Online Supplement of Retrospective estimation of latent COVID-19 infections before Omicron in the U.S.

Rachel Lobay

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S1 Supplementary methods

S1.1 A general description and depiction of convolution

In general, the goal of convolution is to propagate the input signal forward in time using a distribution of probabilities. In the 2D and discrete context, it is simply the elementwise multiplication of the signal for some time by a forward-facing distribution of probabilities, which are then summed to get a value for the outcome. Figure S1 presents a depiction of the convolution procedure for the signal of smoothed cases (orange line). Essentially, to push the cases forward in time, we take the appropriately aligned (forward-in-time) delay distribution and convolve or multiply the case counts by it to get the distribution of convolved case estimates (blue line). This process is repeated as we march forward in time, as shown through the stop-motion panels, such that it eventually covers the entire line of cases. An important takeaway from this is that convolution is not the same as a simple shift of the data points, but rather it utilizes the most relevant probabilities to propagate the data points forward in time. Deconvolution proceeds in the same fashion, but in the opposite direction to go back in time.

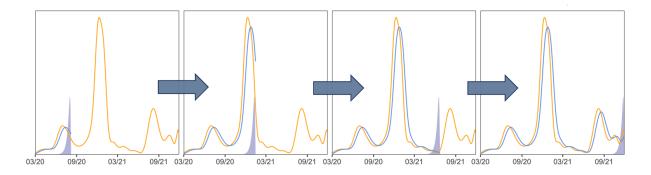


Figure S1: A general depiction of convolving smoothed cases (orange line) with the corresponding delay probabilities (shaded blue area) to get the convolved estimates (blue line) over four different times.

S1.2 Additional details on the date fields in the CDC line list

Since the restricted dataset is updated monthly and cases may undergo revision, we use a single version of it that was released on June 6, 2022. We consider this version to be finalized in that it well-beyond our study end date such that the dataset is unlikely to be subject to further significant revisions.

Table S1 presents the percent of pairwise occurrences for the different possible permutations of events in the line list. Essentially, most cases follow the idealized ordering shown by Figure 1 and so we adhere to this construction as much as possible.

We observe that the line list is prone to high percentages of missing data, notably with respect to our variables of interest. Approximately 62.3% of cases are missing the symptom onset date, 55.4% are missing positive specimen date, and 8.96% of cases are missing the report date. Relatedly, cases with missing report or positive specimen dates may be filled with their symptom onset date¹. So it is possible that all three variables may be imputed with the same date for a case. However, we only actually deal with select pairs of events; we do not use all three at once in our construction of the delay distributions or anywhere else in our analysis. Therefore, we restrict our investigation of missingness to the pairs of events. Figure S2 suggests that this issue impacts states differentially due to the inconsistent proportions of zero delay between positive specimen and report date across states.

Due to the contamination in the zero delay cases (the true extent of which is unknown to us), we omit all such cases where the positive specimen and report dates have zero delay from our analysis. We choose to allow for zero and negative delay for symptom onset to report because correspondence with the CDC confirms the distinct possibility that a person could test positive before symptom onset and it is a reasonable ordering to expect if, for example, the individual is aware that they have been exposed to an infected individual.

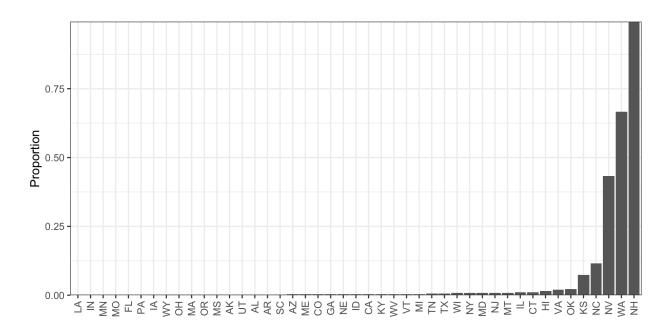


Figure S2: Proportion of complete cases with zero delay between positive specimen and report date in the restricted CDC line list dataset.

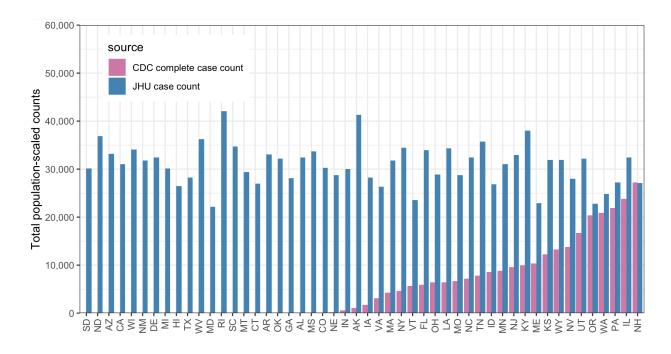


Figure S3: Complete case counts by state in the CDC line list versus the cumulative complete case counts from JHU CSSE as of June 6, 2022. All counts have been scaled by the 2022 state populations as of July 1, 2022 from².

For the same release date, the restricted line list contains 74,849,225 cases (rows) in total compared to 84,714,805 cases reported by the JHU CSSE; that is, line list is missing about

10 million cases. The extent that this issue impacts each state is shown in Figure S3, from which it is clear the fraction of missing cases is substantial for many states, often surpassing 50%¹. In addition, the probability of being missing does not appear to be the same for states, so there is likely bias introduced from using the complete case line list data. We consider such bias to be unavoidable in our analysis due to a lack of alternative line list sources.

In the line list, we observe unusual jarring spikes in reporting in 2020 compared to 2021. Upon plotting by report date, we find that a few states are contributing unusually large case counts on isolated days very late in the reporting process (usually well beyond 50 days). We strongly suspect that these large accumulations of cases over time are due breakdowns of the reporting pipeline (which may be expected to occur more frequently in the year following its instantiation than later in time). Such anomalies are not likely to be reliable indicators of the delay from positive specimen to case report. Therefore, we devise a simple, ad hoc approach to detect and prune these reporting backlogs.

First, we obtain the part of the line list intended for the positive specimen to case report delay estimation, where both such dates are present and where zero and negative delay cases have been omitted. Then, for each of the three dates of June 1, September 1, and December 1, 2020, we bin the reporting delays occurring from 50 days up to the maximum observed delay. For each bin, we obtain the total delay count for each state. We check whether each count on the log scale is at least the median (for the bin) plus 1.5 times the interquartile range and retain only those that exceed this criterion as potential candidates for pruning. Next, we compute the counts by report date for each candidate state. If there is a report date with a count greater than or equal to the pre-specified threshold, then we remove those cases from the line list. Based on inspection and intuition, we set the threshold to 2000 for the first two bins, and then lower it to 500 for the remaining bins. A similar trial and error approach is used to set the bin size (to 50 days).

S1.3 Table on the percent pairwise occurrence of events in the CDC line list

Order of events	Percent pairwise occurrence	Handling
$IO \to SO \to PS \to RE$	PS ≥ SO: 97.1 PS = SO: 33.6 PS >RE: 1.74 PS = RE: 14.6	This is the idealized order of events and so we built the current support sets for SO → PS and PS → RE delay distribution constructions around this such that IO comes first by construction, SO typically precedes PS, but may be the same or come before, and RE comes after PS and SO
$IO \to PS \to SO \to RE$	PS <so: 2.91<br="">SO ≤ RE: 99.3 SO <re: 86.1<="" td=""><td>Allowed for negative delays up to the largest non-outlier value for the 0.05 quantile of delay from PS to SO by state</td></re:></so:>	Allowed for negative delays up to the largest non-outlier value for the 0.05 quantile of delay from PS to SO by state
$IO \rightarrow PS \rightarrow RE \rightarrow SO$	RE <so: 0.7<br="">RE <ps: 1.7<="" td=""><td>Nothing because current handling of the CDC of the line list ensures that the most concerning cases are handled where $SO = PO = RE, SO = RE \text{ and } PO = RE$</td></ps:></so:>	Nothing because current handling of the CDC of the line list ensures that the most concerning cases are handled where $SO = PO = RE, SO = RE \text{ and } PO = RE$

Table S1: Percent pairwise occurrence for the different permutations of events considered in the restricted CDC line list. The abbreviation IO stands for infection onset, SO is symptom onset, PS is positive specimen, and RE is report date. We consider a restricted set of permutations because we assume that IO must come first and that PS must precede report date for a case to be legitimate. Finally, the underlying assumption for the percent pairwise occurrence calculations is that the cases must have both elements present (not missing).

S1.4 Justifications for delay distribution calculations

Let y_t denote the count of new cases reported at time t and x_t denote the count of deconvolved cases with positive specimen at t. For all cases in the line list that had both a positive specimen and a report date, we can count the those that are reported at time t by enumerating them according to positive specimen date (similar to how symptom onset date was used in¹):

$$y_t = \sum_{s=1}^t \sum_{i=1}^{x_s} \mathbf{1}$$
 (the i^{th} positive specimen at s gets reported at t).

Taking the conditional expectation of the above yields

$$\mathbb{E}(y_t \mid x_s, s \le t) = \sum_{s=1}^t \pi_t(s) x_s,$$

where $\pi_t(s) = \mathbb{P}(\text{case report at } t \mid \text{positive specimen date at } s)$ for each $s \leq t$ are the delay probabilities and the $\{\pi_t(s) : s \leq t\}$ sequence comprises the delay distribution at time t. Notice that there are no time restrictions placed on the positive specimen date, except that it must have been between the start of the pandemic and the report date, inclusive. This is unlikely to be a realistic assumption to make as t moves farther away from s.

Thus, we make three key assumptions about these distributions. First, positive specimen tests that are reported to the CDC are always reported within d = 60 days, which is true for the majority of the reported cases. Second, the probability of zero delay is zero, which stems from the contamination of zero-delay in the line list. We update the conditional expectation formula to reflect these two assumptions as in¹:

$$\mathbb{E}(y_t \mid x_s, s \le t) = \sum_{k=1}^{60} p_t(k) x_{t-k}$$

where for k = 1, ..., 60,

$$p_t(k) = \mathbb{P}(\text{case report at } t \mid \text{positive specimen at } t - k).$$

Thirdly, there are times where the empirical probability was observed to be precisely 1 at zero delay and the proportion of CDC relative to JHU cases used for the weight was also 1. Since we believe that having zero delay for all cases is unrealistic and unlikely to be representative of all cases for the state, we inject a small amount of variance manually by setting the the CDC-to-JHU proportion to be the minimum shrinkage proportion observed for the affected state (such instances were isolated to the state of New Hampshire). Aside from these modifications, the construction of the delay distribution proceeds in precisely the same manner as for positive specimen to report date.

S1.5 Estimated delays for a sample of six states

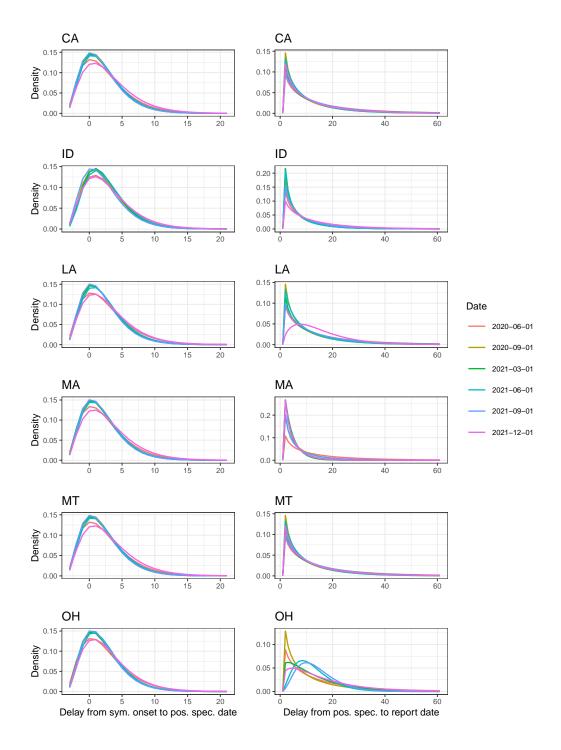


Figure S4: Depictions of the estimated delay from symptom onset to positive specimen date (left) and from positive specimen date to report date (right) over several dates for a sample of six states.

S1.6 Details about seroprevalence data

In the former, the CDC collaborated with 17 blood collection organizations in the largest nationwide COVID-19 seroprevalence survey to date³. The blood donation samples were used to construct monthly seroprevalence estimates for nearly all states from July 2020 to December 2021⁴. In the latter survey, the CDC collaborated with two private commercial laboratories and used blood samples to test for the antibodies to the virus from people that were in for routine or clinical management (presumably unrelated to COVID-19⁵). The resulting dataset contains seroprevalence estimates for a number of multi-week collection periods starting in July 2020 to February 2022.

Both datasets are based on repeated, cross-sectional studies that aimed, at least in part, to estimate the percentage of people who were previously infected with COVID-19 using the percentage of people from a convenience sample who had antibodies against the virus^{4–6}. Adjustments were made in both for age and sex to account for the demographic differences between the sampled and the target populations. However, both datasets are incomplete and they differ in the number and the timing of the data points for each state (Figure S5). Such limitations indicate that reliance upon only one seroprevalence survey is inadvisable. For example, in the commercial dataset, the last estimate for North Dakota is in September 2020. In the blood donor dataset, Arkansas does not have estimates available until October 2020.

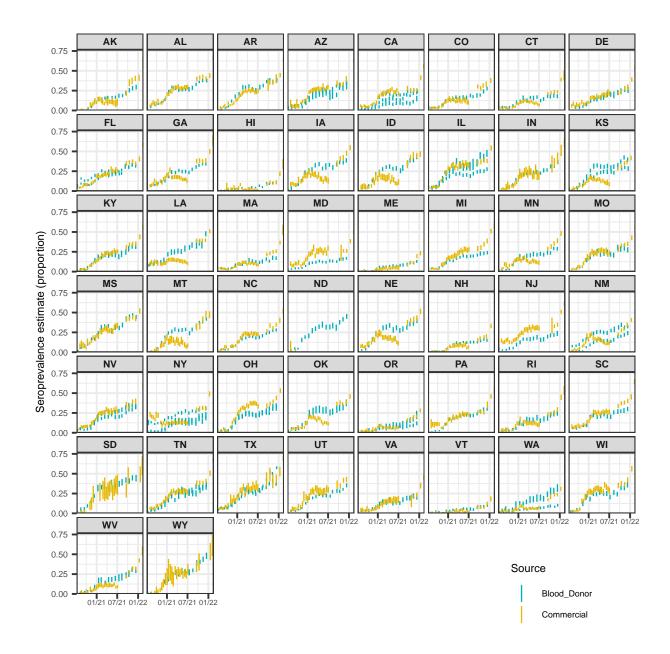


Figure S5: A comparison of the seroprevalence estimates from the Commercial Lab Seroprevalence Survey dataset (yellow) and the 2020–2021 Blood Donor Seroprevalence Survey dataset (blue). Note that the maximum and the minimum of the line ranges are the provided 95% confidence interval bounds to give a rough indication of uncertainty.

The date variables that come with the two seroprevalence datasets are different and so the date variables that we are able to construct from them are not the same. For the commercial dataset, we use the midpoint of the provided specimen collection date variable. A major difference in the structure of the two datasets is that the commercial dataset always has the seroprevalence estimates at the level of the state, while the blood donor dataset can either have estimates for the state or for multiple separate regions within the state. For the

blood donor dataset, we use the median donation date if the seroprevalence estimates are designated to be for entire state. If they are instead for regions in the state, since there is reliably one measurement per region per month, we aggregate the measurements into one per month per state by using a weighted average (to account for the given sample sizes of the regions). The median of the median dates is taken to be the date for the weighted average.

To adapt to the sparseness in the seroprevalence data, we convert our daily data to weekly by summing the reported infections and shifting the observed seroprevalence measurements to the nearest Monday. If there are multiple measurements in a week from a seroprevalence source, then the average is used. We denote these changes by changing the time-based subscript from t to m where m indicates the Monday relative to our June 1, 2020 start date. Since we operate with weekly data where the weeks are designated by Monday, we set the end date to be November 29, 2021.

S1.7 State space representation of the antibody prevalence model

The antibody prevalence model is conceptualized as a Gaussian state space model (as in^{7,8}).

In general, for t = 1, ..., n, let α_t be the $m \times 1$ vector of latent state processes at time t and y_t be the $p \times 1$ vector of observations at time t. Under the assumption that η is a $k \times 1$ vector, the form of the linear Gaussian state space model is

$$y_t = Z\alpha_t + \epsilon_t, \qquad \epsilon_t \sim N(0, H_t)$$
 (1)

$$\alpha_{t+1} = T_t \alpha_t + R_t \eta_t, \quad \eta_t \sim N(0, Q_t)$$
 (2)

where $\alpha_1 \sim N(a_1, P_1)$ and there is independence amongst α_1 , ϵ_t and $\eta_t^{7,8}$. For notational compactness, we let $\alpha = (\alpha_1^\top, \dots, \alpha_n^\top)$ and $y = (y_1^\top, \dots, y_n^\top)$.

The observation equation can be viewed as a linear regression model with the time-varying coefficient α_t , while the second equation is a first-order autoregressive model, which is Markovian in nature⁷.

The underlying idea behind the two equations is that we are assuming that the system evolves according to α_t (as in the second equation), but since those states are not directly observed, we turn to the observations y_t and use their relationship with α_t (as in the first equation) to drive the system forward⁷. So the objective of state space modeling is to obtain the latent states α based on the observations y and this is achieved through Kalman filtering and smoothing.

Kalman filtering gives the following one-step-ahead predictions of the states

$$a_{t+1} = \mathbb{E}[\alpha_{t+1} \mid y_t, \dots, y_1]$$

with covariance,

$$P_{t+1} = \operatorname{Var}(\alpha_{t+1} \mid y_t, \dots, y_1).$$

Then, the Kalman smoother works backwards to the first time to give

$$\hat{a}_t = \mathbb{E}[\alpha_t \mid y_n, \dots, y_1] \tag{3}$$

$$V_t = \operatorname{Var}(\alpha_t \mid y_n, \dots, y_1). \tag{4}$$

The filtering and smoothing steps are based on recursions that are described in Appendix A of⁸ as we use the R package KFAS to estimate our model.

To express the antibody prevalence model in state space form, we define the components in Equations (1) and (2) as follows:

$$R = \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \qquad Z = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix} \qquad H_m = \begin{bmatrix} w_{m,c}\sigma_o^2 & 0 \\ 0 & w_{m,b}\sigma_o^2 \end{bmatrix}$$

$$\alpha_m = \begin{bmatrix} s_m \\ a_m \\ a_{m-1} \\ a_{m-2} \end{bmatrix} \qquad T_m = \begin{bmatrix} \gamma & C_{m-1}^m z_m & 0 & 0 \\ 0 & 3 & -3 & 1 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \qquad Q = \begin{bmatrix} \sigma_s^2 & 0 \\ 0 & \sigma_a^2 \end{bmatrix}$$

$$a_1 = \begin{bmatrix} \tilde{s}_1 \\ \tilde{a}_1 \\ \tilde{a}_1 \end{bmatrix} \qquad P_1 = \begin{bmatrix} \sigma_{\tilde{s}_1}^2 & 0 & 0 & 0 \\ 0 & \sigma_{\tilde{a}_1}^2 & 0 & 0 \\ 0 & 0 & \sigma_{\tilde{a}_1}^2 & 0 \\ 0 & 0 & 0 & \sigma_{\tilde{a}_1}^2 \end{bmatrix}$$

where σ_o^2 is the variance of observations, σ_s^2 is the variance of the seroprevalence estimates, and σ_a^2 is the trend variance. Since we expect the inverse ratios to be more variable than the seroprevalence estimates, we enforce that the estimate of σ_a^2 is a multiple of σ_s^2 . Letting the subscripts b and c denote the blood donor and commercial datasets, $w_{m,c}$ and $w_{m,b}$ are the time-varying inverse variance weights computed from the commercial and blood donor datasets, respectively.

For each source, we compute the weights for the observed seroprevalence estimates using the standard formula for the standard error of a proportion. These weights are then re-scaled so they sum to the number of observed seroprevalence measurements for the source. All days that are unobserved (i.e., lack seroprevalence measurements) are given weights of one. Finally, the ratio of the average observed weights for the sources is used as a multiplier to scale all of the weights for one source. For example, if the average weight of the commercial source is double the average weight of the blood donor source (for an arbitrary state), then we scale all of the weights in the commercial source (including the ones) by two. The main purpose of this step is to ensure that the source with a greater sample size contributes more weight in the model on average.

The prior distribution for α_1 is estimated using both data-driven constraints and externally sourced information. To obtain the initial value of the seroprevalence component, \tilde{s}_1 , we extract the first observed seroprevalence measurement from each source, round down to two

decimal places, and take the average to be \tilde{s}_1 . The corresponding initial variance estimate, $\sigma_{\tilde{s}_1}^2$, is taken to be the mean of the standard errors of the two seroprevalence estimates. For all of the initial values of the trend components, we use the inverse of the ascertainment ratio estimate as of June 1, 2020 for each state from Table 1 in⁹ and denote this by \tilde{a}_1 . The initial variance estimate of $\sigma_{\tilde{a}_1}^2$ is based on the variance implied by the given inverse ascertainment ratio distribution.

The initial σ_o^2 is taken to be the average of the estimated variances from the linear models for the sources where the observed seroprevalence measurements are regressed on the enumerated dates. The initial value of the multiplier is set to be 100 for all states. The σ_s^2 and γ values are fixed and from averaging the estimated values for all states on the real line (obtained under the starting conditions $\sigma_s^2 = 3 \times 10^{-6}$, $\gamma = 0.99$, and σ_o^2 as described).

Following the maximum likelihood estimation of the two non-fixed parameters we use the Kalman filtering and smoothing to obtain the smoothed estimates of the weekly inverse reporting ratios and their covariance matrices as shown in Equations (3) and (4). Forwards and backwards extrapolation is then used to estimate the ratios and covariance outside of the observed seroprevalence range⁷, followed by linear interpolation to fill-in estimates for each day in our considered time period. After we obtain one vector of inverse reporting ratios for each state in this way, we take each inverse reporting ratio and multiply it by the corresponding deconvolved case estimate (that has undergone linear interpolation to correct instances of 0 reported infections) to obtain an estimate of new infections. We are able to convert these numbers of infections to infections per 100,000 population by simple re-scaling (enabled by the fact that normality is preserved under linear transformations).

The 50, 80, and 95% confidence intervals are constructed by taking a Bayesian view of the antibody prevalence model (refer to the subsequent section for the Bayesian specification of the model). That is, for each time, t, we obtain an estimate of the posterior variance of a_t , apply the deconvolved case estimate as a constant multiplier, and then use resulting variance to build a normal confidence interval about the infection estimate. We additionally enforce that the lower bound must be at least the deconvolved case estimate for the time under consideration.

S1.8 Bayesian specification of the antibody prevalence model

In brief, the antibody prevalence model where we let $\beta = \{\gamma, a_1, \dots, a_t\}$ and X be the design matrix, corresponds to a Bayesian model with prior

$$\beta \sim N\left(0, \frac{\sigma^2}{\lambda} \left(A^T D^T D A\right)^{-1}\right)$$

and likelihood

$$s|X, \beta \sim N\left(X\beta, \sigma^2 W^{-1}\right),$$

where A is indicator matrix save for the first column of 0s (corresponding to γ), D represents the discrete derivative matrix of order 3, and W is the inverse variance weights matrix. Then,

the posterior on a_t is normally distributed with mean

$$\left(X^TWX + \lambda A^TD^TDA\right)^{-1}X^TWs$$

and variance

$$\sigma^2 (X^T W X + \lambda A^T D^T D A)^{-1}.$$

S1.9 Scaling by population

Annual estimates of the resident state populations as of July 1 of 2020 and 2021 are taken from the Dec. 2022 press release from the U.S. Census Bureau². Unless otherwise specified, we use the July 1, 2020 estimates.

S1.10 Ablation analysis of infection-hospitalization correlations

To better understand the contribution of the intermediate steps to the lagged correlation analysis, we carry out a brief ablation study in which we calculate the lagged correlation using the following infection estimates: 1. those from the deconvolution procedure under the assumption that the infection onset is the same as the positive specimen date (i.e., excluding the positive specimen to infection onset data and deconvolution); 2. those from the deconvolution procedure under the assumption that the infection onset is the same as the symptom onset date (excluding the incubation period data); 3. those from the deconvolution procedure when utilizing all incubation period and delay data (the deconvolved case estimates); 4. those from applying the antibody prevalence model to produce estimates for both the reported and the unreported cases (the infection estimates).

The results of this study are shown in Figure S6. From this, we can see that the deconvolved case or infection estimates from the intermediate steps are all leading indicators of hospitalizations. However, the degree that each such set of estimates lead hospitalizations depend on its location in the sequence of steps and how close the estimates are to infection onset. For example, the deconvolved cases by positive specimen date tend to precede hospitalizations by about 11 days, while those for the subsequent step indicate that the deconvolved cases by symptom onset tend to precede hospitalizations by a longer time of 13 days. Finally, after adding the variant-specific incubation period data into the deconvolution and obtaining the deconvolved case estimates, we can observe that the reported infections precede hospitalizations by about 17 days.

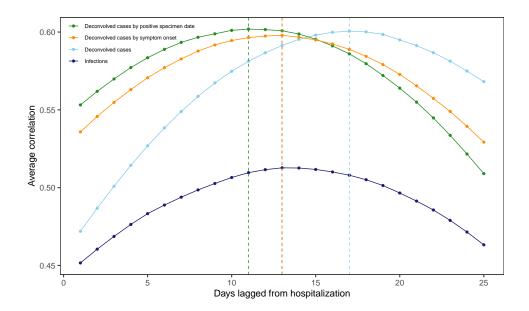


Figure S6: Lagged Spearman's correlation between the infection and hospitalization rates per 100,000 averaged for each lag across U.S. states and days over June 1, 2020 to November 29, 2021, and taken over a rolling window of 61 days. The infection rates are based on the counts for the deconvolved case and infection estimates as well as the reported infections by symptom onset and when the report is symptom onset. Note that each such set of infection counts is subject to a center-aligned 7-day averaging to remove spurious day of the week effects. The dashed lines indicate the lagsfor which the highest average correlation is attained.

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