

# OpenGeoProver Output for RC-Constructibility problem “Wernick 001 (A,B,O — C)”

Used algebraic method (with triangulation)

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## 1 Validation of Construction Protocol

**Construction steps:**

- Free point A
- Free point B
- Free point C
- Perpendicular bisector mc of segment AB
- Perpendicular bisector ma of segment BC
- Intersection point O of point sets ma and mc

**Free points:**

- A
- B
- O

**Points to be constructed:**

- C

**Validation result:** Construction protocol is valid.

## 2 Instantiation of points with symbolic variables

- Point C has been assigned following coordinates:  $(x_1, x_2)$
- Point A has been assigned following coordinates:  $(u_1, u_2)$
- Point B has been assigned following coordinates:  $(u_3, u_4)$
- Point O is locus dependent on points: A, B

- Point O has been assigned following coordinates:  $(u_5, u_6)$
- Locus dependency in polynomial form:

$$p = (2u_6u_4 - 2u_6u_2 + 2u_5u_3 - 2u_5u_1 - u_4^2 - u_3^2 + u_2^2 + u_1^2)$$

### 3 Transformation of geometry conditions for points to polynomial form

#### 3.1 Transformation, step 1

Point to transform: A

Polynomial condition(s): N/A - free point

#### 3.2 Transformation, step 2

Point to transform: B

Polynomial condition(s): N/A - free point

#### 3.3 Transformation, step 3

Point to transform: C

Polynomial condition(s): N/A - free point

#### 3.4 Transformation, step 4

Point to transform: O

Polynomial condition(s): One polynomial

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$$p = -x_2^2 + 2u_6x_2 - x_1^2 + 2u_5x_1 + (-2u_6u_4 - 2u_5u_3 + u_4^2 + u_3^2)$$

### 4 Triangulation of polynomial system

System is underconstrained - cannot proceed

### 5 Result of transformation of RC-constructibility problem to polynomial form

**Success Message:** Failed to transform the RC-constructibility problem to polynomial form - find more details in log file.

**Space Complexity:** The biggest polynomial obtained during application execution contains 0 terms.

**Time Complexity:** Time spent in execution is 0.02 seconds.