

# Mathematics Formula Handbook (Detailed Revision Notes)

## 1) Sequences & Series

### Arithmetic Progression (AP)

Definition: A sequence where the difference between consecutive terms is constant.

General form:  $a, a+d, a+2d, a+3d, \dots$

nth Term:

$$a_n = a + (n-1)d$$

Sum of First n Terms:

$$S_n = n/2 [2a + (n-1)d]$$

$$\text{Alternate: } S_n = n/2 (a + l)$$

$$\text{Special Case (Natural numbers): } S_n = n(n+1)/2$$

### Geometric Progression (GP)

General form:  $a, ar, ar^2, ar^3, \dots$

nth Term:  $a_n = ar^{(n-1)}$

Sum of First n Terms ( $r \neq 1$ ):

$$S_n = a(1 - r^n)/(1 - r)$$

Infinite GP ( $|r| < 1$ ):

$$S = a/(1 - r)$$

### Harmonic Progression (HP)

If AP is  $a, a+d, a+2d, \dots$

HP is  $1/a, 1/(a+d), 1/(a+2d)$

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## 2) Linear Equations & Algebra

### Linear Equation (One Variable):

$$ax + b = 0$$

$$x = -b/a$$

### Linear Equations (Two Variables):

$$a_1x + b_1y = c_1$$

$$a_2x + b_2y = c_2$$

Determinant Method:

$$x = (c_1b_2 - c_2b_1)/(a_1b_2 - a_2b_1)$$

$$y = (a_1c_2 - a_2c_1)/(a_1b_2 - a_2b_1)$$

Quadratic Equation:

$$ax^2 + bx + c = 0$$

$$x = [-b \pm \sqrt{b^2 - 4ac}]/(2a)$$

Discriminant:  $D = b^2 - 4ac$

Algebraic Identities:

$$(a+b)^2 = a^2 + 2ab + b^2$$

$$(a-b)^2 = a^2 - 2ab + b^2$$

$$\begin{aligned} a^2 - b^2 &= (a-b)(a+b) \\ (a+b)^3 &= a^3 + b^3 + 3ab(a+b) \\ (a-b)^3 &= a^3 - b^3 - 3ab(a-b) \end{aligned}$$

Binomial Theorem:  
 $(a+b)^n = \sum(nCk) a^{(n-k)} b^k$

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### 3) Basic Geometry & Mensuration

#### 2D Geometry

Rectangle:  
 Area =  $l \times b$   
 Perimeter =  $2(l + b)$   
 Diagonal =  $\sqrt{l^2 + b^2}$

Square:  
 Area =  $a^2$   
 Perimeter =  $4a$   
 Diagonal =  $a\sqrt{2}$

Triangle:  
 Area =  $\frac{1}{2}bh$   
 Heron's Formula:  
 $s = (a+b+c)/2$   
 Area =  $\sqrt{s(s-a)(s-b)(s-c)}$

Equilateral Triangle:  
 Area =  $(\sqrt{3}/4)a^2$

Circle:  
 Area =  $\pi r^2$   
 Circumference =  $2\pi r$   
 Sector Area =  $(\theta/360)\pi r^2$   
 Arc Length =  $(\theta/360)2\pi r$

Trapezium:  
 Area =  $\frac{1}{2}(a+b)h$

Parallelogram:  
 Area =  $bh$

#### 3D Mensuration

Cube:  
 Surface Area =  $6a^2$   
 Volume =  $a^3$   
 Diagonal =  $a\sqrt{3}$

Cuboid:  
 Surface Area =  $2(lb + bh + hl)$   
 Volume =  $lbh$   
 Diagonal =  $\sqrt{l^2 + b^2 + h^2}$

Cylinder:

$$\text{Volume} = \pi r^2 h$$

$$\text{Curved Surface Area} = 2\pi r h$$

$$\text{Total Surface Area} = 2\pi r(h+r)$$

Cone:

$$\text{Volume} = \frac{1}{3} \pi r^2 h$$

$$\text{Slant height } l = \sqrt{r^2 + h^2}$$

Sphere:

$$\text{Surface Area} = 4\pi r^2$$

$$\text{Volume} = \frac{4}{3} \pi r^3$$

Coordinate Geometry

Distance Formula:

$$\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}$$

Midpoint Formula:

$$((x_1+x_2)/2, (y_1+y_2)/2)$$

Slope:

$$m = (y_2-y_1)/(x_2-x_1)$$

Equation of Line:

$$y = mx + c$$