05/06/2020 telescoping method

In [1]:

```
import numpy
from sympy import *
```

In [6]:

```
def telescoping method(function, point, n t, precision):
                x = Symbol('x')
                a = point - 1
                b = point + 1
                polynomial = series(function, x, x0=0, n=n t).removeO()
                chebyshev = LC(polynomial)*(b - a)**n t/2**(2*n t-1)*chebyshevt(n t, (2*x+a+
b)/(b-a)
                chebyshevN = lambdify(x, chebyshev, 'numpy')(point)
                while abs(chebyshevN) < precision:</pre>
                                  polynomial = polynomial - chebyshev
                                  n t -= 1
                                  chebyshev = LC(polynomial)*(b - a)**n t/2**(2*n t-1)*chebyshevt(n t, (2*n t-1)*chebyshevt(n t,
x+a+b)/(b-a))
                                  chebyshevN = lambdify(x, chebyshev, 'numpy')(point)
                polynomialN = lambdify(x, polynomial, 'numpy')(point)
                return {"value": polynomialN, "degree": n t}
```

In [7]:

```
def telescoping_method_list(function, points, n_t, precision):
    return [telescoping_method(function, point, n_t, precision)["value"] for poi
nt in points]
```

In [8]:

```
x = Symbol('x')
function = ln(1+x)
point = 0
n_t = 15
precision = 0.0001
telescope = telescoping_method(function, point, n_t, precision)
telescope
```

Out[8]:

```
{'value': -2.6157924107142856e-05, 'degree': 10}
```

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In [9]:

```
import matplotlib.pyplot as plt
import numpy as np
space = np.linspace(-0.99, 1, 20)
plt.figure(figsize=(12.8, 9.6))
plt.title('Cpaвнение точной функции и построенного приближения')
plt.plot(space, telescoping_method_list(function, space, n_t, precision), label=
'Приближение')
plt.plot(space, lambdify(x, ln(1+x), 'numpy')(space), label='Точная функция')
plt.legend()
plt.show()
```



