Theory8

1.

(4)(a)

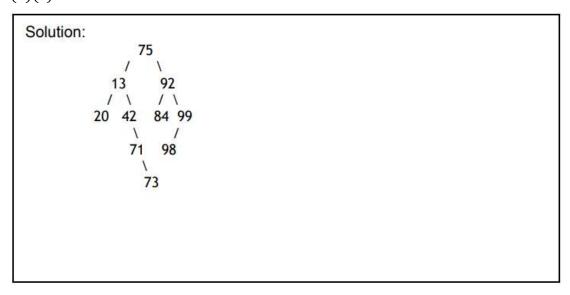
```
Solution:
bool is ht(ht H) {
 if (H == NULL) return false;
  if (!(H->m > 0)) return false;
  if (!(H->n >= 0)) return false;
 //@assert H->m == \length(H->table);
 int nodecount = 0;
 for (int i = 0; i < ______; i++)
    // set p equal to a pointer to first node
    // of chain i in table, if any
    chain* p = H->table[i] ;
    while (__!p__)
      elem e = p->data;
      if ((e == NULL) || (<u>elem_key(e)</u>!= i))
        return false;
      nodecount++;
      if (nodecount > H->n )
        return false;
      p = p->next;
  if ( nodecount != H->n )
    return false;
  return true;
```

(1)(b)

Solution:

/*@ensures \result == NULL || key_equal(k, __elem_key(\result)_);
@*/

2. (1)(a)



(1)(b)

Solution: 42

(3)(c)

```
Solution:
int tree_height(tree* T)
//@requires is_ordered(T, NULL, NULL);
   if (T == NULL)
        return 0;
   int left = 1 + tree_height(T->left);
   int right = 1 + tree_height(T->right);
   if (left < right)
        return right;
   return left;
}
int bst_height(bst B)
//@requires is_bst(B);
//@ensures is_bst(B);
        return tree height(B);
}
```

(5)(d)

```
Solution:
tree* tree delete(tree* T, key k)
   if (T == NULL) {
                                     // key is not in the tree
       return NULL ;
   }
   if (key_compare(k, elem_key(T->data)) < 0) {
          T->left = tree_delete(T->left, k);
      return T;
   } else if (key_compare(k, elem_key(T->data)) > 0) {
        T->right = tree_delete(T->right, k);
      return T;
   } else {// key is in current tree node T
       if (T->left == NULL)
                          // node has only right child
           return T->right ;
       else if (T->right == NULL) // node has only left child
           return T->left ;
       else { // Node to be deleted has two children
           if (T->left->right == NULL) {
               // Replace the data in T with the data
               // in the left child.
                         T->left->right = T->right ;
               // Replace the left child with its left child.
                 T->right = NULL ;
              return T;
           else {
```

```
// Search for the largest child in the
                // left subtree of T and replace the data
                // in node T with this data after removing
                // the largest child in the left subtree. T->data
                = largest_child(T->left); return T;
           }
       }
   }
}
elem largest_child(tree* T)
//@requires T != NULL && T->right != NULL;
{
   if (T->right->right == NULL) {
        elem e = T->right->data
        T->right = T->right->left
        return e;
   }
   return largest_child( T->right->righ->data );
```