{t+s}^j$$

The first order condition can then be written as

$$\tilde{P}_{t}^{j} = \frac{\epsilon_{p}}{\epsilon_{p} - 1} \sum_{s=0}^{\infty} \frac{E_{t} \left\{ \left( \beta \xi_{p}^{j} \right)^{s} \Lambda_{t+s} \tilde{Y}_{t+s}^{j} M C_{t+s}^{j} \right\}}{\sum_{s=0}^{\infty} E_{t} \left\{ \left( \beta \xi_{p}^{j} \right)^{s} \Lambda_{t+s} \tilde{Y}_{t+s}^{j} \Pi_{t,t+s}^{j} \right\}}$$

where  $\tilde{P}_t^j$  is the optimally chosen price for all firms i choosing their prices in period t (so that  $P_t^j(i) = \tilde{P}_t^j$ ), and  $\tilde{Y}_{t+s}$  is the demand they face in t+s.

Alternatively,

$$\frac{\tilde{P}_{t}^{j}}{P_{t}} = \frac{\epsilon_{p}}{\epsilon_{p} - 1} \sum_{s=0}^{\infty} \frac{E_{t} \left\{ \left( \beta \xi_{p}^{j} \right)^{s} \Lambda_{t+s} A_{t+s} P_{t+s} \left( \tilde{Y}_{t+s}^{j} / A_{t+s} \right) \frac{M C_{t+s}^{j}}{P_{t}^{j}} \right\}}{\sum_{s=0}^{\infty} E_{t} \left\{ \left( \beta \xi_{p}^{j} \right)^{s} \Lambda_{t+s} A_{t+s} P_{t+s} \left( \tilde{Y}_{t+s}^{j} / A_{t+s} \right) \left( \Pi_{t,t+s}^{j} / \Pi_{t,t+s} \right) \right\}}$$

where

$$\Pi_{t,s} \equiv \prod_{k=1}^{s} \Pi_{t+k} \text{ for } s \ge 1$$

$$\Pi_{t,t} = 1$$

### E.3 Employment Agencies

Workers have monopoly power over their labor supply. There is a competitive employment agency which combines specialized household labor into a homogeneous labor input sold to firms in sector j according to

$$L_t^j = \left[ \int L_t^j(h)^{\frac{\epsilon^w - 1}{\epsilon^w}} dh \right]^{\frac{\epsilon^w}{\epsilon^w - 1}}.$$

Profit maximization implies that

$$L_t^j(h) = \left(\frac{W_t^j(h)}{W_t^j}\right)^{-\epsilon^w} L_t^j,$$

and the wage paid by firms for homogeneous labor input is

$$W_t^j = \left[ \int_0^1 W_t^j(h)^{1-\epsilon^w} dh \right]^{\frac{1}{1-\epsilon^w}}$$

#### E.4 Households

Each household (h) has labor which is specific to some sector j and utility function given by

$$U_{t} = \sum_{s} E_{t} \beta^{s} b_{t+s} \left[ \ln \left[ X_{t+s}(h) \right] - \varphi^{j} \sum_{j} \frac{1}{1+\nu} L_{t}^{j}(h)^{1+\nu} \right],$$

where

$$X_{t+s}(h) = \prod_{j} \left( \frac{1}{\alpha^{j}} \left( C_{t+s}^{j}(h) - \eta C_{t+s-1}^{j} \right) \right)^{\alpha^{j}},$$

and where  $C_{t+s}^j(i)$ ,  $L_t(i)$  and  $X_{t+s}(i)$  are household choices and  $X_{t+s}$  and  $C_{t+s}^j$  are equilibrium objects that the household takes as given. The formulation corresponds to allowing for two types of "external" habits: habits to aggregate consumption, and habits to consumption of particular goods. The relative relevance of the two types of habits are given by  $\eta$  and  $\mu$ . We will either adopt  $\eta = 0$  and  $\mu > 0$  (only aggregate habits) or  $\eta > 0$  and  $\mu = 0$  (only industry specific habits).

The time-varying parameter  $b_t$  is a shock to the discount factor, affecting both the marginal utility of consumption and the marginal disutility of labor. This intertemporal preference shock follows the stochastic process

$$\log b_t = \rho_b \log b_{t-1} + \varepsilon_{b,t}$$

There are state contingent securities ensuring that in equilibrium consumption and asset holdings are the same for all households. As a result, the household's flow budget constraint is

$$\sum_{j} P_{t}^{j} C_{t}^{j} + \sum_{j,j'} P_{t}^{j'} I_{t}^{j'j} + T_{t} + B_{t} \leq R_{t-1} B_{t-1} + Q_{t}(j) + \Pi_{t} + W_{t}^{j}(j) L_{t}(j) + \sum_{j} R_{t}^{k,j} K_{t-1}^{j},$$

where  $I_t^{j'j}$  is investment in good j' to form capital in sector j,  $T_t$  is lump-sum taxes,  $B_t$  is holdings of government bonds,  $R_t$  is the gross nominal interest rate,  $Q_t(j)$  is the net cas flow from household's j portfolio of state contingent securities, and  $\Pi_t$  is the per-capital profit accruing to households from ownership of the firms.

Households own capital specific to each sector j and rent them to firms at the rate  $R_t^{k,j}$ . The physical capital accumulation equation is

$$K_t^j = (1 - \delta)K_{t-1}^j + \left(1 - S\left(\frac{I_t^j}{I_{t-1}^j}\right)\right)I_t^j,$$

where  $\delta$  is the depreciation rate and  $I_t^j = \prod_{j'} \left(\frac{I_t^{j'j}}{\gamma_I^{j'j}}\right)^{\gamma_I^{j'j}}$  is the investment in sector j. The function S captures the presence of adjustment costs in investment, as in Christiano, Eichenbaum, and Evans (2005). In steady state, S = S' = 0 and S'' > 0.

Every period a fraction  $\xi_w$  of households cannot freely set its wage, but follows the indexation rule

$$W_t^j(j) = W_{t-1}^j(j) (\pi_{t-1}e^{z_{t-1}})^{\iota_w} (\pi e^{\gamma})^{1-\iota_w}.$$

The remaining fraction of households chooses instead an optimal wage  $W_t(j)$  by maximizing

$$E_{t} \left\{ \sum_{s=0}^{\infty} \xi_{w}^{s} \beta^{s} \left[ -b_{t+s} \varphi^{j} \frac{L_{t+s}^{j}(h)^{1+\nu}}{1+\nu} + \Lambda_{t+s} \Pi_{t,t+s}^{w} W_{t}^{j}(h) L_{t+s}^{j}(h) \right] \right\},$$

where

$$\Pi_{t,t+s}^{w} = \prod_{v=1}^{s} (\Pi_{t+v-1} e^{z_{t+v-1}})^{\iota_{w}} (\Pi e^{\gamma})^{v(1-\iota_{w})} \text{ if } s \ge 1$$

$$\Pi_{t,t}^{w} = 1$$

subject to the labor demand function of the employment agencies.

#### E.4.1 Consumption

Given interest rates on riskless debt  $R_t$ , the problem induces the Euler equation:

$$\Lambda_t = \beta R_t E_t \Lambda_{t+1},$$

where  $P_t = \prod_j \left(P_t^j\right)^{\alpha^j}$  is the consumption price index and  $\Lambda_t \equiv \frac{b_t}{P_t X_t}$  is the "nominal" marginal utility of consumption. Given that we get the intra-temporal allocation across industries:

$$C_t^j(h) = \alpha^j \frac{P_t}{P_t^j} X_t(h) + \eta C_{t-1}^j.$$

The model features a representative household, so that in equilibrium,  $X_t = X_t(h)$  and  $C_t^j = C_t(h)$ .

#### E.4.2 Physical Capital

The optimal choice of physical capital stock for sector j satisfies the optimality conditions:

$$\chi_{t}^{j} = \beta E_{t} \left[ R_{t+1}^{k,j} \Lambda_{t+1} + (1 - \delta) \chi_{t+1}^{j} \right],$$

$$P_{t}^{j'} \Lambda_{t} = \gamma_{I}^{j'j} \frac{I_{t}^{j}}{I_{t}^{j'j}} \left[ \chi_{t}^{j} \left[ 1 - S \left( \frac{I_{t}^{j}}{I_{t-1}^{j}} \right) - S' \left( \frac{I_{t}^{j}}{I_{t-1}^{j}} \right) \frac{I_{t}^{j}}{I_{t-1}^{j}} \right] + \beta S' \left( \frac{I_{t+1}^{j}}{I_{t}^{j}} \right) \left( \frac{I_{t+1}^{j}}{I_{t}^{j}} \right)^{2} \chi_{t+1} \right],$$

where  $\chi_t$  is the multiplier on the capital accumulation equation. Defining Tobin's q for sector j as  $Q_t^j = \frac{\chi_t^j}{P_t^{I,j}\Lambda_t} = \frac{P_t\chi_t^j}{P_t^{I,j}b_t[X_t(h)-\mu X_{t-1}]^{-\sigma}}$ , where  $P_t^{I,j} = \prod \left(P_t^{j'}\right)^{\gamma^{j'j}}$ , the relative marginal value of installed capital with respect to consumption, we can also write

$$\begin{split} Q_t^j &= \beta E_t \left[ \frac{R_{t+1}^{k,j} \Lambda_{t+1}}{P_t^{I,j} \Lambda_t} + \frac{P_{t+1}^{I,j} \Lambda_{t+1}}{P_t^{I,j} \Lambda_t} (1 - \delta) Q_{t+1}^j \right], \\ 1 &= \left[ Q_t^j \left[ 1 - S \left( \frac{I_t^j}{I_{t-1}^j} \right) - S' \left( \frac{I_t^j}{I_{t-1}^j} \right) \frac{I_t^j}{I_{t-1}^j} \right] + \beta \frac{\Lambda_{t+1} P_{t+1}^{I,j}}{\Lambda_t P_t^{I,j}} S' \left( \frac{I_{t+1}^j}{I_t^j} \right) \left( \frac{I_{t+1}^j}{I_t^j} \right)^2 Q_{t+1}^j \right]. \end{split}$$

#### E.4.3 Wages

The F.O.C. for a wage chosen by household h to work in industry j is to maximize

$$E_{t} \left\{ \sum_{s=0}^{\infty} \xi_{w}^{s} \beta^{s} \left[ -b_{t+s} \varphi \frac{L_{t+s}^{j}(h)^{\nu}}{1+\nu} + \Lambda_{t+s} \Pi_{t,t+s}^{w} W_{t}^{j}(h) L_{t+s}^{j}(h) \right] \right\},$$

subject to the demand of the employment agency.

$$L_t^j(h) = \left(\frac{W_t^j(h)}{W_t^j}\right)^{-\epsilon^w} L_t^j,$$

The F.O.C. is

$$E_{t} \left\{ \sum_{s=0}^{\infty} \xi_{w}^{s} \beta^{s} \left[ b_{t+s} \varphi \left[ \left( \frac{\Pi_{t,t+s}^{w} W_{t}^{j}(h)}{W_{t+s}^{j}} \right)^{-\epsilon^{w}} L_{t+s}^{j} \right]^{1+\nu} \frac{1}{W_{t}^{j}(h)} \right] \right\}$$

$$= E_{t} \left\{ \sum_{s=0}^{\infty} \xi_{w}^{s} \beta^{s} \left[ \Lambda_{t+s} \Pi_{t,t+s}^{w} \left[ \left( \frac{\Pi_{t,t+s}^{w} W_{t}^{j}(h)}{W_{t+s}^{j}} \right)^{-\epsilon^{w}} L_{t+s}^{j} \right] \right] \right\},$$

which can be rewritten as

$$\left( \tilde{W}_t^j \right)^{1+\nu\epsilon^w} = \frac{\epsilon^w}{\epsilon^w - 1} \frac{E_t \left\{ \sum_{s=0}^\infty \xi_w^s \beta^s \left[ b_{t+s} \varphi^j \left[ \left( \frac{\Pi_{t,t+s}^w}{W_{t+s}^j} \right)^{-\epsilon^w} L_{t+s}^j \right]^{1+\nu} \right] \right\}}{E_t \left\{ \sum_{s=0}^\infty \xi_w^s \beta^s \Lambda_{t+s} \Pi_{t,t+s}^w \left( \frac{\Pi_{t,t+s}^w}{W_{t+s}^j} \right)^{-\epsilon^w} L_{t+s}^j \right\} }$$

## E.5 The government

A monetary policy authority sets the nominal interest rate following a feedback rule of the form

$$\frac{R_t}{R} = \left(\frac{R_{t-1}}{R}\right)^{\rho_R} \left[ \left(\frac{\Pi_t}{\Pi}\right)^{\phi_{\pi}} \left(\frac{Y_t}{Y_{t-1}}\right)^{\phi_X} \right]^{1-\rho_R} \eta_{mp,t},$$

where R is the steady-state of the gross nominal interest rate. As in Smets and Wouters (2003), interest rates responds to deviations of inflation from its steady state, as well as to the level and growth rate of the GDP  $(Y_t = \sum \gamma^j \frac{P_t^j}{P_t} Y_t^j)$ . The monetary policy rule is also perturbed by a monetary policy shock  $\eta_{mp,t}$ , which evolves according to

$$\log \eta_{mp,t} = \rho_{mp} \log \eta_{mp,t-1} + \epsilon_{mp,t},$$

where  $\epsilon_{mp,t}$  is i.i.d.  $N(0, \sigma_{mp}^2)$ .

Fiscal policy is fully Ricardian. The government finances its budget deficit by issuing short term bonds. Public spending is determined exogenously as a time varying fraction of output:

$$G_t = \left(1 - \frac{1}{\zeta_t}\right) Y_t$$

where the government spending shock  $\zeta_t$  follows the stochastic process

$$\log \zeta_t = (1 - \rho) \log g + \rho \log \zeta_{t-1} + \varepsilon_{g,t}.$$

Public spending is a cobb-douglas aggregate of spending in different sectors. The government chooses sector-specific spending to minimize the cost of  $G_t$ :

$$\begin{aligned} \left\{G_t^j\right\}_j &= \arg\min\sum_j P_t^j G_t^j \\ s.t. : \prod \left(G_t^j\right)^{\alpha_G^j} &= G_t \end{aligned}$$

so that

$$G_t^j = \alpha_G^j \frac{P_t^G}{P_t^j} G_t$$

where 
$$P_t^G = \prod \left(\frac{P_t^j}{\alpha_j^G}\right)^{\alpha_j^G}$$

## E.6 Market clearing

The aggregate resource constraint for each sector j is

$$C_t^j + \sum_{i'} I_t^{jj'} + \sum_{i'} M_t^{jj'} + G_t^j = Y_t^j$$

#### E.7 Model Solution and Calibration

To solve the model we first write it in terms of stationary variables (detrended the permanent part of TFP for real output variables and by the price level for nominal variables), loglinearize it and find the rational expectations equilibrium using Dynare.

The calibration follows Justiniano et al. (2010) wherever possible and uses sectoral linkages and consumer shares obtained from the input-output tables made available by the BEA.

# F Asymptotic Posterior Distribution of $D^Z$

We can make some progress towards characterizing the asymptotic behavior of the marginal posterior of D. Our prior  $p(D^Z, \theta)$  is absolutely continuous with respect to the likelihood function  $\mathcal{L}(D^Z, \theta|Z)$  where Z is the array of all observations on  $Z_t$  and  $\theta$  is the vector of all parameters except  $D^Z$ . WAR and factor model identification arguments imply that under standard regularity conditions (including linearity and Gaussian innovations) all parameters except  $D^Z$  are identified - even with infinite data we can only identify  $D^ZD^{Z'}$ . All other parameters converge to a unique limiting value  $\theta^*$  such that the asymptotic posterior  $p^*(D^Z,\theta|Z)$  (with conditional distribution  $p^*(D^Z|Z,\theta)$  and marginal distribution  $p^*(D^Z|Z)$ ) is given by

$$p^*(D^Z, \theta^*|Z) = p^*(D^Z|Z, \theta = \theta^*) = p^*(D^Z|Z)$$

This equivalence between joint, conditional, and marginal asymptotic posterior is due to the fact that asymptotically the marginal posterior for  $\theta$  will be degenerate and only have mass at  $\theta^*$ .

Let's define the limit of  $D^ZD^{Z'}$  as the sample size T grows large:

$$\lim_{T \to \infty} D^Z D^{Z'} = \phi$$

where this limit should be understood to mean that asymptotically the joint posterior  $p(D^Z, \theta|Z)$  will be equal to 0 except when  $\theta = \theta^*$  and  $D^ZD^{Z'} = \phi$ . Then the asymptotic marginal posterior of  $D^Z$  (denoted by  $p^*(D^Z|Z)$ ) is the prior restricted to those values of  $D^Z$  consistent with  $\phi$ :

$$p^*(D^Z|Z) = p(D^Z|D^ZD^{Z'} = \phi)$$

Applying Bayes' rule to the conditional prior yields:

$$p(D^Z|D^ZD^{Z'} = \phi) = \frac{p(D^ZD^{Z'} = \phi|D^Z)p(D^Z)}{p(D^ZD^{Z'} = \phi)}$$

The first term in the numerator  $p(D^ZD^{Z'}=\phi|D^Z)$  can be interpreted as an indicator

<sup>&</sup>lt;sup>36</sup>Since our priors on blocks of parameters are either Gaussian or inverse Wishart this assumption is satisfied in our model.

function because it will only be non-zero when a value for  $D^Z$  is consistent with  $D^ZD^{Z'}=\phi$ . The second term in the numerator is just the prior  $p(D^Z)$ . The term in the denominator is a normalizing constant that will be independent of  $D^Z$  for all values of  $D^Z$  such that  $D^ZD^{Z'}=\phi$ .

# G Validating the approach: A Monte Carlo Experiment

This section describes the results of a Monte Carlo experiment that is meant to highlight that the overall impact of structural shocks in our environment is identified independently of identifying restrictions for any specific structural shock. All variables in this example are stationary, even though this is not necessary for our method. The aggregate level consists of 4 variables, whereas each sector (of which we have 100) consists of 2 variables. There are two structural shocks (elements of  $\varepsilon_t$ ). The additional, non-structural, shocks ( $w_t$  and  $w_t^i$ ) are correlated within units (sectors or the aggregate level). We assume that most of the variance of the one-step ahead forecast errors at the sectoral level and a substantial fraction of the variance at the aggregate level is in fact due to these additional shocks - Figure 12 displays the fraction of the one-step ahead forecast error due to structural shocks for the variables at the aggregate and sectoral levels. These numbers are meant to convey that this is in fact a hard inference problem - most of the variation in the simulated data is not due to structural shocks. We simulate 130 datapoints and assume a lag length of 1 in all specifications (which is the correct specification). We use the agnostic prior for this estimation.

The Gaussian priors for all coefficients are centered at 0 with a variance of 10 and are thus loose given the magnitude of the parameters used in the estimation. A loose Wishart prior is used for the covariance of the residual error terms.

Even without any specific identifying restrictions on structural shocks, the next two figures show that in finite samples, our approach is able to correctly predict the overall effect of structural shocks. Figure 13 plots the true and estimated (median) effects of the structural shocks on aggregate variables. As outlined in our discussion of identification, these results highlight that while the individual effects of structural shocks can not be estimated without identifying assumption in our framework, the overall effect of all structural disturbances is well identified.

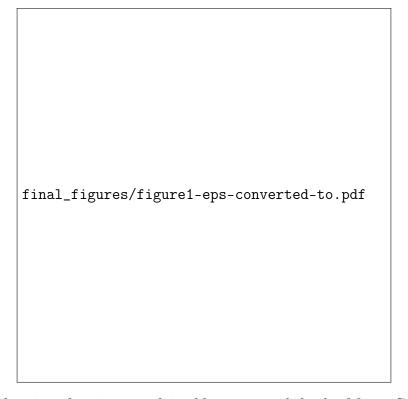


Figure 12: True fraction of variance explained by structural shocks, Monte Carlo experiment, index of variables on the x-axis.

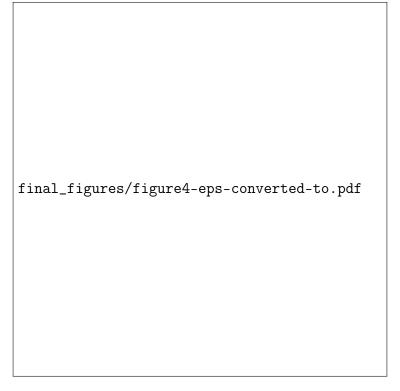


Figure 13: True effect and estimated median effect of the structural shocks on the four aggregate variables, Monte Carlo experiment.

# H Why don't we use more aggregated sectoral data?

Sectoral data are available at various levels of aggregation. We choose to use data that is as disaggregated as possible. To justify this choice, we will study a very simple example. Consider an economy consisting of two equally sized sectors (we could easily generalize this argument to more sectors, but this extension would not add anything to our argument). We disregard aggregate variables here because they are not important for the argument. We also consider one observable per sector. So the state space system we study is

$$u_t^1 = \varepsilon_t + w_t^1 \tag{34}$$

$$u_t^2 = \varepsilon_t + w_t^2 \tag{35}$$

$$\varepsilon_t = \varepsilon_t \tag{36}$$

where  $w_t^1 \sim (N(0, \Sigma^1))$  and  $w_t^2 \sim (N(0, \Sigma^2))$  are two independent Gaussian processes, and, as before,  $\varepsilon_t \sim (N(0, 1))$ . For simplicity, we have normalized the D to 1 in this example in both sectors. Alternatively, we could study a system where we aggregate the two sectors (we use equal weights here because we have assumed for simplicity that the sectors have equal size):

$$\overline{u}_t = \varepsilon_t + \overline{w}_t \tag{37}$$

$$\varepsilon_t = \varepsilon_t$$
 (38)

Here we have  $\overline{w}_t = \frac{1}{2}(w_t^1 + w_t^2)$  and thus  $\overline{w}_t \sim N(0, \frac{1}{4}(\Sigma^1 + \Sigma^2))$ . First note that we abstract in this example from two aspects that would make a researcher want to use more disaggregated data:

- 1. We don't model any dynamics in the sector. It is well known in the time series literature that aggregating VAR processes generally leads to VARMA processes for the aggregated variables. To at the very least be able to approximate these VARMA dynamics in our framework we would need to incorporate more lags of observables into the sectoral equations when using more aggregated data.
- 2. We focus here on the case of one aggregate shock. If there is more than one shock and different sectors have heterogeneous exposures to the different shocks then averaging over this heterogeneous exposure can lead to a substantial loss of information.

Coming back to our example, we can ask which of the two systems leads to a more precise estimate of the shock  $\varepsilon_t$ . We focus here on the variance of the estimation error for  $\varepsilon_t$  <sup>37</sup>.

<sup>&</sup>lt;sup>37</sup>To be precise, we study  $var(\varepsilon_t|I_t)$  where  $I_t$  is the information set including time t observations

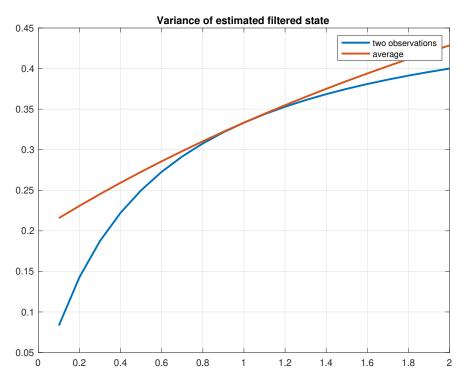


Figure 14: Variance of estimation error.

While it is easy to derive the formulas for the variance in closed form in our simple examples, we can already illustrate the main point with a numerical example. We fix the variance of  $w_t^1$  at 1 and vary the variance of  $w_t^2$  from 0.1 to 2. We then compute the estimated variance for both environments (one with two observables, one with the average observable). Figure 14 shows our main result: it is always preferable to use more disaggregated data. the only point of indifference occurs when the variances of the w shocks are exactly equal. Turning to the analytical solutions,  $var(\varepsilon_t|I_t)$  in the case when we observe both sectors separately is given by

$$var^{\text{two sectors}}(\varepsilon_t | I_t^{\text{two sectors}}) = 1 - (1 \ 1) \left( \begin{pmatrix} 1 & 1 \\ 1 & 1 \end{pmatrix} + \begin{pmatrix} \Sigma^1 & 0 \\ 0 & \Sigma^2 \end{pmatrix} \right)^{-1} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$
(39)

The corresponding formula for the case where the average is observed is

$$var^{\text{average}}(\varepsilon_t|I_t^{\text{average}}) = 1 - \frac{1}{1 + \frac{1}{4}(\Sigma^1 + \Sigma^2)}$$
 (40)

Both these equations are standard Kalman filtering formulas. One can then show that the following always holds:

$$var^{\text{two sectors}}(\varepsilon_t|I_t^{\text{two sectors}}) \le var^{\text{average}}(\varepsilon_t|I_t^{\text{average}})$$
 (41)

Furtmore, the equality is strict unless  $\Sigma^1 = \Sigma^2$ . The proof amounts to tedious but straightforward algebra. The result should not be surprising: you can never be worse off by using more information. Note that one could in our simple example take a weighted average of the sectors to achieve the same variance as in the case with two observables, but in practice this is not feasible because the weights would depend on the variances of the noise terms (the w terms), which are not known before estimation.

# I Impulse Responses to Other Economic Shocks

Note that the responses to the household consumption shock and the monetary shock are in the main text (Figures 3 and 6).

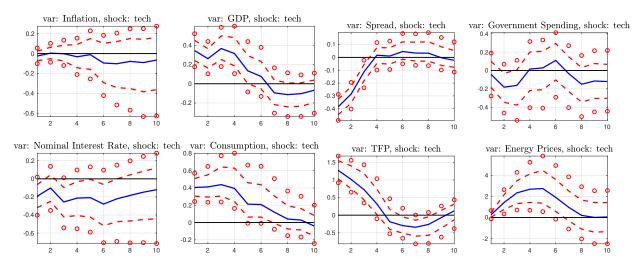


Figure 15: Responses to Technology Shock. Dashed lines are 16th and 84th Posterior Percentile Bands, Dots are 5th and 95th Posterior Percentiles. The x-axis Shows Time in Quarters.

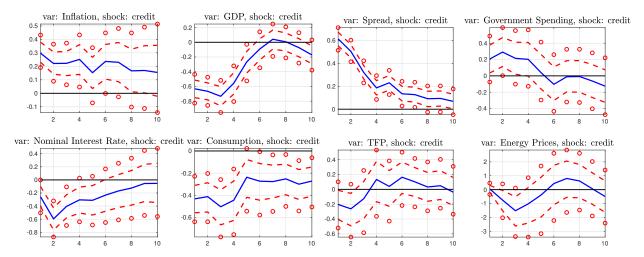


Figure 16: Responses to Credit Shock. Dashed lines are 16th and 84th Posterior Percentile Bands, Dots are 5th and 95th Posterior Percentiles. The x-axis Shows Time in Quarters.

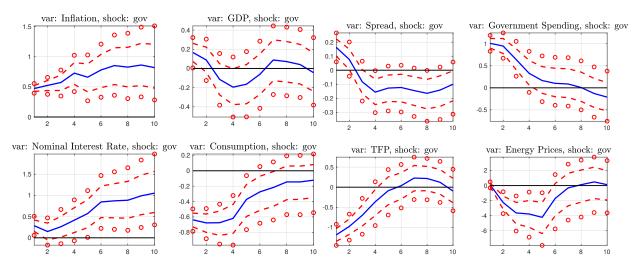


Figure 17: Responses to Government Spending Shock. Dashed lines are 16th and 84th Posterior Percentile Bands, Dots are 5th and 95th Posterior Percentiles. The x-axis Shows Time in Quarters.

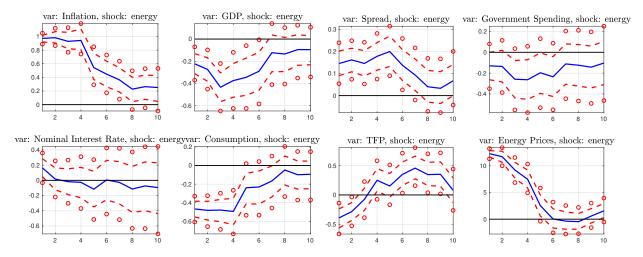


Figure 18: Responses to Energy Price Shock. Dashed lines are 16th and 84th Posterior Percentile Bands, Dots are 5th and 95th Posterior Percentiles. The x-axis Shows Time in Quarters.

### J Robustness checks

To economize on space, we focus in our robustness checks on the importance/variance decomposition (for business cycle frequencies) of the consumption shock for aggregate variables. Relative to the main text we also show the 5th and 95th percentiles of this variance decomposition. Therefore, we start by showing the results for our benchmark case. Throughout all these specifications the household consumption shock remains a key driver of economic activity.

### J.1 Benchmark

	5th Percentile	Mean	95th Percentile
$\pi$	10.3	16.1	20.1
$\operatorname{gdp}$	24.7	35.2	41.7
i	25.2	27.9	32.2
$\mathbf{c}$	37.8	42.8	48.1
spread	5.3	9.1	11.5
g	9.3	28.4	38.4
tfp	4.5	10.3	15.5
energy	5.8	9.3	12.2

Table 7: Variance decomposition across business cycle frequencies, consumption shock. Benchmark specification.

## J.2 Larger Prior Variance on Impact of Consumption Shock

Next, we increase the prior standard deviation for the impact of the consumption shock on aggregate consumption equal to  $1/2 \times abs$  ( $E[D_c]$ ), where  $D_c$  is the prior mean of the impact of the household shock on aggregate consumption.<sup>38</sup>

	5th Percentile	Mean	95th Percentile
$\pi$	23.0	30.5	39.2
$\operatorname{gdp}$	26.9	33.5	37.5
i	22.5	29.2	36.8
c	49.8	52.6	54.3
spread	14.1	19.2	27.5
g	12.9	25.9	33.0
tfp	10.2	16.8	27.6
energy	7.5	9.8	13.9

Table 8: Variance decomposition across business cycle frequencies, consumption shock. Larger prior variance.

### J.3 Shorter Sample

To assess whether or not our results are driven by the Great Recession, we re-estimate the model ending our sample in 2004:Q3.

	5th Percentile	Mean	95th Percentile
$\pi$	18.3	20.5	22.9
$\operatorname{gdp}$	18.5	23.0	29.8
i	20.1	27.2	43.3
c	25.6	27.7	30.8
spread	5.5	12.8	17.1
g	10.6	21.5	27.4
tfp	14.4	18.1	21.6
energy	14.8	17.5	21.0

Table 9: Variance decomposition across business cycle frequencies, consumption shock. Shorter sample.

<sup>&</sup>lt;sup>38</sup>For our benchmark, we use  $0.1 \times abs$  ( $E[D_c]$ ). The prior standard deviation for the aggregate impact of the other aggregate shocks is set in the same fashion.

# J.4 Fewer Lags

We now reduce the number of lags L and  $L^X$  to 4 from our benchmark specification of 6.

	5th Percentile	Mean	95th Percentile
$\pi$	9.1	13.1	24.6
$\operatorname{gdp}$	34.9	42.8	46.4
i	12.8	19.3	35.6
c	34.6	38.5	39.7
spread	11.7	12.5	14.7
g	7.7	12.3	15.2
tfp	8.3	11.5	21.7
energy	2.1	6.6	16.0

Table 10: Variance decomposition across business cycle frequencies, consumption shock. Fewer lags.