

GEORGIA INSTITUTE OF TECHNOLOGY

COLLEGE OF ENGINEERING

BMED3300 - BIOTRANSPORT

QUIZ 2 (SPRING 2014) – KEMP

STUDENT NAME: Solution

GTID NUMBER: _____

RECITATION SECTION: _____

(Section A is Wednesdays at 12 noon; Section B is Wednesdays at 10 am)

Closed book

All non-communicating calculator types allowed

Time allotted: 15 minutes

Do all work in this booklet

Reminder: for questions requiring numerical answers, units are required and worth 50%

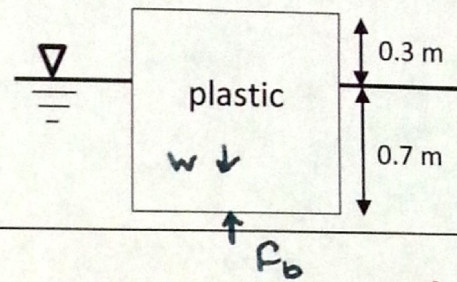
Question	Maximum Mark	Actual Mark
1	6	
2	6	
Total	12	

Maximum possible marks are 12. However, the quiz will be marked out of 10, i.e. if you get 8/12, that is equivalent to 80%.

Hydrostatic pressure in an incompressible fluid: $p = p_0 + \rho gh$

Archimedes' principle: $F_b = \rho g V_{disp}$

1. A solid cube of plastic (dimensions 1 m x 1 m x 1 m) floats in water. The density of the water is 10^3 kg/m^3 and 0.3 m of block is above the surface of the water. What is the density of the plastic cube?



Do your GIM analysis here

- There will be a buoyant force on cube, plus the weight of the cube (1)
- Steady
- Use Archimedes' principle (1)
- System is cube

$$W = \rho_c L^3 g \quad (1)$$

$L = \text{side length} = 1 \text{ m}$

$\rho_c = \text{density of cube}$

$$F_b = \rho_w L^2 h g \quad (1)$$

$h = 0.7 \text{ m}$

$\rho_w = \text{density of water}$

Need to have correct p's for marks

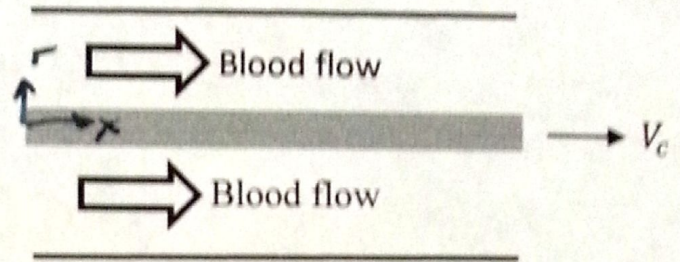
At equilibrium, $W = F_b \quad (1)$

$$\therefore \rho_c L^3 g = \rho_w L^2 h g$$

$$\rho_c = \frac{h}{L} \rho_w = (0.7)(1000 \frac{\text{kg}}{\text{m}^3}) = 700 \frac{\text{kg}}{\text{m}^3} \quad (1)$$

(6)

2. Consider a cylindrical catheter of radius ϵR that is placed in a blood vessel of radius R . Assume that the catheter is concentric with the centerline of the blood vessel. **The catheter is being inserted into the artery and so is moving left to right at speed V_c .** We wish to determine the change in flow rate relative to a vessel of the same radius without a catheter. Assume steady flow and that the pressure drop is the same with and without the catheter.



- What co-ordinate system would you use to solve this problem?
- What physical principle(s) would you use to solve this problem?
- What boundary condition(s) could you apply, given that the catheter is moving in this problem?
- Describe in words the forces that will affect the flow of blood in this vessel.

Note that you do not need to solve the problem; you only need to answer the questions above.

Do your GIM analysis here (parts a -d)

- cylindrical co-ordinates centered on catheter (see diagram) ①
 - conservation of mass + momentum balance (continuity + N-S eq'n's) [need both]. ①
 - No slip: $u_x(r = \epsilon R) = V_c$
 $u_x(r = R) = 0$. ②
 - pressure gradient driving the flow
 - friction due to vessel wall & catheter surface, transmitted through blood by viscosity.
 ②
- ⑥