

LPS ECON-103-601, Fall 2015
Instructor: Kory Kantenga
HW Due 09.01.15

Math Prereqs

Please return to the Economics Department in the TA Box with your name *and my name* on it by 17.00 Tuesday, Sep 1. Show all work clearly and in order. Points will be awarded based on a correct solution. A solution should always justify the steps taken and explain the assumptions needed to reach a final answer (e.g. how do you know you are not dividing by zero in the last step?).

Q1

Suppose we observe the sequence $\{x_n, y_n\}_{n=1}^N$ and know that $y_n = b \cdot x_n + e_n$ but cannot observe $\{e_n\}_{n=1}^N$. Using all of the data available and one assumption of your choice on e_n .

- a) Determine your b .
- b) Is b unique for your assumption? Justify your answer.

Q2

Let $f(a) = \sum_{n=1}^N (x_n - a)^2 + (y - a)^2$. Characterise the extrema of f .

Q3

Let $\{a_n\}_{n=1}^N$ be a non-zero sequence. Are the following statements TRUE or FALSE? Justify your answers.

- a) $\left(\sum_n a_n\right)^m = \left(\sum_n a_n^m\right)$
- b) $\left(\sum_n a_n b_n\right) / \left(\sum_n a_n^2\right) = \sum_n \frac{a_n b_n}{\sum_n a_n^2}$

Q4

- a) Find a value of c such that $\int_a^b \int_0^x f(cx, y) dy dx = 1$ where $f(x, y) = x^2 y^3$.
- b) Find the Hessian of $f(x, y)$ (i.e. $\frac{\partial^2 f}{\partial x^2}, \frac{\partial^2 f}{\partial y^2}, \frac{\partial^2 f}{\partial x \partial y}$) where $f(x, y) = \cos(x^2 \sqrt{y})$. Is $f(x, y)$ convex, concave, neither or both? Justify your answer.