

Homework Sets: 6.1 { 3, 7, 13, 18, 33, 34}

**3a)** No. There are elements that in R that are not in T. 2 is in R but not in T, and 2 is not divisible by 6.

**3b)** Yes. Every number divisible by 6 is divisible by 2.

$n = 6m \dots 6m = 2(3m)$ .  $3m$  is an integer so  $2 \cdot (\text{some integer})$  proves that  $n$  is divisible by 2.

**3c)** Yes. Every number divisible by 6 is divisible by 3.

$n = 6m \dots 3(2m)$ .  $2m$  is an integer so  $3 \cdot (\text{some integer})$  proves that  $n$  is divisible by 3.

(A)  $x = 6a + 4$  for some integer  $a$

(B)  $y = 18b - 2$  for some integer  $b$

(C)  $z = 18c + 16$

**7a)** A is not a subset of B

$6a + 4 = 18b - 3$  (solve for  $b$ )

$6a + 7 = 18b \dots = (6a + 7) / 18 = b$

$b = (6a + 7) / 18$  (not an integer)

**7b)** B is a subset of A

$18b - 2 = 6a + 4$  (solving for  $a$ )

$18b - 6 = 6a$

$a = 3b - 1$

$b = (a + 1) / 3$

$18(a+1)/3 - 2 = (18a + 18) / 3 - 2 = 6a + 6 - 2 = 6a + 4$

**7c)** Finding B subset C and C subset B will determine the proof of the statement.The statement is proven below:

**Solve for C**

$18b - 2 = 18c + 16$

$18b - 18 = 18c$

$c = b - 1$

**Substitute in b-1 for c**

$18(b-1) + 16 = 18b - 18 + 16 = 18b - 2$

**Now solve for B**

$18b - 2 = 18c + 16$

$18b = 18c + 18$

$b = c + 1$

Is  $B = C$ ?

$18(c+1) - 2 = 18(b - 1) + 16$

$18c + 18 - 2 = 18b - 18 + 16$

$18c + 16 = 18b - 2$

**18c + 16 is in C therefore it is an element of B. B and C are subsets of eachother, we know that B = C.**

**13a)** True. Positive integers are real numbers.

**13b)** False.  $-\sqrt{2}$  is a real number but not rational.

**13c)** False.  $2/3$  is not a real number.

**13d)** False. 0 is only an element in  $\mathbb{Z}$ , not  $\mathbb{Z}^-$  or  $\mathbb{Z}^+$ .

**13e)** True. It would just be an empty set because  $\mathbb{Z}^-$  only contains negative integers and  $\mathbb{Z}^+$  only contains positive integers.

**13f)** True. Q is a subset of R.

**13g)** True. Q is a subset of R, and R is a subset of Q. Therefore the Q and R is true.

**13h)** True.  $\mathbb{Z}^+$  is a subset of R (and vice versa). Therefore  $\mathbb{Z}^+$  and R is true.

**13i)** False.  $2/3$  might be in the set on the right, but not on the set in the left.

**18a)** No. 0 would be in a set of all real numbers  $\{0, 1, 2, 3\dots n\}$ . An empty set has no elements.

**18b)** No.  $\{\} = \{\{\}\}$ . An empty set equal to a set which contains one element (which is an empty set).

**18c)** Yes. The empty set is a member of the set that contains one element.

**18d)** No. An empty set is not an element of an empty set.

**33a)**  $= \{ \emptyset \}$ . Partition of an empty set.

**33b)**  $= P(\{\emptyset\}) = \{ \emptyset, \{ \emptyset \} \}$

**33c)**  $= P\{ \emptyset, \{ \emptyset \} \} = \{ \emptyset, \{\{ \emptyset \}\}, \{ \emptyset, \{ \emptyset \} \} \}$

$A1 = \{ 1, 2, 3 \}$

$A2 = \{ u, v \}$

$A3 = \{ m, n \}$

**34a)**

$= \{ (1, (u, m)), (1, (u, n)), (1, (v, m)), (1, (v, n)),$   
 $(2, (u, m)), (2, (u, n)), (2, (v, m)), (2, (v, n)),$   
 $(3, (u, m)), (3, (u, n)), (3, (v, m)), (3, (v, n)) \}$

**34b)**

$= \{ ((1, u), m), ((1, u), n), ((1, v), m), ((1, v), n),$   
 $((2, u), m), ((2, u), n), ((2, v), m), ((2, v), n),$   
 $((3, u), m), ((3, u), n), ((3, v), m), ((3, v), n)) \}$

**34c)**

$= \{ (1, u, m), (1, u, n), (1, v, m), (1, v, n),$   
 $(2, u, m), (2, u, n), (2, v, m), (2, v, n),$   
 $(3, u, m), (3, u, n), (3, v, m), (3, v, n)) \}$