Public Key Encryption with keyword Search

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Abstract

We study the problem of searching on data that is encrypted using a public key system. Consider user Bob who sends email to user Alice encrypted under Alice's public key. An email gateway wants to test whether the email contains the keyword "urgent" so that it could route the email accordingly. Alice, on the other hand does not wish to give the gateway the ability to decrypt all her messages. We define and construct a mechanism that enables Alice to provide a key to the gateway that enables the gateway to test whether the word "urgent" is a keyword in the email without learning anything else about the email. We refer to this mechanism as Public Key Encryption with keyword Search. As another example, consider a mail server that stores various messages publicly encrypted for Alice by others. Using our mechanism Alice can send the mail server a key that will enable the server to identify all messages containing some specific keyword, but learn nothing else. We define the concept of public key encryption with keyword search and give several constructions.

1 Introduction

Suppose user Alice wishes to read her email on a number of devices: laptop, desktop, pager, etc. Alice's mail gateway is supposed to route email to the appropriate device based on the keywords in the email. For example, when Bob sends email with the keyword "urgent" the mail is routed to Alice's pager. When Bob sends email with the keyword "lunch" the mail is routed to Alice's desktop for reading later. One expects each email to contain a small number of keywords. For example, all words on the subject line as well as the sender's email address could be used as keywords. The mobile people project [24] provides this email processing capability.

Now, suppose Bob sends encrypted email to Alice using Alice's public key. Both the contents of the email and the keywords are encrypted. In this case the mail gateway cannot see the keywords and hence cannot make routing decisions. As a result, the mobile people project is unable to process secure email without violating user privacy. Our goal is to enable Alice to give the gateway the ability to test whether "urgent" is a keyword in the email, but the gateway should learn nothing else about the email. More generally, Alice should be able to specify a few keywords that the mail gateway can search for, but learn nothing else about incoming mail. We give precise definitions in section 2.

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To do so, Bob encrypts his email using a standard public key system. He then appends to the resulting ciphertext a *Public-Key Encryption with keyword Search* (PEKS) of each keyword. To send a message M with keywords W_1, \ldots, W_m Bob sends

$$E_{A_{pub}}(M) \ \parallel \ \mathsf{PEKS}(A_{pub}, W_1) \ \parallel \ \cdots \ \parallel \ \mathsf{PEKS}(A_{pub}, W_m)$$

Where A_{pub} is Alice's public key. The point of this form of encryption is that Alice can give the

gateway a certain trapdoor T_W that enables the gateway to test whether one of the keywords associated with the message is equal to the word W of Alice's choice. Given $\mathsf{PEKS}(A_{pub}, W')$ and T_W the gateway can test whether W = W'. If $W \neq W'$ the gateway learns nothing more about W'. Note that Alice and Bob do not communicate in this entire process. Bob generates the searchable encryption for W' just given Alice's public key.

In some cases, it is instructive to view the email gateway as an IMAP or POP email server. The server stores many emails and each email contains a small number of keywords. As before, all these emails are created by various people sending mail to Alice encrypted using her public key. We want to enable Alice to ask queries of the form: do any of the messages on the server contain the keyword "urgent"? Alice would do this by giving the server a trapdoor T_W , thus enabling the server to retrieve emails containing the keyword W. The server learns nothing else about the emails.

Related work. A related issue deals with privacy of database data. There are two different scenarios: *public* databases and *private* databases, and the solutions for each are different. *Private databases:* In this settings a user wishes to upload its private data to a remote database and

wishes to keep the data private from the remote database administrator. Later, the user must be

able to retrieve from the remote database all records that contain a particular keyword. Solutions to this problem were presented in the early 1990's by Ostrovsky [26] and Ostrovsky and Goldreich [17] and more recently by Song at al. [28]. The solution of Song. at al [28] requires very little communication between the user and the database (proportional to the security parameter) and only one round of interaction. The database performs work that is linear in its size per query. The solution of [26, 17] requires poly-logarithmic rounds (in the size of the database) between the user and the database, but allows the database to do only poly-logarithmic work per query. An additional privacy requirement that might be appealing in some scenarios is to hide from the database administrator any information regarding the access pattern, i.e. if some item was retrieved more then once, some item was not retrieved at all, etc. The work of [26, 17] achieves this property as well, with the same poly-logarithmic cost¹ per query both for the database-user interaction and the actual database work. We stress that both the constructions of [26, 17] and the more recent work of [10, 28, 16] apply only to the private-key setting for users who own their data and wish to upload it to a third-party database that they do not trust.

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Public Databases Here the database data is public (such as stock quotes) but the user is unaware of it and wishes to retrieve some data-item or search for some data-item, without revealing to the database administrator which item it is. The naive solution is that the user can download the entire database. Public Information Retrieval (PIR) protocols allow user to retrieve data from a public database with far smaller communication then just downloading the entire database. PIR was first shown to be possible only in the setting where there are many copies of the same database

basic $O(\sqrt{n})$ solution was recently shown to be applicable for some practical applications [10].

and none of the copies can talk to each other [5]. PIR was shown to be possible for a single database by Kushilevitz and Ostrovsky [22] (using homomorphic encryption scheme of [19]). The communication complexity of [22] solution (i.e. the number of bits transmitted between the user

1 The poly-logarithmic construction of [26, 17] requires large constants, which makes it impractical; however their

We stress though that in all these settings the database is public, and the user is trying to retrieve or find certain items without revealing to the database administrator what it is searching for. In the setting of a single public database, it can be shown that the database must always perform work which is at least linear in the size of the database.

Our problem does not fit either of the two models mentioned above. Unlike the private-key

and the database) is $O(n^{\epsilon})$, where n is the size of the database and $\epsilon > 0$. This was reduced to poly-logarithmic overhead by Cachin, Micali, and Stadler [4]. As pointed out in [22], the model of PIR can be extended to one-out-of-n Oblivious Transfer and keyword searching on public data, and received a lot of additional attention in the literature (see, for example, [22, 8, 20, 9, 23, 25, 27].

setting, data collected by the mail-server is from third parties, and can not be "organized" by the user in any convenient way. Unlike the publicly available database, the data is not public, and hence the PIR solutions do not apply. We point out that in practical applications, due to the computation cost of public key encryption,

our constructions are applicable to searching on a small number of keywords rather than an entire file. Recently, Waters et al. [30] showed that public key encryption with keyword search can be used to build an encrypted and searchable audit log. Other methods for searching on encrypted data are described in [16, 12].

Public key encryption with searching: definitions 2

f(s) < 1/q(s) for any polynomial q and sufficiently large s. We start by precisely defining what is a secure Public Key Encryption with keyword Search

Throughout the paper we use the term negligible function to refer to a function $f: \mathbb{R} \to [0,1]$ where

(PEKS) scheme. Here "public-key" refers to the fact that ciphertexts are created by various people using Alice's public key. Suppose user Bob is about to send an encrypted email to Alice with keywords W_1, \ldots, W_k (e.g., words in the subject line and the sender's address could be used as keywords, so that k is relatively small). Bob sends the following message:

$$\left[E_{A_{pub}}[msg], \ \mathsf{PEKS}(A_{pub}, W_1), \dots, \mathsf{PEKS}(A_{pub}, W_k)\right] \tag{1}$$

searching for specific keywords. For the rest of the paper, we use as our sample application a mail server that stores all incoming email. Our goal is to enable Alice to send a short secret key T_W to the mail server that will enable the server to locate all messages containing the keyword W, but learn nothing else. Alice produces

where A_{pub} is Alice's public key, msg is the email body, and PEKS is an algorithm with properties discussed below. The PEKS values do not reveal any information about the message, but enable

this trapdoor T_W using her private key. The server simply sends the relevant emails back to Alice. We call such a system non-interactive public key encryption with keyword search, or as a shorthand "searchable public-key encryption".

Definition 2.1. A non-interactive public key encryption with keyword search (we sometimes abbreviate it as "searchable encryption") scheme consists of the following polynomial time randomized algorithms:

- 1. KeyGen(s): Takes a security parameter, s, and generates a public/private key pair A_{pub} , A_{priv} .
 - 2. $PEKS(A_{pub}, W)$: for a public key A_{pub} and a word W, produces a searchable encryption of W. 3. Trapdoor (A_{priv}, W) : given Alice's private key and a word W produces a trapdoor T_W .

a trapdoor $T_W = \mathsf{Trapdoor}(A_{priv}, W)$, outputs 'yes' if W = W' and 'no' otherwise.

4. Test (A_{pub}, S, T_W) : given Alice's public key, a searchable encryption $S = \mathsf{PEKS}(A_{pub}, W')$, and

Alice runs the KeyGen algorithm to generate her public/private key pair. She uses Trapdoor to generate trapdoors T_W for any keywords W that she wants the mail server or mail gateway to search for. The mail server uses the given trapdoors as input to the Test() algorithm to determine whether a given email contains one of the keywords W specified by Alice.

Next, we define security for a PEKS in the sense of semantic-security. We need to ensure that an PEKS (A_{pub}, W) does not reveal any information about W unless T_W is available. We define security against an active attacker who is able to obtain trapdoors T_W for any W of his choice. Even under such attack the attacker should not be able to distinguish an encryption of a keyword W_0 from an encryption of a keyword W_1 for which he did not obtain the trapdoor. Formally, we define security against an active attacker A using the following game between a challenger and the attacker (the security parameter s is given to both players as input).

PEKS Security game:

defined in [2].

- The challenger runs the KeyGen(s) algorithm to generate A_{pub} and A_{priv}. It gives A_{pub} to the attacker.
 The attacker can adaptively ask the challenger for the trapdoor T_W for any keyword
- W ∈ {0,1}* of his choice.
 3. At some point, the attacker A sends the challenger two words W₀, W₁ on which it wishes to be challenged. The only restriction is that the attacker did not previously ask for the
- trapdoors T_{W_0} or T_{W_1} . The challenger picks a random $b \in \{0,1\}$ and gives the attacker $C = \mathsf{PEKS}(A_{pub}, W_b)$. We refer to C as the challenge PEKS .

 4. The attacker can continue to ask for trapdoors T_W for any keyword W of his choice as
- long as $W \neq W_0, W_1$. 5. Eventually, the attacker \mathcal{A} outputs $b' \in \{0, 1\}$ and wins the game if b = b'.
- o. Eventually, the accuracy of outputs of C [0,1] and wind the Same is 0 = 0

PEKS for W_0 or W_1 . We define \mathcal{A} 's advantage in breaking the PEKS as

In other words, the attacker wins the game if he can correctly guess whether he was given the

$$Adv_{\mathcal{A}}(s) = |\Pr[b = b'] - \frac{1}{2}|$$

Definition 2.2. We say that a PEKS is semantically secure against an adaptive chosen keyword attack if for any polynomial time attacker \mathcal{A} we have that $\mathrm{Adv}_{\mathcal{A}}(s)$ is a negligible function.

Chosen Ciphertext Security. We note that Definition 2.2 ensures that the construction given in Eq. (1) is semantically secure whenever the public key encryption system $E_{A_{pub}}$ is semantically secure. However, as is, the construction is not chosen ciphertext secure. Indeed, a chosen ciphertext attacker can break semantic security by reordering the keywords in Eq. (1) and submitting the resulting ciphertext for decryption. A standard technique can make this construction chosen

ciphertext secure using the methods of [7]. We defer this to the full version of the paper.

2.1 PEKS implies Identity Based Encryption

Public key encryption with keyword search is related to Identity Based Encryption (IBE) [29, 2]. Constructing a secure PEKS appears to be a harder problem than constructing an IBE. Indeed, the following lemma shows that PEKS implies Identity Based Encryption. The converse is probably false. Security notions for IBE, and in particular chosen ciphertext secure IBE (IND-ID-CCA), are

Lemma 2.3. A non-interactive searchable encryption scheme (PEKS) that is semantically secure against an adaptive chosen keyword attack gives rise to a chosen ciphertext secure IBE system (IND-ID-CCA).

Proof sketch: Given a PEKS (KeyGen, PEKS, Trapdoor, Test) the IBE system is as follows:

- 1. Setup: Run the PEKS KeyGen algorithm to generate A_{pub}/A_{priv} . The IBE system parameters are A_{pub} . The master-key is A_{priv} .
- 2. KeyGen: The IBE private key associated with a public key $X \in \{0,1\}^*$ is

$$d_X = \left[\mathsf{Trapdoor}(A_{priv},\, X \| 0), \;\; \mathsf{Trapdoor}(A_{priv},\, X \| 1)\right],$$

where || denotes concatenation.

- 3. Encrypt: Encrypt a bit $b \in \{0,1\}$ using a public key $X \in \{0,1\}^*$ as: $CT = \mathsf{PEKS}(A_{pub}, X || b)$.
- 4. Decrypt: To decrypt $CT = \mathsf{PEKS}(A_{pub}, X \| b)$ using the private key $d_X = (d_0, d_1)$. Output '0' if $\mathsf{Test}(A_{pub}, CT, d_0) =$ 'yes' and output '1' if $\mathsf{Test}(A_{pub}, CT, d_1) =$ 'yes'

One can show that the resulting system is IND-ID-CCA assuming the PEKS is semantically secure against an adaptive chosen message attack.

This shows that building non-interactive public-key searchable encryption is at least as hard as building an IBE system. One might be tempted to prove the converse (i.e., IBE implies PEKS) by defining

$$\mathsf{PEKS}(A_{pub}, W) = E_W[0^k] \tag{2}$$

give a secure searchable encryption scheme. The problem is that the ciphertext CT could expose the public key (W) used to create CT. Generally, an encryption scheme need not hide the public key that was used to create a given ciphertext. But this property is essential for the PEKS construction given in (2). We note that public key privacy was previously studied by Bellare et al. [1]. The construction in (2) requires an IBE system that is public-key private.

i.e. encrypt a string of k zeros with the IBE public key $W \in \{0, 1\}^*$. The Test algorithm attempts to decrypt $E_W[0]$ and checks that the resulting plaintext is 0^k . Unfortunately, this does not necessarily

Generally, it appears that constructing a searchable public-key encryption is a harder problem than constructing an IBE scheme. Nevertheless, our first PEKS construction is based on a recent construction for an IBE system. We are able to prove security by exploiting extra properties of this system.

3 Constructions

We give two constructions for public-key searchable encryption: (1) an efficient system based on a variant of the Decision Diffie-Hellman assumption (assuming a random oracle) and (2) a limited system based on general trapdoor permutations (without assuming the random oracle), but less efficient.

3.1 Construction using bilinear maps

and Franklin [2] recently used bilinear maps on elliptic curves to build an efficient IBE system. Abstractly, they use two groups G_1, G_2 of prime order p and a bilinear map $e: G_1 \times G_1 \to G_2$ between them. The map satisfies the following properties:

Our first construction is based on a variant of the Computational Diffie-Hellman problem. Boneh

1. Computable: given $g, h \in G_1$ there is a polynomial time algorithms to compute $e(g, h) \in G_2$. 2. Bilinear: for any integers $x, y \in [1, p]$ we have $e(g^x, g^y) = e(g, g)^{xy}$

We build a non-interactive searchable encryption scheme from such a bilinear map. The construction is based on [2]. We will need hash functions $H_1: \{0,1\}^* \to G_1$ and $H_2: G_2 \to \{0,1\}^{\log p}$.

3. Non-degenerate: if g is a generator of G_1 then e(g,g) is a generator of G_2 .

The size of G_1, G_2 is determined by the security parameter.

Our PEKS works as follows:

• KeyGen: The input security parameter determines the size, p, of the groups G_1 and G_2 . The algorithm picks a random $\alpha \in \mathbb{Z}_p^*$ and a generator g of G_1 . It outputs $A_{pub} = [g, h = g^{\alpha}]$ and

- $A_{priv} = \alpha$.

 PEKS (A_{pub}, W) : First compute $t = e(H_1(W), h^r) \in G_2$ for a random $r \in \mathbb{Z}_p^*$.

 Output PEKS $(A_{pub}, W) = [g^r, H_2(t)]$.
- Trapdoor (A_{priv}, W) : output $T_W = H_1(W)^{\alpha} \in G_1$. • Test (A_{pub}, S, T_W) : let S = [A, B]. Test if $H_2(e(T_W, A)) = B$.
- If so, output 'yes'; if not, output 'no'.

We prove that this system is a non-interactive searchable encryption scheme semantically secure against a chosen keyword attack in the random oracle model. The proof of security relies on the

difficulty of the Bilinear Diffie-Hellman problem (BDH) [2, 21].

Bilinear Diffie-Hellman Problem (BDH): Fix a generator g of G_1 . The BDH problem is as follows: given $g, g^a, g^b, g^c \in G_1$ as input, compute $e(g, g)^{abc} \in G_2$. We say that BDH is intractable if all polynomial time algorithms have a negligible advantage in solving BDH.

We note that the Boneh-Franklin IBE system [2] relies on the same intractability assumption

for security. The security of our PEKS is proved in the following theorem. The proof is set in the random oracle model. Indeed, it is currently an open problem to build a secure IBE, and hence a PEKS, without the random oracle model.

Theorem 3.1. The non-interactive searchable encryption scheme (PEKS) above is semantically secure against a chosen keyword attack in the random oracle model assuming BDH is intractable.

Proof: Suppose \mathcal{A} is an attack algorithm that has advantage ϵ in breaking the PEKS. Suppose \mathcal{A} makes at most q_{H_2} hash function queries to H_2 and at most q_T trapdoor queries (we assume q_T and

makes at most q_{H_2} hash function queries to H_2 and at most q_T trapdoor queries (we assume q_T and q_{H_2} are positive). We construct an algorithm \mathcal{B} that solves the BDH problem with probability at least $\epsilon' = \epsilon/(eq_Tq_{H_2})$, where e is the base of the natural logarithm. Algorithm \mathcal{B} 's running time is approximately the same as \mathcal{A} 's. Hence, if the BDH assumption holds in G_1 then ϵ' is a negligible

function and consequently ϵ must be a negligible function in the security parameter. Let g be a generator of G_1 . Algorithm \mathcal{B} is given $g, u_1 = g^{\alpha}, u_2 = g^{\beta}, u_3 = g^{\gamma} \in G_1$. Its goal is to output $v = e(g, g)^{\alpha\beta\gamma} \in G_2$. Algorithm \mathcal{B} simulates the challenger and interacts with forger \mathcal{A}

as follows:

 H_1 queries algorithm \mathcal{B} maintains a list of tuples $\langle W_i, h_i, a_i, c_i \rangle$ called the H_1 -list. The list is initially empty. When \mathcal{A} queries the random oracle H_1 at a point $W_i \in \{0,1\}^*$, algorithm \mathcal{B} responds as follows:

2. Otherwise, \mathcal{B} generates a random coin $c_i \in \{0,1\}$ so that $\Pr[c_i = 0] = 1/(q_T + 1)$.

1. If the query W_i already appears on the H_1 -list in a tuple $\langle W_i, h_i, a_i, c_i \rangle$ then algorithm \mathcal{B}

 H_1, H_2 -queries. At any time algorithm \mathcal{A} can query the random oracles H_1 or H_2 . To respond to

- 4. Algorithm \mathcal{B} adds the tuple $\langle W_i, h_i, a_i, c_i \rangle$ to the H_1 -list and responds to \mathcal{A} by setting $H_1(W_i) = h_i$. Note that either way h_i is uniform in G_1 and is independent of \mathcal{A} 's current
- If $c_i = 0$, \mathcal{B} computes $h_i \leftarrow u_2 \cdot g^{a_i} \in G_1$. If $c_i = 1$, \mathcal{B} computes $h_i \leftarrow g^{a_i} \in G_1$.

KeyGen. Algorithm \mathcal{B} starts by giving \mathcal{A} the public key $A_{pub} = [g, u_1]$.

responds with $H_1(W_i) = h_i \in G_1$.

3. Algorithm \mathcal{B} picks a random $a_i \in \mathbb{Z}_p$.

is initially empty.

view as required. Similarly, at any time \mathcal{A} can issue a query to H_2 . Algorithm \mathcal{B} responds to a query for $H_2(t)$ by picking a new random value $V \in \{0,1\}^{\log p}$ for each new t and setting $H_2(t) = V$. In

addition, \mathcal{B} keeps track of all H_2 queries by adding the pair (t, V) to an H_2 -list. The H_2 -list

Trapdoor queries. When \mathcal{A} issues a query for the trapdoor corresponding to the word W_i algorithm \mathcal{B} responds as follows: 1. Algorithm \mathcal{B} runs the above algorithm for responding to H_1 -queries to obtain an $h_i \in G_1$ such that $H_1(W_i) = h_i$. Let $\langle W_i, h_i, a_i, c_i \rangle$ be the corresponding tuple on the H_1 -list. If

- $c_i = 0$ then \mathcal{B} reports failure and terminates. 2. Otherwise, we know $c_i = 1$ and hence $h_i = g^{a_i} \in G_1$. Define $T_i = u_1^{a_i}$. Observe that $T_i = H(W_i)^{\alpha}$ and therefore T_i is the correct trapdoor for the keyword W_i under the public key $A_{pub} = [g, u_1]$. Algorithm \mathcal{B} gives T_i to algorithm \mathcal{A} .
- challenged on. Algorithm \mathcal{B} generates the challenge PEKS as follows: 1. Algorithm \mathcal{B} runs the above algorithm for responding to H_1 -queries twice to obtain a $h_0, h_1 \in G_1$ such that $H_1(W_0) = h_0$ and $H_1(W_1) = h_1$. For i = 0, 1 let $\langle W_i, h_i, a_i, c_i \rangle$ be the corresponding tuples on the H_1 -list. If both $c_0 = 1$ and $c_1 = 1$ then \mathcal{B} reports failure

Challenge. Eventually algorithm \mathcal{A} produces a pair of keywords W_0 and W_1 that it wishes to be

- and terminates. 2. We know that at least one of c_0 , c_1 is equal to 0. Algorithm \mathcal{B} randomly picks a $b \in \{0,1\}$
 - such that $c_b = 0$ (if only one c_b is equal to 0 then no randomness is needed since there is only one choice).
 - 3. Algorithm \mathcal{B} responds with the challenge PEKS $C = [u_3, J]$ for a random $J \in \{0, 1\}^{\log p}$. Note that this challenge implicitly defines $H_2(e(H_1(W_b), u_1^{\gamma})) = J$. In other words,

$$J = H_2(e(H_1(W_b), u_1^{\gamma})) = H_2(e(u_2 g^{a_b}, g^{\alpha \gamma})) = H_2(e(g, g)^{\alpha \gamma (\beta + a_b)})$$

With this definition, C is a valid PEKS for W_b as required.

More trapdoor queries. A can continue to issue trapdoor queries for keywords W_i where the only restriction is that $W_i \neq W_0, W_1$. Algorithm \mathcal{B} responds to these queries as before.

picks this pair (t, V) from the H_2 -list then $t/e(u_1, u_3)^{a_b} = e(g, g)^{\alpha\beta\gamma}$ as required. This completes the description of algorithm \mathcal{B} . It remains to show that \mathcal{B} correctly outputs $e(g,g)^{\alpha\beta\gamma}$ with probability at least ϵ' . To do so, we first analyze the probability that \mathcal{B} does

Output. Eventually, \mathcal{A} outputs its guess $b' \in \{0,1\}$ indicating whether the challenge C is the result of $PEKS(A_{pub}, W_0)$ or $PEKS(A_{pub}, W_1)$. At this point, algorithm \mathcal{B} picks a random pair (t, V)from the H_2 -list and outputs $t/e(u_1, u_3)^{a_b}$ as its guess for $e(g, g)^{\alpha\beta\gamma}$, where a_b is the value used in the Challenge step. The reason this works is that, as we will show, $\mathcal A$ must have issued a query for either $H_2(e(H_1(W_0), u_1^{\gamma}))$ or $H_2(e(H_1(W_1), u_1^{\gamma}))$. Therefore, with probability 1/2the H_2 -list contains a pair whose left hand side is $t = e(H_1(W_b), u_1^{\gamma}) = e(g, g)^{\alpha \gamma(\beta + a_b)}$. If \mathcal{B}

not abort during the simulation. We define two events: \mathcal{E}_1 : \mathcal{B} does not abort as a result of any of \mathcal{A} 's trapdoor queries. \mathcal{E}_2 : \mathcal{B} does not abort during the challenge phase.

We first argue as in [6] that both events \mathcal{E}_1 and \mathcal{E}_2 occur with sufficiently high probability.

Claim 1: The probability that algorithm \mathcal{B} does not abort as a result of \mathcal{A} 's trapdoor queries is at least 1/e. Hence, $\Pr[\mathcal{E}_1] \geq 1/e$. *Proof.* Without loss of generality we assume that \mathcal{A} does not ask for the trapdoor of the same

keyword twice. The probability that a trapdoor query causes \mathcal{B} to abort is $1/(q_T+1)$. To see this, let W_i be A's i'th trapdoor query and let $\langle W_i, h_i, a_i, c_i \rangle$ be the corresponding tuple on the H_1 -list.

Prior to issuing the query, the bit c_i is independent of \mathcal{A} 's view — the only value that could be given to A that depends on c_i is $H(W_i)$, but the distribution on $H(W_i)$ is the same whether $c_i = 0$ or $c_i = 1$. Therefore, the probability that this query causes \mathcal{B} to abort is at most $1/(q_T + 1)$. Since A makes at most q_T trapdoor queries the probability that B does not abort as a result of all

trapdoor queries is at least $(1 - 1/(q_T + 1))^{q_T} \ge 1/e$. Claim 2: The probability that algorithm \mathcal{B} does not abort during the challenge phase is at least $1/q_T$. Hence, $\Pr[\mathcal{E}_2] \geq 1/q_T$.

following property: $c_0 = c_1 = 1$ where for i = 0, 1 the tuple $\langle W_i, h_i, a_i, c_i \rangle$ is the tuple on the H_1 -list corresponding to W_i . Since \mathcal{A} has not queried for the trapdoor for W_0, W_1 we have that both c_0, c_1 are independent of \mathcal{A} 's current view. Therefore, since $\Pr[c_i = 0] = 1/(q_T + 1)$ for i = 0, 1, and the two values are independent of one another, we have that $\Pr[c_0 = c_1 = 1] = (1 - 1/(q_T + 1))^2 \le 1 - 1/q_T$.

Proof. Algorithm \mathcal{B} will abort during the challenge phase if \mathcal{A} is able to produce W_0, W_1 with the

Observe that since A can never issue a trapdoor query for the challenge keywords W_0, W_1 the two events \mathcal{E}_1 and \mathcal{E}_2 are independent. Therefore, $\Pr[\mathcal{E}_1 \wedge \mathcal{E}_2] \geq 1/(eq_T)$.

Hence, the probability that \mathcal{B} does not abort is at least $1/q_T$.

To complete the proof of Theorem 3.1 it remains to show that \mathcal{B} outputs the solution to the given BDH instance with probability at least ϵ/q_{H_2} . To do we show that during the simulation \mathcal{A}

issues a query for $H_2(e(H_1(W_b), u_1^{\gamma}))$ with probability at least ϵ .

Claim 3: Suppose that in a real attack game \mathcal{A} is given the public key $[g, u_1]$ and \mathcal{A} asks to be challenged on words W_0 and W_1 . In response, \mathcal{A} is given a challenge $C = [g^r, J]$. Then, in the

real attack game \mathcal{A} issues an H_2 query for either $H_2(e(H_1(W_0), u_1^r))$ or $H_2(e(H_1(W_1), u_1^r))$ with probability at least 2ϵ .

Proof. Let \mathcal{E}_3 be the event that in the real attack \mathcal{A} does not issue a query for either one of $H_2(e(H_1(W_0), u_1^r))$ and $H_2(e(H_1(W_1), u_1^r))$. Then, when \mathcal{E}_3 occurs we know that the bit $b \in \{0, 1\}$ indicating whether C is a PEKS of W_0 or W_1 is independent of \mathcal{A} 's view. Therefore, \mathcal{A} 's output b' will satisfy b = b' with probability at most $\frac{1}{2}$. By definition of \mathcal{A} , we know that in the real attack $|\Pr[b=b']-1/2| \geq \epsilon$. We show that these two facts imply that $\Pr[\neg \mathcal{E}_3] \geq 2\epsilon$. To do so, we first derive simple upper and lower bounds on Pr[b = b']:

mple upper and lower bounds on
$$\Pr[b = b']$$
:
$$\Pr[b = b'] = \Pr[b = b'|\mathcal{E}_3] \Pr[\mathcal{E}_3] + \Pr[b = b'|\neg \mathcal{E}_3] \Pr[\neg \mathcal{E}_3]$$

$$\leq \Pr[b = b'|\mathcal{E}_3] \Pr[\mathcal{E}_3] + \Pr[\neg \mathcal{E}_3] = \frac{1}{2} \Pr[\mathcal{E}_3] + \Pr[\neg \mathcal{E}_3]$$

$$= \frac{1}{2} + \frac{1}{2} \Pr[\neg \mathcal{E}_3],$$

$$\Pr[b = b'] \ge \Pr[b = b'|\mathcal{E}_3] \Pr[\mathcal{E}_3] = \frac{1}{2} \Pr[\mathcal{E}_3] = \frac{1}{2} - \frac{1}{2} \Pr[\neg \mathcal{E}_3].$$

It follows that $\epsilon \leq |\Pr[b=b'] - 1/2| \leq \frac{1}{2} \Pr[\neg \mathcal{E}_3]$. Therefore, in the real attack, $\Pr[\neg \mathcal{E}_3] \geq 2\epsilon$ as required.

Now, assuming \mathcal{B} does not abort, we know that \mathcal{B} simulates a real attack game perfectly up to the moment when \mathcal{A} issues a query for either $H_2(e(H_1(W_0), u_1^{\gamma}))$ or $H_2(e(H_1(W_1), u_1^{\gamma}))$. Therefore, by Claim 3, by the end of the simulation \mathcal{A} will have issued a query for either $H_2(e(H_1(W_0), u_1^{\gamma}))$ or $H_2(e(H_1(W_1), u_1^{\gamma}))$ with probability at least 2ϵ . It follows that \mathcal{A} issues a query for $H_2(e(H_1(W_b), u_1^{\gamma}))$

with probability at least ϵ . Consequently, the value $e(H_1(W_b), u_1^{\gamma}) = e(g^{\beta+a_b}, g)^{\alpha\gamma}$ will appear on the left hand side of some pair in the H_2 -list. Algorithm \mathcal{B} will choose the correct pair with probability at least $1/q_{H_2}$ and therefore, assuming \mathcal{B} does not abort during the simulation, it will produce

the correct answer with probability at least ϵ/q_{H_2} . Since \mathcal{B} does not abort with probability at least $1/(eq_T)$ we see that \mathcal{B} 's success probability overall is at least $\epsilon/(eq_Tq_{H_2})$ as required.

3.2A limited construction using any trapdoor permutation

polynomial function, we will later show how to remove this additional assumption.) We will also need a family of semantically-secure encryptions where given a ciphertext it is computationally hard to say which public-key this ciphertext is associated with. This notion was formalized by Bellare et al. [1]. We say that a public-key system that has this property is source-indistinguishable. More precisely, source-indistinguishability for an encryption scheme (G, E, D) is defined using the

Our second PEKS construction is based on general trapdoor permutations, assuming that the total number of keywords that the user wishes to search for is bounded by some polynomial function in the security parameter. (As a first step in our construction, we will make an even stronger assumption that the total number of words $\Sigma \subset \{0,1\}^*$ in the dictionary is also bounded by a

and E/D are encryption/decryption algorithms). The security parameter s is given to both players. Source Indistinguishability security game:

following game between a challenger and an attacker \mathcal{A} (here G is the key generation algorithm,

- 1. The challenger runs algorithm G(s) two times to generate two public/private key pairs $(PK_0, Priv_0)$ and $(PK_1, Priv_1)$.
- 2. The challenger picks a random $M \in \{0,1\}^s$ and a random $b \in \{0,1\}$ and computes an encryption $C = PK_b(M)$. The challenger gives (M, C) to the attacker.
 - 3. The attacker outputs b' and wins the game if b = b'.

In other words, the attacker wins if he correctly guesses whether he was given the encryption of M under PK_0 or under PK_1 . We define \mathcal{A} 's advantage in winning the game as:

$$AdvSI_{\mathcal{A}}(s) = |\Pr[b = b'] - \frac{1}{2}|$$

Definition 3.2. We say that a public-key encryption scheme is source indistinguishable if for any polynomial time attacker \mathcal{A} we have that $AdvSI_{\mathcal{A}}(s)$ is a negligible function. We note that Bellare et al. [1] define a stronger notion of source indistinguishability than the

one above by allowing the adversary to choose the challenge message M. For our purposes, giving the adversary an encryption of a random message is sufficient. Source indistinguishability can be attained from any trapdoor permutation family, where for a given security parameter all permutations in the family are defined over the same domain. Such a

encrypt a bit b we pick a random x, and output $[f(x), GL(x) \oplus b]$ where GL is the Goldreich-Levin hard-core bit [19]. We therefore obtain the following lemma: **Lemma 3.3.** Given any trapdoor permutation family we can construct a semantically secure source

family can be constructed from any family of trapdoor permutations as described in [1]. Then to

indistinguishable encryption scheme. More constructions are given in [1]. We note that source indistinguishability is an orthogonal

property to semantic security. One can build a semantically secure system that is not source

indistinguishable (by embedding the public key in every ciphertext). Conversely, one can build a source indistinguishable system that is not semantically secure (by embedding the plaintext in every ciphertext). A simple PEKS from trapdoor permutations. When the keyword family Σ is of polynomial

indistinguishable public-key system (G, E, D). We let s be the security parameter for the scheme. • KeyGen: For each $W \in \Sigma$ run G(s) to generate a new public/private key pair $PK_W/Priv_W$ for the source-indistinguishable encryption scheme. The PEKS public key is

size (in the security parameter) it is easy to construct searchable encryption from any source-

• $\mathsf{PEKS}(A_{pub}, W)$: Pick a random $M \in \{0, 1\}^s$ and output $\mathsf{PEKS}(A_{pub}, W) = (M, E[PK_W, M])$, i.e. encrypt M using the public key PK_W .

 $A_{pub} = \{PK_W \mid W \in \Sigma\}.$ The private key is $A_{priv} = \{Priv_W \mid W \in \Sigma\}.$

- Trapdoor (A_{priv}, W) : The trapdoor for word W is simply $T_W = Priv_W$.
- Test (A_{pub}, S, T_W) : Test if the decryption $D[T_W, S] = 0^s$. Output 'yes' if so and 'no' otherwise.

encryption scheme (G, E, D) is source-indistinguishable.

Note that the dictionary must be of polynomial size (in s) so that the public and private keys are

of polynomial size (in s). This construction gives a semantically secure PEKS as stated in the following simple theorem.

Semantically secure PEKS is defined as in Definition 2.2 except that the adversary is not allowed to make chosen keyword queries.

Theorem 3.4. The PEKS scheme above is semantically secure assuming the underlying public key

Proof sketch: Let $\Sigma = \{W_1, \dots, W_k\}$ be the keyword dictionary. Suppose we have a PEKS attacker \mathcal{A} for which $\mathrm{Adv}_{\mathcal{A}}(s) > \epsilon(s)$. We build an attacker \mathcal{B} that breaks the source indistin-

guishability of (G, E, D) where $AdvSI_{\mathcal{B}}(s) > \epsilon(s)/k^2$.

The reduction is immediate: \mathcal{B} is given two public keys PK_0 , PK_1 and a pair (M, C) where M is random in $\{0,1\}^s$ and $C = PK_b(M)$ for $b \in \{0,1\}$. Algorithm \mathcal{B} generates k-2 additional public/private keys using G(s). It creates A_{pub} as a list of all k public keys with PK_0, PK_1

embedded in a random location in the list. Let W_i, W_j be the words associated with the public

keys PK_0 , PK_1 . \mathcal{B} sends A_{pub} to \mathcal{A} who then responds with two words W_k , $W_\ell \in \Sigma$ on which \mathcal{A} wishes to be challenged. If $\{i,j\} \neq \{k,\ell\}$ algorithm \mathcal{B} reports failure and aborts. Otherwise, \mathcal{B} in the work of Dodis et al. [13]. They propose reducing the size of the public-key using cover-free set systems. We apply the same idea below to reduce the size of the public key in the PEKS above.

Reducing the public key size. The drawback of the above scheme is that the public key length grows linearly with the total dictionary size. If we have an upper-bound on the total number of keyword trapdoors that the user will release to the email gateway (though we do not need to know these keywords a priori) we can do much better using cover free families [15] and can allow keyword.

sends the challenge (M, C) to \mathcal{A} who then responds with a $b' \in \{0, 1\}$. Algorithm \mathcal{B} outputs b' as its response to the source indistinguishability challenge. We have that b = b' if algorithm \mathcal{B} did not abort and \mathcal{A} 's response was correct. This happens with probability at least $\frac{1}{2} + \epsilon/k^2$. Hence,

We note that this PEKS can be viewed as derived from an IBE system with a limited number of identities. For each identity there is a pre-specified public key. Such an IBE system is implied

 $AdvSI_{\mathcal{B}}(s) > \epsilon(s)/k^2$ as required.

The PEKS(d, t, k, q) construction is as follows:

keyword trapdoors that the user will release to the email gateway (though we do not need to know these keywords a-priori) we can do much better using cover-free families [15] and can allow keyword dictionary to be of exponential size. Since typically a user will only allow a third party (such as e-mail server) to search for a limited number of keywords so that assuming an upper bound on the number of released trapdoors is within reason. We begin by recalling the definition of cover-free families.

Definition 3.5. Cover-free families. Let d, t, k be positive integers, let G be a ground set of size d, and let $F = \{S_1, \ldots, S_k\}$ be a family of subsets of G. We say that subset S_i does not cover S_i if

it holds that $S_i \not\subseteq S_j$. We say that family F is t-cover free over G if each subset in F is not covered by the union of t subsets in F. Moreover, we say that a family of subsets is q-uniform if all subsets in the family have size q.

We will use the following fact from [14].

Lemma 3.6. [14] There exists a deterministic algorithm that, for any fixed t, k, constructs a q-uniform t-cover free family F over a ground set of size d, for $q = \lceil d/4t \rceil$ and $d \leq 16t^2(1 + \log(k/2)/\log 3)$.

The PEKS. Given the previous PEKS construction as a starting point, we can significantly reduce

the size of public file A_{pub} by allowing user to re-use individual public keys for different keywords. We associate to each keyword a subset of public keys chosen from a cover free family. Let k be the size of the dictionary $\Sigma = \{W_1, \ldots, W_k\}$ and let t be an upper bound on the number of keyword trapdoors released to the mail gateway by user Alice. Let d, q satisfy the bounds of Lemma 3.6.

- KeyGen: For $i=1,\ldots,d$ run algorithm G(s) to generate a new public/private key pair $PK_i/Priv_i$ for the source-indistinguishable encryption scheme. The PEKS public key is $A_{pub} = \{PK_1,\ldots,PK_d\}$. The private key is $A_{priv} = \{Priv_1,\ldots,Priv_d\}$. We will be using a q-uniform
 - t-cover free family of subsets $F = \{S_1, \ldots, S_k\}$ of $\{PK_1, \ldots, PK_d\}$. Hence, each S_i is a subset of public keys. • PEKS (A_{pub}, W_i) : Let $S_i \in F$ be the subset associated with the word $W_i \in \Sigma$. Let $S_i = \{S_i, \ldots, S_k\}$

 $\{PK^{(1)},\ldots,PK^{(q)}\}$. Pick random messages $M_1,\ldots,M_q\in\{0,1\}^s$ and let $M=M_1\oplus\cdots\oplus M_q$.

Output the tuple:
$$\mathsf{PEKS}(A_{pub}, W_i) = \left(M, \ E[PK^{(1)}, M_1], \ \dots, \ E[PK^{(q)}, M_q]\right)$$

• Trapdoor (A_{priv}, W_i) : Let $S_i \in F$ be the subset associated with word $W_i \in \Sigma$. The trapdoor for word W_i is simply the set of private keys that correspond to the public keys in the set S_i .

• Test (A_{pub}, R, T_W) : Let $T_W = \{Priv^{(1)}, \dots, Priv^{(q)}\}$ and let $R = (M, C_1, \dots, C_q)$ be a PEKS. For $i = 1, \dots, q$ decrypt each C_i using private key $Priv^{(i)}$ to obtain M_i . Output 'yes' if $M = M_1 \oplus \cdots \oplus M_q$,

and output 'no' otherwise.

The size of the public key file A_{pub} is much smaller now: logarithmic in the size of the dictionary. The downside is that Alice can only release t keywords to the email gateway. Once t trapdoors

are released privacy is no longer guaranteed. Also, notice that the size of the PEKS is larger now (logarithmic in the dictionary size and linear in t). The following corollary of Theorem 3.4 shows

that the resulting PEKS is secure. **Corollary 3.7.** Let d, t, k, q satisfy the bounds of Lemma 3.6. The PEKS(d, t, k, q) scheme above is semantically secure under a chosen keyword attack assuming the underlying public key encryption scheme (G, E, D) is source-indistinguishable and semantically secure, and that the adversary makes

no more than t trapdoors queries. **Proof sketch:** Let $\Sigma = \{W_1, \dots, W_k\}$ be the keyword dictionary. Suppose we have a PEKS attacker \mathcal{A} for which $Adv_{\mathcal{A}}(s) > \epsilon(s)$. We build an attacker \mathcal{B} that breaks the source indistin-

guishability of (G, E, D). Algorithm \mathcal{B} is given two public keys PK_0 , PK_1 and a pair (M,C) where M is random in $\{0,1\}^s$ and $C = PK_b(M)$ for $b \in \{0,1\}$. Its goal is to output a guess for b which it does by interacting with \mathcal{A} . Algorithm \mathcal{B} generates d-2 additional public/private keys using G(s). It creates A_{pub} as

a list of all d public keys with PK_0, PK_1 embedded in a random location in the list. Let W_i, W_j

be the words associated with the public keys PK_0 , PK_1 . \mathcal{B} sends A_{pub} to \mathcal{A} . Algorithm \mathcal{A} issues up to t trapdoor queries. \mathcal{B} responds to a trapdoor query for $W \in \Sigma$ as follows: let $S \in F$ be the subset corresponding to the word W. If $PK_0 \in S$ or $PK_1 \in S$ algorithm \mathcal{B} reports failure and aborts. Otherwise, \mathcal{B} gives \mathcal{A} the set of private keys

 $\{Priv_i \mid i \in S\}.$ At some point, Algorithm \mathcal{A} outputs two words $W'_0, W'_1 \in \Sigma$ on which it wishes to be challenged.

Let $S'_0, S'_1 \in F$ be the subsets corresponding to W'_0, W'_1 respectively. Let \mathcal{E} be the event that $PK_0 \in S_0'$ and $PK_1 \in S_1'$. If event \mathcal{E} did not happen then \mathcal{B} reports failure and aborts.

We now know that $PK_0 \in S_0'$ and $PK_1 \in S_1'$. For j = 0, 1 let $S_j' = \{PK_j^{(1)}, \dots, PK_j^{(q)}\}$. We

arrange things so that $PK_0 = PK_0^{(c)}$ and $PK_1 = PK_1^{(c)}$ for some random $1 \le c \le q$. Next, \mathcal{B} picks random $M_1, \ldots, M_{c-1}, M_{c+1}, \ldots, M_q \in \{0,1\}^s$ and sets $M_c = M$. Let $M' = M_1 \oplus \cdots \oplus M_q$.

Algorithm \mathcal{B} defines the following hybrid tuple: $R = \left(M', E[PK_0^{(1)}, M_1], \dots, E[PK_0^{(c-1)}, M_{c-1}], C, \right)$

$$E[PK_1^{(c+1)}, M_{c+1}], \ldots, E[PK_1^{(q)}, M_q]$$

It gives R as the challenge PEKS to algorithm \mathcal{A} . Algorithm \mathcal{A} eventually responds with some $b' \in \{0,1\}$ indicating whether R is $\mathsf{PEKS}(A_{pub}, W'_0)$ or $\mathsf{PEKS}(A_{pub}, W'_1)$. Algorithm \mathcal{B} outputs b'as its guess for b. One can show using a standard hybrid argument that if \mathcal{B} does not abort then

 $|\Pr[b=b']-\frac{1}{2}|>\epsilon/q^2$. The probability that \mathcal{B} does not abort at a result of a trapdoor query is at least 1-(tq/d). The probability that \mathcal{B} does not abort as a result of the choice of words W_0', W_1'

is at least $(q/d)^2$. Hence, \mathcal{B} does not abort with probability at least 1/poly(t,q,d). Repeatedly running \mathcal{B} until it does not abort shows that we can get advantage ϵ/q^2 in breaking the source indistinguishability of (G, E, D) in expected polynomial time in the running time of A.

4 Construction using Jacobi symbols

of distinguishing quadratic residues from non-residues modulo N=pq where $p=q=3 \pmod 4$. Unfortunately, Galbraith [11] shows that the Cocks system as described in [3] is not public-key private in the sense of Bellare et al. [1]. Therefore it appears that the Cocks system cannot be directly used to construct a PEKS. It provides a good example that constructing a PEKS is a harder problem than constructing an IBE.

Given the relation between Identity Based Encryption and PEKS it is tempting to construct a PEKS from an IBE system due to Cocks [3]. The security of Cocks' IBE system is based on the difficulty

We briefly explain why the basic Cocks system is not public key private. Let $N \in \mathbb{Z}$ be a product of two primes. For a public key $x \in \mathbb{Z}_N$ and a bit $b \in \{0,1\}$ define $P_{x,b}$ to be the set

$$P_{x,b} = \{ r + \frac{x}{r} \mid r \in \mathbb{Z}_N \text{ and } (r/N) = (-1)^b \} \subseteq \mathbb{Z}_N$$

where (r/N) denotes the Jacobi symbol of r over N. Fix some $b \in \{0, 1\}$. To show that the system is not public key private it suffices to show an algorithm that given two distinct public keys x and y in \mathbb{Z}_N can distinguish the uniform distribution on $P_{x,b}$ from the uniform distribution on $P_{y,b}$. The algorithm works as follows (it is given as input $x, y \in \mathbb{Z}_N$ and $z \in \mathbb{Z}_N$ where z is either sampled from $P_{x,b}$ or from $P_{y,b}$):

- 1. Compute $t = z^2 4x \in \mathbb{Z}_N$.
- 2. If the Jacobi symbol (t/N) = 1 output " $z \in P_{x,b}$ ". Otherwise output " $z \in P_{y,b}$ ".

When z is sampled from $P_{x,b}$ then $t = z^2 - 4x = (r - (x/r))^2$ and hence t will always have Jacobi symbol 1 over N. When z is sampled from $P_{y,b}$ then we expect t to have Jacobi symbol 1 over N with probability about 1/2. Therefore, the algorithm has advantage 1/2 in correctly identifying where z is sampled from. Since a Cocks ciphertext contains many such samples, the algorithm above determines whether a ciphertext is encrypted under the public key x or the public key y with overwhelming probability. Note there is no need to know the plaintext b.

5 Conclusions

We defined the concept of a public key encryption with keyword search (PEKS) and gave two constructions. Constructing a PEKS is related to Identity Based Encryption (IBE), though PEKS seems to be harder to construct. We showed that PEKS implies Identity Based Encryption, but the converse is currently an open problem. Our constructions for PEKS are based on recent IBE

constructions. We are able to prove security by exploiting extra properties of these schemes.

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