

## Worked Example: The Trapezoidal Rule

The *trapezoidal rule* is a numerical integration scheme in which the area under a curve is approximated by a collection of trapezoidal subdivisions whose individual areas are added together. Consider the integral of some function  $f(x)$  over the limits from  $x = a$  to  $x = b$ . If this integral is to be approximated by  $N$  trapezoidal divisions, then the approximate value of the integral is given by:

$$\int_{x=a}^{x=b} f(x) dx \cong -\frac{\Delta x}{2} \cdot [f(a) + f(b)] + \Delta x \cdot \sum_{i=0}^{i=N} f(a + i \cdot \Delta x)$$

The parameter  $\Delta x$  is the assumed uniform width of the divisions:

$$\Delta x \equiv \frac{b - a}{N}$$

Using the formulation above, create a VI to approximate the integral of the function  $f(x) = x + 2x \cdot \cos(x^2)$ , between any two limits  $a$  and  $b$ , and for any desired divisions  $N$ . Note that in general, numerical integration techniques are most practical for use when the exact answer is otherwise indeterminate, or for fundamentally discrete data.

