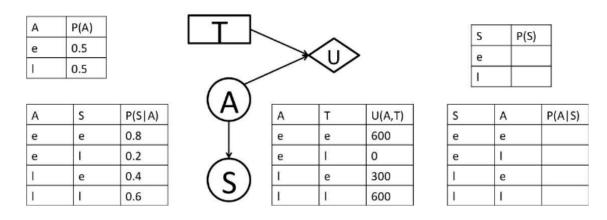
Please use the LaTeX template to produce your writeups. See the Homework Assignments page on the class website for details. Hand in at: https://webhandin.eng.utah.edu/index.php.

1 Decision Networks and VPI



Your parents are visiting you for graduation. You are in charge of picking them up at the airport. Their arrival time (A) might be early (e) or late (l). You decide on a time (T) to go to the airport, also either early (e) or late (l). Your sister (S) is a noisy source of information about their arrival time. The probability values and utilities are shown in the tables above.

Compute P(S), P(A|S) and compute the quantities below.

$$P(S = e) = 1.2 \Rightarrow \frac{1.2}{0.8 + 1.2} = 0.6$$

 $P(S = l) = 0.8 \Rightarrow \frac{0.8}{0.8 + 1.2} = 0.4$

$$P(A = e|S = e) = \frac{P(S = e|A = e)P(A = e)}{P(s = e)} = \frac{0.8(0.5)}{0.6} = 2/3$$

$$P(A = l|S = e) = 1 - 2/3 = 1/3$$

$$P(A = l|S = l) = \frac{P(S = l|A = l)P(A = l)}{P(s = e)} = \frac{0.6(0.5)}{0.4} = 3/4$$

$$P(A = e|S = l) = 1 - 3/4 = 1/4$$

1.
$$EU(T = e) = 0.5(600) + 0.5(300) = 450$$

2.
$$EU(T = l) = 0.5(0) + 0.5(600) = 300$$

3.
$$MEU(\{\}) = \max_T EU(T, A) = 450$$

4. Optimal action with no observations

$$T = e$$

Now we consider the case where you decide to ask your sister for input.

1.
$$EU(T = e|S = e)$$

= $P(A = e|S = e)EU(T = e|A = e) + P(A = l|S = e)EU(T = e|A = l)$
= $2/3(600) + 1/3(300) = 500$

2.
$$EU(T = l|S = e)$$

= $P(A = e|S = e)EU(T = l|A = e) + P(A = l|S = e)EU(T = l|A = l)$
= $2/3(0) + 1/3(600) = 200$

3.
$$MEU(\{S = e\})$$

= $\max_T \sum_A P(A|S = e)EU(T|A) = 500$

4. Optimal action with observation $\{S=e\}$

$$T = e$$

5.
$$EU(T = e|S = l)$$

= $P(A = l|S = l)EU(T = e, A = l) + P(A = e|S = l)EU(T = e, A = e)$
= $3/4(300) + 1/4(600) = 375$

6.
$$EU(T = l|S = l)$$

= $P(A = l|S = l)EU(T = l, A = l) + P(A = e|S = l)EU(T = l, A = e)$
= $3/4(600) + 1/4(0) = 450$

7.
$$MEU(\{S=l\})$$

 $\max_T \sum_A P(A|S=l)EU(T) = 450$

- 8. Optimal action with observation S=l T=l
- 9. VPI(S)= $MEU(\{S=e\})P(S=e) + MEU(\{S=l\})P(S=l) - MEU(\{\})$ = 500(0.6) + 450(0.4) - 450 = 30

2 Wherefore art thou Romeo?

Romeo and Juliet are two lovesick robots; they function best when each knows where the other is. Romeo has become lost, and is trying to figure out where he is so he can tell Juliet. Romeo is on the grid below, which also lists transition probabilities and properties of the sensors. At each step, Romeo senses, and then transitions to an adjacent room to get to the next time step. Romeo observed the following evidence while wandering in grief over his inability to tell Juliet where he is: 2 walls, 2 walls, 3 walls.

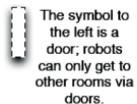
Forward Algorithm Compute the most likely location, given the evidence.

Viterbi Algorithm Compute the most likely sequence of steps he took in the maze for the above evidence.

Probability of transitioning to any adjoining room is uniform (e.g., if you could go either north or south, but not east or west, you go north with probability 1/2 and south with probability 1/2).

The initial probabilities are uniform: the robot is in any square at time t=0 with probability 1/7.





Robots sense the number of walls in the current room without doors. Their sensors are noisy, however. With probability 3/4 the robot will sense the correct number of walls. With probability 1/4, the robot will sense one more than the actual number of walls. For example, if the robot is in square D, it will sense 2 with probability 3/4 and 3 with probability 1/4.

