- Data Rich but Model Resistant: An Evaluation of
 Data-Limited Methods to Manage Fisheries with Failed
 Age-based Stock Assessments
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7 Abstract

8 Introduction

structured are used to estimate annual stock abundance (biomass), fishing mortality rates, and management reference points (Maunder and Punt 2013). These models must undergo 11 peer review, where an independent panel of experts determines whether or not results from the model are suitable as the basis for determining stock status and for setting catch advice. There are a number of model diagnostics that are used to evaluate uncertainty and stability of assessment model results, but one that is commonly used and carries substantial 15 weight during review is the retrospective pattern. A retrospective pattern is a systematic 16 inconsistency among a series of sequential assessment estimates of population size (or other 17 related assessment variables), based on increasing time periods of data used in the model fitting (Mohn 1999). These inconsistencies in assessment estimates are indicative of one or more mismatches between model assumptions and patterns in the data used to fit the model. Large or persistent retrospective patterns indicate an instability in model results, and may therefore be the basis for a peer review panel to determine that model results are not suitable for management purposes (Punt et al. 2020). Many stock assessments in the Northeast U.S. have a history of strong retrospective patterns, whereby estimates of biomass are typically revised downward and estimates of fishing 25 mortality rate are revised upward as new data are added to the model. NOAA Fisheries, the New England Fishery Management Council, the Mid-Atlantic Fishery Management Council, and the Atlantic States Marine Fisheries Commission manage these stocks, and retrospective issues remain a challenge for managers when setting catch advice and tracking stock status. This problem has been particularly acute for, but not limited to, stocks in the New England groundfish complex (NEFSC 2002, 2005, 2008, 2015a, 2015b, 2017, 2019; Deroba et al. 2010), managed under NOAA Fisheries and the New England Council's Northeast Multispecies (Groundfish) fishery management plan.

In the U.S., integrated fisheries stock assessment models that are most frequently age-

The magnitude of the retrospective pattern is typically measured with a statistic called Mohn's rho (Mohn 1999). Mohn's rho can be used to adjust terminal year estimates of biomass in anticipation that the retrospective pattern will persist, and so some accounting for the pattern will provide a more accurate estimate. Stock assessments where the so-called rho-adjusted value is outside the 90% confidence interval of the terminal year estimate of spawning stock biomass (SSB) or fishing mortality rate are classified as strong retrospective patterns. In these cases, the rho-adjusted values are used for status determination and to modify the starting population for projections used to provide catch advice (Brooks and Legault 2016).

There is no formal criteria in the region for rejecting an assessment based on Mohn's rho, but large, positive values of rho (especially those persisting) have played an important role in the rejection of recent age-based assessments including Atlantic mackerel (Scomber scombrus)

large, positive values of rho (especially those persisting) have played an important role in the rejection of recent age-based assessments, including Atlantic mackerel (*Scomber scombrus*), Georges Bank Atlantic cod (*Gadus morhua*), Georges Bank yellowtail flounder (*Limanda ferruginea*), and witch flounder (*Glyptocephalus cynoglossus*) (Deroba et al. 2010; Legault et al. 2014; NEFSC 2015a, 2015b). In each of these cases, and another where the assessment rejection was not based on the retrospective pattern (black sea bass, *Centropristis striatus*, NEFSC 2012), the Councils have relied on a variety data-limited approaches for setting catch advice for these stocks (McNamee et al. 2015; NEFSC 2015a, 2015b; Wiedenmann 2015). These approaches have all been ad-hoc, and a recent analysis suggested that some of the data-limited approaches may not be suitable for stocks in the Northeast U.S. with a history of high exploitation rates (Wiedenmann et al. 2019). In addition, large, positive retrospective patterns persist for a number of other stocks in the region (NEFSC 2019), raising concerns that additional stocks may rely on data-limited approaches in the future. Therefore, there is an immediate need to identify suitable data-limited approaches for setting catch advice and for stocks with age-based assessments that did not pass review.

We developed a management strategy evaluation (MSE; e.g., Punt et al. 2016) to evaluate the suitability of alternative data-limited methods for setting target catches when age-based

stock assessments fail. In particular, focus was placed on methods that use survey indices of abundance, or more generally, index based methods (IBMs).

Methods

64 Overview

The MSE used here attempted to approximate a process where an age-based assessment was rejected due to a retrospective pattern, requiring catch advice to be determined using an IBM. As such, the operating model (OM) used to define the "true" underlying biological and fishery dynamics was also age-based. The OM was run for an initial 50 year period of time (called the base period) that controls the historical population dynamics and fishing pressure, and allows for sufficient data to be simulated in the observation model to be used in the different IBMs. After the base period, a given management approach (i.e., IBM) was applied to set the target catch for the stock, which is then removed from the population with some degree of implementation error. This process is repeated at a fixed interval for 40 years in what is called the feedback period. Multiple OMs were developed so that the performance of the IBMs could be compared among several sources of uncertainty that are especially common in the northeast US, but relevant more broadly. The set of OMs included two versions with time varying dynamics in the last 20 years of the base period, that if left misspecified as time invariant, would be sufficient to generate retrospective patterns resulting in the rejection of an age-based stock assessment, requiring transition to an IBM. The details of each of these components are described in sections below.

81 Operating and Observation Models

The Woods Hole Assessment Model (WHAM, Miller and Stock 2020; Stock and Miller 2021)

was used as the basis for the OM in the MSE. WHAM is an R package and the general

model is built using the Template Model Builder package (Kristensen et al. 2016). While

WHAM can serve as a stock assessment model used to estimate parameters, it can also

simulate the data needed for age-based stock assessments and IBMs given a range of input
parameters. WHAM was used to simulate data with known properties during the base and
feedback periods. Catch and index observations upon which the IBMs largely relied were
simulated according to user supplied biological and fishery parameters for each scenario (see
below). Catches during the feedback period were iteratively updated based on an IBM and
harvest control rule that used the simulated observations to make catch advice. Catch advice
from a given combination of IBM and control rule was specified in two year blocks, a typical
catch specification timeframe for New England and Mid-Atlantic Council managed fisheries.
WHAM used these catches, along with the user supplied biological and fishery data, to have
the simulated population respond to the IBM, thereby completing the closed-loop simulation
aspect of an MSE.

The age-structured OM had ten ages, with the oldest age being a plus group. Maturityand weight-at-age were time and simulation invariant and equaled values intended to be groundfish-like for the region (Table 1??). The OM simulated catch and age composition data for a single fishery with logistic selectivity (Table 1??; see below). Annual, total catch observations (metric tons) were simulated as lognormal deviations from the underlying "true" 101 catches with a coefficient of variation (CV) equal to 0.1. Fishery age composition data was 102 assumed to follow a multinomial distribution with an effective sample size (ESS) equal to 103 200. Two fishery independent surveys were simulated and were intended to represent the 104 spring and fall, coastwide bottom trawl surveys conducted in the region. Both surveys were 105 assumed to have time invariant logistic selectivity and constant catchability. Annual sur-106 vey observations were simulated as lognormal deviations from the underlying "true" survey 107 catches with a CV of 0.3 in the spring survey and 0.4 in the fall. Survey age composition 108 data were assumed to follow a multinomial distribution with an ESS equal to 100 in both 109 seasons. 110

Annual recruitment was simulated as autoregressive, lag-1 (AR-1) deviations from an underlying Beverton-Holt stock-recruitment relationship with steepness equal to 0.74. The degree of correlation in the AR-1 process equaled 0.4 with a conditional standard deviation about this relationship equal to 0.5. Unfished recruitment was time- and simulation invariant and equaled 10-million age-1 fish. All these stock-recruitment values were based on an average of groundfish parameters estimated for the region.

117 Index Based Methods Explored

The range of IBMs evaluated was generally constrained to those that have been used or were 118 considered plausible (e.g., based on data requirements) for the Northeast Shelf. Ultimately, 119 thirteen IBMs were selected for evaluation. Although catch-curve analyses are not currently 120 applied in the region, they were included here since age information is available for most of the stocks, and because Wiedenmann et al. (2019) showed they performed well in application to groundfish stocks. Two additional IBMs (Islope and Itarget) not currently used in the 123 region were also evaluated, as these have been tested in other applications and shown promise 124 (Geromont and Butterworth 2015a, 2015b; Carruthers et al. 2016; Wiedenmann et al. 125 2019). An ensemble of models was also considered based on recent findings that improved 126 performance can result from combining the results from multiple models (Anderson et al. 127 2017; Rosenberg et al. 2018; Spence et al. 2018; Stewart and Hicks 2018). The catch 128 advice from the ensemble approach equaled the median of the catch advice from a range 129 of other methods (Table 2). The DLM approach was excluded from the ensemble due 130 to the relatively long computing time required. Other methods were excluded (CC-FM, 131 ES-FM, ES-Fstable) because they were slight variations of a more generic IBM (i.e., CC-132 and ES-) and including them all may have unduly overweighted the performance of the 133 ensemble towards these methods. In these cases, the methods retained in the ensemble 134 had superior performance than the alternatives based on preliminary results, or had already 135 been considered for application in the region. The full range of methods included in this 136 analysis were detailed below with equations (Table 2). The performance of each method was 137 compared using a range of metrics with data that would lead to retrospective patterns in an 138 age-based stock assessment (see below).

Other data-limited methods exist for setting catch advice that were not included in this evaluation, and they vary widely in complexity, data inputs, and assumptions required (e.g., 141 Carruthers and Hordyk 2018). Length based methods were not evaluated to keep the overall 142 number of methods tractable, and due to the availability of age based information in the 143 region. Methods that require only catch data or snap shots of survey data were not considered 144 due to the availability of the relatively long and contiguous Northeast Fisheries Science 145 Center's spring and fall, coastwide bottom trawl surveys. Complete catch histories are 146 not available for stocks in the region (i.e., from the inception of fishing). Furthermore, 147 assumptions of surplus production models are likely violated due to time varying productivity 148 (e.g., in recruitment or natural mortality), and surplus production model fits resulted in 149 different estimates of biomass over time compared to age-based assessments for many stocks 150 (Wiedenmann et al. 2019). Consequently, methods that required complete catch histories, 151 assumed underlying surplus production population dynamics, or required assumptions about 152 relative depletion (e.g., DCAC in MacCall 2009; DB-SRA in Dick and MacCall 2011) were 153 also omitted from consideration. 154

Each of the methods evaluated produces a single target catch value that was fixed over a two 155 year interval. If the methods were being applied in year y, then target catches are set for 156 years y+1 and y+2 (denoted $C_{targ,y+1:y+2}$). In practice, the timing of setting target catches 157 in the region generally occurs in late summer or early fall in between the spring and fall 158 surveys, and before complete catch data are available. Therefore, in year y complete catch 159 data are available through year y-1, and survey data are available for the spring survey 160 through year y and for the fall survey through year y-1. In practice, the data-limited 161 methods that have been applied have used an average of the spring and fall index, and that 162 approach was followed here. If a method for setting catches uses an average of spring and 163 fall, the average index in year y included the spring data in year y and the fall data in year 164 y - 1: 165

166
$$\bar{I}_y = \frac{I_{fall,y-1} + I_{spr,y}}{2}$$
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167 Control Rules

Most IBMs do not have the ability to estimate a biomass reference point (e.g., B_{MSY}), which 168 made consideration of so called biomass-based harvest control rules that reduce F or catch 169 in response to estimated changes in relative stock status impossible. Lack of clarity exists, 170 however, on whether the catch advice from IBMs should be treated as an overfishing limit 171 (OFL) or an acceptable biological catch (ABC). OFLs are equated to the catch that would 172 result from applying F_{MSY} , whereas an ABC is a catch reduced from the OFL to account 173 for scientific uncertainty. Each IBM was evaluated using two "harvest control rules": 1) the 174 catch advice from a given IBM was applied directly and assumed to serve as a proxy for 175 the catch associated with F_{MSY} , thereby being equated to an OFL (catch multiplier = 1), 176 and 2) the catch advice from a given IBM was reduced by 25% to account for unspecified scientific uncertainty, thereby being equated to an ABC (catch multiplier = 0.75). Catches were reduced by 25% to approximate an ABC because using the catch associated with 0.75 179 F_{MSY} is a common default ABC control rule in the region. 180

Application of a Statistical Catch-at-Age Assessment (SCAA)

A SCAA model was also applied to all scenarios to generate catch advice for comparison 182 with the IBMs. Although virtual population analysis (VPA) are also used for some age-183 based assessments in the region, SCAA models are more widely used. Applications of the SCAA model assumed that the assessment had the correct underlying structure for selec-185 tivity, and CVs and ESS were specified at their true underlying values. The SCAA model estimated annual recruitment deviations assuming no underlying stock-recruit relationship, 187 annual fully-selected fishing mortality rates, fishery and survey selectivity parameters (lo-188 gistic), abundance-at-age in year one of the period being assessed, and survey catchabilies. 189 Mohn's rho was calculated (7 year peels) for abundance at age for all model fits during the 190 feedback period and used to retro-adjust abundance at age for projections (divided by one 191 plus Mohn's rho). Catch advice was determined by specifying fully-selected $F = 0.75F_{40\%}$,

always assuming M=0.2.

194 Study Design

In addition to the two control rules applied for each IBM described above, three aspects of 195 the OM were varied in a full factorial study design: fishing history, fishery selectivity, and 196 cause of the retrospective pattern. Two variants of fishing history were considered, with fully selected fishing mortality during the base period either constant at a level equal to $2.5F_{MSY}$ (always overfishing; referred to as "OF" below) or equaling $2.5F_{MSY}$ in the first 199 half of the base period then a knife-edged decline to F_{MSY} for the second half of the base period (referred to as "KF" below). These patterns in fishing mortality rate were based on 201 observed patterns for Northeast groundfish (Wiedenmann et al. 2019). These two different 202 fishing intensities during the latter half of the base period led to different starting conditions 203 for the feedback period. 204

Two variations of the OM were considered with either time invariant, asymptotic, fishery selectivity in the base and feedback periods (referred to as "S1" below), or a change in selectivity after the first half of the base period so that the age at 50% selectivity increased from approximately 3.7 to 5 (referred to as "S2" below; Table 1). The asymptotic selectivity pattern was based on Northeast groundfish fishery selectivity patterns. The change in the selectivity pattern when selectivity varied through time approximated an increase in mesh size in the fishery to avoid younger fish.

Two different sources of stock assessment misspecification leading to retrospective patterns were considered, temporal changes in natural mortality and misreported catch. The degree to which natural mortality and unreported catch changed through time was determined by attempting to achieve an average Mohn's rho of approximately 0.5 for SSB when an SCAA model (i.e., configured using WHAM) was used to fit the simulated data. We also fit the same SCAA configuration to data without misspecified M or catch to verify that retrospective patterns were not present on average (Figure 1.2). A third source of misspecification was also

219 attempted, time varying survey catchability, but this source of misspecification was unable 220 to produce severe enough retrospective patterns and was abandoned.

For the natural mortality misspecification, the true natural mortality changed from 0.2 to 221 0.32 for the OF fishing history or to 0.36 for the KF fishing history, with the differences 222 between fishing histories necessary to produce the desired retrospective pattern severity. In 223 each case, natural mortality trended linearly from 0.2 to the higher value between years 224 31 and 40 of the base period. Natural mortality remained constant at the higher level 225 throughout the feedback period. Those IBMs that required a natural mortality rate used 226 the value from before any change in natural mortality (0.2) because the change in natural 227 mortality is meant to be unknown. 228

For catch misspecification, a scalar multiple of the true catch observation is provided as the observed catch to the IBMs. The scalar is 0.2 for fishing intensity OF and both selectivity 230 patterns, 0.44 for fishing intensity KF and selectivity scenario S2, or 0.4 for fishing history 231 KF and selectivity S1. The shift in scalar trended linearly from 1 to the lower value between 232 years 31 and 40 of the base period. These scalars were applied only to the aggregate catch 233 so that they affect all catches at age equally. When catch misspecification was applied in 234 conjunction with an IBM during the feedback period, the true catch in the OM equaled the 235 catch advice provided by the IBM multiplied by the inverse of the scalar multipliers (i.e., 236 the true catches were higher than the IBM catch advice). Thus, when the scalar multipliers 237 were applied to the true catch from the OM in order to provide observed catches at the 238 next application of the IBM, the observed catch equaled the catch advice from the previous 239 application of the IBM, on average. In other words, managers and analysts would be given 240 the perception that the IBM catch advice was being caught by the fishery, when in fact the 241 true catches were always higher. 242

Fourteen methods for setting catches were explored (13 IBMs and the SCAA) and were applied to all 16 scenarios, which created 224 factorial combinations in the study design. For

each element of the full factorial combinations, 1,000 simulations were conducted. Two IBMs
(AIM and ES-Fstable) had two failed simulations each, which were caused by relatively high
catch advice (i.e., requiring relatively high F) that triggered errors in the Newton-Raphson
iterations used to determine that F that would produce the desired catch. This small number
of failures was unlikely to effect results and conclusions, and so were not considered further.
A naming convention was developed to more easily label and track results among scenarios
(Table 3).

Some sensitivity runs were also conducted with all sources of retrospective pattern removed for two of the scenarios. All the IBMs, except DLM and SCAA were applied to these sensitivity runs. WE SHOULD CUT THIS, CORRECT?

255 Performance Metrics

A total of 50 performance metrics were recorded during the simulations, but many were 256 redundant and displayed similar tradeoffs among the IBMs and SCAA model. So six metrics 257 thought to be of broad interest were reported here, each calculated and reported separately 258 for a short-term (i.e., first six years of the feedback period) and long-term (i.e., last 20 years 259 of the feedback period) period. These metrics were selected to represent the tradeoffs in 260 terms of benefits to the fishery and risks to the stock. The specific metrics reported were: 261 mean catch relative to MSY, mean interannual variation in catch (A'mar et al. 2010), mean $\frac{SSB}{SSB_{MSY}}$, mean number of years among simulation with SSB less than half SSB_{MSY} , mean number of years among realizations that fully-selected fishing mortaity was greater than the F_{MSY} , and mean $\frac{F}{F_{MSY}}$.

Results

Overall performance varied widely across methods, and the individual performance of a method was sensitive to the different scenarios explored. Performance for each method was sensitive the source of the retrospective pattern (missing catch or M), the exploitation history, the time period the method was applied (short- or long-term), and whether or not a
25% buffer was applied when setting the catch advice from a given method. Overall, similar
results occurred for the scenarios with one or two selectivity blocks, so the impact of the
selectivity scenarios was not discussed further.

274 Aggregate performance

In Figure 1, median performance measures are shown, calculated across all scenarios combined. In general, methods that resulted in high mean F/F_{MSY} (Figure 1B) resulted in lower stock biomass (Figure 1A), higher risks of overfishing (Figure 1E) and of being overfished (Figure 1F), and vice-versa. Higher F values were also associated with higher catches (Figure 1C), on average, and a greater variability in catch, but there were some methods that produced lower F values that also resulted in high catch variability (CC-FM, CC-FSPR; Figure 1D).

A number of methods performed poorly overall, resulting in high exploitation rates and low 282 stock size, on average (Figure 1). These methods include AIM, three of the four expanded 283 survey biomass methods (ES-FM, ES-FSP, and ES-Fstable), and the skate method. The 284 Itarget and Ensemble methods also resulted in $SSB < SSM_{MSY}$ and $F > F_{MSY}$, on average, 285 though departures from the MSY levels were not as severe as the other methods (Figure 1). 286 The remaining methods (CC-FM, CC-FSPR, DLM, ES-Frecent, Islope, Ismooth, and SCAA) 287 were able to limit overfishing and keep biomass above SSB_{MSY} , on average, although for 288 four of these methods (CC-FM, CC-FSPR, DLM, and Ismooth) biomass was was more than 50% higher than SSB_{MSY} (Figure 1). 290

291 Scenario-dependent performance

The source of the retrospective pattern had a large impact on results for a given method. The relationship between SSB/SSB_{MSY} and C/MSY is shown across scenarios for the different sources of retrospective error. Stock size and catch (relative to MSY levels) are clustered for many of the methods with no overlap between M and unreported catch sources (AIM, ES-

FM, ES-FSPR, ES-Fstable, Itarget, Skate, Ensemble, and SCAA). For all of these methods. SSB/SSB_{MSY} was lower when unreported catch was the source of the retrospective pattern, 297 and C/MSY was also lower except for the Itarget and the SCAA methods (Figure 2). The 298 source of the retrospective pattern also had a large impact on the other performance measures 299 (Figure 3). In general, when unreported catch was the source of the retrospective pattern 300 interannual variability in catch was higher, overfishing was more frequent and with a larger 301 F/F_{MSY} , and the stock had a higher risk of being overfished (Figure 3). Six methods (AIM, 302 ES-FM, ES-FSPR, ES-Fstable, Itarget, Skate, Ensemble) resulted in overfishing in nearly 303 every year of the feedback period (often with very high F/F_{MSY}) when missing catch was 304 the source of the retrospective pattern (Figure 3B, 3E). The SCAA method also resulted in 305 frequent overfishing under the missing catch scenario, but less so when the stock was more 306 depleted at the start of the feedback period (Figure 1E). 307

Exploitation history also impacted the performance of many of the other methods. For four 308 methods (Islope, Ismooth, DLM and ES-Frecent), exploitation rates were higher when the 309 stock experienced overfishing for the entire base period, but the impact was more dramatic 310 in the short-term. Over time as these methods were used, F declined and remained below 311 F_{MSY} in the long-term (Figure 4A), allowing stock recovery. The majority of the other 312 methods also resulted in greater exploitation rates in the short-term, though some methods 313 kept F/F_{MSY} < 1 regardless of the time-period (CC-FM, CC-FSPR, and SCAA), while 314 others (AIM, ES-F stable, Skate, Ensemble) kept $F/F_{MSY}>1$ over the short- and long-term 315 (Figure 4A). For the ES-FM and ES-FSPR methods, there was not a consistent pattern in 316 exploitation rates when comparing the short- and long-term periods (Figure 4A). 317

As expected, application of a buffer to the catch advice resulted in lower exploitation rates compared to no buffer across all methods, but the magnitude of the impact differed by method(Figure 4B). Use of the buffer tended to result in greater reductions in F for the poor-performing methods that resulted in $F/F_{MSY} >> 1$. Methods like AIM, ES-FM, ES-FSPR, ES-Fstable and Skate all had large reductions in F when the buffer was applied, but

the reduction was insufficient to reduce $F/F_{MSY} < 1$ (Figure 4B). For some methods (CC-FM, CC-FSPR, SCAA), the median F/F_{MSY} was always below 1 with or without the buffer, 324 whereas for other methods (DLM, ES-Frecent, Islope, Ismooth, Itarget, and Ensemble) there 325 were instances where using a buffer pushed F/F_{MSY} below 1 (though it depended on the 326 exploitation history; Figure 4B). 327 The median performance measures reported thus far do not express the full range of results 328 across individual runs, however. When all the simulations are plotted, there is clearly a wide 329 range of possible outcomes for the population, indicating that performance for a particular se-330 ries of environmental conditions, expressed through recruitment deviations, can vary widely. 331 For example, Figure 5 shows the long-term average SSB/SSB_{MSY} and C/MSY relationship 332 across runs for a single scenario. Different patterns in the relationship between the SSB and 333 catch ratios resulted, with methods falling into two groups. In the first group, there is a near linear relationship between SSB/SSB_{MSY} and C/MSY (AIM, ES-Fstable, ES-FSPR, ES-335 M, Itarget, Skate, Ensemble, and SCAA; Figure 5). In the second group (CC-FSPR, CC-FM, 336 DLM, ES-Frecent, Ismooth, and Islope) have a much more diffuse relationship, with a wide 337 range of C/MSY for a given SSB/SSB_{MSY} . The linear or diffuse relationships persisted 338 across scenarios, although the upper limit of C/MSY was greatly reduced for the diffuse 339 methods when the buffer was applied to the catch advice. 340

Discussion

A range of a data-limited methods for setting catch advice was evaluated for stocks where assessment models may be rejected due to strong, positive retrospective patterns. A method was considered to perform well if it limited overfishing without resulting in light exploitation rates ($F \ll F_{MSY}$), thereby allowing depleted stocks to recover to SSB_{MSY} (or for healthy stocks to remain there), and for high and stable catches (close to MSY). Overall, none of the methods evaluated performed best across the scenarios exploring the different sources of

the retrospective pattern (unreported catch or increasing M) and different levels of historical fishing intensity. A number of methods did perform well in many cases, however, while others 349 performed consistently poorly, resulting in frequent and intense overfishing $(F >> F_{MSY})$. 350 Currently, in the Northeast U.S., if an assessment model is rejected due to a large rho 351 value, the catch advice from that model is ignored and some data-limited approach is used. 352 However, the rho-adjusted SCAA model performed better than a number of the alternatives 353 explored here. Therefore, there should not necessarily be an expectation that a data-limited 354 method will perform better than the rejected assessment model. The SCAA only resulted 355 in high exploitation rates $(F >> F_{MSY})$ when catches were unreported and the stock was 356 in good condition (SSB SSB_{MSY}). In contrast, this method was particularly effective when the stock was depleted and there was uneported catch. When M was the source of the retrospective pattern, the rho-adjusted SCAA method typically resulted in light exploitation rates, on average. 360

The methods that adjusted recent average catches based on trends in the survey (I_{smooth} and 361 I_{slope}) also performed well overall. The method using the expanded survey biomass with the 362 recent exploitation rate (ES - Frecent) performed quite similarly to I_{smooth} overall. Only 363 when there were unreported catches and the stock was depleted did these three methods 364 result in high Fs and limited stock recovery. Another benefit of these methods is that they 365 had low interannual variability in catch advice, with I_{slope} I_{smooth} consistently having the 366 lowest catch variability of all the methods evaluated. The I_{smooth} method is currently used 367 to set catches for Georges Bank cod (NEFSC (2019)) and red hake (*Urophycis chuss*; CITE). 368 Variations of the ES-Frecent are used for witch flounder and GB yellowtail flounder (I said 369 variations here to account for the SSC - not sure if we want to expand more on this). While 370 the findings here generally support the continued use of the I_{smooth} and $ES_{F}recent$ methods, 371 they may not be well suited for depleted stocks where unreported catches are believed to be an issue (I realize GB cod fits this description quite well, but I don't know if we want to 373 raise that issue here and advocate for a more conservative option given all the issues with the recent $GB \ cod \ quota$.

Three methods were consistently risk-averse across scenarios, limiting the frequency and 376 magnitude of overfishing and resulting in high stock biomass. These methods were the two 377 catch curve options (CC - FM) and CC - FSPR) and DLM. The catch curve methods 378 produced a wider range of average catches across scenarios, and also had greater interannual 379 variability in catches compared to DLM. While the lower exploitation rates from these 380 approaches may be undesirable due to foregone yield, there may be circumstances where 381 they are preferred. For example, for stocks that are believed to be heavily depleted, low 382 exploitation rates would allow for a more rapid recovery. 383

A number of methods performed poorly, particularly when catches were unreported. These 384 methods include three of the expanded survey biomass approaches (ES-Fstable, ES-FM,385 ES-FSPR), AIM, and Skate. The AIM model has been widely used across stocks in 386 the region (NEFSC (2002); NEFSC (2005); NEFSC (2008)), although there is a decreasing 387 trend in its use across model resistant stocks in the region (NEFSC (2019)). The findings 388 here suggest that alternative approaches should be considered in cases where AIM is still 389 used and there is concern over unreported catches. The Skate method is used to manage the 390 skate complex in the Northeast U.S. (a group of seven co-managed species). Interestingly, 391 six of the seven species are considered in good condition with high survey biomass indices in 392 recent years (CITE). That the Skate method performed poorly in our analysis but performs 393 well for the skate complex illustrates how the performance of methods in this analysis may 394 be sensitive to the scenarios and species life history considered. Therefore, care is needed 395 when trying to generalize these results across stocks that may have different life histories, 396 exploitation histories, and without unreported catches or increases in M. 397

An interesting finding of this study is the linear versus diffuse patterns between SSB and catch across methods. These patterns have implications for the trade-offs among methods, with linear relationships resulting in more consistent exploitation rates across stock

- sizes. Therefore, these methods have higher certainty of a given catch at a given stock size.
- However, they also tended to result in lower stock sizes, on average, across methods. The
- more diffuse relationships resulted in more variable exploitation rates across stock sizes, with
- some situations where the population biomass was quite high but the catch was low (relative
- to MSY), resulting in a very low F. The reasons behind these different patterns remains
- unclear, and future work to explore these patterns is warranted.
- Paragraph on the overall difference between catch and M? Not sure if we want to get into
- this because we'll have to raise the issue of the different reference points.
- This study is a first attempt to identify suitable methods for setting catch advice when stock
- assessment models are rejected due to large, positive retrospective patterns. Although no
- single method performed best across scenarios, a number of generally suitable and unsuitable
- methods were identified under specific conditions. The results of this work can help scientists
- and managers select a subset of possible options for consideration to set catch advice when
- assessment models are rejected. The approach developed here can, and should be expanded
- to consider other cases not explored here, as performance of individual methods os very likely
- 416 case-dependent.

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- Generic statuent about views expressed not reflecting NOAA... Anything else?

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Tables

543 Table 1.

Age	Maturity	Weight (kg)	Fishery	Fishery
			Selectivity	Selectivity (after
			(before change if	change if
			applicable)	applicable)
1	0.04	0.15	0.07	0.02
2	0.25	0.5	0.17	0.05
3	0.6	0.9	0.36	0.12
4	0.77	1.4	0.61	0.27
5	0.85	2.0	0.81	0.50
6	0.92	2.6	0.92	0.74
7	1.0	3.2	0.97	0.89
8	1.0	4.1	0.99	0.96
9	1.0	5.9	1.0	0.99
10+	1.0	9.0	1.0	1.0

Method	Details
Ismooth	$C_{targ,y+1:y+2} = \overline{C}_{3,y}(e^{\lambda})$ where $\overline{C}_{3,y}$ is the most recent
	three year average $\overline{C}_{3,y} = \frac{1}{3} \sum_{t=1}^{t=3} C_{y-t}$ and λ is the slope
	of a log linear regression of a LOESS-smoothed average
	index of abundance (spring and fall) with span $= 0.3$:
	$\hat{I}_y = loess(\hat{I}_y)$ and $LN(\widehat{I}_y) = b + \lambda y$
Islope	$C_{targ,y+1:y+2} = 0.8\overline{C}_{5,y}(1+0.4e^{\lambda})$ where $\overline{C}_{5,y}$ is the most
	recent five-year average catch through year $y-1$:
	$\overline{C}_{5,y} = \frac{1}{5} \sum_{t=1}^{t=5} C_{y-t}$ and λ is the slope of a log-linear
	regression of the most recent five years of the averaged
	index.
Itarget	$C_{targ,y+1:y+2} = \left[0.5C_{ref}\left(\frac{\overline{I}_{5,y} - I_{thresh}}{I_{target} - I_{thresh}}\right)\right] \overline{I}_{5,y} \ge I_{thresh}$
	$C_{targ,y+1:y+2} = \left[0.5C_{ref} \left(\frac{\overline{I}_{5,y}}{I_{thresh}}\right)^2\right] \overline{I}_{5,y} < I_{thresh} C_{ref} \text{ is}$
	the average catch over the reference period (years 26
	through 50): $C_{ref} = \frac{1}{25} \sum_{y=26}^{y=50} C_y I_{target}$ is 1.5 times the
	average index over the reference period:
	$I_{target} = \frac{1}{25} \sum_{y=26}^{y=50} \overline{I}_y \ I_{thresh} = 0.8 \ I_{target}$, and is the most
	recent five year average of the combined spring and fall
	index: $\overline{I}_{5,y} = \frac{1}{5} \sum_{t=1}^{t=5} \overline{I}_{y-t+1}$
skate	$C_{targ,y+1:y+2} = F_{rel}\overline{I}_{3,y}$ where $F_{rel} = median\left(\frac{\overline{C}_{3,\mathbf{Y}}}{\overline{I}_{3,\mathbf{Y}}}\right)$ is
	the median relative fishing mortality rate calculated
	using a 3 year moving average of the catch and average
	survey index across all available years (\mathbf{Y}) :
	$\overline{C}_{3,y} = \frac{1}{3} \sum_{t=1}^{t=3} C_{y-t}$ and $\overline{I}_{3,y} = \frac{1}{3} \sum_{t=1}^{t=3} I_{y-t+1}$
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Method	Details	
An Index Method (AIM)	AIM first calculates the annual relative F :	
	$F_{rel,y} = \frac{C_y}{\frac{1}{3} \sum_{t=1}^{t=3} \overline{I}_{y-t+1}}$ and the annual replacement ratio:	
	$\Psi_y = \frac{\bar{I}_y}{\frac{1}{5}\sum_{t=5}^{t=5}\bar{I}_{y-t}}$. These values are used in a regression:	
	$LN(\Psi_y) = b + \lambda LN(F_{rel,y})$ to determine $F_{rel,*}$, which is	
	the value of $F_{rel,y}$ where the predicted $\Psi = 1$ or	
	$LN(\Psi) = 0$. $F_{rel,*}$ is called either the "stable" or	
	"replacement" F , and is used to calculate the target	
	catch: $C_{targ,y+1:y+2} = \overline{I}_y F_{rel,*}$.	
Dynamic Linear Model (DLM)	Langan (2021).	
Expanded survey biomass	$C_{targ,y+1:y+2} = B_{\bar{I},y}\mu_{targ}$ where $B_{\bar{I}}$ is the average of	
method 1 $F_{40\%}$ (ES-FSPR)	estimated fully-selected biomass from each survey:	
	$B_{\bar{I},y} = \frac{1}{2} \left(\frac{I_{spr,y}}{q_{spr}} + \frac{I_{fall,y-1}}{q_{fall}} \right)$ and target exploitation	
	fraction, μ_{targ} is calculated as: $\mu_{targ} = \frac{F_{targ}}{Z_{targ}} \left(1 - e^{-Z_{targ}} \right)$	
	$F_{targ} = F_{40\%}$ and $Z_{targ} = F_{targ} + M$	
Expanded survey biomass	Same as the above expanded survey method, but with	
method 2 $F = AIM$	μ_{targ} equal to the stable exploitation fraction $F_{rel,*}$	
replacement (ES-Fstable)	calculated using the AIM approach (see above).	
Expanded survey biomass	Same as the above expanded survey methods, but with	
method 3 $F = M$ (ES-FM)	the target exploitation rate set to the assumed M :	
	$F_{targ} = M.$	
Expanded survey biomass	Same as the above expanded survey methods, but with	
method 4 F = recent average	the target exploitation fraction set to the most recent	
(ES-Frecent)	three year average exploitation fraction: $\mu_{targ} = \frac{\sum_{y=2}^{y} \mu_y}{3}$	
	$\mu_y = rac{C_{y-1}}{B_{ar{I},y}}$	

Method	Details	
Catch curve Method 1 $F_{40\%}$	$C_{targ,y+1:y+2} = \frac{F_{targ}}{Z_{avg,y}} B_{cc,y} \left(1 - e^{-Z_{avg,y}}\right)$ where B_{cc} is the	
(CC-FSPR)	estimated biomass: $B_{cc,y} = \frac{C_{y-1}}{\frac{F_{avg,y}}{Z_{avg,y}} \left(1 - e^{-Z_{avg,y}}\right)}$ with	
	$Z_{avg,y} = \frac{Z_{spring,y} + Z_{fall,y-1}}{2} F_{avg,y-1} = Z_{avg,y-1} - M \text{ and,}$	
	$F_{targ} = F_{40\%}.$	
Catch curve Method 2 ${\cal M}$	Same as catch curve method 1 above, but with	
(CC-FM)	$F_{targ} = M.$	
Ensemble	Median of catch advice provided by AIM, CCFSPR,	
	ES-Frecent, ES-FSPR, Islope, Itarget, Ismooth, and	
	Skate methods.	

545 Table 3.

Position	Factors	Values
1	retrospective source	C = catch M = natural mortality
		N = none
2	fishing history	F = Fmsy in second half of base
		period $O = overfishing$
		throughout base period
3	fishery selectivity blocks	1 = constant selectivity 2 =
		selectivity changes in second half
		of base period
4	catch advice multiplier	A = applied as is from IBM R =
		reduced (multiplied by 0.75) from
		IBM

Figures 546

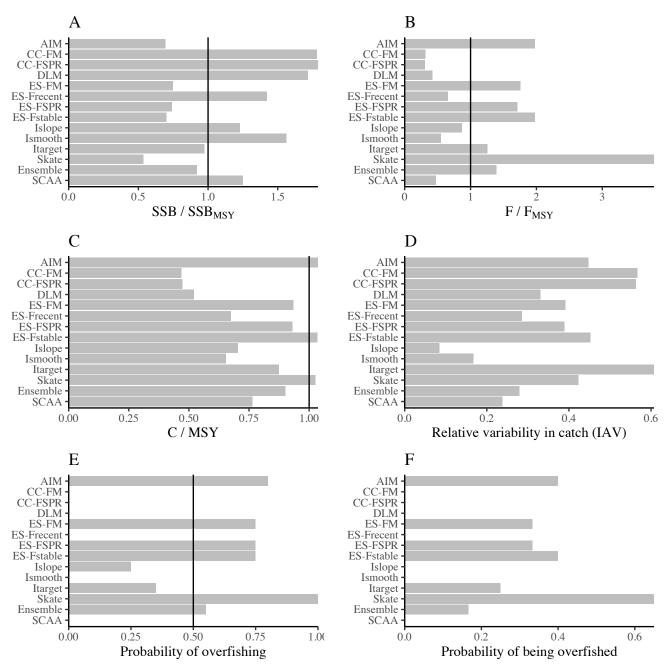


Figure 1: Median performance measures across all scenarios and runs for each method. Vertical lines are shown at a value of 1 for the performance measures that are relative to the MSY reference points (A,B,C), and at a value of 0.5 for the probability of overfishing (E).

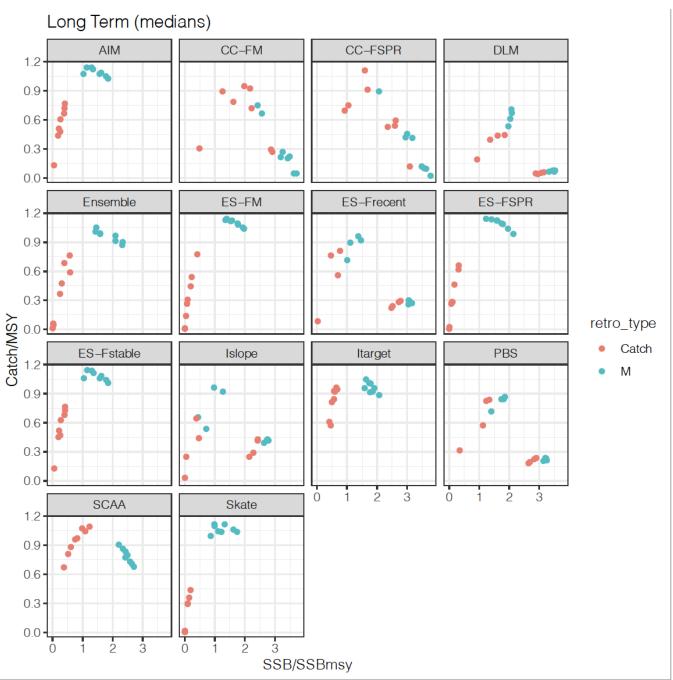


Figure 2: Relationship between long-term average spawning biomass and average catch (relative to MSY levels) for each method. Each point represents the median for a given scenario, separated by the source of the retrospective pattern (catch or M). **NOTE to coauthors: this was taken from the mass output figures Chris provided. If we want to keep this we'll want to 1) change font to Times, 2) reorder to consistent with other Figs (alphabetical except for Ensebmle and SCAA which are last), 3) change the points for retro source so distinguishable in BandW, 4 change X axis title to SSB_{MSY}).

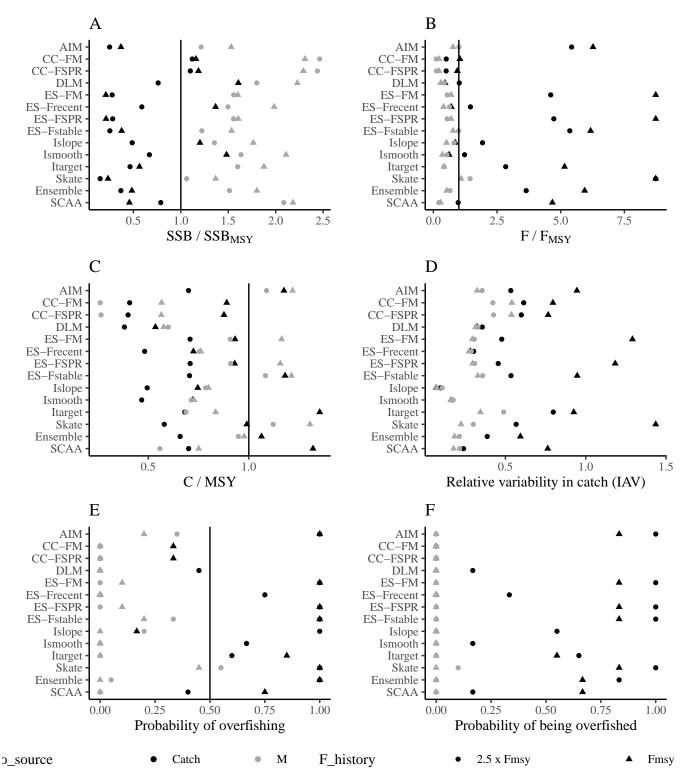


Figure 3: Median performance measures for each method, with separated out by the source of the retrospective error (catch = black, M = gray) and the exploitation history in the base period (always overfishing at $2.5xF_{MSY}$ (circle), or F reduced to F_{MSY} during base period (triangle)). Vertical lines are shown at a value of 1 for the performance measures that are relative to the MSY reference points (A,B,C), and at a value of 0.5 for the probability of overfishing (E).

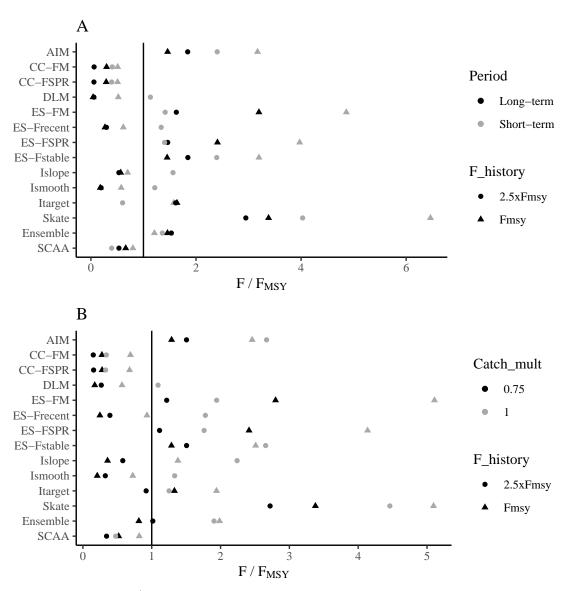


Figure 4: Median F/F_{MSY} for each method, with results separated by the exploitation history in the base period (always overfishing at $2.5xF_{MSY}$ (circle), or F reduced to F_{MSY} during base period (triangle)) showing A) short- (gray) versus long-term (black) values, and B) with (black) or without (gray) a buffer applied when setting the catch (catchmult = 0.75 or 1).

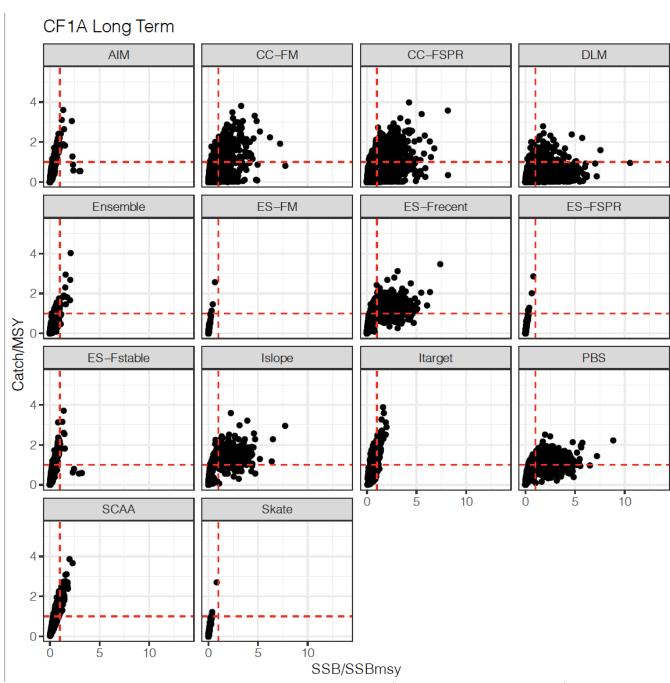


Figure 5: Relationship between long-term average catch / MSY and average SSB/SSB_{MSY} by method. Each point represents the average for a single iteration for the scenario where catch was the source of the retrospective pattern with F reduced to F_{MSY} in the second half of the base period, there was a single selectivity block, and where no buffer was applied to the catch advice (catch multiplier = 1).