

**GEORGIA INSTITUTE OF TECHNOLOGY**  
**School of Civil & Environmental Engineering**  
**CEE 2300 – Environmental Engineering Principles**

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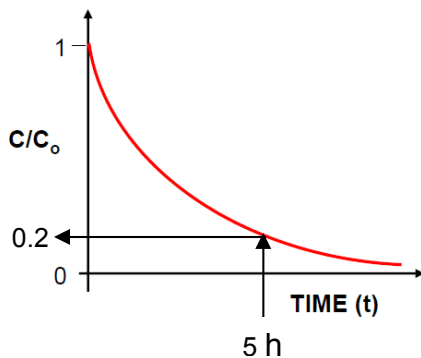
**EXAM 2 – SOLUTIONS**

1. (25 points) Briefly define/explain/answer the following:

1-a (5 pts) Priority Pollutants

The federal Clean Water Act (CWA), Section 307 defines a list of 129 priority pollutants for which the U.S. EPA must establish ambient water-quality criteria (the basis of state water-quality standards) and effluent limitations (rules controlling environmental releases from specific industrial categories based on the "best available technology economically achievable"). The initial list of priority pollutants was based on a 1977 consent decree that settled a legal challenge to the U.S. EPA's program for controlling hazardous pollutants (Natural Resources Defense Council; June 9, 1976).

1-b (5 pts) Plot the normalized concentration of a pollutant ( $C/C_0$  on the y-axis) versus time ( $t$  on the x-axis) for a batch reactor achieving 80% pollutant destruction in 5 hours assuming that pollutant destruction follows first-order kinetics.



1-c (5 pts) First Law of Thermodynamics.

Energy cannot be created or destroyed, excluding nuclear reactions (but energy can be converted)(conservation of energy).

1-d (5 pts) Second Law of Thermodynamics.

Energy conversion is not 100% efficient; thus, loss of useful energy occurs, typically through waste heat. In other words, there will always be some waste heat released during energy conversions.

1-e (5 pts) Convective Heat Transfer (give an example)

Heat transfer in which a fluid (gas or liquid) at one temperature comes in contact with a substance at another temperature. Example: heating a room with hot water radiator or a stove.

2. (25 points) For a continuous-flow, completely mixed reactor (i.e., CSTR), do the following:
- 2-a. Set up a mass balance equation for a zero-order contaminant removal rate and then solve it for the steady-state detention time ( $\theta$ ).
- 2-b. For a CSTR system with a flow rate ( $Q$ ) equal to 1,000 m<sup>3</sup>/day, an influent contaminant concentration ( $C_o$ ) equal to 200 mg/L, and a zero-order reaction rate constant ( $k$ ) equal to 20 mg/L · day, calculate the steady-state detention time ( $\theta$ , days) and the reactor volume ( $V$ , m<sup>3</sup>) necessary to achieve a contaminant removal efficiency equal to 90%.

**Solution:**

2-a: Zero-order rate:  $dC/dt = -k$

Write a mass balance for steady-state:  $V dC/dt = 0 = Q C_o - Q C_t - k V$

Divide by  $Q$  and set  $V/Q = \theta =$  hydraulic retention time ( $T$ )

$$0 = C_o - C_t - k \theta$$

Solve for  $\theta$ :  $\theta = (C_o - C_t)/k$

2-b: For an influent contaminant concentration of 200 mg/L and a reactor removal efficiency of 90%,

$$C_t = (1 - 0.9) 200 = 20 \text{ mg/L}$$

$$\theta = (200 - 20) \text{ mg/L} \times (1/20) \text{ L} \cdot \text{day/mg} = 9 \text{ days}$$

$$\text{But, } \theta = V/Q \Rightarrow V = \theta Q = (9 \text{ d}) 1000 \text{ m}^3/\text{d} = 9,000 \text{ m}^3$$

3. (25 points) A homeowner is considering buying a new natural gas furnace. Assume natural gas is 100% methane delivered at 25°C and 1 atm pressure. The methane lower heating value (LHV or net heat of combustion) at 25°C is -802.2 kJ/mol of methane, whereas its higher heating value (HHV or gross heat of combustion) at 25°C is -890.2 kJ/mol of methane. For a typical home in Georgia with an annual gas consumption equivalent to 20,000 kWh and the price of 1 m<sup>3</sup> of natural gas at \$0.26, calculate the annual savings in dollars related to natural gas consumption if the homeowner buys a condensing as opposed to a non-condensing furnace.

Note: 1 kWh = 3,600 kJ

**Solution:**

Gas volume/mol at 25°C and 1 atm:

$$V = n R T/P = 1 \text{ mol} \times 0.082 \text{ L atm/mol K} \times 298 \text{ K} \times 1/1 \text{ atm} = 24.4 \text{ L/mol} = 0.0244 \text{ m}^3/\text{mol}$$

**A) Annual gas cost for a non-condensing furnace:**

$$\begin{aligned} \text{Energy/m}^3 \text{ gas} &= (802.2 \text{ kJ/mol gas}) \times (1/3,600 \text{ kWh/kJ}) \times (1 \text{ mol gas}/0.0244 \text{ m}^3 \text{ gas}) = \\ &= 9.13 \text{ kWh/m}^3 \text{ gas} \end{aligned}$$

$$\text{Gas cost} = (20,000 \text{ kWh/yr}) \times (1/9.13 \text{ kWh/m}^3 \text{ gas}) \times (\$0.26/\text{m}^3 \text{ gas}) = \$569.6/\text{year}$$

**B) Annual gas cost for a condensing furnace:**

$$\begin{aligned} \text{Energy/m}^3 \text{ gas} &= (890.2 \text{ kJ/mol gas}) \times (1/3,600 \text{ kWh/kJ}) \times (1 \text{ mol gas}/0.0244 \text{ m}^3 \text{ gas}) = \\ &= 10.13 \text{ kWh/m}^3 \text{ gas} \end{aligned}$$

$$\text{Gas cost} = (20,000 \text{ kWh/yr}) \times (1/10.13 \text{ kWh/m}^3 \text{ gas}) \times (\$0.26/\text{m}^3 \text{ gas}) = \$513.3/\text{year}$$

$$\text{Savings} = \$569.6 - \$513.3 = \$56.3/\text{year} \quad \text{Or } (\$56.3/\$569.6) \times 100 = 9.9\% \text{ savings}$$

**Alternative, shorter solution:**

$$\text{Yearly gas consumption: } 20,000 \text{ kWh} \times 3,600 \text{ kJ/kWh} = 7.2 \times 10^7 \text{ kJ/year}$$

$$\text{Difference condensing vs. non-condensing furnace: } 890.2 - 802.2 = 88 \text{ kJ/mol methane}$$

$$\text{Savings: } 88/890.2 = 0.0989 \text{ per mol methane}$$

$$(7.2 \times 10^7 \text{ kJ/year}) \times (1/802.2 \text{ kJ/mol}) \times 0.0989 = 8,872 \text{ mol methane/year}$$

$$(8,872 \text{ mol methane/year}) \times (0.0244 \text{ m}^3/\text{mol}) \times \$0.26/\text{m}^3 = \$56.3/\text{year}$$

4. **(25 points)** An uncovered swimming pool loses 1 inch of water off of its 1,000 ft<sup>2</sup> surface per week due to evaporation. The heat of vaporization for water at the pool temperature is 1,050 BTU/lb. The cost of energy to heat the pool is \$10 per million BTU. A salesman claims that a \$500 pool cover that reduces evaporative water losses by two-thirds will pay for itself in one 15-week swimming season. Can it be true?

Note: 1 ft = 12 in; water specific weight = 62.4 lb/ft<sup>3</sup>

**Solution:**

Energy lost due to water evaporation:

$$1 \text{ in/week} \times 15 \text{ wks} \times 1 \text{ ft}/12 \text{ in} \times 1,000 \text{ ft}^2 \times 62.4 \text{ lb/ft}^3 \times 1,050 \text{ BTU/lb} = 81.9 \times 10^6 \text{ BTU/season}$$

Cover saves:

$$2/3 \times 81.9 \times 10^6 \text{ BTU/season} \times \$10/10^6 \text{ BTU} = \$546/\text{year}$$

ANSWER: Yes, a \$500 cover does pay for itself in less than one season.