

Solutions to Homework 5

$$1) a) F(x) = \begin{cases} 0 & \text{if } x \leq 0 \\ \frac{x^2}{4} & \text{if } 0 < x < 2 \\ 1 & \text{if } x \geq 2 \end{cases}$$

$$b) P\left(X > \frac{3}{2}\right) = 1 - P\left(X \leq \frac{3}{2}\right) = 1 - \frac{\left(\frac{3}{2}\right)^2}{4} = 1 - \frac{9}{16} = \frac{7}{16}$$

$$2) a) \left(\frac{1}{2}\right)^3 \left(\frac{1}{4}\right)^2$$

$$b) \binom{3}{1} \left(\frac{1}{2}\right)^3 \left(\frac{1}{4}\right)^2 + \binom{2}{1} \left(\frac{1}{4}\right) \left(\frac{3}{4}\right) \left(\frac{1}{2}\right)^3$$

$$c) \binom{3}{1} \left(\frac{1}{2}\right)^3 \left(\frac{3}{4}\right)^2 + \binom{2}{1} \left(\frac{1}{4}\right) \left(\frac{3}{4}\right) \left(\frac{1}{2}\right)^3$$

$$3) F(x) = 1 - e^{-\lambda x} \quad \text{as we derived in class}$$

$$P\left(X > \frac{2}{\lambda}\right) = 1 - F\left(\frac{2}{\lambda}\right) = e^{-2}$$

$$4) f(x) = \begin{cases} 6x - 6x^2 & 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$