1

- (1pt) Using the euclidean metric  $(L_2)$ , calculate the distance between (4,13) and (-8,5).
- (1pt) Using the manhattan metric  $(L_1)$ , calculate the distance between (7,5) and (4,-4).
- (1pt) Using the chebyshev metric  $(L_{\infty})$ , calculate the distance between (1,10) and (14,12).

2

Suppose you are given the following training set.

| Example      | Feature 1 | Feature 2 | Label |
|--------------|-----------|-----------|-------|
| A            | 5         | 6         | 0     |
| В            | 4         | 8         | 0     |
| $\mathbf{C}$ | 1         | 0         | 1     |
| D            | 8         | 9         | 0     |
| ${ m E}$     | 4         | 3         | 1     |

- (1pt) What class would 1-nearest-neighbor assign the test example (2,1)?
- (2pt) What class would 1-nearest-neighbor assign the test example (0,0)?
- (4pt) What class would 3-nearest-neighbor assign the test example (4,5)?

3

Suppose you are given the following examples.

| Example      | Feature 1 | Feature 2 |
|--------------|-----------|-----------|
| A            | 1         | 0         |
| В            | 3         | 0         |
| $\mathbf{C}$ | 5         | 0         |
| D            | 7         | 0         |
| $\mathbf{E}$ | 9         | 0         |
| $\mathbf{F}$ | 1         | 4         |
| $\mathbf{G}$ | 3         | 4         |
| $\mathbf{H}$ | 5         | 4         |
| I            | 7         | 4         |
| J            | 9         | 4         |
| K            | 11        | 0         |
| ${f L}$      | 13        | 0         |
| $\mathbf{M}$ | 15        | 0         |
| O            | 11        | 4         |
| P            | 13        | 4         |
| Q            | 15        | 4         |

- (1pt) Plot the above examples on a graph.
- (1pt) Suppose we initialize k-means-clustering (k=2) with the points I and J. Circle the clusters that the algorithm converges upon.