

Name: Solutions

GTID: _____

MSE 2001 B: Principles and Applications of Engineering Materials

Midterm exam 3, July 15, 2014, 10am – 11am

Please read this cover sheet carefully before continuing with the exam.

Please remove everything from your desk except this test itself, writing instruments, and a calculator.

All pages are numbered at the bottom of the page. Make sure that you have all 9 pages including this cover page (p.1). Work all problems in the spaces below the problem statement. You can use the back side of the pages for scratch, but I will not grade answers written on the back side. Do not remove the staple or tear out any pages except the last two pages (p.8 & p.9).

I will not grade your exam if you fail to sign on the line below.

I acknowledge the above terms for taking this exam. I commit to uphold the ideals of honor and integrity by refusing to betray the trust bestowed upon me as a member of the Georgia Tech community. I pledge my honor that I have not violated the Honor Code during this examination.

Student's signature: _____

1. Circle the correct answer (15 points)

(1) At high altitudes the boiling point of water is

- (a) above 100 °C (b) below 100 °C

(2) A copper-aluminum alloy contains 10% weight percentage of copper. The atomic mass of Cu is larger than that of Al. The atomic percentage of copper in this alloy is

- (a) above 10% (b) below 10%;

(3) When there is a clustering tendency in the solid phase of a two-component system, the solidus boundary will bend

- (a) downward (b) upward

(4) The general formula for a peritectoid reaction is

- (a) $\gamma + \beta \leftrightarrow \alpha$ (b) $\gamma \leftrightarrow \alpha + \beta$

(5) The lower the temperature is, the faster the rate of solidification will be.

- (a) True (b) False

(6) When the amount of undercooling ΔT is increased, the critical radius r^* for homogeneous nucleation will

- (a) increase (b) decrease

(7) In cloud seeding, silver iodide is added to trigger

- (a) homogeneous nucleation (b) heterogeneous nucleation

(8) When you dip your finger into a soda drink, small carbon dioxide bubbles will emerge around your finger. This is because your skin provides ____ for the evaporation of CO_2 :

- (a) preferred nucleation sites (b) heat as activation energy

(9) The most important phase transformation in a 0.77% (wt% of C) steel is a

- (a) eutectic reaction (b) eutectoid reaction

(10) Which of the following mixtures of ferrite + cementite has a layered texture?

- (a) pearlite (b) bainite

(11) Pearlite formed at higher temperature is coarser than that formed at lower temperature. This results from the temperature dependence of

- (a) diffusion of carbon atoms (b) thermal expansion of the alloy

(12) As the carbon content in steel increases, ___ undercooling is required to induce the martensitic phase transformation.

(a) less

(b) more

(13) For a eutectoid steel, the transformation from austenite (γ) to _____ is a diffusionless process.

(a) martensite

(b) spheroidite

(14) The process to transform martensite into spheroidite is called

(a) tempering;

(b) quenching

(15) "Coring" usually occurs during

(a) equilibrium solidification

(b) non-equilibrium solidification

2. (10 points)

The figure shows the Ag-Cu phase diagram.

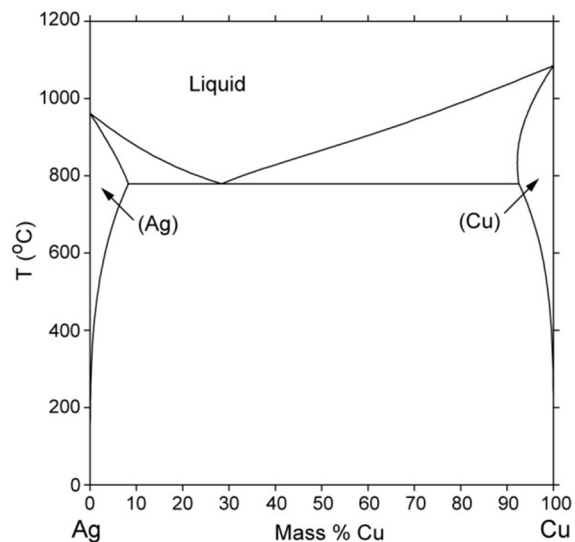
(a) Write down the type and equation for the invariant reaction in the diagram. (1 pt)

(b-d) Sketch the cooling curve for an Ag-Cu alloy with

(b) 0% Cu (pure Ag)

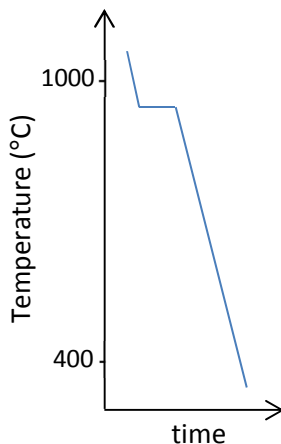
(c) 29% Cu

(d) 50% Cu

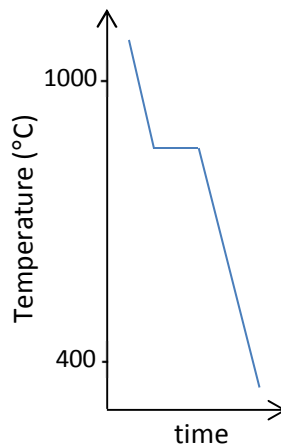


(a) The invariant reaction is _____ [L \rightarrow Ag + Cu, eutectic]

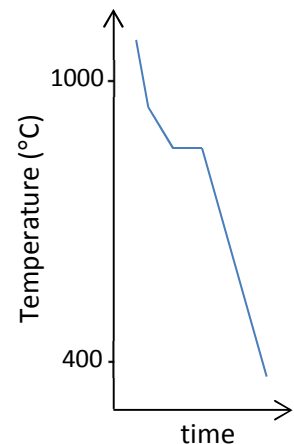
(b)



(c)



(d)



3. (25 points)

Answer the following questions based on the Nb-Ge phase diagram on page 8.

(a, 10 pt) Find five invariant reactions. Express each reaction in the following format (a fake example): Eutectic at 1234 °C with composition 56% Ge, L \rightarrow α + Nb₇Ge₈

eutectic at 1865 °C with composition 27%Ge, L \rightarrow β + Nb₅Ge₃
eutectic at 1580 °C with composition 59%Ge, L \rightarrow Nb₅Ge₃ + NbGe₂
peritectic at 1900 °C with composition 18%Ge, L + Nb \rightarrow β
congruent melting at 2180 °C with composition 37%Ge, L \rightarrow Nb₅Ge₃
congruent melting at 1680 °C with composition 66%Ge, L \rightarrow NbGe₂

(b, 5 pt)

Calculate the Gibbs degrees of freedom for the following state points:

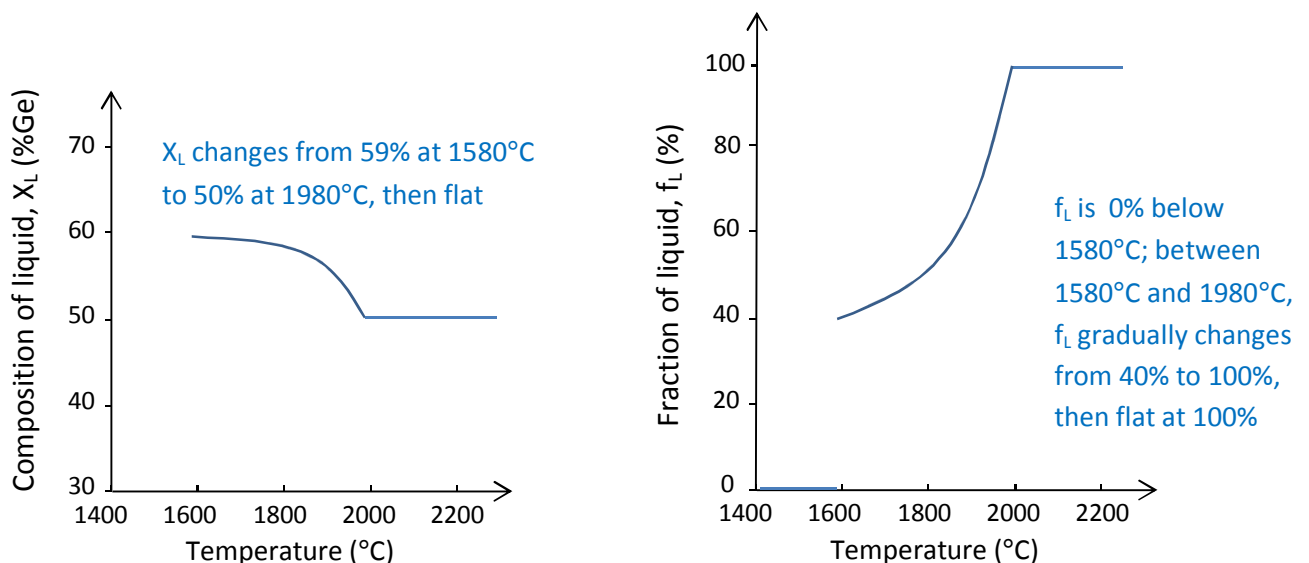
Point 1: $X_0 = 18\%$ Ge at 1900 °C, $F =$ 0; Point 2: $X_0 = 90\%$ Ge at 1000 °C, $F =$ 1

Point 3: $X_0 = 40\%$ Ge at 1600 °C, $F =$ 2; Point 4: $X_0 = 30\%$ Ge at 2000 °C, $F =$ 1

Point 5: $X_0 = 60\%$ Ge at 2000 °C, $F =$ 2

(c, 10 pt)

An Nb-Ge alloy with $X_0 = 50\%$ Ge is slowly heated from 1400°C to 2200°C. Sketch (1) The composition of the liquid phase (X_L) as a function of temperature; (2) The fraction of the liquid phase (f_L) as a function of temperature.



4. (20 points)

The phase diagram for the Cu-Ag binary system is shown on p.9.

(a) For an alloy of composition 40 wt%Ag cooled slowly from the melt, what is the mass fraction of pro-eutectic α -phase at the room temperature?

(note: pro-eutectic α means the α -phase formed before the eutectic isotherm)

Using the lever at a temperature just above the eutectic temperature will give us the mass fractions of the pro-eutectic phase:

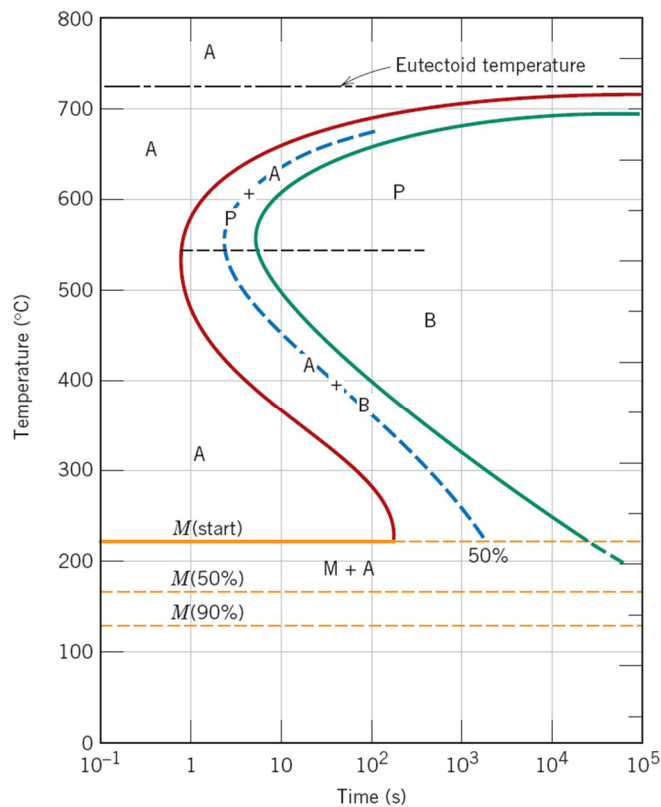
$$M_{PRO-\alpha} = \frac{C_{EUT} - C_0}{C_{EUT} - C_{\alpha}} = \frac{71.9 - 40.0}{71.9 - 8.0} = 50\%.$$

(b) An alloy of composition 20 wt%Ag is heated to a temperature within the (α + Liquid) phase region. If the composition of the liquid phase is 50 wt%Ag, determine (1) the temperature of the alloy; (2) the mass fraction of the liquid phase (f_L) at this temperature.

Draw a vertical line at 50% wt%Ag, and it intersects with the liquidus boundary of the (α +L) zone at the temperature of 875 °C

Draw a tie line at this temperature, and we find $f_L = (20-8)/(50-8) = 0.286$

5. (15 points)



The figure shows the isothermal transformation diagram for a eutectoid steel.

A: Austenite

B: Bainite

M: Martensite

P: Pearlite

(a) Describe the phases present and the microstructures that would occur with quench path:

Instantaneously quench to 450°C → hold for 10 seconds → quench to room temperature.

450°C for 10s: ~50% of austenite is transformed to bainite and ~50% remaining austenite. After quenched to room temperature, 50% bainite and 50% martensite.

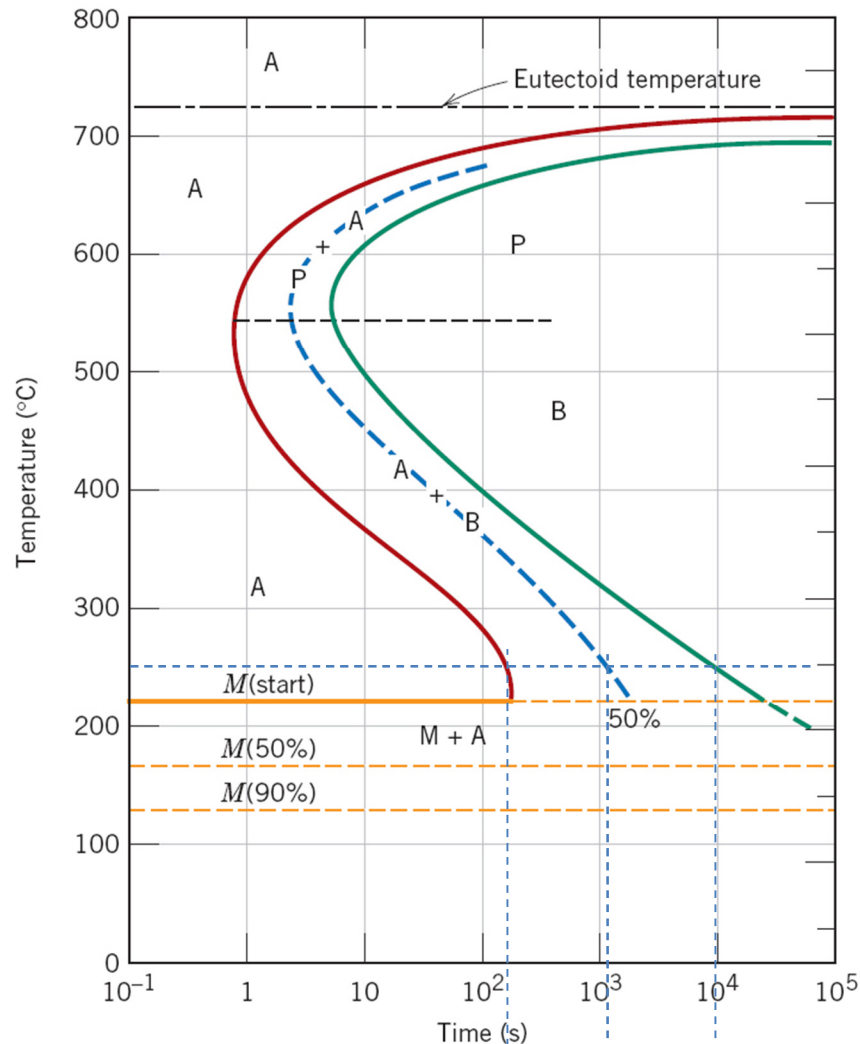
(b) A piece of carbon steel (unknown microstructure) with the eutectoid composition (0.77% C) is to be recycled. Describe a heat treatment that would result in 100% fine pearlite.

Above 727°C hold to form 100% austenite (γ), then instantaneously quench to 550°C (or up until 600°C). Hold for at least 8 seconds.

(c) A piece of eutectoid carbon steel is held at 800°C for sufficiently long. The steel is then to be quenched at a constant cooling rate. Estimate the slowest possible cooling rate (unit: °C/second) that would result in 100% martensite.

To avoid the starting C curve for ($\gamma \rightarrow \alpha + \text{Fe}_3\text{C}$) transformation, the minimum rate is approximately $(800^\circ\text{C} - 500^\circ\text{C}) / 1 \text{ sec} = 300^\circ\text{C/s}$

6. (15 points)



We see again the isothermal transformation diagram for a eutectoid steel.

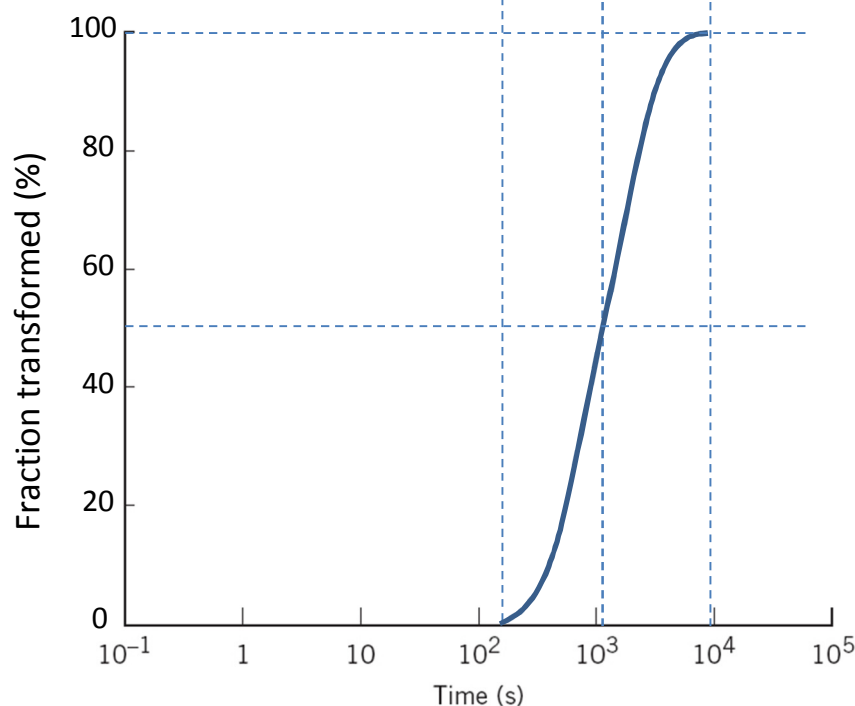
(a, 10 pt) Based on the C curves, sketch the fraction transformed as a function of time for the Austenite \rightarrow Bainite transformation at the temperature of 250°C

(b, 5 pt) The fraction of transformed material can be described by the JMA equation:

$$X = 1 - \exp[-(kt)^n]$$

In this reaction, $n \approx 2$.

Estimate the constant k .



Look at the 50% point:

$$n = 2$$

$$X = 0.5$$

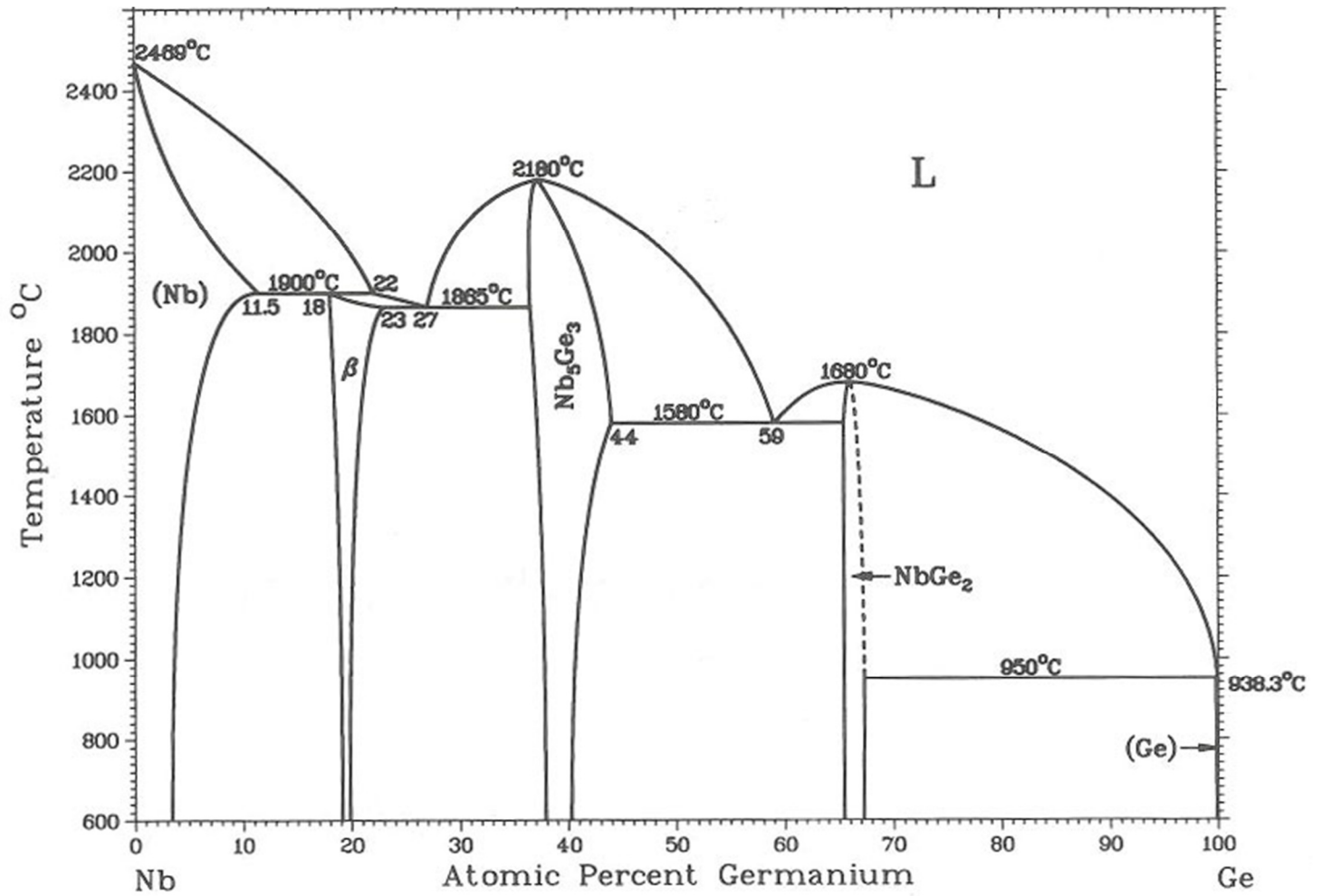
$$t \approx 1000 \text{ sec}$$

Solve for k ,

$$\text{we get } k = 0.00083/\text{sec}$$

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Nb-Ge phase diagram for problem #3



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Cu-Ag phase diagram for problem #4

