



*Model Explanation*

There are two ideas presented here. The first is that the number of initiates is entirely dependent on the number of initiators and that since we have divided initiators into Low- and High-Rate Initiators, there is in theory, some threshold rate of initiation which makes a distinction between L and H. Thus we present  $\lambda_L$  and  $\lambda_H$  as the average number of initiates per initiator for the given time-step the model is being run on. The second is that the number of high initiators is perhaps dependent on the number of low-initiators, thus we set  $\eta$  as a constant

which represents a proportion of L to H which the model shall seek to maintain.

$$\alpha : L(t) * \lambda_L + H(t) * \lambda_H$$

$\beta : -\frac{\eta * H(t) - L(t)}{\eta + 1}$ ,  $\beta > 0$  indicates a transition from  $L$  to  $H$  and a  $\beta < 0$  indicates a transition from  $H$  to  $L$

$$\gamma : 0$$

$\eta$  : a set constant which  $\frac{L(t)}{H(t)}$  maintains

$\lambda_L$  = the average number of initiates for a Low-Risk Initiator

$\lambda_H$  = the average number of initiates for a High-Risk Initiator

$dL : L(t) * x_L$  where  $x_L$  represents the "death" rate of this pop

$dH : H(t) * x_H$  where  $x_H$  represents the "death" rate of this pop

$$L(t + 1) = L(t) + \alpha - \beta - dL$$

$$\begin{aligned} &= L(t) + L(t) * \lambda_L + H(t) * \lambda_H - \left(-\frac{\eta * H(t) - L(t)}{\eta + 1}\right) - L(t) * x_L \\ &= L(t) + L(t) * \lambda_L + H(t) * \lambda_H + \frac{\eta * H(t) - L(t)}{\eta + 1} - L(t) * x_L \\ &= L(t) \left(1 + \lambda_L - \frac{1}{\eta + 1} - x_L\right) + H(t) \left(\lambda_H + \frac{\eta}{\eta + 1}\right) \end{aligned}$$

$$H(t + 1) = H(t) + \beta + \gamma - dH$$

$$\begin{aligned} &= H(t) + \left(-\frac{\eta * H(t) - L(t)}{\eta + 1}\right) + 0 - H(t) * x_H \\ &= H(t) - \frac{\eta * H(t) - L(t)}{\eta + 1} - H(t) * x_H \\ &= H(t) \left(1 - \frac{\eta}{\eta + 1} - x_H\right) + L(t) \left(\frac{1}{\eta + 1}\right) \end{aligned}$$