

**Homework 5, ISyE 2027**  
**Due June 17, Wednesday**

1. Suppose  $X$  is an exponential random variable with parameter  $\lambda$ . Compute its median.
2. The probability density function of  $X$  is given by

$$f(x) = \begin{cases} \frac{x^{-1/2}}{2} & \text{for } 0 < x < 1 \\ 0 & \text{otherwise} \end{cases}$$

- (a) What is the cumulative distribution function of  $X$ ?
- (b) What is the median of  $X$ ?
3. Suppose  $P(X = x) = x/21$  for  $x = 1, 2, 3, 4, 5, 6$ . Find the median of  $X$ .