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COMP 558 - Assignment 3

Question 1

I used the “imtool” Matlab function to output the images and be able to look at pixel coordinates (x,y) of the images.

I then selected 8 matching points for each image and proceeded to estimate a fundamental matrix in the following way:

- 1) Data normalization.
- 2) Solving least squares problem to estimate the entries of F_{norm} .
- 3) Mapping these entries to the entries of F via a de-normalization matrix linear transformation on F_{norm} .
- 4) Enforcing a rank 2 constraint on F by modifying its svd S matrix composition and replacing $S(3,3)=0$;

Fundamental Matrix for Stereo 1 output:

Q1. Rank of Generated Fundamental Matrix is:

2

Q1. Fundamental Matrix for Image Pair #1 is:

$$\begin{bmatrix} -0.0000 & 0.0000 & -0.0057 \\ -0.0000 & 0.0000 & 0.0041 \\ 0.0065 & -0.0152 & 1.1846 \end{bmatrix}$$

Fundamental Matrix for Stereo 2 output:

Q1. Rank of Generated Fundamental Matrix #2 is:

2

Q1. Fundamental Matrix for Image Pair #2 is:

$$\begin{bmatrix} 0.0000 & -0.0000 & 0.0005 \\ 0.0000 & -0.0000 & 0.0049 \\ -0.0002 & -0.0044 & -0.1468 \end{bmatrix}$$

Question 2

I generate a Fundamental Matrix for each of the image pairs through the following steps:

We run a RANSAC algorithm for which we establish a number of iterations, consensus_set limit and consensus_set criteria.

Also before the first iteration I do the following:

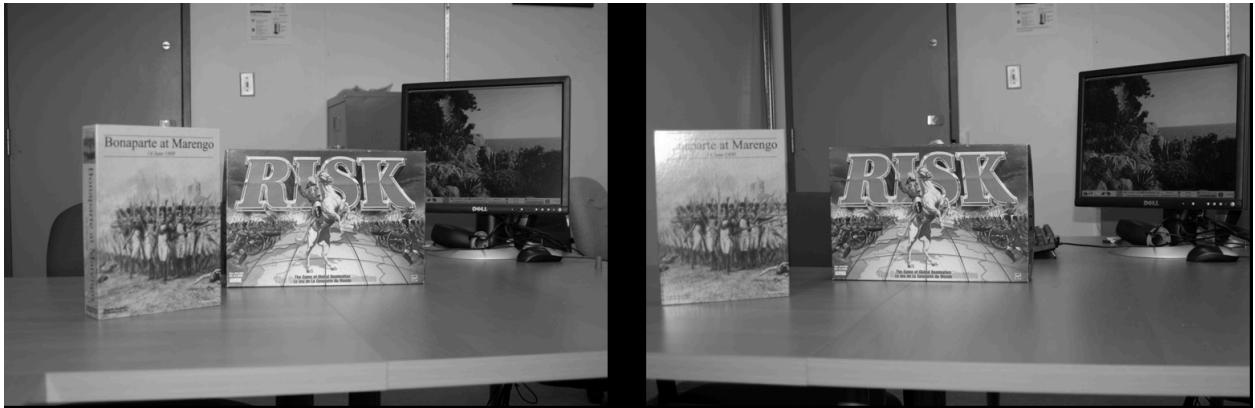
For each of the RANSAC iterations I do the following:

- 1.- Randomly select 8 SURF-points
- 2.- Generate matrix F with these points
- 3.- Iterate remaining SURF-points and check how many are in the consensus set by checking Epipolar constraint $x_2^T F x_1 = 0$. (i.e. which and how many SURF points satisfy this constraint).
- 4.- If the generated matrix F is the best fit up to now then we store it as a good model.
- 5.- We output fundamental matrix with the largest consensus set refitted with points in the consensus set.

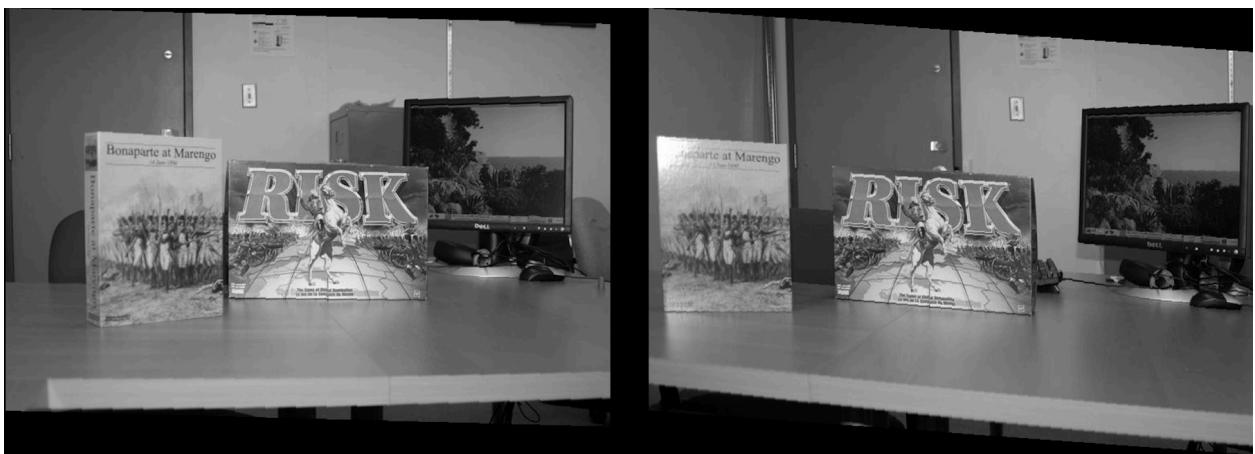
Question 3

Stereo Images (Pair 1):

Not Rectified:



Rectified:



Using Matrix F:

```
[ -1.22385320147802e-10 -2.50616093221418e-08 0.000451599943821839;
 7.81213585694305e-09 1.81365234376140e-08 0.00617765081138932;
 -0.000203816506415516 -0.00776863296924383 0.291008688968557]
```

Stereo Images (Pair 2):

Not Rectified:



Rectified:



Using Matrix F:

```
[-1.53462543900070e-09 -3.81367453594227e-08  0.000959839530888257;
 4.32486782071492e-08   -7.73082718392819e-09 -0.00701186455415368;
 -0.000779682823153024  0.00697016201977165   -0.0364890075064721]
```

Question 4

(I = 1 for Pair 1, I = 2 for Pair 2).

Using the computed Fundamental Matrix F_i for each of the Stereo Images in Q3 that yield a good rectification result. We compute Essential Matrix E .

In this question we are given intrinsic parameters of both cameras (for each image pair), which we store in matrix K_i .

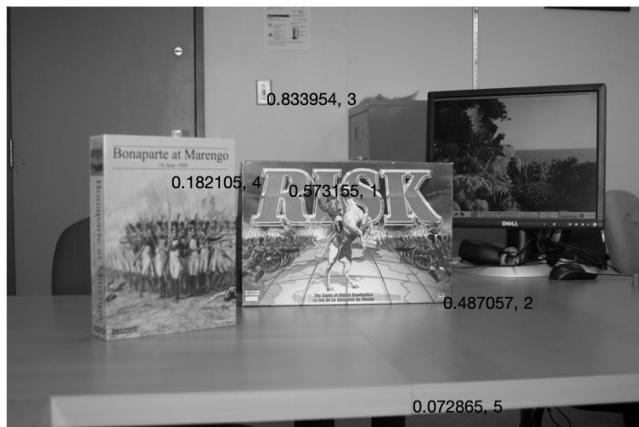
So we get that $E_i = K_i^{-1} F_i K_i$.

We extract the extrinsic parameters in the following way from Essential Matrix E_i .

- T is the right null space from matrix E (positive and negative)
- R is equal to $U^* W^* V'$ or $U^* W'^* V'$ where W is a defined matrix

I tried all possible combinations and determined which one gave the best results for each pair of images, to obtain a , b and c scalars. The optimal results are the following.

The further away a point is from the camera, the larger it's depth value is.

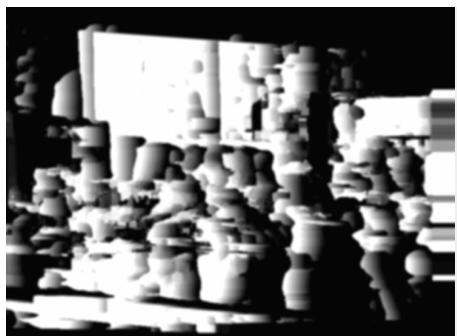


Question 5

I used a Lukas-Kanade 1D approach to compute image disparity and depth.

For image pair 1:

Disparity map:

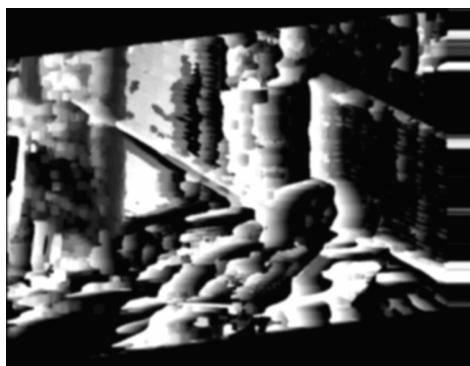


Depth map:



For image pair 2:

Disparity map:



Depth map:



From the results I can gather that we get a better disparity and therefore depth map for image pair 2 since it's points don't vary too much along the x axis since we are using Lukas-Kanade1D Algorithm along that axis.

We have that the results aren't that clear for Image pair 1. This is due to a larger variation on corresponding points, camera from the right seems to have a more tilted

view of the 3D Scene which causes rectification to not be as accurate and therefore Lukas-Kanade can't portray disparity and depth as correctly as it should.