

Improving Deconvolution Methods in Biology through Open Innovation Competitions: an Application to the Connectivity Map

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Abstract

Report results fo open innovation competition aimed at solving a gene-related deconvolution problem.

Keywords: biology; open innoation competitions; crowdsourcing; deconvolution; gene expressions; cell lines.

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TODOS:

- Check length requirements for Nat. Met.
- Intro [AB]
- Methods TN [DONE]
- Clustering
- Add disaggregated data

A Brief Communication is a more concise format used typically to report a significant improvement to a tried-and-tested method, its modification and adaptation to an important original application, or an important new tool or resource of broad interest for the scientific community. This format typically does not exceed 3 printed pages. Brief Communications begin with a brief unreferenced abstract (3 sentences, no more than 70 words), which will appear on Medline. The title is limited to 10 words (or 90 characters). The main text is typically 1,000-1,500 words, including the abstract and contains no headings with the exception of a single heading for Methods to point readers to the online Methods section providing all technical details necessary for the independent reproduction of the methodology. Brief Communications normally have no more than 2 display items, although this may be flexible at the discretion of the editor, provided the page limit is observed. As a guideline, Brief Communications allow up to 20 references, and article titles are omitted from the reference list.

Brief Communications include received/accepted dates. They may be accompanied by supplementary information. Brief Communications are peer reviewed.

1 Introduction

Multianalyte methods for high-throughput gene-expression profiling have found widespread application in biology. The extent of these applications, however, tend to be limited by the type and number of available analytes, which typically results in prohibitive costs for big data generation. Using an assay called L1000 that measures the mRNA transcript abundance of 978 “landmark” genes from human cells, the Connectivity Map (CMap) group at the Broad Institute has developed a novel approach that matches pairs of genes to the same analyte type, or bead, to double the count of profiled genes, thus lowering greatly costs [1].

A central component of this approach is to statistically deconvolve and compare gene type-specific expression profiles for sets of two genes in mixed-gene samples. Similar deconvolution problems are ubiquitous in biology and several solutions have been proposed in a variety of different contexts. Examples include algorithms to identify cell type-specific gene expression differences in complex tissues [2] or dynamic changes in cell populations [3], or ways to discover the target proteins of small molecules [Jung, 2015].

CMap’s current deconvolution algorithm (called D-Peak) is based on the k-means clustering algorithm, which automatically partitions a set of gene-expression measurements into k clusters by minimizing the within-cluster sum of squares, and then assigns the two largest clusters to each gene type within each matched pair of genes.

The current k-means approach works well in practice but has several limitations as well. It tends to split clusters incorrectly when data are not reasonably well separated, it is sensitive to outliers, and it is computationally demanding (an efficient k-means algorithm, such as Lloyd’s, has a running time that scales as $O(kn)$ where n is the number of observations and k the number of clusters).

As a research tool to test for alternative solutions, we used an open innovation competition [4, 5]. In this paper, we report the outcomes of the competition, which successfully engaged a variety of computer scientist, software developers and bioinformatics in the problem, resulting in a cost-effective exploration of competing approaches (random forest, gaussian mixture models, and convolutional nets) that would have been otherwise prohibitive.

2 Methods

Towards developing an open innovation competition, we first transformed the deconvolution problem into a supervised classification task. Using the L1000 assay, we profiled six 384-well plates, each containing different sets of compound and shRNA treatments (see Supporting Info, 7.1). We did it twice by varying the detection mode used for acquiring the data between two methods. The first method, called UNI, associates each gene to one single analyte color, which leads to higher costs, but it does not require deconvolution. The second method, called DUO, associates sets of two genes per analyte color, which reduces costs but requires deconvolution to transform the composite gene-expression signal into two separate gene-specific expression values. We then used the data obtained from the UNI method (one gene per analyte type) as the “ground truth” for the competition; and the data obtained from the DUO method (two genes per analyte type) as the input to predict the equivalent UNI data. The datasets are now publicly available [LINK to REPO].

We randomly split the generated data into training, testing, and holdout datasets of equal size (2 plates each). All the contestants had access to the training data to develop and validate their solutions offline. The testing data were used to evaluate solutions during the contest and populate the live leaderboard. Holdout data were used to evaluate competitors’ final submissions and guard against over-fitting. Prizes were awarded based on performance on the holdout dataset.

To evaluate submissions, we developed a scoring function that combines standard measures of accuracy based on the distance (e.g., correlation) between the predicted values and the ground truth, as well as computational speed (see Supporting Info, 7.3).

The competition run on the platform Topcoder (Wipro, India) for 10 days. A total of \$23,000 in cash prizes was offered to competitors as incentive to be divided among the top 9 submissions (prize

split: \$8000, \$6000, \$4000, \$2000, \$1000, \$800, \$600, \$400, \$100).

3 Results

3.1 Participation

The contest attracted 294 participants, who made 820 code submissions with an average of about 18 submissions per participant. The top finishers in the contest employed a variety of different analysis approaches, including decision tree regressors (DTR), Gaussian mixture models (GMM), convolutional neural networks (CNN), and customized versions of k-means, all with notably improved performance relative to the benchmark. Table 1 lists the top 9 finishers and the languages and algorithms each used.

Table 1: Summary of contestant solutions

rank	handle	language	method	category
1	garden999	Java	random forest regressor	DTR
2	Ardavel	C++	Gaussian mixture model	GMM
3	mkagenius	C++	modified k-means	k-means
4	Ramzes2	Python/C++	ConvNet	CNN
5	vladaburian	Python/C++	Gaussian mixture model	GMM
6	balajipro	Python/C++	modified k-means	k-means
7	AliGebily	Python	boosted tree regressor	DTR
8	LastEmperor	Python	modified k-means	k-means
9	mvaudel	Java	other	other

3.2 Overall accuracy and speed

We tested the accuracy and speed of the competitors’ solutions on the holdout L1000 data obtained by applying the DUO detection method (two genes per analyte color) and utilizing as the ground truth the data obtained by employing the UNI detection method (one gene per analyte color).

Correlation. We computed the gene-level rank correlation with the ground truth for each of the top nine algorithms and the benchmark. Overall, the correlation with the ground truth was high for all the solutions ($\rho > 0.56$). All the competitors had a distribution of the genewise rank correlation that was right-shifted compared to the k-means benchmark, indicating more accurate predictions (Fig.

2). Indeed, the median rank correlation of the competitors that was significantly higher than the equivalent for the benchmark, although the size of the observed improvements was modest (2-3 percentage points).

Extreme modulations. Of particular interest was to test the accuracy of the competitors' solutions on the differential expression (DE) values, which are obtained by applying a series of transformations to the data after the deconvolution [see 1, for the details]. We focused on the improvements in the detection of, so called, "extreme modulations." These are genes that notably up- or down-regulated by perturbation and hence exhibit an exceedingly high (or low) DE values relative to a set threshold. Using the Area under the ROC (using UNI detections of extremely modulated genes as the ground-truth), we found that all the competitors achieved a good detection performance (AUC = xxx); and, also in this case, we observe improvements, although modest, from all the competitors' solutions (between xxx and xxx percent). [ADD AND DISCUSS FIGURE / how about moving TSNE results here – just as a robustness check that no obvious clustering occurs at differential expression level – meaning quality is ok – ?]

Gene knockdowns. We further tested differences in the probability of detection of the extreme modulations for knockdown genes (explain). For this comparison, we computed the metric also for the UNI data, and compared performance of... We observe a high performance in accuracy. xxx we computed the KD success frequency for each algorithm and the benchmark. This metric is the fraction of the 376 landmark-targeting shRNA experiments in the holdout data for which the predictions met these success criteria. We used the UNI ground-truth data to estimate the maximum achievable KD success frequency, which in this case was 0.8. We observe that all but 2 of the top 9 contestant algorithms achieve a higher KD success frequency than the benchmark solution (Fig. ??). These results suggest that the algorithm improvements, as assessed by the accuracy metrics used in the contest, translate to improvements in biologically relevant metrics used in common applications of L1000 data.

Inter-replicate variance. Agreement between experimental replicates is crucial xxx [ref] "The inter-replicate variation of gene expression-quantities is of the utmost importance to biologists because lower variance means higher reproducibility." [refXXX]. Our data contain several replicates which enabled us to study improvements in inter-replicability variance. See figure Fig. 3.

Speed. Speed improvements over the benchmark were substantial (Fig. ??). The benchmark took about 4 minutes per plates. In contrast, the fastest algorithm took as little as 4 seconds per plate (a 60x speedup compared to the benchmark), and the slowest was well below one minute per plate. We observed no particular trade-off between speed and accuracy. The fastest algorithm ("ardavel"), that was based a gaussian mixture model, achieved a good level of accuracy as well, and ranked second overall. On the other hand, the algorithm with the best performance in terms of accuracy ("gardn999"), which was based on a decision tree regression, also achieved a decent speed performance compared to the benchmark. Thus, at least within the context of the implemented solutions, we found a negligible trade-off between speed and accuracy.

3.2.1 Reduction variation across replicate samples

One of the issues with the benchmark k-means solution is that it does little to mitigate the discrepancy in prediction accuracy between the genes measured with high and low bead proportions.

Todos: - boxplots of replicate variance, stratified by algo and hi/lo bead - barplot of average variance per algo, showing that winning algo has lowest variance and discrepancy b/w hi/lo bead is minimized

3.3 Clustering submissions

3.3.1 2D projection

Given the variety of methods represented amongst the prize-winning solutions, we sought to assess whether there were notable differences in the predictions generated. Using the holdout dataset, we generated a two-dimensional projection of the *UNI* ground truth data and *DUO*-derived benchmark and constant predictions for both *DECONV* and *DE* data using t-distributed stochastic neighbor embedding (t-SNE, van der Maaten et al [ref]). Each point represents a single ground truth or predicted sample.

We observe that in *DECONV* data the samples primarily cluster by pertubagen type, with the exception of the ground truth *UNI* data, which appears distinct from the deconvoluted samples (Fig. ?? A and B). Separating the samples by algorithm reveals commonalities in the predictions generated by similar algorithms (Fig. ?? C). For example, the decision tree regressor (DTR) algorithms have similar ‘footprints’ in the projection, as do the k-means and Gaussian mixture model (GMM) algorithms. This suggests that in general similar algorithms generate predictions with similar properties.

After the standard transformation to *DE* data we observe that the t-SNE projection is much more homogenous, indicating that pertubagen type and algorithm-specific affects have been greatly reduced (Fig. ?? D). This is reassuring, given that in production mode downstream analysis of this data will be based on *DE*. It also suggests that integrating multiple deconvolution algorithms into an ensemble method might be feasible.

3.3.2 Clustering by gene-Level performance

We observed that the global structure of *DE* data seemed independent of algorithm type in general. We additionally sought to understand whether there were differences between the algorithms at the individual gene level. To assess this, we identified the best performing algorithm (by correlation metric) for each of the 976 landmark genes. We observe that while the contest winner is the best performer for the majority of genes, over 70% of the genes achieve better correlation with a different

algorithm, and all but 2 algorithms are the best performers for at least 5% of the genes. This suggests that there may be complementarity between the algorithms, which could potentially be leveraged by an ensemble approach.

3.4 Ensemble approaches

Figure 3. (A) Scatterplot runtime vs accuracy for ensemble (slides p. 163)

Speed vs accuracy trade-off. Integration one or multiple methods?

3.5 Minors:

- signs of overfitting (compare training vs testing)

4 Discussion

Summary of the results presented in the methods section.

Discussion generality of the solutions

- Novel? Have any of these solutions previously been applied to deconvolution problems?
- Specific to this problem or general to others?

Discuss implications of these methods for CMap production

- Preliminary results on past data conversion
- Directions for pipeline integration and generation of future data
- Cost savings
- Implementation strategy and outcomes
- Increase in data processing throughput

5 Figures

5.1 Scoring accuracy

5.2 Accuracy vs. Speed

Median difference

reading data/UNI_DUO_gene_spearman_correlations_holdout_n20x976.gctx

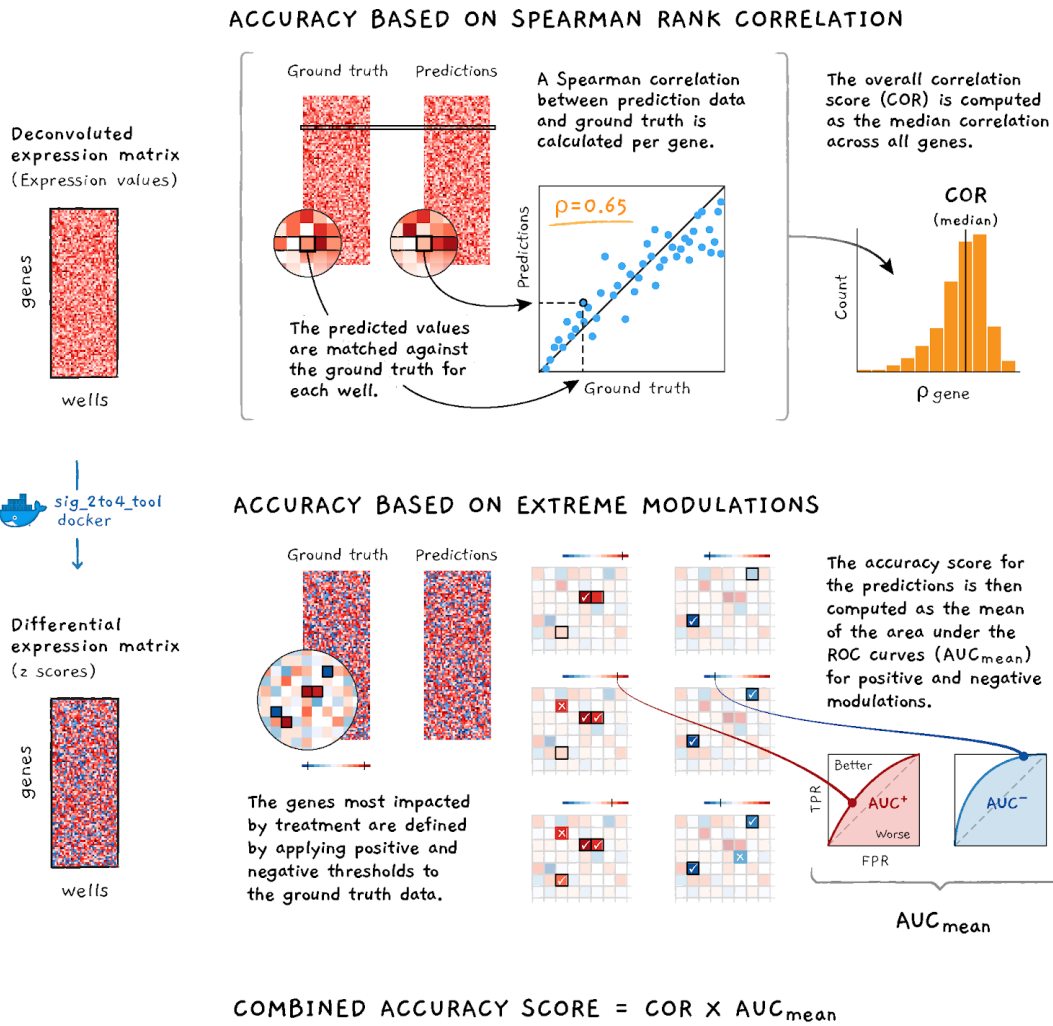


Figure 1: **Schematic illustrating accuracy components of scoring function.** The accuracy component is computed as the product of gene-wise Spearman correlations with ground truth and the area under the curve AUC of extreme modulations.

```
## done
```

5.3 Inter-replicate variance

5.4 Variance by experiments

6 Runtime and speedups

6.1 Accuracy

6.2 Gene knockdowns

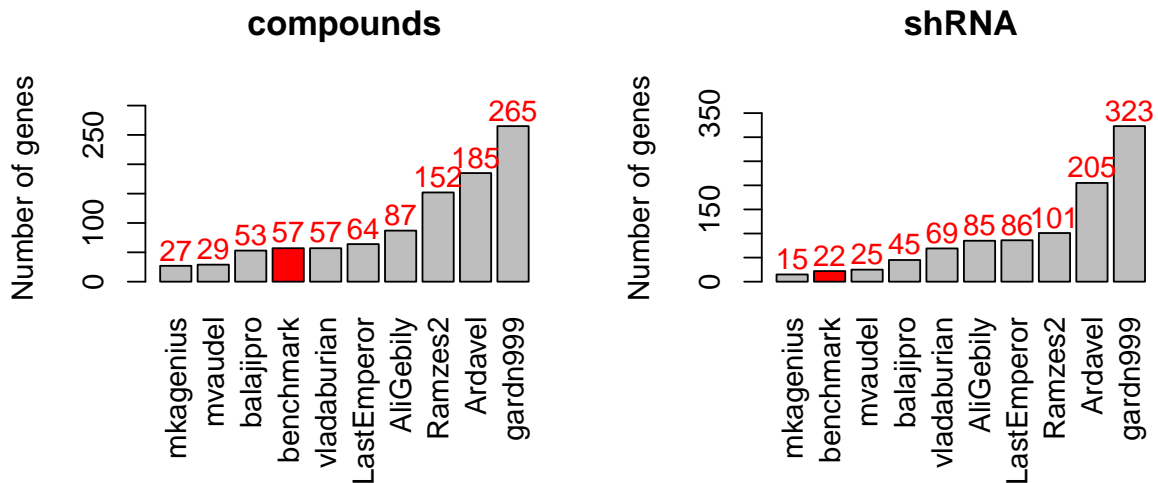
6.3 High / Low bead discrepancy

6.4 Clustering of solutions

6.5 Complementarity

```
## reading data/UNI_DVO_gene_spearman_correlations_holdout_n20x976.gctx
```

```
## done
```



TODO: barplot of # of genes for which each algo. gives best prediction - possible group by plate/low vs. high

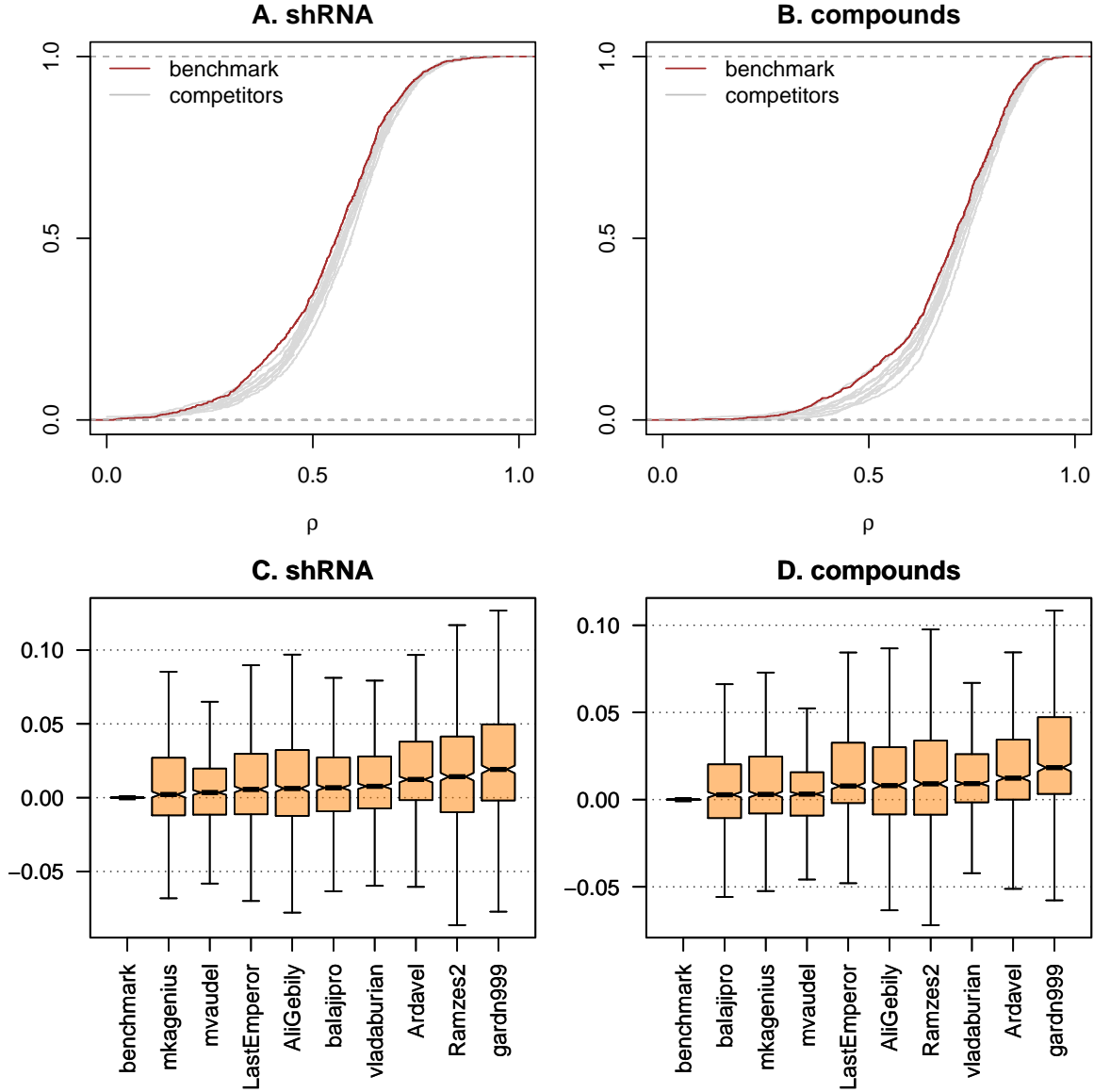


Figure 2: Accuracy. Top panels show empirical CDF of the distribution of the genewise spearman correlation (ρ) between the ground-truth gene-expressions (as detected by UNI) and predictions obtained by the competitors and the benchmark through the deconvolution of DUO data, for the subset of the shRNA (A.) and compounds experiments (B.). The competitors' eCDFs are right-shifted compared to the benchmark, indicating more accurate predictions. Bottom panels show box plots of the distribution of the genewise difference in spearman correlation of the gene-expression values obtained by the competitors and the benchmark through the deconvolution of DUO data (outliers excluded), for the shRNA experiments (C.) and the compound experiments (D.). Results show the median size of the accuracy improvements was modest, ranging between 2 and 3 percentage points.

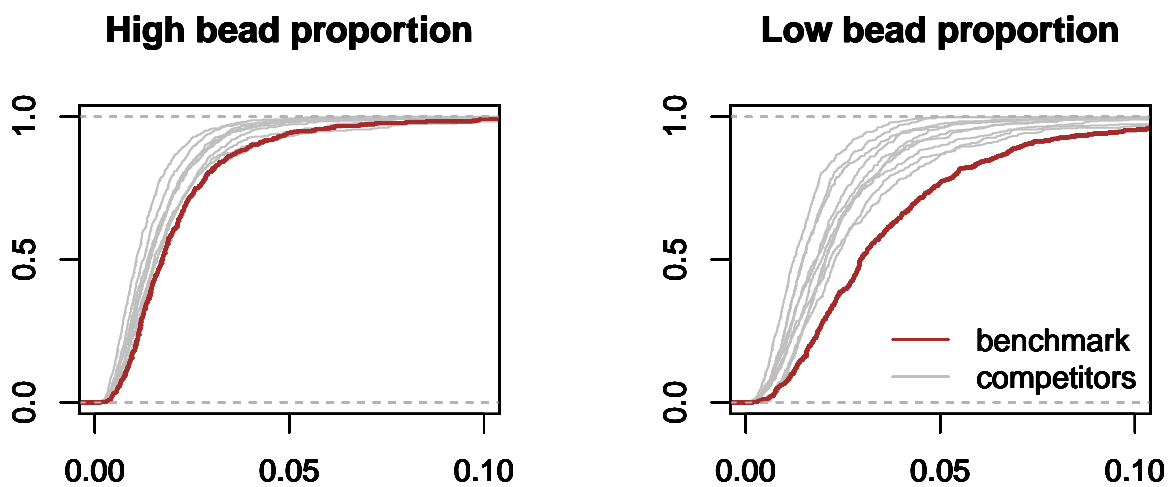


Figure 3: Inter-replicate variance.

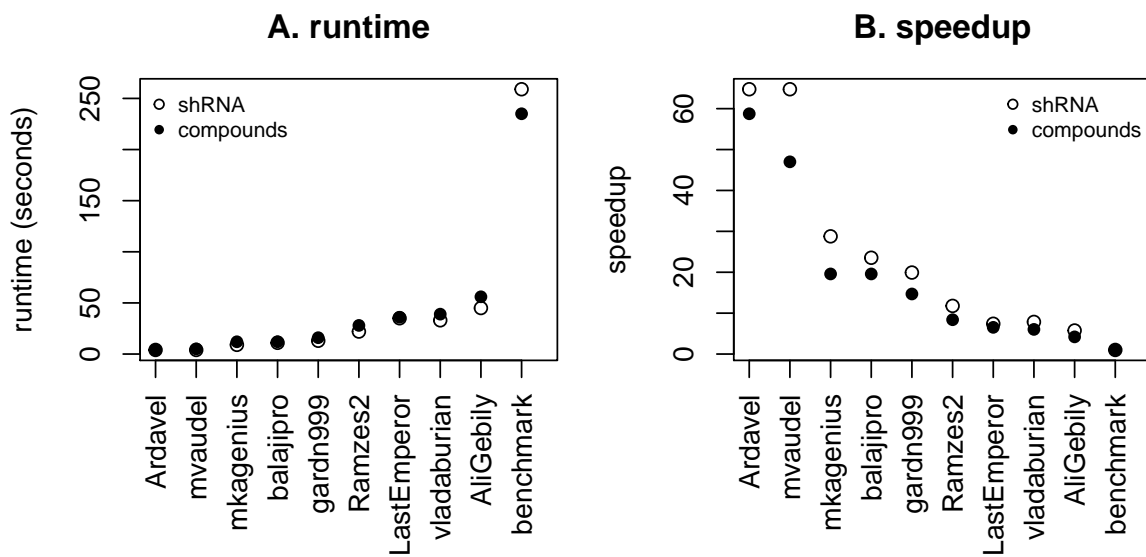


Figure 4: **Speed improvements.** Distribution of the per-plate runtime (in seconds) and speedups over the benchmark ($t_{\text{benchmark}}/t_{\text{competitor}}$) for each of the competitors' algorithms

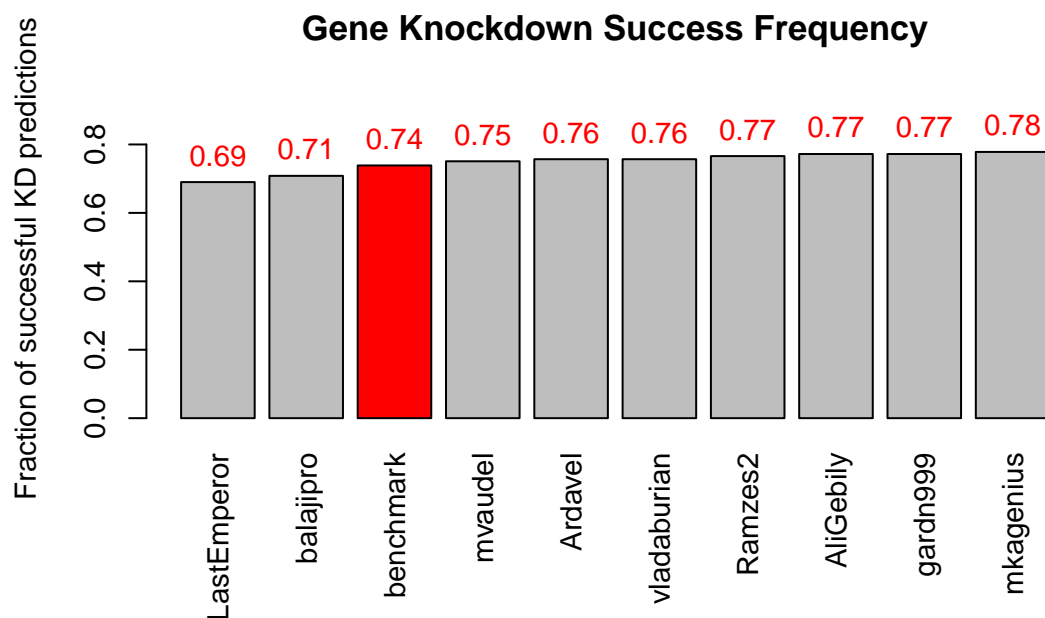
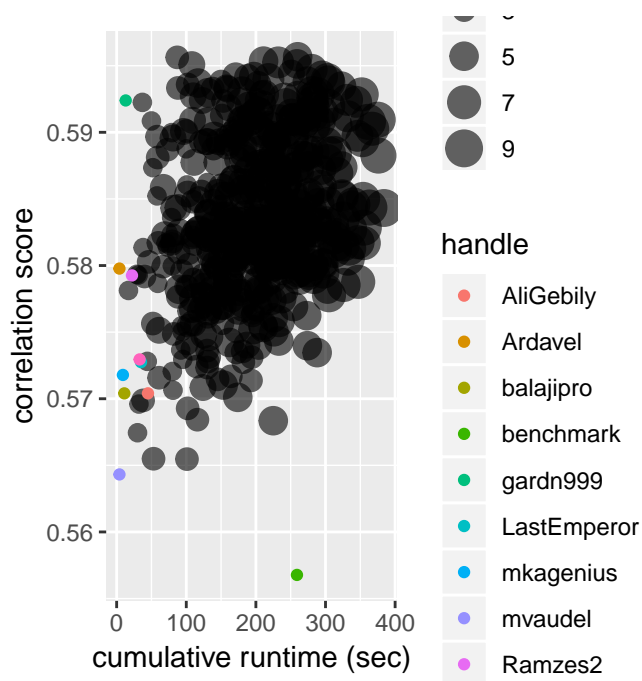


Figure 5: **KD success frequency.** Bars represent the fraction of landmark-targeting shRNAs experiments in which the DE values indicated successful knockdown (KD). Success criteria are a z-score of less than -2 and a gene-wise rank of less than 10. Results are shown for the one plate of shRNA holdout data, containing 376 landmark-targeting shRNA experiments.

6.6 Ensemble



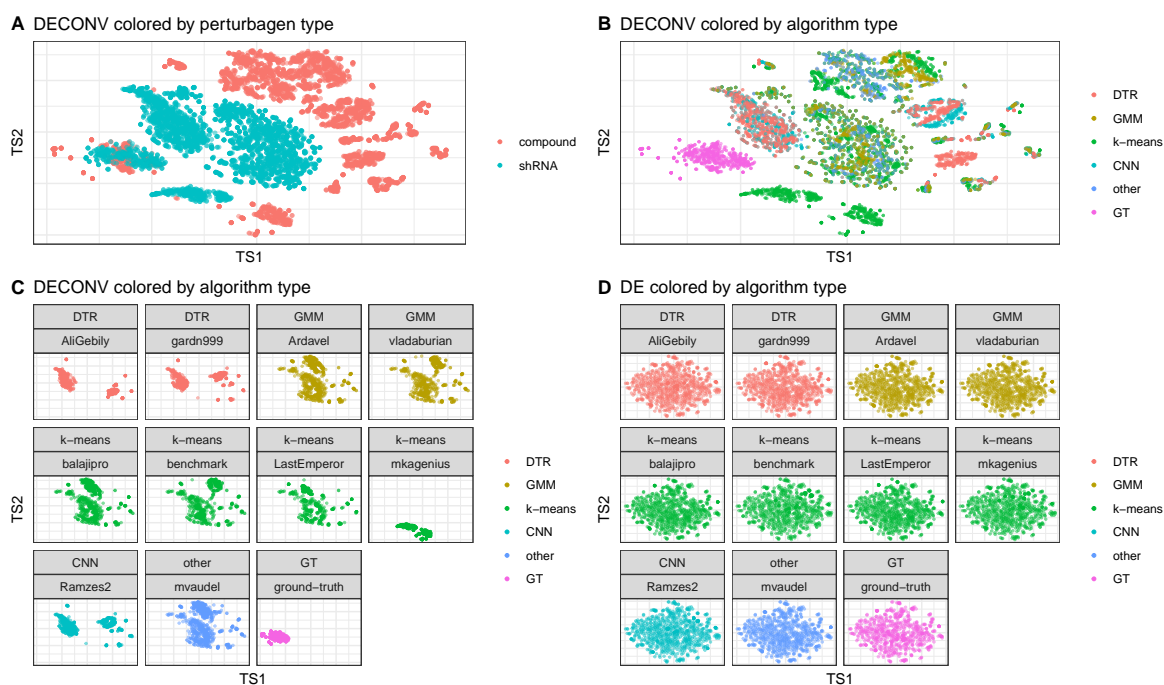
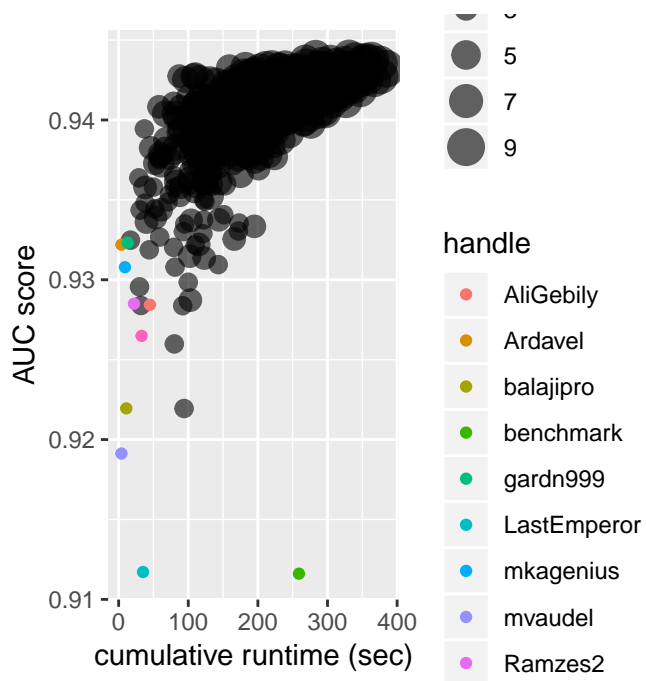
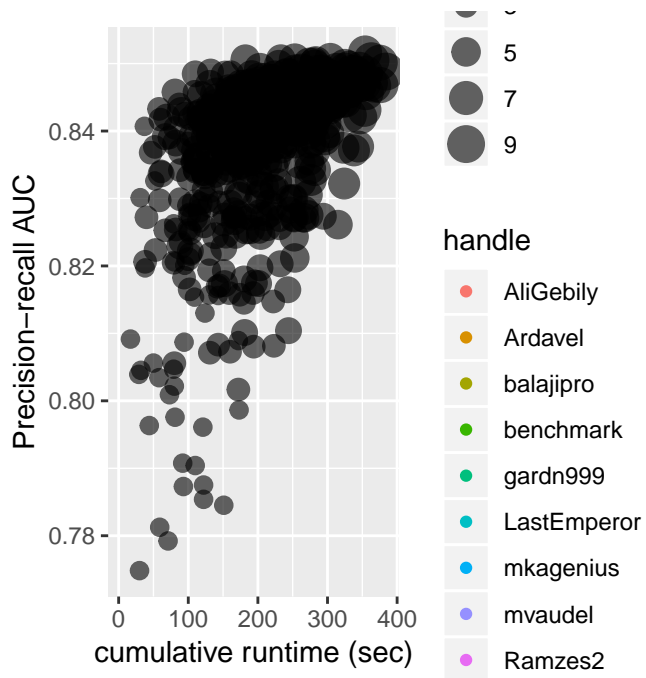


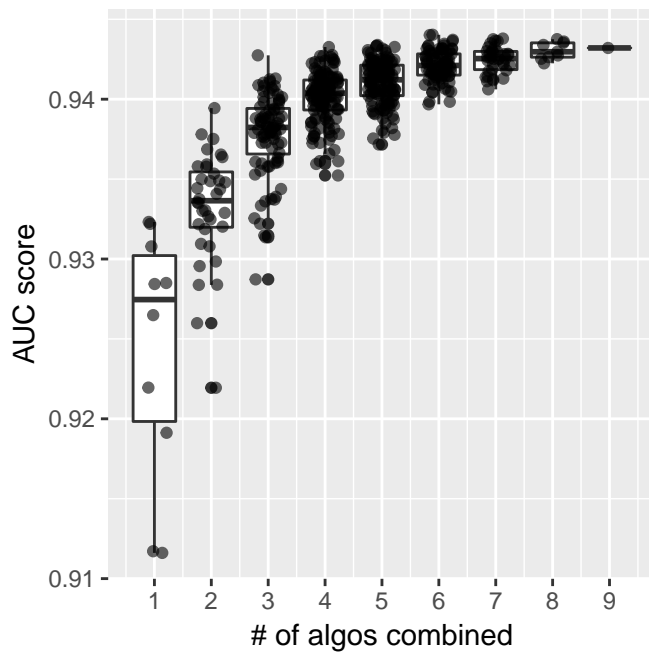
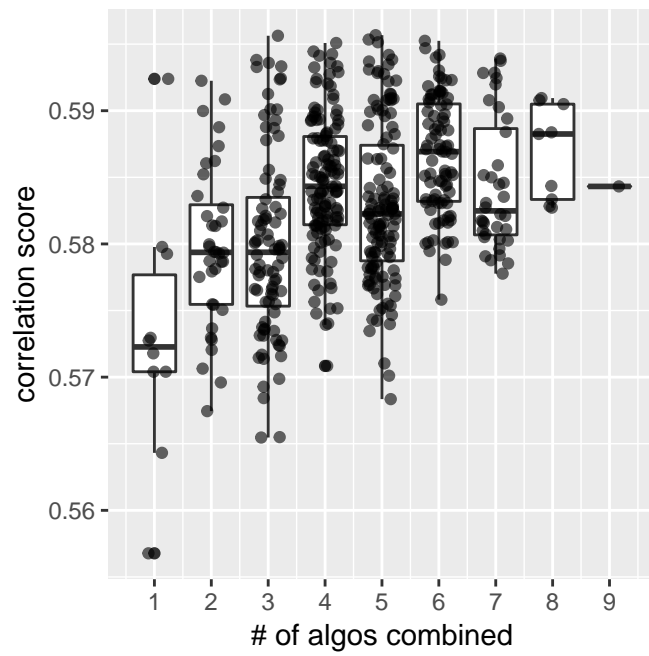
Figure 6: t-SNE projection of deconvoluted data. Each point represents the 2D projection of a sample generated by UNI ground truth (GT) or by applying a deconvolution algorithm to DUO data. t-SNE was run on the 2 plates of holdout data, one each containing compound and shRNA treatments. DECONV data colored by perturbagen type (A) and algorithm type (B). DECONV (C) and DE (D) data colored by algorithm type and stratified by each individual implementation.



Warning: Removed 10 rows containing missing values (geom_point).

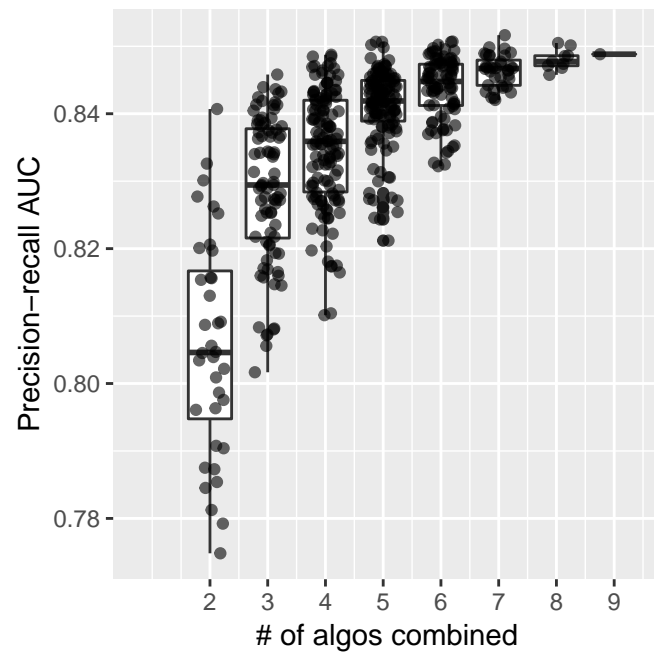
Warning: Removed 10 rows containing missing values (geom_point).





Warning: Removed 10 rows containing non-finite values (stat_boxplot).

Warning: Removed 10 rows containing missing values (geom_point).



7 Supporting information

TODO: update equations to use Latex

7.1 Data generation for contest

To generate data for this contest, we profiled six 384-well perturbagen plates, each containing mutually exclusive sets of compound and shRNA treatments. Multiple treatment types were used to avoid potentially over-fitting to any one. The compound and shRNA perturbagen plates were arbitrarily grouped into pairs, and to avoid any potential ‘information leakage’ each pair was profiled in a different cell line. The resulting lysates were amplified by ligation mediated amplification (LMA, Subramanian 2017). The amplicon was then split and detected in both *UNI* and *DUO* detection modes. The three pairs of data were arbitrarily assigned to training, testing, and holdout categories, where in each case the *UNI* data served as the ground truth. Training data were made available for all the contestants to develop and validate their solutions offline. The testing data were used to evaluate solutions during the contest and populate the live leaderboard. Holdout data were used to evaluate competitors’ final submissions and guard against over-fitting. Prizes were awarded based on performance on the holdout dataset.

Table 2: Data generated

Category	Type
training	Compounds
testing	Compounds
holdout	Compounds
training	shRNA
testing	shRNA
holdout	shRNA

7.2 L1000 Experimental Scheme

The L1000 assay uses Luminex bead-based fluorescent scanners to detect gene expression changes resulting from treating cultured human cells with chemical or genetic perturbations [Subramanian 2017]. Experiments are performed in 384-well plate format, where each well contains an independent sample. The Luminex scanner is able to distinguish between 500 different bead types, or colors, which CMap uses to measure the expression levels of 978 landmark genes using two detection approaches.

In the first detection mode, called *UNI*, each of the 978 landmark genes is measured individually on one of the 500 Luminex bead colors. In order to capture all 978 genes, two detection plates are used, each measuring 489 landmarks. The two detection plates' worth of data are then computationally combined to reconstruct the full 978-gene expression profile for each sample.

By contrast, in the *DUO* detection scheme two genes are measured using the same bead color. Each bead color produces an intensity histogram which characterizes the expression of the two distinct genes. In the ideal case, each histogram consists of two peaks each corresponding to a single gene. The genes are mixed in 2:1 ratio, thus the areas under the peaks have 2:1 ratio (see Figure 1), which enables the association of each peak with the specific gene. **The practical advantage of the DUO detection mode is that it uses half of the laboratory reagents as UNI mode, and hence DUO is and has been the main detection mode used by CMap.**

After *DUO* detection, the expression values of the two genes are computationally extracted in a process called 'peak deconvolution,' described in the next section.

7.2.1 Benchmark k-means solution

CMap's current solution to this problem is based on a k-means clustering algorithm called *dpeak* that works as follows:

For each measurement, the *dpeak* partitions the list of realizations into $k \geq 2$ distinct clusters and identifies two of the clusters whose ratio of membership is as close as possible to 2:1. The algorithm then takes the median intensity of each of the two clusters, assigning these values to the appropriate gene (i.e., matching clusters with more observations to the gene mixed in higher proportion).

After deconvoluting each sample on a plate, *dpeak* then uses the plate-wide distributions to perform adjustments on a per-well basis, correcting peaks that may have been misassigned (see Appendix).

Known problems with the current approach are that k-means is generally a biased and inconsistent estimator of the peaks of a bimodal distribution [ref]. It also sometimes fails to detect peaks with few observations or it incorrectly identifies these peaks as extraneous and disregards them. Another limitation is that it is computationally expensive (the current Matlab implementation takes about 30 minutes on a 12-core server to process one set of 384 experiments).

Additionally, because half the landmark genes are measured using two-fold less bead than the other half, these low-proportion genes are subject to increased variability, which the benchmark k-means solution does not mitigate. Hence, there is an unequal noise distribution in the benchmark's deconvoluted expression profiles.

7.3 Scoring function

Contest submissions were scored based on accuracy and speed.

7.3.1 Accuracy

Accuracy measures were obtained by comparing the contestant's predictions, which were derived from *DUO* data, to the equivalent *UNI* ground truth data generated from the same samples.

The scoring function combines two measures of accuracy: correlation and AUC, which are applied to deconvoluted (*DECONV*) data and one to differential expression (*DE*) data, respectively (See figure XX).

DE is derived from *DECONV* by applying a series of transformations (parametric scaling, quantile normalization, and robust z-scoring) that are described in detail in Subramanian et al. 2017[ref]. The motivation for scoring *DE* data in addition to *DECONV* is because it is at this level where the most biologically interesting gene expression changes are observed. Of particular interest is obtaining significant improvement in the detection of, so called, "extreme modulations." These are genes that notably up- or down-regulated by perturbation and hence exhibit an exceedingly high (or low) *DE* values relative to a fixed threshold.

7.3.1.1 Accuracy based on Spearman correlation

The first accuracy component is based on the Spearman rank correlation between the predicted *DECONV* data and the corresponding *UNI* ground truth data.

For a given dataset p , let $MDUO, p$ and $MUNI, p$ denote the matrices of the estimated gene intensities for $G = 976$ genes (rows) and $S \sim 384$ experiments (columns) under *DUO* and *UNI* detection. Compute the Spearman rank correlation matrix between the rows of $MDUO, p$ and the rows of $MUNI, p$; take the median of the diagonal elements of the resulting matrix (i.e., the values corresponding to the matched experiments between *UNI* and *DUO*) to compute the median correlation per dataset:

$$COR_p = \text{median}(\text{diag}(\text{spearman}(MDUO, p, MUNI, p)))$$

7.3.1.2 Accuracy based on AUC of extreme modulations

The second component of the scoring function is based on the Area Under the receiver operating characteristic Curve (AUC) that uses the competitor's *DE* values at various thresholds to predict the *UNI*'s *DE* values being higher than 2 ("high") or lower than -2 ("low").

For a given bead type a in a given dataset p , let AUC_p, c denote the corresponding area under the curve where $c = \{ \text{high} \mid \text{low} \}$, where high means $UNIDE, p \geq 2$, and low means $UNIDE, p \leq -2$; then, compute the arithmetic mean of the area under the curve per class to obtain the corresponding score per dataset:

$$AUC_p = (AUC_{p, \text{high}} + AUC_{p, \text{low}}) / 2.$$

7.3.2 Speed

For a given dataset p , the speed component of the score is computed as the run time in seconds for deconvoluting the data in each plate.

7.3.3 Aggregegated score

The accuracy and speed components were integrated into a single aggregate scores as follow:

$$\text{SCORE} = \text{SCORE}_{\max} \cdot (\max(\text{COR}_p, 0))^2 \cdot \text{AUC}_p \cdot \exp(-T_{\text{solution}} / (3 \cdot T_{\text{benchmark}})),$$

where $T_{\text{benchmark}}$ is the deconvolution time required by the reference D-Peak implementation.

7.3.4 Accuracy based on knockdown predictions

In addition to the Spearman correlation and extreme modulation AUC metrics used in the contest, we were also able to asses each algorithms ability to correctly predict the successful knockdown (KD) of landmark genes. The shRNA experiments used to generate the contest data were constructed such that each shRNA specifically targeted one of the landmark genes. Hence, the expectation in each of those experiments is that the targeted landmark gene should exhibit a greatly reduced expression level, which should manifest in a very low z-score in *DE* data. Additionally, we expect that the targeted landmark gene should be most dramatically down-regulated in the samples in which it was directly targeted. To assess this, we compute a gene-wise rank by *DE* z-score across all samples in a given plate. Criteria for indicating a successful KD are $zs \leq -2$ AND $rank \leq -10$.

7.4 To read

- Compound signature detection on LINCS L1000 big data used a fuzzy c-means Gaussian Mixture Model (GMM) to process raw L1000 data, showing better performance compared to KNN. This method is described below:

To deconvolute such overlapped peaks, we assumed that the fluorophore intensities of each analyte type (corresponding to a specific mRNA type) had a Gaussian distribution. The distribution of the mixture of analytes GeneH(i) and GeneL(i) corresponding to the expression levels of GeneH and GeneL, respectively, should be subject to a bimodal Gaussian distribution, with the proportion of 1.25 to 0.75. We initialized the estimations of the two Gaussian distributions using fuzzy c-means clustering [11] and estimated the GMM parameters using the Nelder-Mead method [12]. Thus, the overlapped peaks were deconvoluted as the two estimated Gaussian peaks and the expression levels of the two genes sharing the same analyte were extracted. Mathematical details are included in the Supplementary Methods (the GMM model).

- Deconvolution of linear systems by constrained regression and its relationship to the Wiener theory
- Efficient Bayesian-based multiview deconvolution
- A Bayesian deconvolution strategy for immunoprecipitation-based DNA methylome analysis
- Gene expression deconvolution in linear space
- Cell type-specific gene expression differences in complex tissues

References

- [1] Aravind Subramanian et al. "A next generation connectivity map: L1000 platform and the first 1,000,000 profiles". In: *Cell* 171.6 (2017), pp. 1437–1452.
- [2] Shai S Shen-Orr et al. "Cell type-specific gene expression differences in complex tissues". In: *Nature methods* 7.4 (2010), p. 287.
- [3] Peng Lu, Aleksey Nakorchevskiy, and Edward M Marcotte. "Expression deconvolution: a reinterpretation of DNA microarray data reveals dynamic changes in cell populations". In: *Proceedings of the National Academy of Sciences* 100.18 (2003), pp. 10370–10375.
- [4] Karim R Lakhani et al. "Prize-based contests can provide solutions to computational biology problems". In: *Nature biotechnology* 31.2 (2013), p. 108.
- [5] Andrea Blasco et al. "Advancing Computational Biology and Bioinformatics Research Through Open Innovation Competitions". In: *bioRxiv* (2019), p. 565481.