Cosmological Perturbations

Following [1, ch. 5].

$$g = g^{(0)} + \epsilon g^{(1)} + O(\epsilon^2) \tag{1}$$

$$g^{(0)}_{\mu\nu}\,\mathrm{d} x^\mu\,\mathrm{d} x^\nu = -N^2(t)\,\mathrm{d} t^2 + a^2(t)\,\mathrm{d} \Omega_3^2 \eqno(2)$$

$$g_{00}^{(1)} = -E, (3)$$

$$g_{i0}^{(1)} = g_{i0}^{(1)} = a(F_{,i} + G_i), \tag{4}$$

$$g_{ij}^{(1)} = a^2 \left(A \delta_{ij} + B_{,i,j} + C_{i,j} + C_{j,i} + D_{ij} \right). \tag{5}$$

References

[1] Steven Weinberg. Cosmology. Oxford University Press, 2008. ISBN: 9780198526827. URL: https://global.oup.com/academic/product/cosmology-9780198526827.