

Table 3.3.2 Properties of the Laplace transform.

$x(t)$	$X(s) = \int_0^\infty f(t)e^{-st} dt$
1. $af(t) + bg(t)$	$aF(s) + bG(s)$
2. $\frac{dx}{dt}$	$sX(s) - x(0)$
3. $\frac{d^2x}{dt^2}$	$s^2X(s) - sx(0) - \dot{x}(0)$
4. $\frac{d^nx}{dt^n}$	$s^n X(s) - \sum_{k=1}^n s^{n-k} g_{k-1}$ $g_{k-1} = \left. \frac{d^{k-1}x}{dt^{k-1}} \right _{t=0}$
5. $\int_0^t x(t) dt$	$\frac{X(s)}{s} + \frac{g(0)}{s}$ $g(0) = \left. \int x(t) dt \right _{t=0}$
6. $x(t) = \begin{cases} 0 & t < D \\ g(t-D) & t \geq D \end{cases}$ $= u_s(t-D)g(t-D)$	$X(s) = e^{-sD}G(s)$
7. $e^{-at}x(t)$	$X(s+a)$
8. $tx(t)$	$-\frac{dX(s)}{ds}$
9. $x(\infty) = \lim_{s \rightarrow 0} sX(s)$	
10. $x(0+) = \lim_{s \rightarrow \infty} sX(s)$	