
Lab 2

CLINT OLSEN

ECEN 4532: DSP LAB

February 20, 2018



University of Colorado
Boulder

Contents

Introduction	2
Assignment 1	2
Assignment 2	2
Assignment 3	2
Assignment 4	5
Assignment 5	8
Assignment 6	11
Assignment 7	11
Assignment 8	11
Assignment 9	14
Assignment 10	17
Assignment 11	19
Code Appendix	23

Introduction

This lab is a continuation of the first lab in this course, which focused on low-level characteristics of audio analysis using MATLAB. In this lab, analysis will be continued on the same audio signals, but at a higher level of analysis. Aspects such as rhythm and tonality will be characterized for various genres and will be mathematically and graphically represented to show the correlation between the data analysis and tangible aural properties. This will be the beginnings of obtaining information about music that can lead to a better means of categorizing and organizing individual tracks autonomously.

Assignment 1

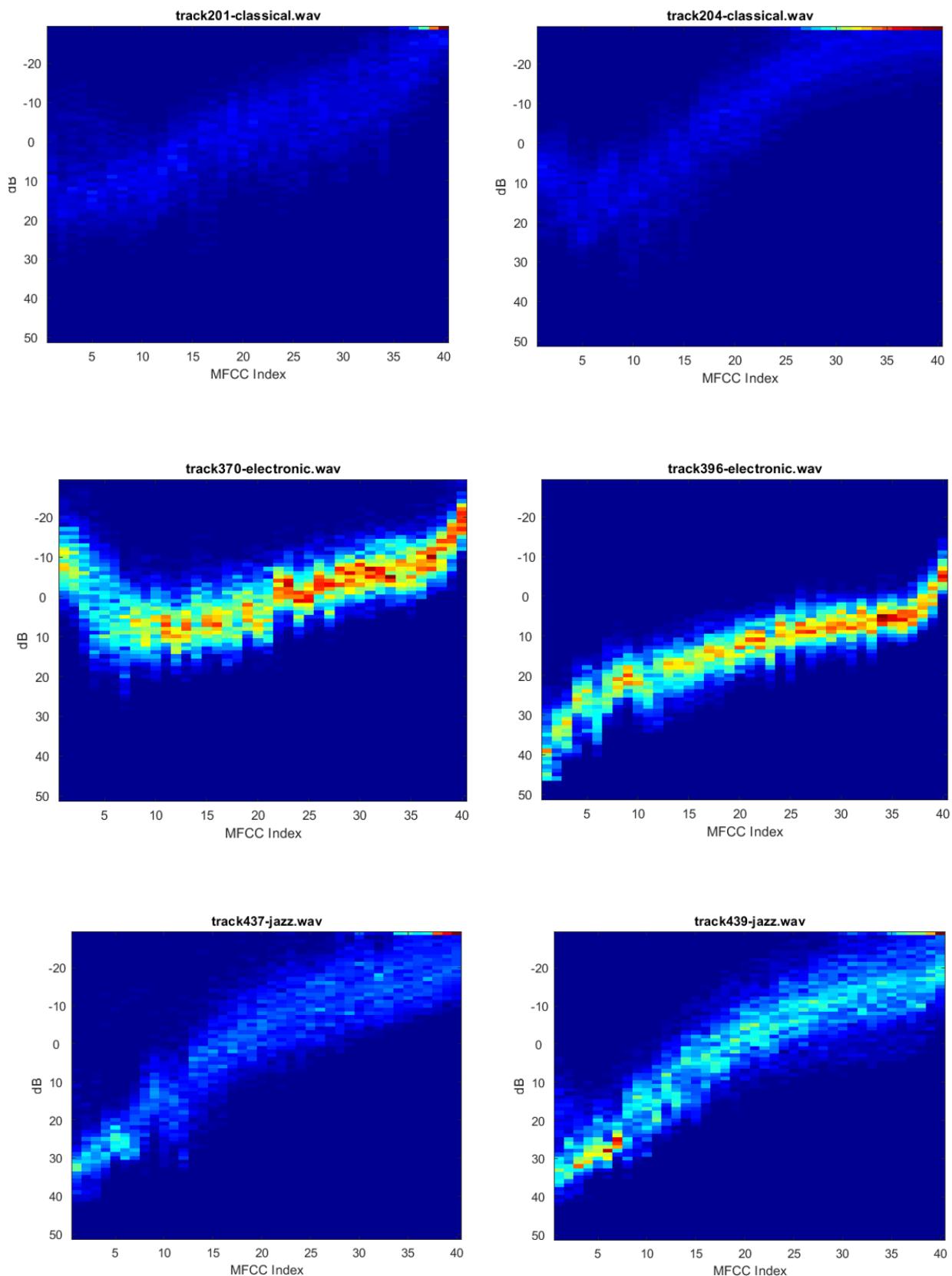
This assignment is just an extension of the last part of the previous lab, where the MFCC coefficients were calculated for describing the power distribution of the frequency content of a given signal after being passed through the 40 bank cochlear filter bank. Extra computation is performed here to convert the values of these coefficients to the dB scale. See Assignment 1 Appendix for MATLAB code.

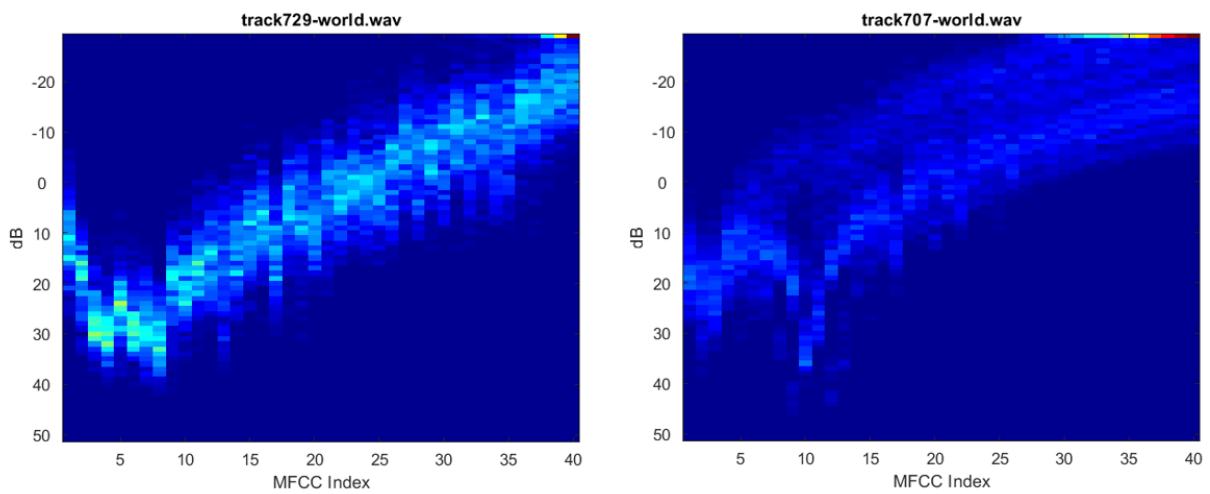
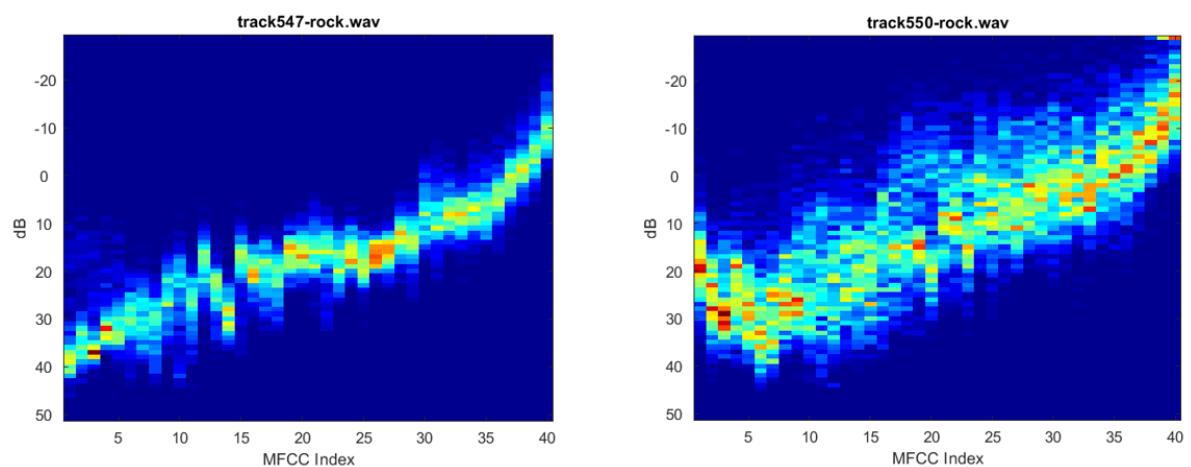
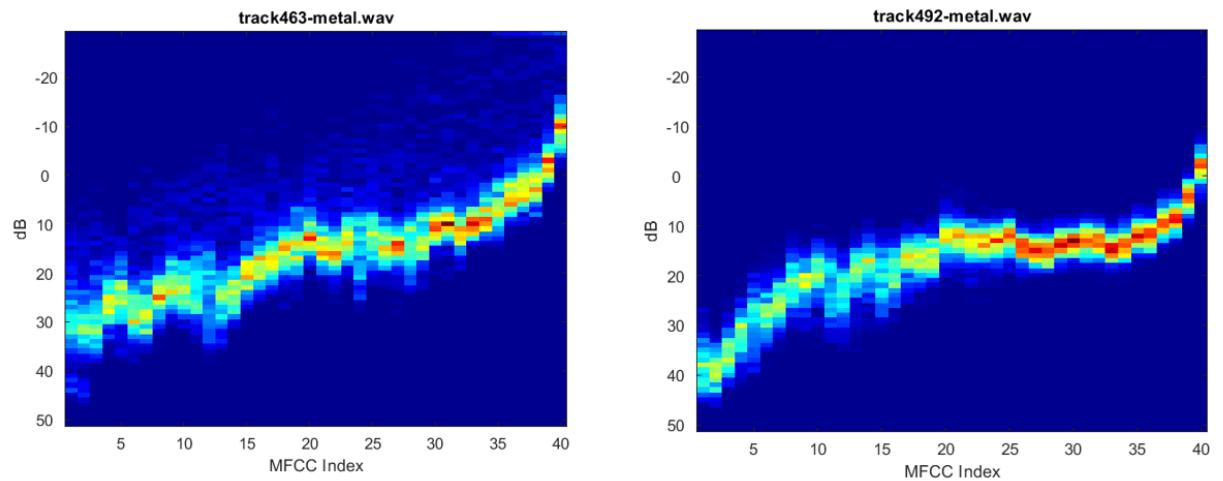
Assignment 2

In order to visualize the MFCC coefficients, this portion of the lab focuses on creating a 81×40 matrix of counts to characterize the intensity of the frequency content at different power levels for each frequency response of the cochlear filter bank. This is done by summing the number of times a given power level is achieved at a particular filter. The dimension of the matrix come from the range of the dB scale used (-20 to 60 dB) resulting in 81 rows in the matrix, and the 40 columns from the 40 MFCC coefficients for each filter banks used in the cochlear filter bank. The MATLAB code for the development of this matrix is shown in the Assignment 2 Appendix.

Assignment 3

Below are the plots associated with the spectral histogram for each of the 12 tracks:

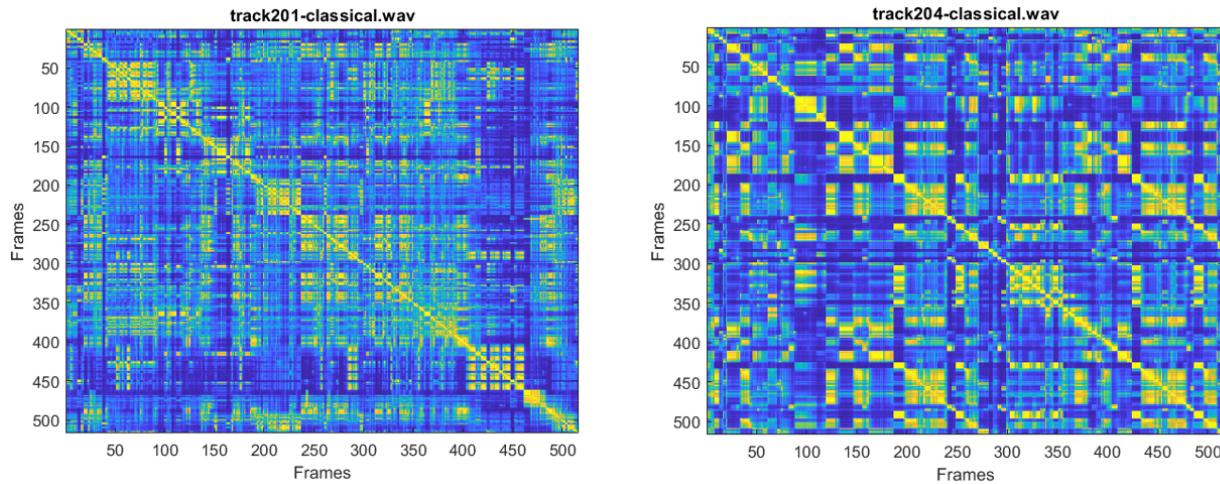


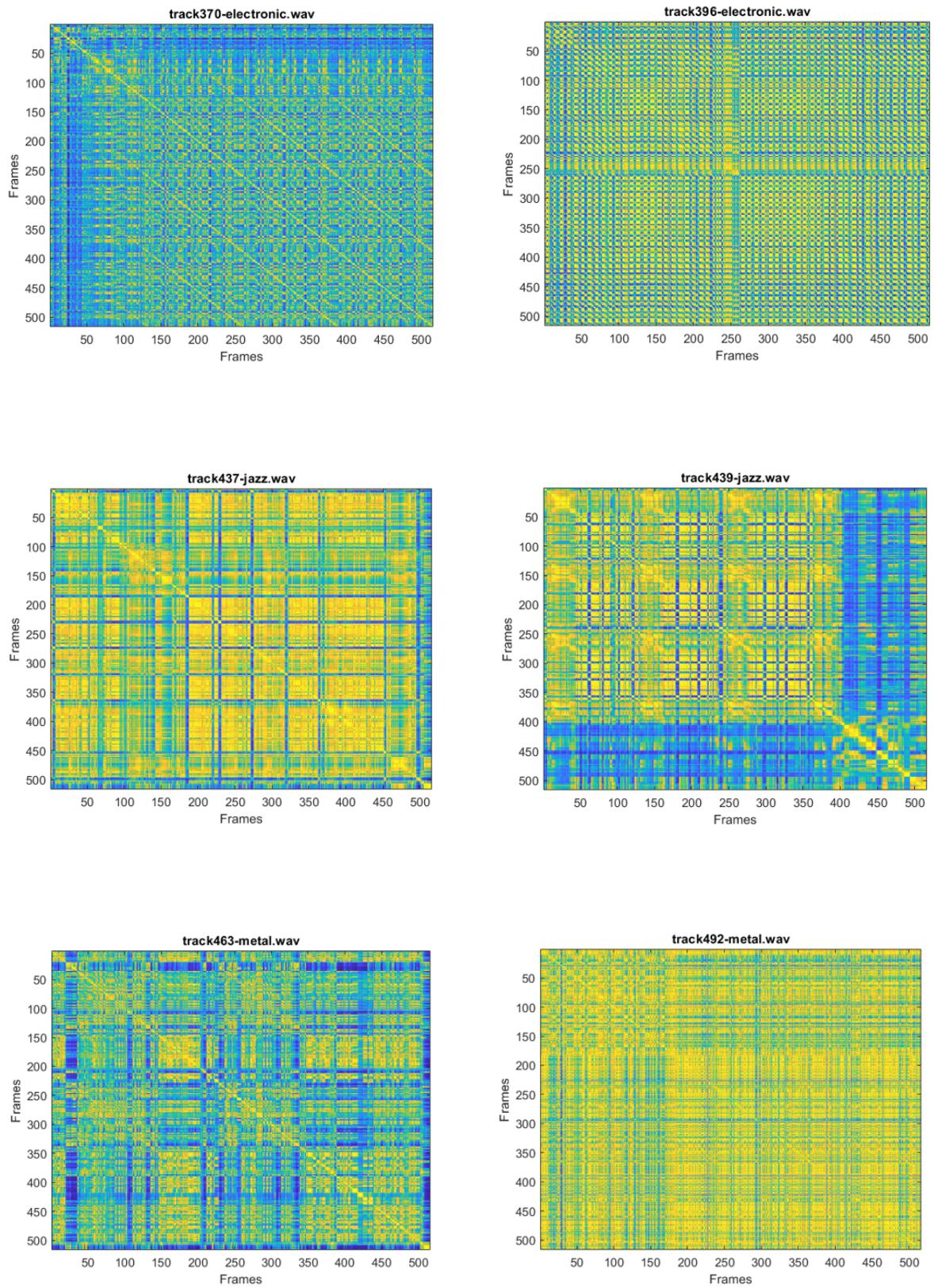


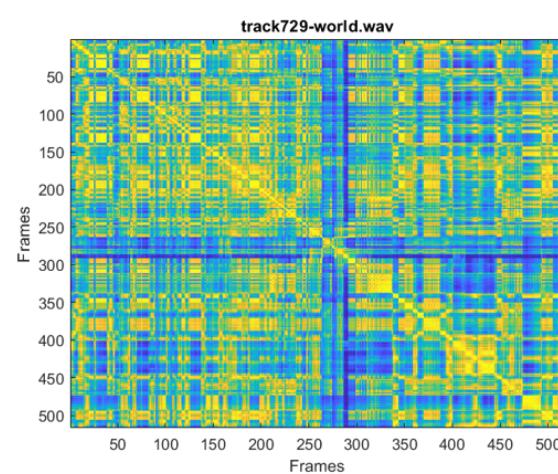
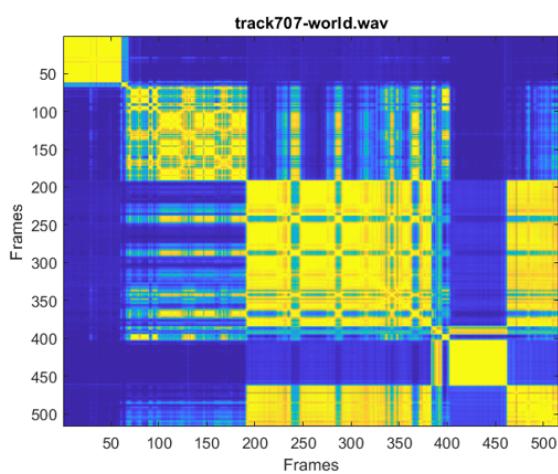
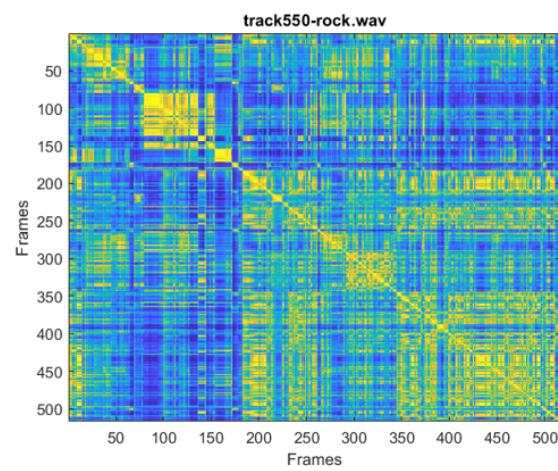
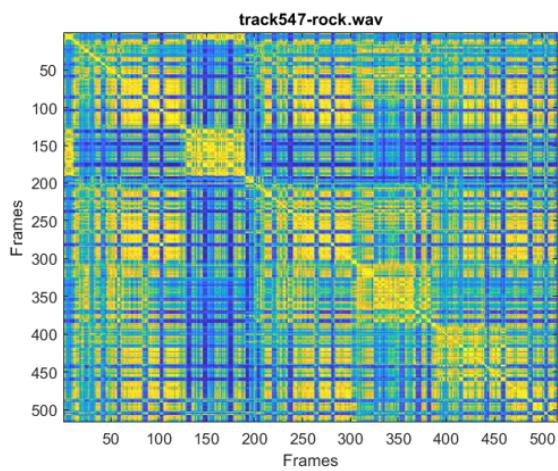
Many interesting things can be seen from the above plots. Each genre has a unique character to it in terms of the spectral intensity that correlates well to what is actually heard. For example, the metal tracks have many high intensity MFCC coefficients at a high decibel levels in comparison to a track such as jazz 437, which has some high count of low frequency components at high decibel values, but overall lacks the constant high power across frequencies that the metal tracks have. These graphs can give an overall impression of the dynamic quality of a track and what frequencies these dynamics occur, based on the MFCC coefficients.

Assignment 4

One way to begin building a sense of rhythm mathematically is to look at the similarity of vectors (in this case frames) within a given audio track. This can be done using the dot product which is a mathematical method to determine how "similar" two given vectors are. To start, each frame in an audio track can be dotted with each other to build a basic characterization of how similar frames are. This is shown for each track through the use of a similarity matrix constructed by the MATLAB code in the Assignment 4 Appendix:



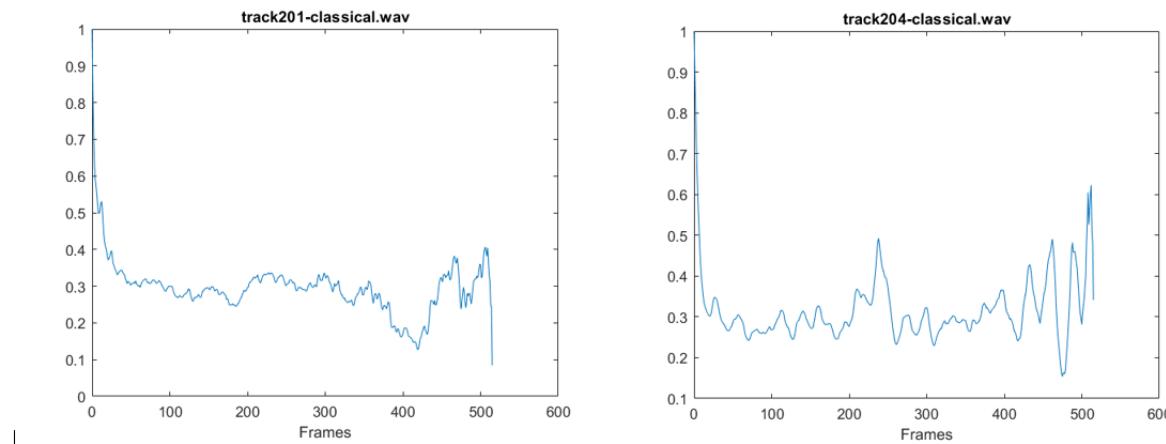


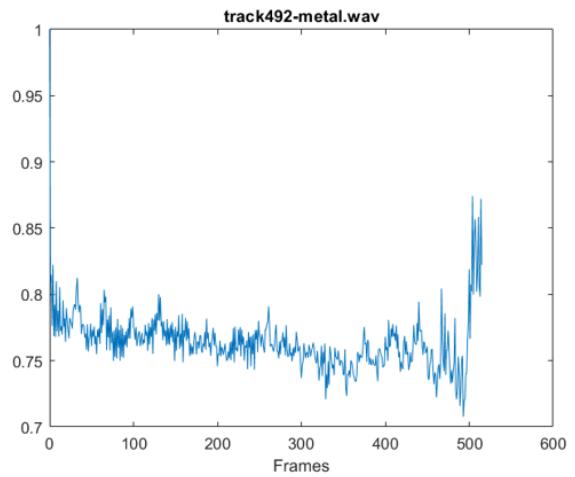
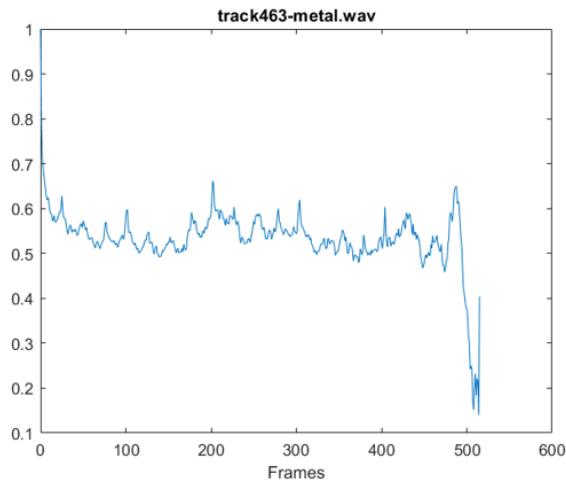
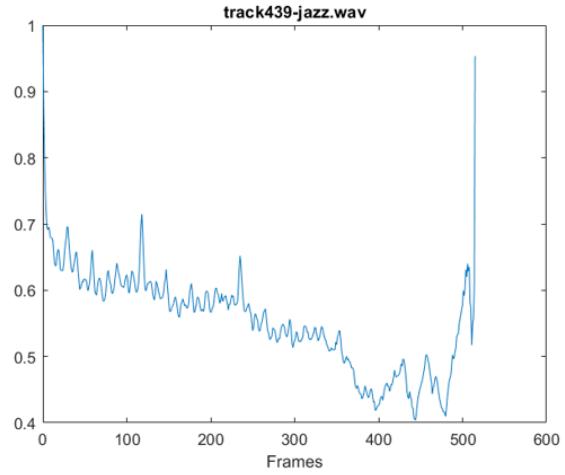
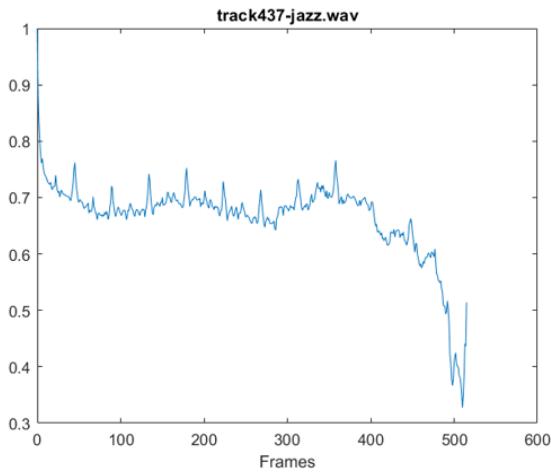
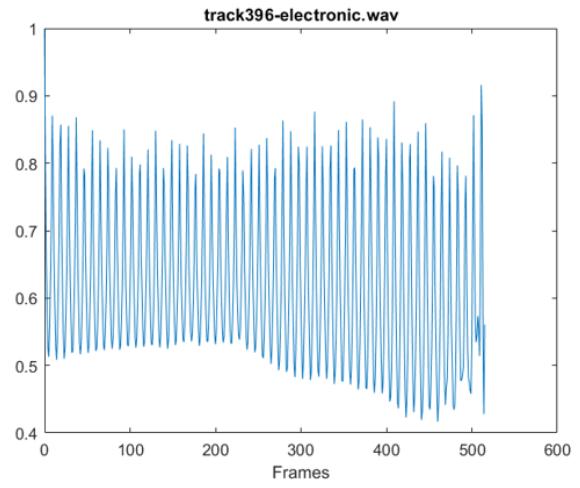
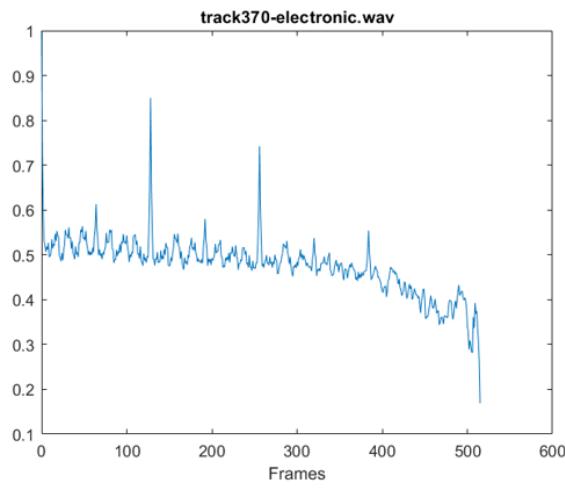


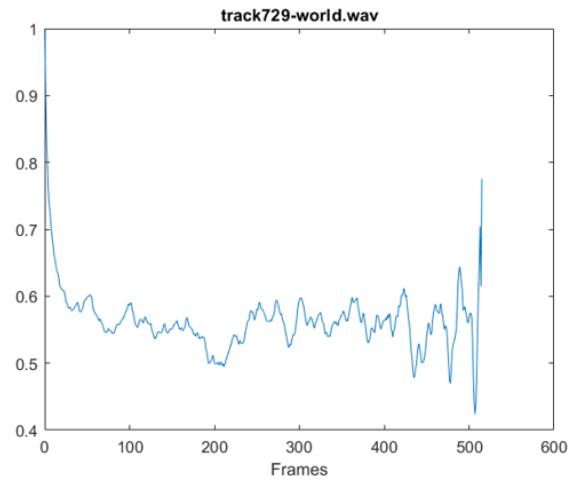
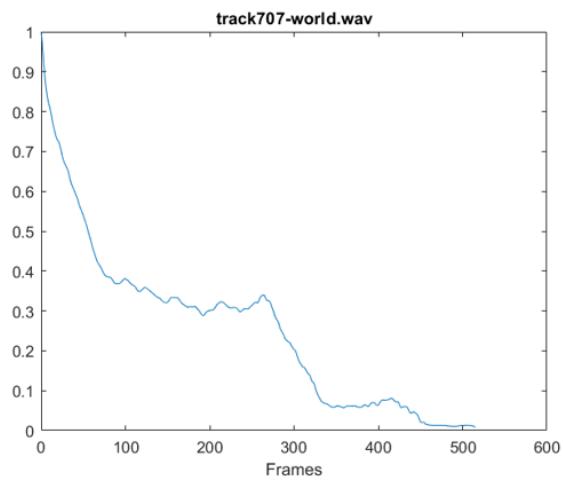
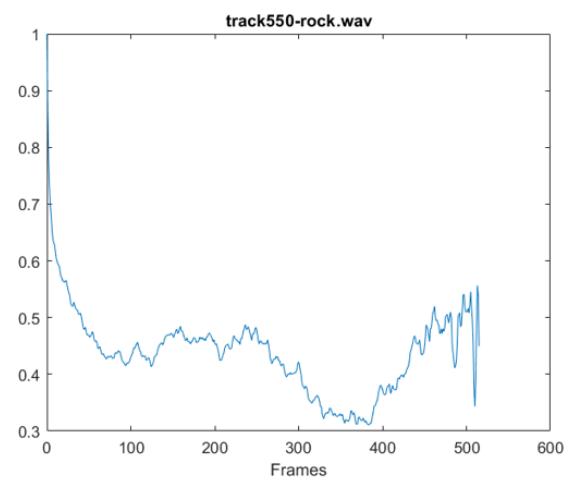
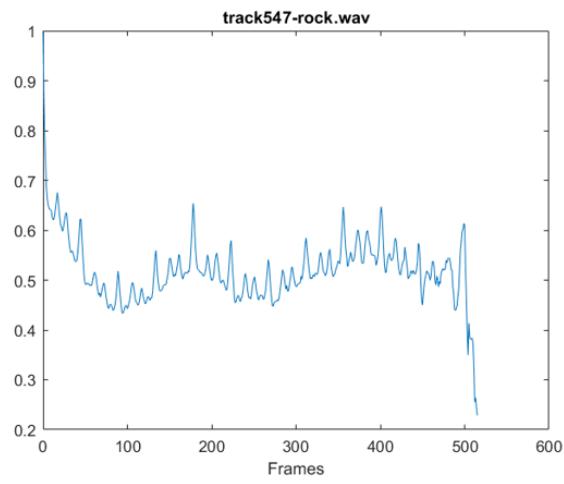
These interesting looking plots can give a lot of information regarding the audio characteristics of a audio track. Each index of the matrix holds the value of how "related" the frame at i is to a frame at j . The magnitude of this value is the dot product of the two frame vectors. Two interesting examples of this can show rhythmic consistency and sustained notes. In the electronic 396, it can be seen that the yellow colors are evenly separated, showing that most frames are similar to those of a particular number of frames away from them. Upon listening to this track, the electronic bass drum is very constant, so this even spacing gives a sense of the steady rhythm produced by the bass drum. In looking at the world 707 track, there are blocks of frames next to each other that share commonalities for long periods of time. This can be attributed to sustained notes over many frames that are evident when listening to track.

Assignment 5

As referenced in the last portion of the lab, the similarity matrix can give a sense of rhythm, if there is a consistent correlation between frames that are a certain distance apart. This is called lag between the frames, which can be used to begin determining the tempos within a track. This is done by summing all of the elements above the main diagonal in the similarity matrix, normalizing, and seeing for which lag value of l in the summation yields the highest result (See Assignment 5 Appendix for MATLAB code). This tells us the period between rhythmic repetition. Below is the results of this computation for the 12 tracks:







The best example to look at to understand these plots is the electronic 396 track. It can be seen that there are many evenly spaced spikes that correlate to high similarity to the number of frames away where that spike exists on the x axis. In this example, each spike is spaced multiples of a particular lag, which determines the tempo. However, looking at the classical and world tracks, the lack of consistent spikes indicates little presence of a set tempo, which is true in regards to the more free form nature of the genres. Also, rhythmic patterns cannot be seen because these genres do not have a strong tempo driving force like the bass drum in the electronic tracks.

Assignment 6

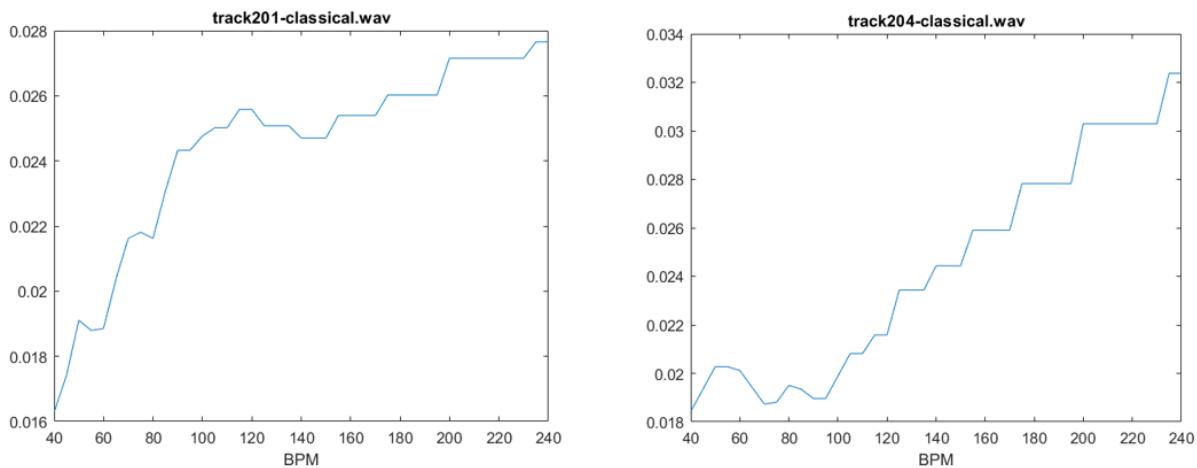
In order to determine the true tempo of a track in BPM, we can again use the similarity matrix. First, the median of the matrix must be determined for use in computing the lag value associated with a given tempo in beats per minute (BPM). The MATLAB code for this can be found in the Assignment 6 Appendix.

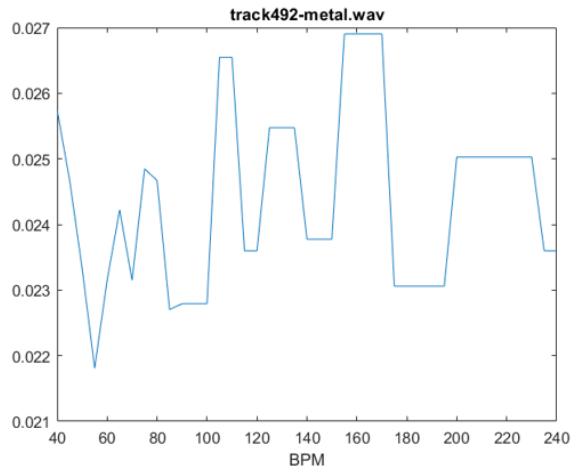
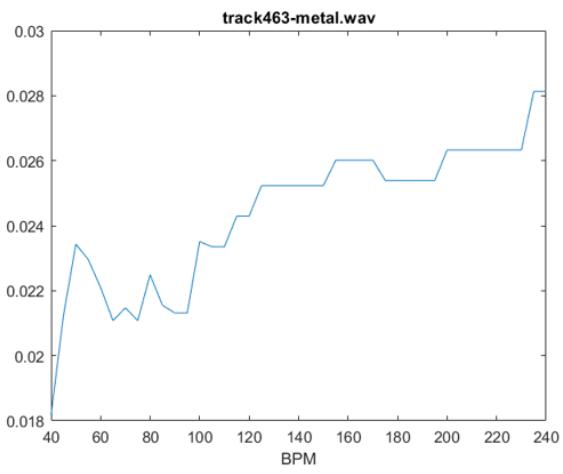
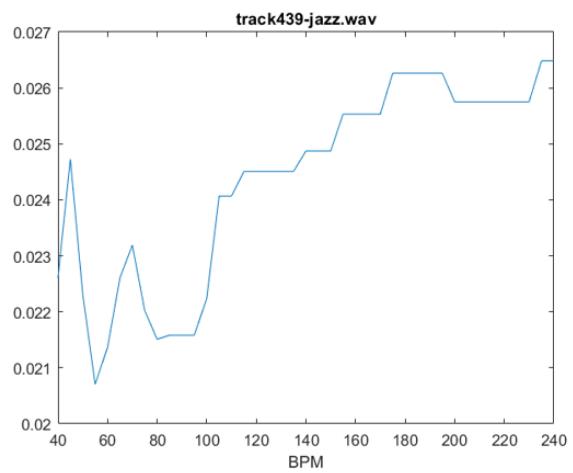
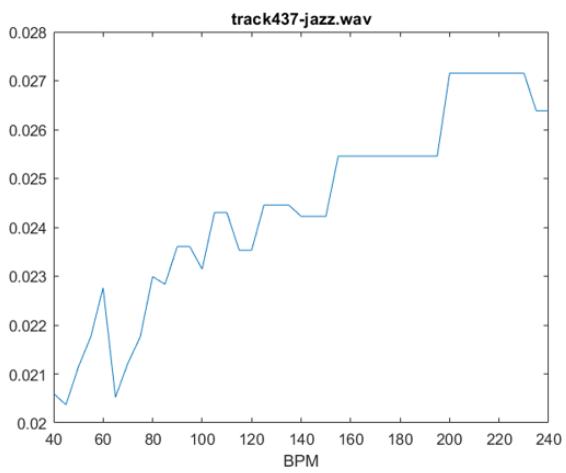
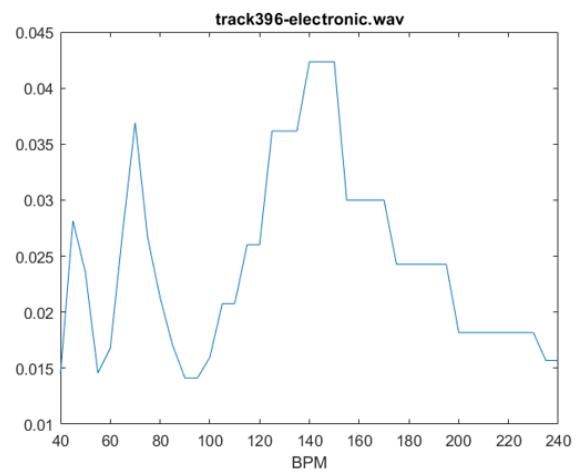
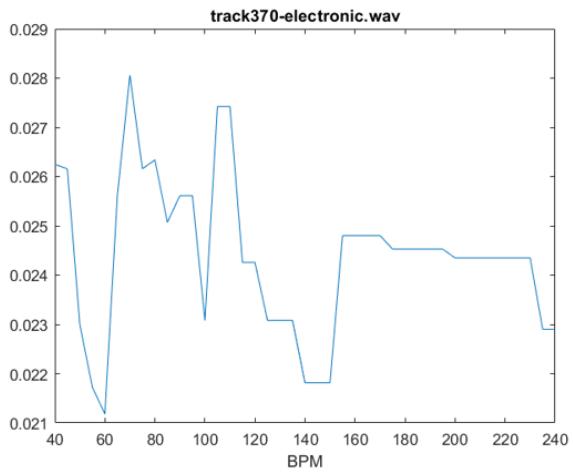
Assignment 7

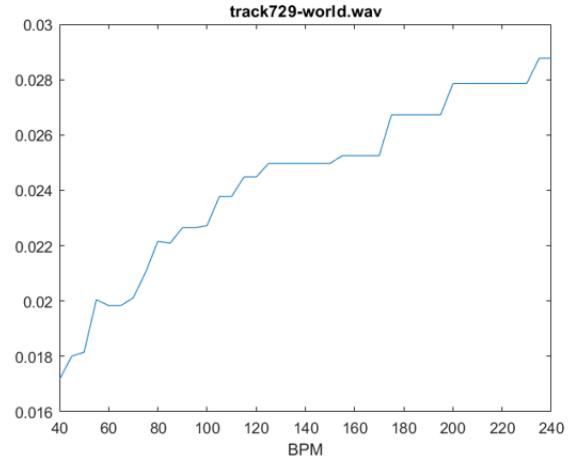
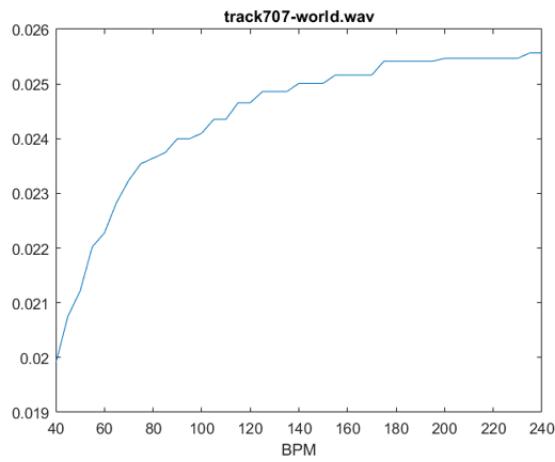
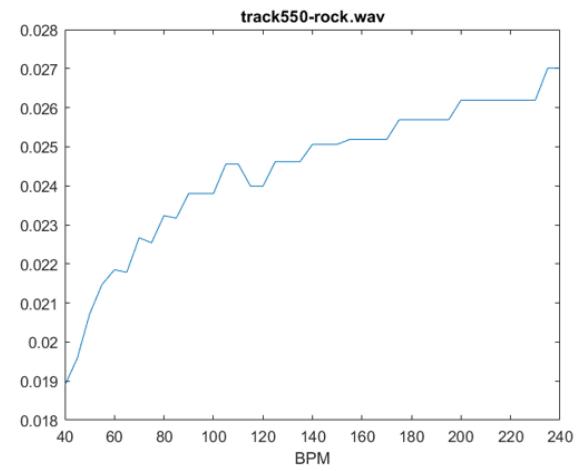
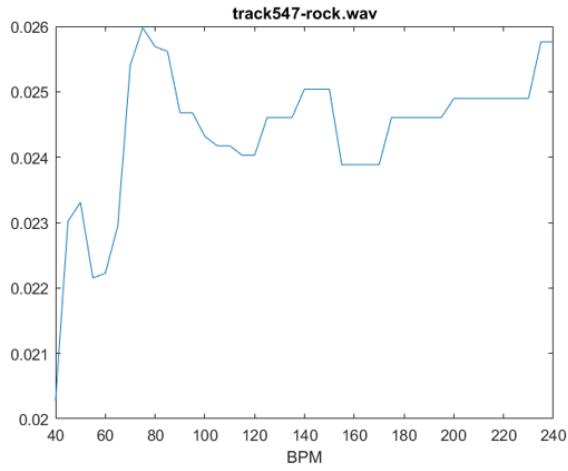
The next step in determining the BPM is to calculate the number of times that the similarity matrix is larger than the median of the matrix at various lag values correlated with BPM values from 40 to 240 in steps of 5 BPM. This will result in large counts for highly similar lags that are common throughout the track. The code for this is shown the Assignment 7 Appendix.

Assignment 8

Finally, a histogram of the BPM values determined for a track can be plotted for each of the 12 track:



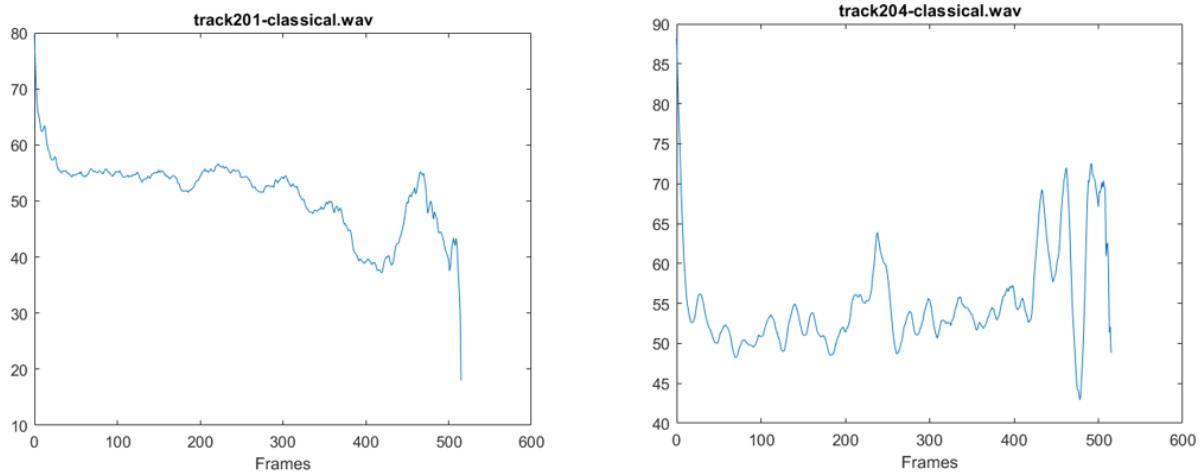


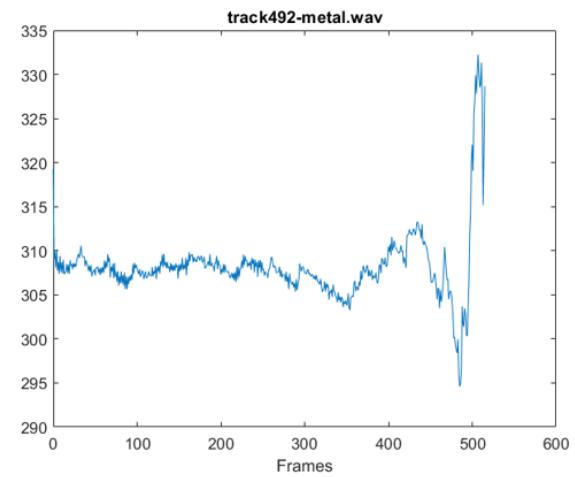
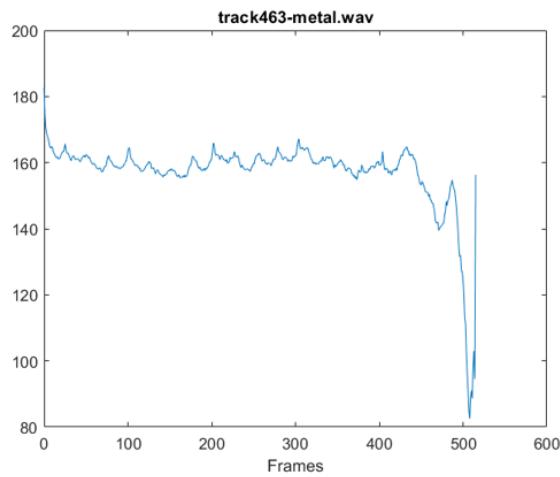
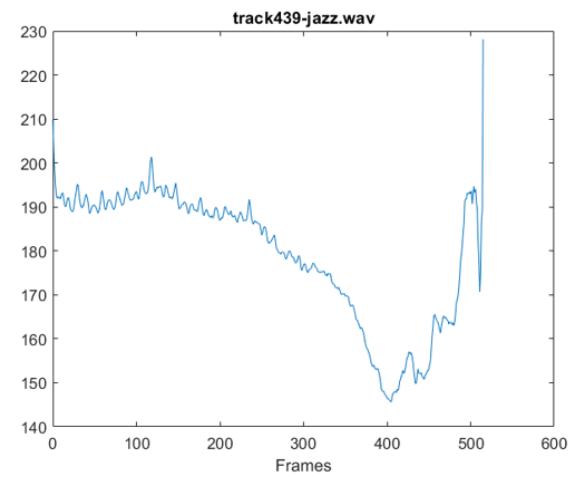
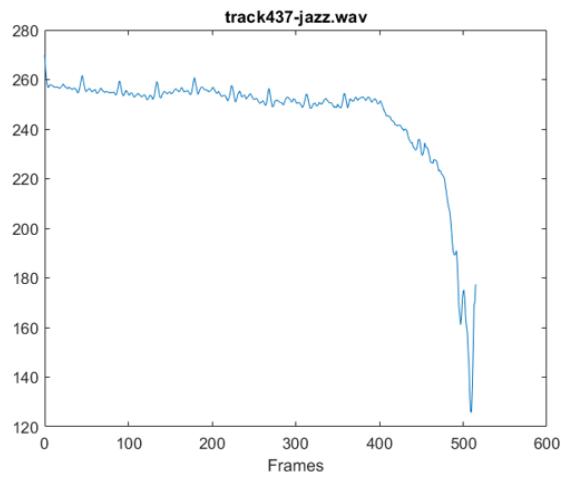
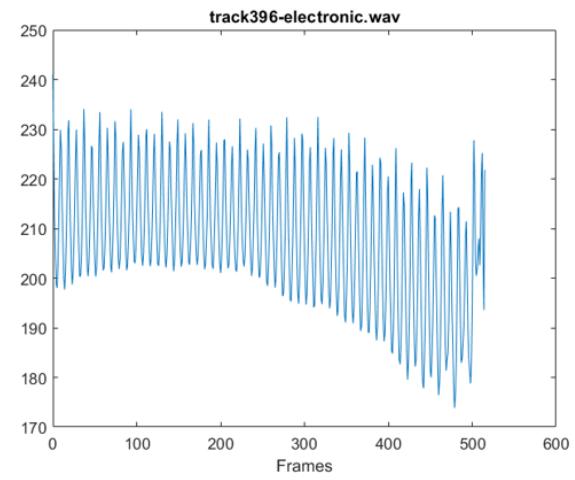
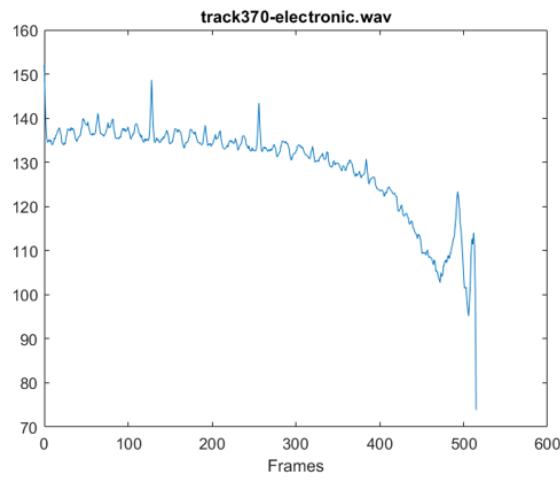


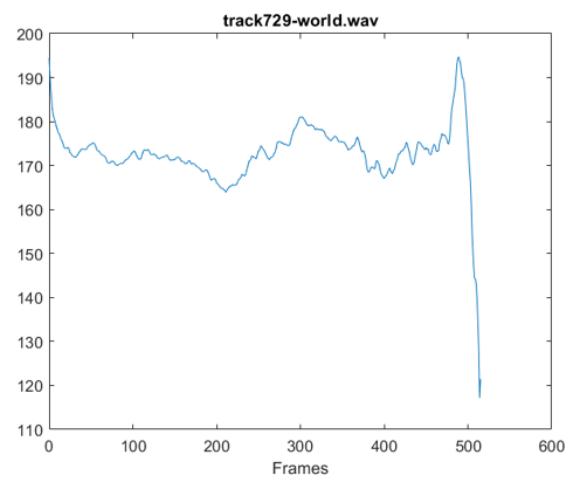
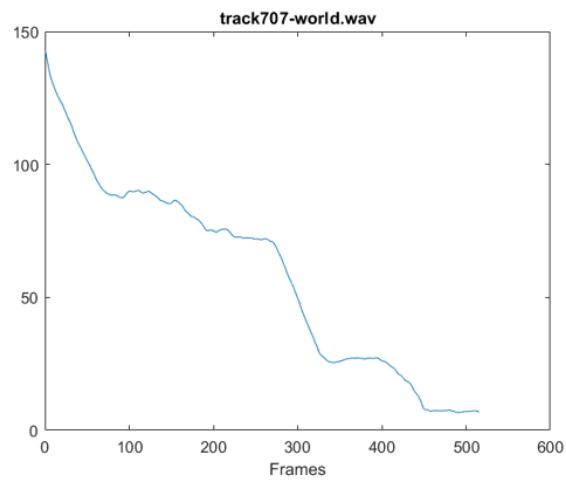
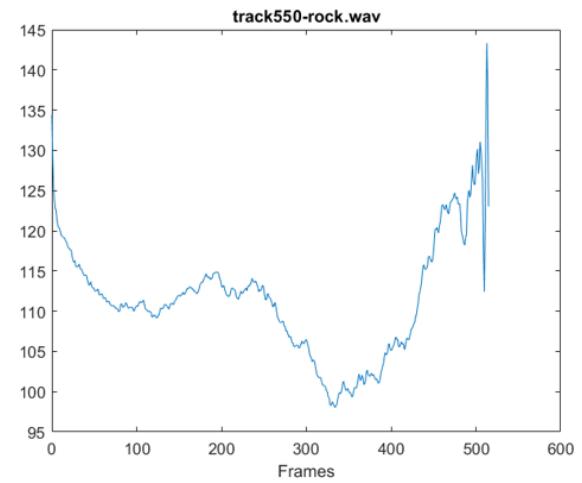
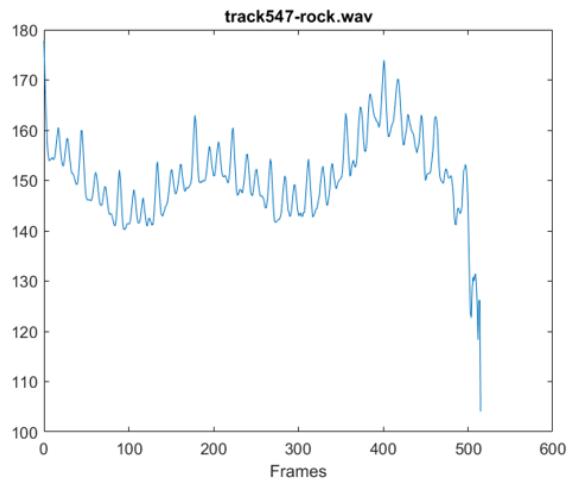
Once again, the electronic 396 track gives a great example of rhythmic consistency to understand what is occurring in the graph. A large spike can be seen right around 145 BPM, which means that the similarity matrix held many values greater than its median at the lag value that correlated to 145 BPM. Interestingly enough, I took the original track and tapped the tempo into a metronome tool, which showed the actual tempo of the song is 140 BPM, so this is a good approximation for the tempo of a given song. This is only true, however, if there is a strong rhythmic force driving the song, like the bass drum in electronic 396. The World 707 track is almost a perfectly smooth curve, which indicates there is nothing interesting that can be determined about the tempo, because in this case, the world track is more Rubato in tempo.

Assignment 9

In order to get an even better approximation for the rhythmic patterns within a track, the autocorrelation can be used instead of the previous algorithm in Assignment 5. The difference with this approach is that the correlation is found through taking the dot product of the similarity matrix with itself at different lag values to determine the lag that correlates with a particular BPM. This is a better approximation due to the need for a reference to compare the result with. The MATLAB code for this is shown in the Assignment 9 Appendix and the plots for the autocorrelation of the 12 tracks is shown below:



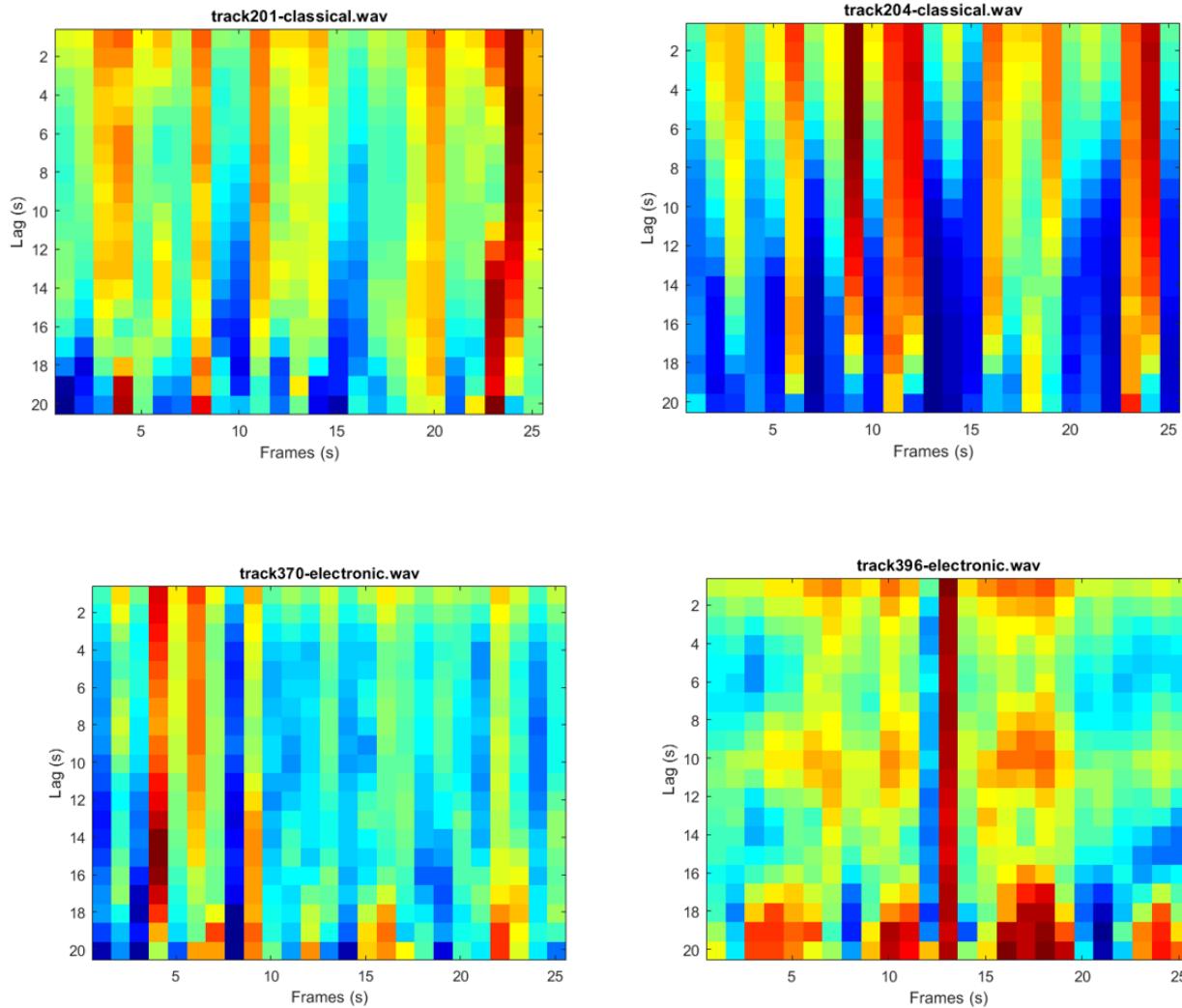


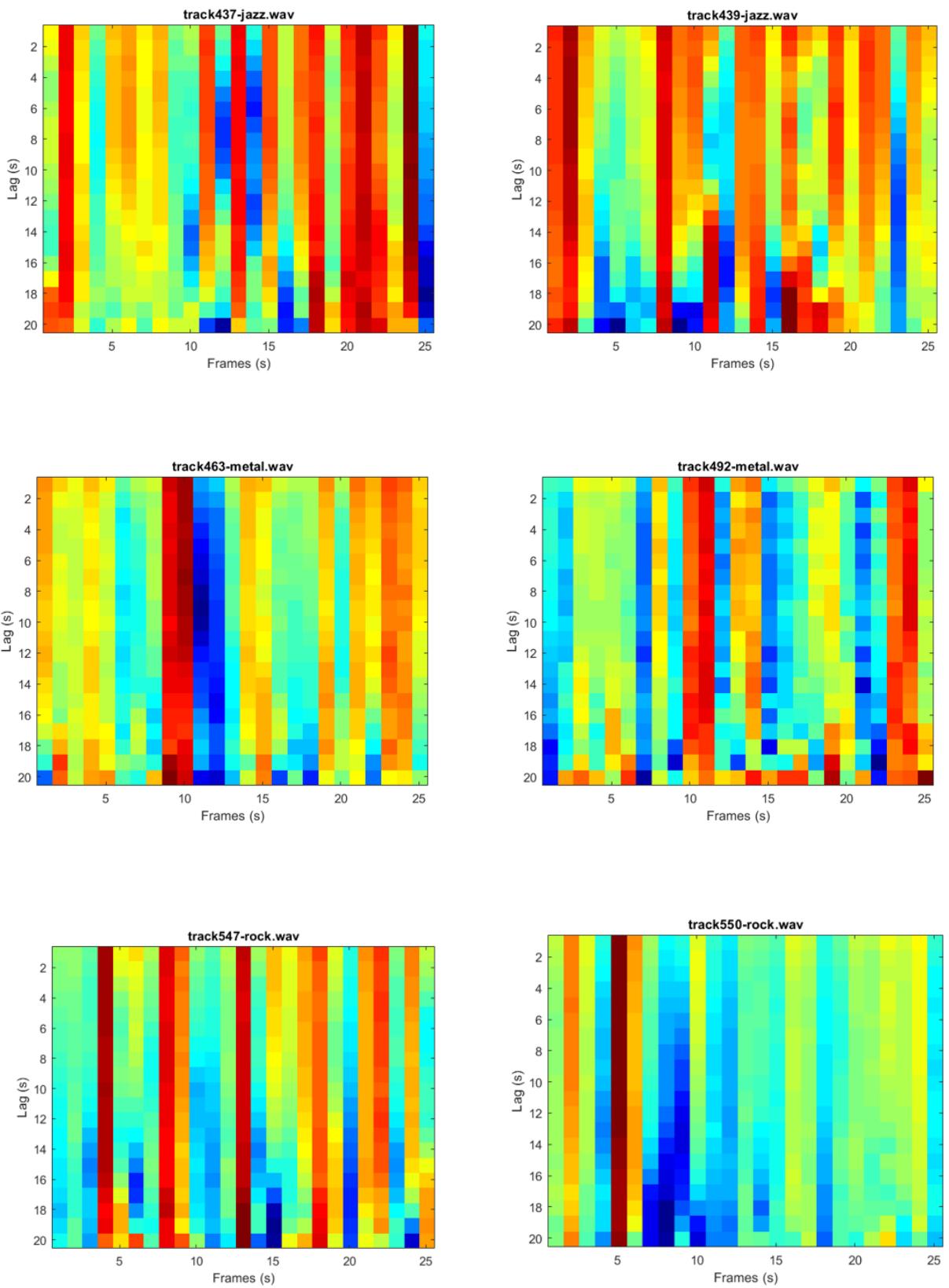


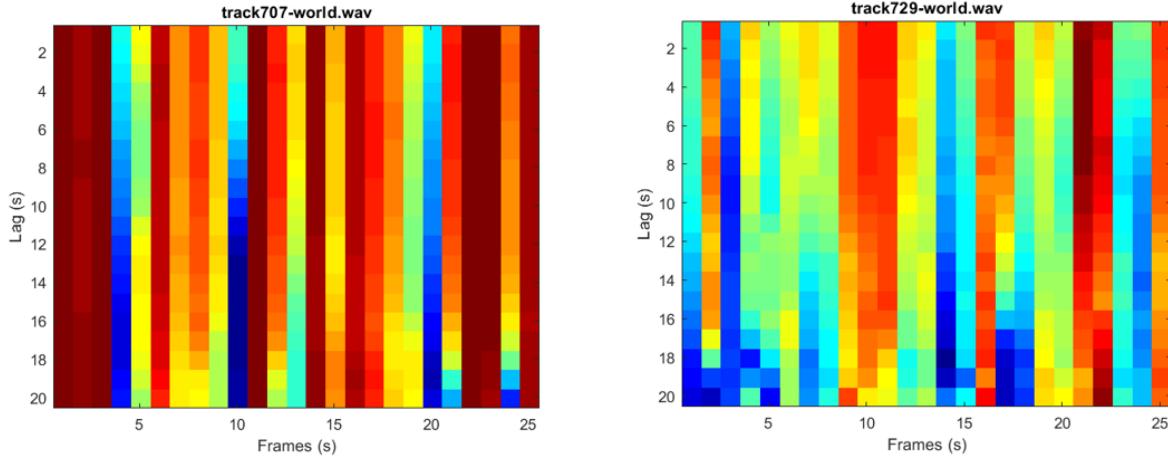
The results of this computation are similar to the first rhythmic calculation where tracks such as electronic give a strong rhythmic pattern, but the world and classical tracks do not. The graphs are also just a bit more refined and if this data was used to determine the BPM, there would be less error involved with resulting BPM value.

Assignment 10

A further evaluation of the rhythmic characteristic of a track is to calculate the autocorrelation of the autocorrelation which gives a sense of how the rhythmic content changes over time. To do this, a small section of the song will be analyzed into a matrix to display. The MATLAB code for this is found in the Assignment 10 Appendix and the plots for the 12 tracks are shown below:



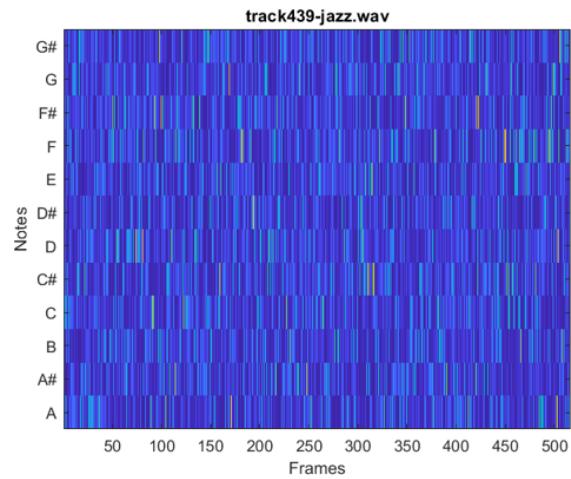
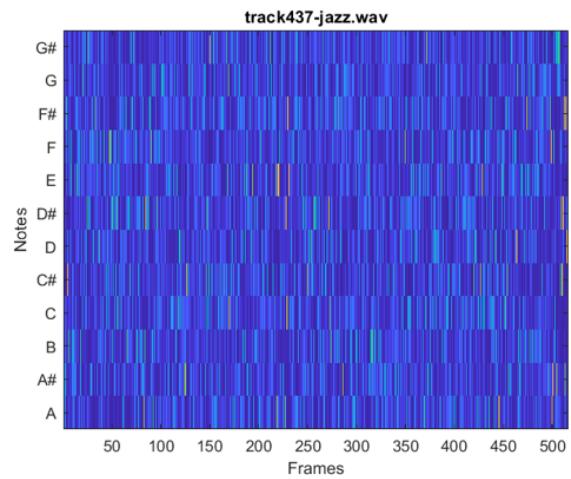
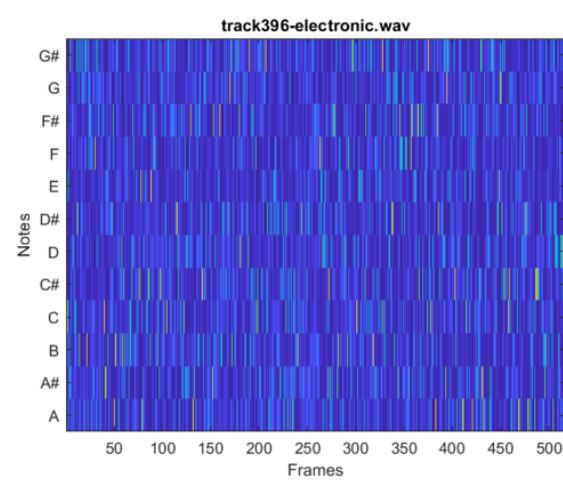
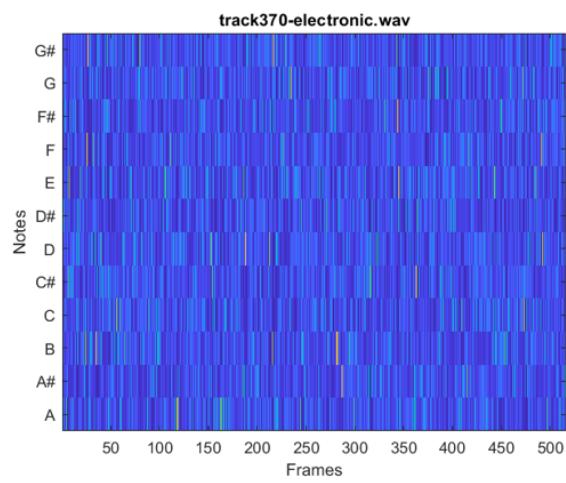
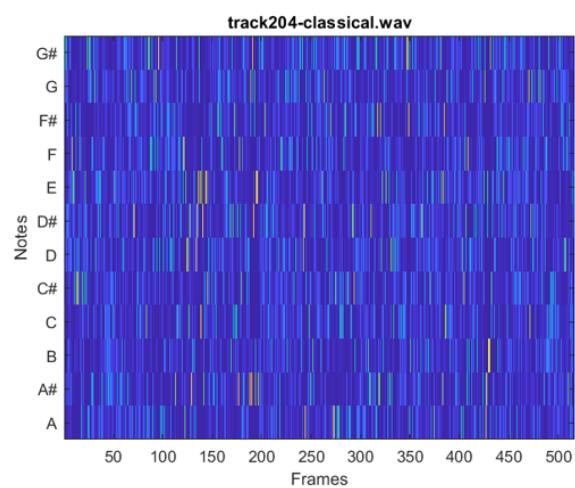
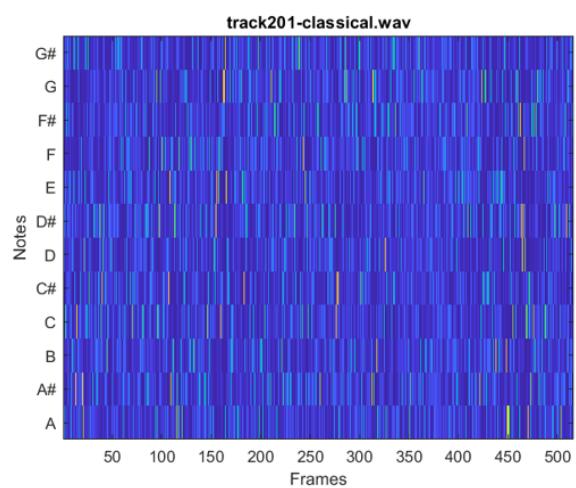


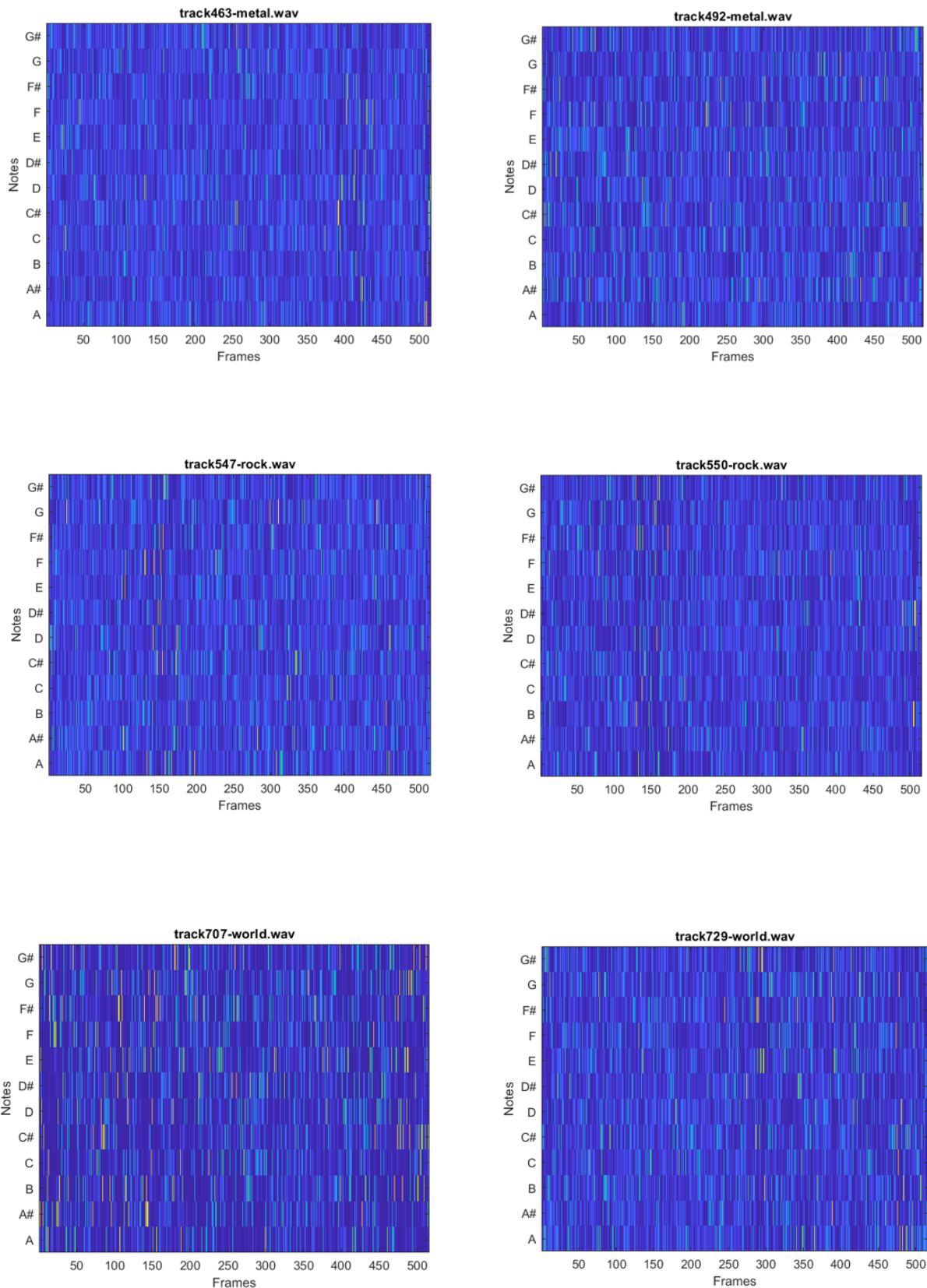


One interesting thing that can be seen from this analysis is the detecting the presence of sustained notes in a track. The World 707 has large strips of high correlation from top to bottom across all lags, which show the note is sustained and similar across many frames and lags. This is present in the track when physically hearing it as well. This sustain can be seen and heard in the jazz tracks as well. The rock and electronic tracks show good examples of a rhythmic pattern because the brighter stripes at evenly frames show strong correlation, indicating a rhythm, which can also be determined from listening.

Assignment 11

The final analysis to be performed on this lab is to analyze the melodic and harmonic content of a track using chroma detection. This analysis will use the Fourier transform and the detection of local maxima in the frequency domain to map these frequencies to actual notes in the logarithmically spaced tempered scale. The many notes associated with these local maxima throughout a frame of audio give the harmonic content of that particular frame, which can then be used to build a Pitch Class profile for that particular frame, which shows which notes on a tempered scale from A to G# are present and how prominent they are. This would allow another algorithm to determine the key signature and mode of a given piece of music. The MATLAB code for the Pitch Class Profile computation is given in the Assignment 11 Appendix and the chroma plots for the 12 tracks are shown below:





The chroma plots are difficult to analyze due to the fact that all of the harmonics may not be completely discarded when performing the quantization with peak detection, but many of the strongly present notes in the track can still be seen. For example the classical track 201 is a piano piece composed by Robert Schumann and this portion of the collection is in G major. Upon inspection it can be seen that there is a strong presence of notes in the G major scale, such as the triad of the standard G chord G, B and D, as well as many other notes that could be used within complex chords throughout the piece. Also, the chroma can give information regarding sustain where a signal note holds the same energy over many frames, such as in the world 707 track on the C note around frame 300.

Code Appendix

Lab 2 Driver Script

```
1 %%%%%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Driver Script
5 %%%%%%
6
7 %% Assignment 1
8
9 %Audio File Information
10 filename = 'track729-world.wav';
11 N = 512;
12 info = audioinfo(filename);
13
14 %Filter bank info
15 fbank = cochlearFilterbank(N,filename);
16 Nb = 40;
17 K = N/2 + 1;
18
19 %Extract 24 seconds from the audio file
20 track = extractTSeconds(24,filename);
21
22 %Variables for MFCC values
23 mfccdB = zeros(floor(length(track)/N),Nb);
24 mfcc = zeros(floor(length(track)/N),Nb);
25
26 % Find mfcc coef. for each frame in track
27 for n=1:floor(length(track)/N)
28     %Extract N samples based on frame number
29     xn = track(1+((N)*(n-1)):1+((N)*(n-1)) + (N-1));
30
31     %Perform the fft and extract the desired components up to K and
32     %determine the MFCC coefficients
33     Y = abs(fft(xn));
34     Xn = Y(1:K);
35     [mfccdB(n,:)] = mfccComp(N,Xn,fbank,Nb);
36 end
37
38 dbMax = max(max(mfccdB));
39 dbMin = min(min(mfccdB));
40 %% Assignment 2
41 %Calculate the Spectrum Histogram from the mfcc coef.
42 hist = spectrumHist(60,-20,81,40,mfccdB);
43
44 %% Assignment 3
45 % Plot the generated histogram
46 colormap('Jet');
47 figure;
48 imagesc((hist));
49 set(gca, 'YTickLabel', [-20:10:60]) % 20 ticks
50 xlabel('MFCC Index');
51 ylabel('dB');
52 title(filename);
53
54 %% Assignment 4
55 %Generate the similarity matrix
56 S = similarityMatrix(mfcc);
57
58 %Plot the similarity matrix
59 colormap('Jet');
60 figure;
61 imagesc(S);
62 xlabel('Frames');
63 ylabel('Frames');
64 title(filename);
65
66 %% Assignment 5
67
68 %Generate Rhythm Pattern
69 Nf = floor(length(track)/N);
70 B = rhythm1(Nf,S);
71
72 %Plot the rhythmic similarity
73 l = 0:1:Nf-1;
74 figure;
75 plot(l,B);
76 xlabel('Frames');
77 title(filename);
78
79 %% Assignment 6
80 %Calculate the median of the Similarity Matrix
81 Sbar = matrixMedian(S);
82
83 %% Assignment 7
84 %Calculate the l values for BPM values between 40 and 240 in steps of 5
85 BPM = bpm(filename,S,Sbar,N,Nf);
```

```

86 [maxBPM I] = max(BPM);
87 trackBPM = 40+(I*5);
88
89 %% Assignment 8
90 %Plot the Normalized BPM vector
91 bpmHist(BPM,filename);
92
93 %% Assignment 9
94 %Calculate and Plot the AutoCorrelation
95 rhythm2(Nf,S,filename);
96
97 %% Assignment 10
98 %Calculate the Rhythmic Variation AC
99 lsize = 20;
100 msize = 20;
101 AC = rhythmicVariation(S,lsize,msize,Nf);
102 ltime = info.SampleRate/(lsize*N);
103 mtime = info.SampleRate/(msize*N);
104 colormap('jet')
105 figure;
106 imagesc(mtime,ltime,AC);
107 title(filename);
108 xlabel('Frames (s)')
109 ylabel('Lag (s)')
110
111 %% Assignment 11
112 %Calculate the Normamлизed pitch class for the track segment
113 PCP = chroma(track,N);
114
115 %% Assignment 12
116 %Plot the Chroma for the tempered scale
117 notes = {'G#', 'G', 'F#', 'F', 'E', 'D#', 'D', 'C#', 'C', 'B', 'A#', 'A'};
118 colormap('jet')
119 figure;
120 imagesc(PCP);
121 set(gca, 'YTick', [1:1:12], 'YTickLabel', notes) % 12 ticks for each note
122 title(filename);
123 xlabel('Frames');
124 ylabel('Notes');

```

Assignment 1

```

1 %%%%%%%%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 1: MFCC Coefficients to DB
5 %%%%%%%%
6
7 function [mfccdB mfcc] = mfccComp(N, Xn, Hp, Nb)
8 %Define K as half of the frame size N
9 K = N/2 + 1;
10
11 %Define the vector to hold the coefficients for each filter
12 mfcc = zeros(1,Nb);
13 mfccdB = zeros(1,Nb);
14
15 %Compute the coefficents for each filter in the bank.
16 for p=1:Nb
17     for k=1:K
18         mfcc(p) = mfcc(p)+(abs(Hp(p,k)*Xn(k)))^2;
19     end
20     mfccdB(p) = 50 + 10*log10(mfcc(p)); %Convert to dB
21 end
22
23 end

```

Assignment 2

```

1 %%%%%%%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 2: Spectrum Histogram
5 %%%%%%%%
6
7 function hist = spectrumHist(maxdB, mindB, rows,cols , mfccdB)
8 %Declare the power levels x filter banks count matrix for histogram (81 possible dB values , 40
9 %filter banks)
10 hist = zeros(rows,cols);
11
12 %Loop through mfcc coefficients to find power levels
13 for i=1:length(mfccdB)
14     for j=1:length(mfccdB(i,:))
15         val = round(mfccdB(i,j));
16         if val < mindB %Assign to min dB level
17             hist((mindB+(-mindB+1)),j) = hist((mindB+(-mindB+1)),j) + 1;
18         elseif val > maxdB %Assign to max dB level
19             hist((maxdB+(-mindB)+1),j) = hist((maxdB+(-mindB)+1),j) + 1;

```

```

20         else
21             hist((val+(-mindB+1)),j) = hist((val+(-mindB+1)),j) + 1;
22         end
23     end
24
25 %Normalize the sum of each column to 1
26 for i=1:length(mfccdB(1,:))
27     val = sum(hist(:,i));
28     hist(:,i) = hist(:,i) ./ val;
29 end
30
31 end

```

Assignment 4

```

1 %%////////////////////////////////////////////////////////////////////////%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 4: Similarity Matrix
5 %%////////////////////////////////////////////////////////////////////////%
6
7 function simMatrix = similarityMatrix(mfcc)
8 %Declare the similarity matrix
9 simMatrix = zeros(length(mfcc),length(mfcc));
10
11 %Calculate the correlation between each frame in track through the dot
12 %product
13 for i=1:length(mfcc)
14     for j=1:length(mfcc)
15         simMatrix(i,j) = ((dot(mfcc(i,:),mfcc(j,:)))/(norm(mfcc(i,:))*norm(mfcc(j,:))));
16     end
17 end
18 end

```

Assignment 5

```

1 %%////////////////////////////////////////////////////////////////////////%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 5: Rhythmic Pattern 1
5 %%////////////////////////////////////////////////////////////////////////%
6
7 function B = rhythm1(Nf, S)
8 %Declare the Rhythm Martix
9 B = zeros(1,Nf);
10
11 for l=0:(Nf-1)
12     for n=1:Nf-1
13         B(l+1) = B(l+1) + S(n,n+l); %Count diagonal at different lags
14     end
15     B(l+1) = (1/(Nf-1))*B(l+1); %Complete computation
16 end
17 end

```

Assignment 6

```

1 %%////////////////////////////////////////////////////////////////////////%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 6: Median of Matrix
5 %%////////////////////////////////////////////////////////////////////////%
6
7 function Sbar = matrixMedian(S)
8 %Calculate the Median of Matrix S
9 Sbar = median(S(:));
10 end

```

Assignment 7

```

1 %%////////////////////////////////////////////////////////////////////////%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 7: BPM
5 %%////////////////////////////////////////////////////////////////////////%
6
7 function BPM = bpm(filename,S, Sbar, N, Nf)
8 %Declare the lag array and bpm array
9 lag = zeros(1,41);
10 bpm = 40:5:240; % Space BPM from 40-240 at steps of 5 BPM
11 BPM = zeros(1,41);
12
13 %Extract sampling freq

```

```

14     info = audioinfo(filename);
15     Fs = info.SampleRate;
16
17 %Calculate the lag values for each BPM
18 lag = (60*Fs) .* (1./(bpm.*N));
19
20 %Calculate the number of times S(i,i+1) is larger than Sbar
21 for l=1:length(lag)
22     for i=1:(Nf-round(lag(1)))
23         if S(i,i+round(lag(1))) > Sbar
24             BPM(l) = BPM(l) + 1;
25         end
26     end
27 end
28

```

Assignment 8

```

1 %%%%%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 8: BPM Histogram
5 %%%%%%
6
7 function PH = bpmHist(bpm,filename)
8 %Normalize the BPM vector
9 val = sum(bpm);
10 PH = bpm ./ val;
11
12 %Plot this normalized BPM vector between 40 and 240 BPM
13 figure;
14 plot(40:5:240,PH);
15 title(filename);
16 xlabel('BPM');
17

```

Assignment 9

```

1 %%%%%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 9: Rhythmic Pattern 2
5 %%%%%%
6
7 function ac = rhythm2(Nf, S,filename)
8 %Declare the Rhythm Martix Autocorrelation
9 ac = zeros(length(S(:,1)),Nf);
10 AC = zeros(1,Nf);
11
12 %Calculate the Autocorrelation
13 for i=1:length(S(:,1))
14     for l=0:Nf-1
15         for j=1:Nf-1
16             ac(i,l+1) = ac(i,l+1) + S(i,j)*S(i,j+1);
17         end
18         ac(i,l+1) = (1/(Nf-1))*ac(i,l+1);
19     end
20 end
21
22 %Normalize the Autocorrelation
23 for l=1:Nf
24     for i=1:Nf
25         AC(l) = AC(l) + ac(i,l);
26     end
27 end
28
29 %Plot the AC
30 figure;
31 plot(0:1:Nf-1,AC);
32 xlabel('Frames');
33 title(filename);
34
35

```

Assignment 10

```

1 %%%%%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 10: Rhythmic Variation
5 %%%%%%
6
7 function AC = rhythmicVariation(S, lsize, msize, Nf)
8 %Declare variable to hold AC matrix

```

```

9     AC = zeros(lsize , floor(Nf/msize));
10    %Perform the double summation for the AC on itself
11    for l=0:lsize-1
12        for m=0:(floor(Nf/msize)-1)
13            AC(l+1,m+1) = 1/(msize*(msize-1))*sum(sum(S((1:msize) + msize*m, (1:msize-1) + msize*m) ...
14                .*S((1:msize) + msize*m, (1:msize-1) + msize*m + 1)));
15        end
16    end
17 end

```

Assignment 11

```

1 %%%
2 % Clint Olsen
3 % ECEN 4532: DSP Lab
4 % Lab 2: Assignment 11: Pitch Class Profile
5 %%%
6
7 function PCP = chroma(track, N)
8 % Frequency of the lowest octave A on piano
9 f0 = 27.5;
10 K = N/2 + 1;
11 PCP = zeros(12,floor(length(track)/N));
12
13 for n=1:floor(length(track)/N)
14 %Extract N samples based on frame number
15 xn = track(1+((N)*(n-1)):1+((N)*(n-1)) + (N-1));
16
17 %Perform the fft and extract the desired components up to K
18 Y = abs(fft(kaiser(N,0.5).*xn));
19 Xn = Y(1:K);
20
21 %Find the local maxima values and locations
22 [fk I] = findpeaks(Xn);
23
24 %Find the nearest semitones and map to corresponding note,
25 %regardless of octave
26 PL = floor(12*log2(fk./f0));
27 PH = ceil(12*log2(fk./f0));
28 CL = mod(PL,12);
29 CH = mod(PH,12);
30
31 %Create the weighted sum of the semitones for each frame
32 rL = 12*log2(fk./f0) - PL;
33 wL = (cos(pi.*rL./2)).^2;
34 rH = 12*log2(fk./f0) - PH;
35 wH = (cos(pi.*rH./2)).^2;
36
37 %Calculate the PCP values
38 for k=1:length(CH)
39     PCP(CL(k)+1,n) = PCP(CL(k)+1,n) + wL(k)*(Xn(k)).^2;
40     PCP(CH(k)+1,n) = PCP(CH(k)+1,n) + wH(k)*(Xn(k)).^2;
41 end
42
43 %Normalize the column vector over all semitones
44 PCP(:,n) = PCP(:,n)./(sum(PCP(:,1:12),n)));
45
46 end

```