

Mathematics Formula Handbook (Detailed Revision Notes)

1) Sequences & Series

Arithmetic Progression (AP)

Definition: A sequence where the difference between consecutive terms is constant.

General form: $a, a+d, a+2d, a+3d, \dots$

nth Term:

$$a_n = a + (n-1)d$$

Sum of First n Terms:

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

Alternate: $S_n = \frac{n}{2} (a + l)$

Special Case (Natural numbers): $S_n = \frac{n(n+1)}{2}$

Geometric Progression (GP)

General form: a, ar, ar^2, ar^3, \dots

nth Term: $a_n = ar^{(n-1)}$

Sum of First n Terms ($r \neq 1$):

$$S_n = \frac{a(1 - r^n)}{(1 - r)}$$

Infinite GP ($|r| < 1$):

$$S = \frac{a}{(1 - r)}$$

Harmonic Progression (HP)

If AP is $a, a+d, a+2d, \dots$

HP is $\frac{1}{a}, \frac{1}{(a+d)}, \frac{1}{(a+2d)}$

2) Linear Equations & Algebra

Linear Equation (One Variable):

$$ax + b = 0$$

$$x = -\frac{b}{a}$$

Linear Equations (Two Variables):

$$a_1x + b_1y = c_1$$

$$a_2x + b_2y = c_2$$

Determinant Method:

$$x = \frac{(c_1b_2 - c_2b_1)}{(a_1b_2 - a_2b_1)}$$

$$y = \frac{(a_1c_2 - a_2c_1)}{(a_1b_2 - a_2b_1)}$$

Quadratic Equation:

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{(2a)}$$

Discriminant: $D = b^2 - 4ac$

Algebraic Identities:

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$a^2 - b^2 = (a-b)(a+b)$$

$$(a+b)^3 = a^3 + b^3 + 3ab(a+b)$$

$$(a-b)^3 = a^3 - b^3 - 3ab(a-b)$$

Binomial Theorem:

$$(a+b)^n = \sum (nCk) a^{(n-k)} b^k$$

3) Basic Geometry & Mensuration

2D Geometry

Rectangle:

$$\text{Area} = l \times b$$

$$\text{Perimeter} = 2(l + b)$$

$$\text{Diagonal} = \sqrt{l^2 + b^2}$$

Square:

$$\text{Area} = a^2$$

$$\text{Perimeter} = 4a$$

$$\text{Diagonal} = a\sqrt{2}$$

Triangle:

$$\text{Area} = \frac{1}{2}bh$$

Heron's Formula:

$$s = \frac{(a+b+c)}{2}$$

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)}$$

Equilateral Triangle:

$$\text{Area} = \left(\frac{\sqrt{3}}{4}\right)a^2$$

Circle:

$$\text{Area} = \pi r^2$$

$$\text{Circumference} = 2\pi r$$

$$\text{Sector Area} = \left(\frac{\theta}{360}\right)\pi r^2$$

$$\text{Arc Length} = \left(\frac{\theta}{360}\right)2\pi r$$

Trapezium:

$$\text{Area} = \frac{1}{2}(a+b)h$$

Parallelogram:

$$\text{Area} = bh$$

3D Mensuration

Cube:

$$\text{Surface Area} = 6a^2$$

$$\text{Volume} = a^3$$

$$\text{Diagonal} = a\sqrt{3}$$

Cuboid:

$$\text{Surface Area} = 2(lb + bh + hl)$$

$$\text{Volume} = lbh$$

$$\text{Diagonal} = \sqrt{l^2 + b^2 + h^2}$$

Cylinder:

$$\text{Volume} = \pi r^2 h$$

$$\text{Curved Surface Area} = 2\pi r h$$

$$\text{Total Surface Area} = 2\pi r(h+r)$$

Cone:

$$\text{Volume} = \frac{1}{3} \pi r^2 h$$

$$\text{Slant height } l = \sqrt{r^2 + h^2}$$

Sphere:

$$\text{Surface Area} = 4\pi r^2$$

$$\text{Volume} = \frac{4}{3} \pi r^3$$

Coordinate Geometry

Distance Formula:

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Midpoint Formula:

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Slope:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Equation of Line:

$$y = mx + c$$