

name: **SOLUTION**

Closed book/notes; 50 minutes; 75 points.

| 1. | (25 pts) Short answer. Put answers in spaces provided. | |
|----|---|---------------------|
| a) | Approximately how much air does an adult inhale per day? ~ 15 m³ (5-30 m³) | (1) |
| | Approximately how much water does an adult ingest per day? ~2 L (1-8 L) | (1) |
| | Give a limitation in assessing human health risk using results from each of the following. | |
| | animal studies: extrapolation across species and to low dose | |
| | epidemiologic studies: statistical not causal; confounding issues | (2) |
| | What are the two leading causes of death in the U.S.? | |
| | (1) <u>heart attack</u> (2) <u>cancer</u> | (2) |
| b) | Biomass fuels have a similar carbon intensity (gC/MJ) as coal. So why is their use | |
| | proposed as a means to reduce global warming? consumes CO2 when grown | (1) |
| | On an energy basis, is natural gas, oil, coal or uranium most abundant? uranium | (1) |
| | On an energy basis, is natural gas, oil, coal or uranium most used? oil | (1) |
| | Energy intensity (MJ/GDP) in the U.S. and Canada is higher than in many European | |
| | countries with similar standard of living. Give two reasons why this might be so. | |
| | (1) <u>low population density – greater need to transport goods</u> | |
| | (2) less efficient; more wasteful – e.g. large cars, excessive heating & cooling | (2) |
| | True or false. Since the 1970s, U.S. per capita energy consumption has been steady. <u>true</u> | (1) |
| c) | At what rate is the atmospheric CO_2 concentration increasing? $\sim 2 \text{ ppm/yr} (0.5-4 \text{ ppm/yr})$ | (1) |
| | List three strategies for stabilizing or reducing CO ₂ levels in the atmosphere. | |
| | (1) <u>switch fuels – C ⁻</u> (2) <u>sequester – capture/store</u> (3) <u>reduce demand – eff. –</u> | (3) |
| | In addition to CO ₂ , identify two other greenhouse gases. | |
| | (1) <u>CH4</u> (2) <u>N2O (also CFCs)</u> | (2) |
| | True or false. Increased airborne particles have had a net cooling effect on the earth. true | (1) |
| | How much earth warming (°C) has been observed since 1800? ~0.8 °C (0.4-2 °C) | (1) |
| d) | Approximately what percentage of water cycling between the earth and atmosphere | |
| | is available via runoff from land to ocean? ~8% (1-15%) | (1) |
| | What two processes govern water transfer from the earth to the atmosphere? | |
| | (1) <u>evaporation</u> (2) <u>transpiration</u> | (2) |
| e) | True or false. Since ambient air quality monitoring began in Atlanta in 1970, | |
| | increased vehicle use has resulted in higher ambient CO levels. false | |
| | increased energy use has resulted in higher ambient SO ₂ levels. false | <i>(</i> 2 <i>)</i> |

2. (30 pts) Short problems (mass). Show all work, and put answers in spaces provided.

a) Worldwide, estimate the annual carbon emissions from production of 2x10⁶ MW of electricity from coal. Use the following average data: 40% power plant efficiency, 30 MJ/kg net heating value, 80% (mass) carbon content, 99% carbon emission. (W = J/s)

$$2 \times 10^6 \text{ MW} / 0.4 / 30 \text{ MJ/kg} \times 0.8 \times 0.99 = 1.32 \times 10^5 \text{ kgC/s}$$

 $1.32 \times 10^5 \times 60 \times 60 \times 24 \times 365 = 4.16 \times 10^{12} \text{ kgC/yr}$

Answer (A/B/C/D):
$$4.16 \times 10^{12} / 4.38 \times 10^{12} / 4.63 \times 10^{12} / 4.90 \times 10^{12}$$
 kgC/yr (4)

The total mass of the atmosphere is about $5x10^{18}$ kg. If all of the emitted carbon calculated above remained in the atmosphere as CO_2 , what would be the annual increase in CO_2 concentration (ppm). MW data: air = 29 g/mol (average); C = 12 g/mol; O = 16 g/mol

$$4.16 \times 10^{12} \text{ kgC/yr} / 5 \times 10^{18} \text{ kg x } 10^6 = 0.83 \text{ ppm (mass)}$$

 $0.83 \times 29 / 12 = 2.01 \text{ ppm (vol)}$

Answer (A/B/C/D):
$$2.01/2.12/2.24/2.37$$
 ppm(vol)/yr (4)

b) Diesel fuel (a pure hydrocarbon with H/C molar ratio of 1.6) is burned in 40% excess air (21% O₂ and 79% N₂). Calculate the air-to-fuel mass ratio, first writing the combustion reaction of fuel and air going to CO₂, H₂O, N₂, and O₂.

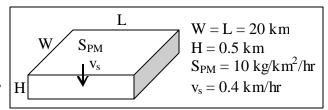
Atomic mass (g/mol): C = 12, H = 1, O = 16, N = 14

combustion rxn: $CH_{1.6} + 1.96 (O_2 + 79/21 N_2) \rightarrow 1 CO_2 + 0.8 H_2O + 0.56 O_2 + 7.37 N_2$

$$(1.96 \times 32 + 1.96 \times 3.76 \times 28) / (12+1.6) = 19.8$$

Answer (A/B/C/D):
$$19.8/21.2/22.6/24.0$$
 kg-air/kg-fuel (8)

c) In the well mixed urban airshed shown at right, there is an area PM emission source (S_{PM}) and a sink due to settling (settling velocity v_s). There is no wind (in or out). Write a steady state mass balance equation, then solve for PM concentration (ug/m³).



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PM mass balance eq:
$$\underline{0 = 0 - 0 + A S - v_s A C}$$

$$C = S / v_s = 10 / 0.4 = 25 \text{ kg/km}^3 = 25 \text{ mg/m}^3$$

Answer (A/B/C/D):
$$25/33/50/100$$
 mg/m³ (8)

For a sudden reduction in the source emission, write an unsteady PM mass balance equation. Provide a characteristic time (hr) for the change in PM concentration, and define its meaning.

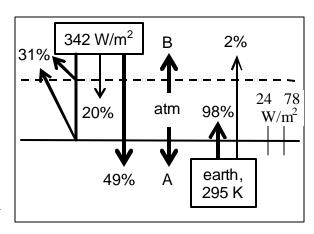
PM mass balance eq: $V dC/dt = AS - v_s AC$

$$dC / (S/v_s - C) = V/(v_s A) dt = H/v_s dt \rightarrow t_{ch} = H/v_s = 0.5/0.4 = 1.25 hr$$

Answer (A/B/C/D): $t_{ch} = 1.3/1.7/2.5/5.0$ hr

definition: time to reach 63% of new steady state (6)

- 3. (20 pts) Energy balance problems. Show all work, and put answers in spaces provided.
- a) Write steady-state energy balances for the earth-atmosphere system shown at right, which includes radiative fluxes (sun, atmosphere and earth) and convective and evaporative fluxes (24 and 78 W/m²). For the incoming solar energy (342 W/m²), percentages reflected and absorbed and transmitted by the atmosphere are shown. The earth radiates as a blackbody (σ T⁴ where $\sigma = 5.67 \times 10^{-8}$ W/m²/K⁴), with percentages absorbed by the atmosphere and escaping to space shown. Its temperature is



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given. The atmosphere radiates differently to earth (A) and to space (B). Estimate the temperatures of the upper and lower atmosphere, assuming it radiates as a gray body (ϵ σ T^4 where $\epsilon = 0.98$).

Earth energy balance equation:
$$\underline{0.49 \text{ S} + \text{A} = \text{E} + 24 + 78}$$
 (4)

Atmosphere energy balance equation: $\underline{0.2 \text{ S} + 0.98 \text{ E} + 24 + 78 = \text{A} + \text{B}}$ (4)

$$\begin{array}{lll} E = 5.67x10^{-8} \; x \; (295)^4 = 429.4 \; W/m^2 \\ A = 363.8 \; W/m^2 & \rightarrow & T_{lower \; atm} = (363.8/0.98/5.67x10^{-8})^{^{1/4}} = 284 \; K \\ B = 227.4 \; W/m^2 & \rightarrow & T_{lower \; atm} = (227.4/0.98/5.67x10^{-8})^{^{1/4}} = 253 \; K \end{array}$$

A/B/C/D:
$$T_{upper atm} = \frac{253/252/251/250}{K}$$
 K
A/B/C/D: $T_{lower atm} = \frac{284}{284} \frac{283}{282}$ K (4)

b) In a diesel engine, isentropic compression ($PV^{1.4} = constant$) of air occurs with a compression ratio, V_1/V_2 , of 13. For air intake conditions of $P_1 = 1$ atm and $T_1 = 300$ K, calculate the temperature after compression and before combustion (T_2). Ideal gas law: PV = nRT

isentropic process:
$$P_2 = P_1 \ (V_1/V_2)^{1.4} = 1 \ x \ (13)^{1.4} = 36.3 \ atm$$
 ideal gas law: $T_2 = T_1 \ (P_2/P_1) \ (V_2/V_1) = 300 \ x \ 36.3 \ / \ 13 = 837 \ K$

A/B/C/D:
$$T_2 = 837/862/886/909$$
 K (4)

Fuel is injected (air-to-fuel mass ratio = 20) and combustion occurs at constant pressure. Using an average gas specific heat (c_p) of 1100 J/kg/°C and a net fuel heating value of 45 MJ/kg, calculate the gas temperature increase from combustion without heat loss (T_3-T_2) .

$$\begin{split} E_{fuel} &= m_{fuel} \ x \ 45 x 10^6 \ J/kg = E_{air} = m_{air} \ x \ 1100 \ J/kg/^{\circ} \ C \ x \ DT \\ DT &= (m_{fuel}/m_{air}) \ x \ 45 x 10^6 \ / \ 1100 = (1/20) \ x \ 45 x 10^6 \ / \ 1100 = 2045 \ ^{\circ} \ C \end{split}$$

$$T_3 - T_2 = 2045 \,^{\circ} C$$
 (4)