

Name: _____SOLUTIONS_____

GTID: _____

MSE 2001 A: Principles and Applications of Engineering Materials

Midterm exam 3, July 15, 2013, 10am – 11am

Please remove everything from your desk except this test itself, writing instruments, and a calculator.

All pages are numbered at the bottom center of the page. Make sure that you have all 6 pages including this cover page (p.1). Work all problems in the spaces below the problem statement. You can use the back side of the pages for scratch, but I will not grade answers written on the back side. Do not remove the staple or tear out any pages except the last page (p.6).

I will not grade your exam if you fail to sign on the line below.

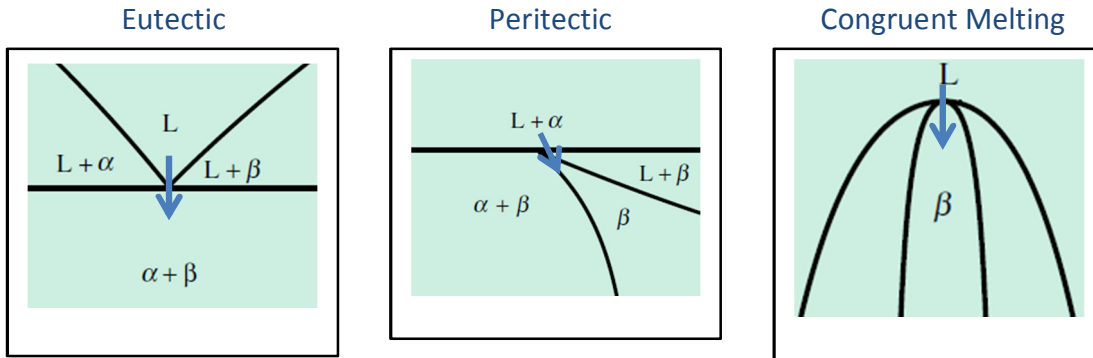
I acknowledge the above terms for taking this exam. I commit to uphold the ideals of honor and integrity by refusing to betray the trust bestowed upon me as a member of the Georgia Tech community. I pledge my honor that I have not violated the Honor Code during this examination.

Student's signature: _____

1. Match the correct pairs (17 pts)

- | | |
|----------------------------|---|
| A. Liquidus | _O_ Controlled by diffusion |
| B. Solidus | _I_ Fe_3C |
| C. Hypoeutectoid Steel | _A_ Temperature above which only a liquid exists |
| D. Hypereutectoid Steel | _K_ Re-heating to relieve stresses |
| E. Martensite | _N_ Interface between different crystal structures |
| F. Spheroidite | _Q_ Produce solid materials from powders |
| G. Pearlite | _G_ Layered Structure of $\alpha + \text{Fe}_3\text{C}$ |
| H. Bainite | _L_ A short heat treatment to regain ductility |
| I. Cementite | _C_ Contains $< 0.77 \text{ wt\% C}$ |
| J. Ferrite | _H_ Fe_3C needles in an α phase |
| K. Tempering | _P_ Formation of a new phase |
| L. Anneal | _B_ Temperature below which only a solid exists |
| M. Semicohherent interface | _M_ Solid-solid interface with periodic dislocations |
| N. Incoherent interface | _F_ Forms when tempering for too long |
| O. Growth | _J_ α -iron |
| P. Nucleation | _D_ Contains $> 0.77 \text{ wt\% C}$ |
| Q. Sintering | _E_ The strongest of all common phases in steels |

2. Draw a schematic for each of the following three invariant reactions (3 pts)



3. Using the Mg-Cu phase diagram on the last page, answer the following questions (30 pts)

(a) What are the components of this phase diagram? _____ Mg and Cu _____ List their melting points _____ Mg: 650°C; Cu: 1084.87°C _____

(b) How many solid solutions appear in this phase diagram? __4__ Name them: _____
 _____ Mg, Cu, Mg₂Cu, MgCu₂ _____

(c) What is the maximum solid solubility of Cu in Mg? __0.013 at% Cu _____
 What is the maximum solid solubility of Mg in Cu? __100-93.07 = 6.93 at% Mg _____

(d) Are there any line compounds? __Yes__ If so, name them _____ Mg₂Cu _____

(e) Are there any peritectics in this phase diagram? __No__ How many? _____ If yes, indicate the melting point(s) and phase names and write the equation for one of them.

(Note: "equation" means something like $L + \text{Solid A} \rightarrow \text{Solid B}$)

(f) Are there any eutectics or eutectoids in this phase diagram? __Yes__ How many? __3__
 If yes, indicate their eutectic temperature and compositions. _____

X₀=14.5% at T=485°C; X₀=42% at T=552°C; X₀=76.9% at T=725°C;

Write the equation for one of them _____ For example, the first one is $L \rightarrow \text{Mg} + \text{Mg}_2\text{Cu}$ _____

(g) Are there any other invariant reactions not yet mentioned? __Yes__ If yes, what are they and at what temperatures and compositions do they occur?

There are two congruent melting reactions:

X₀=33% at T=568°C: $L \rightarrow \text{Mg}_2\text{Cu}$; X₀=66% at T=797°C: $L \rightarrow \text{MgCu}_2$;

(h) Using the Gibbs phase rule, calculate the number of degrees of freedom for points A, B, C and D on the Mg-Cu phase diagram.

Point A: $x_0 = 76.9$ at% Cu at 725°C ;

Point B: $x_0 = 25$ at% Cu at 500°C ;

Point C: $x_0 = 67$ at% Cu at 500°C ;

Point D: $x_0 = 50$ at% Cu at 1000°C .

Point A: $F_A = 2-3+1=0$

Point B: $F_B = 2-2+1=1$

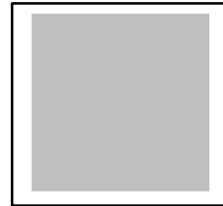
Point C: $F_C = 2-1+1=2$

Point D: $F_D = 2-1+1=2$

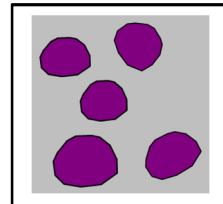
4. Based on the Mg-Cu phase diagram on the last page, for an alloy containing 55% Cu represented by the vertical line, answer the following questions (30 pts)

(a) Indicate the phases present, their composition and microstructure at the following temperatures (12 pts)

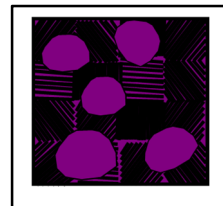
Phases Present Compositions
 $T_1 = 900^\circ\text{C}$ L $X_L = 55\%$



$T_2 = 650^\circ\text{C}$ L and MgCu_2 $X_L = 48\%$; $X_{\text{MgCu}_2} = 65\%$



$T_3 = 500^\circ\text{C}$ Mg_2Cu and MgCu_2 $X_{\text{Mg}_2\text{Cu}} = 33\%$; $X_{\text{MgCu}_2} = 65\%$



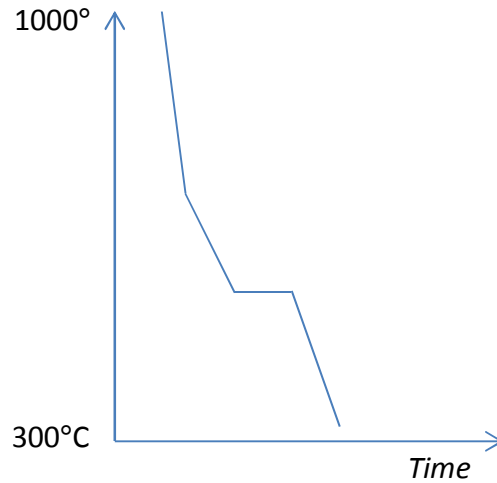
(b) Given 250 g of $X_0 = 55$ at% Cu, what are the relative amounts of the phases present at 900°C ? What are the relative amounts of the phases present at 650°C ? Show all of your work. (12 pts)

At 900°C , all is in liquid form. 250 g of L.

At 650°C , L and MgCu_2 co-exist. Use lever rule: $X_L = 48\%$; $X_{\text{MgCu}_2} = 65\%$

$$f_L = \frac{0.65-0.55}{0.65-0.48} = 0.59; f_{\text{MgCu}_2} = 0.41. \quad m_L = 250 \times 0.59 = 147 \text{ g}; \quad m_{\text{MgCu}_2} = 103 \text{ g}.$$

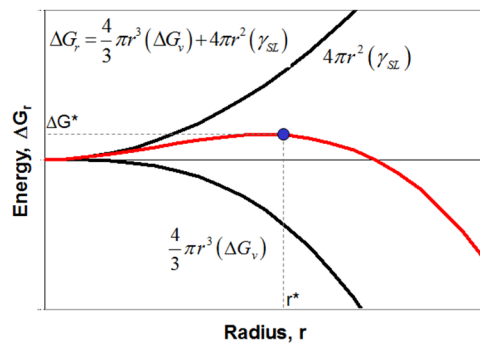
(c) Sketch the equilibrium cooling curve for this alloy ($X_0 = 55 \text{ at\% Cu}$) (6pt)



5. For homogeneous nucleation, the change in free energy to create a nucleus of size r is given by the equation (10 pts),

$$\Delta G(r) = \frac{4}{3}\pi r^3(\Delta G_v) + 4\pi r^2\gamma_{s/l}$$

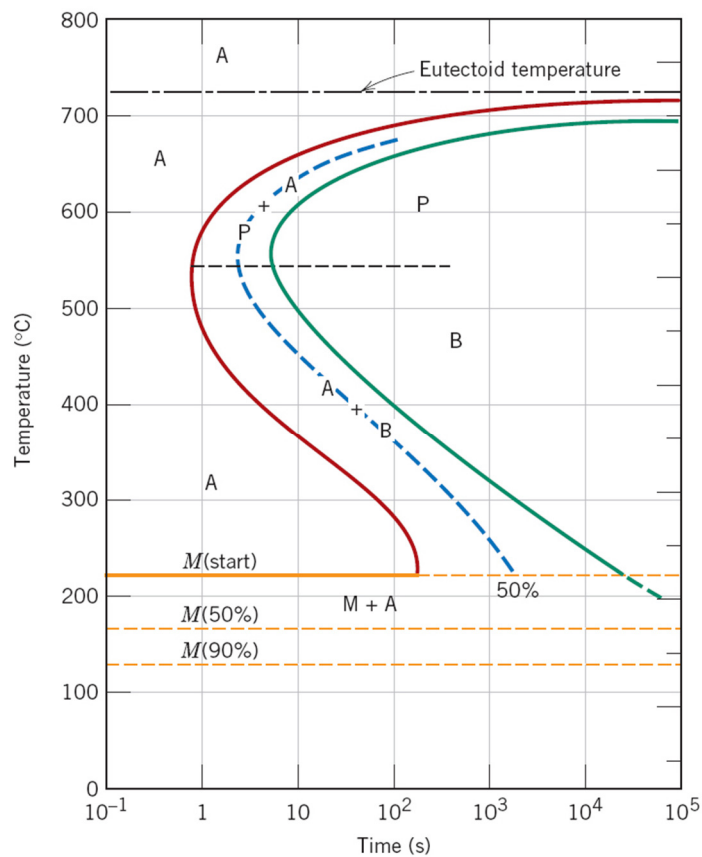
(a) Schematically plot $\Delta G(r)$ as a function of radius for a homogeneous nucleation process. On the same plot, sketch and label the two free energy terms that determine $\Delta G(r)$, the energy barrier for nucleation ΔG^* and the critical radius, r^* . (6 pts)



(b) How do the energy barrier for nucleation ΔG^* and the critical radius r^* change with increased undercooling ΔT ? (4 pts)

Both ΔG^* and r^* decrease with increased undercooling ΔT .

6. Based on the isothermal transformation diagram for a eutectoid steel, answer the following questions (10 pts),



A: Austenite

B: Bainite

M: Martensite

P: Pearlite

(a) Describe the phases present and the microstructures that would occur when a piece of eutectoid steel is held at 800°C for long, and then processed using the following quench path:

Instantaneous quench at 360°C → hold for 100 seconds → rapid quench to room temperature

50% bainite and 50% martensite

(b) Describe a heat treatment that would result in the following microstructure for a plain carbon eutectoid steel:

A 50-50 mixture of coarse pearlite and martensite

For example, hold at 800°C to form austenite, then instantaneously quench to 650°C and hold for 30s (now 50% austenite is transformed to coarse pearlite and 50% austenite left), then instantaneously quench to room temperature.

(Please feel free to tear out this page)

Mg-Cu phase diagram

