

Let  $\infty$  and  $-\infty$  denote two distinct objects neither of which is in  $\mathbb{R}$ . Define an addition and scalar multiplication on  $\mathbb{R} \cup \{\infty\} \cup \{-\infty\}$  as you could guess from the notation. Specifically, the sum and products of two real number is as usual, and for  $t \in \mathbb{R}$  define

$$t\infty = \begin{cases} -\infty & \text{if } t < 0, \\ 0 & \text{if } t = 0, \\ \infty & \text{if } t > 0 \end{cases}$$

$$t(-\infty) = \begin{cases} \infty & \text{if } t < 0, \\ 0 & \text{if } t = 0, \\ -\infty & \text{if } t > 0 \end{cases}$$

$$t + \infty = \infty + t = \infty, \quad t +$$