Assignment 2

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install.packages("ISLR")

library(ISLR)

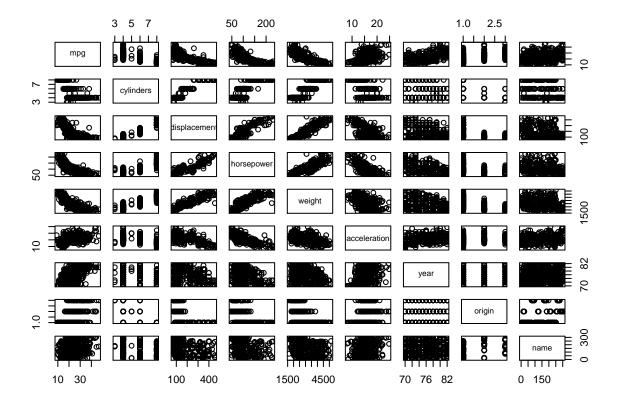
Warning: package 'ISLR' was built under R version 3.6.3

library(MASS)

Warning: package 'MASS' was built under R version 3.6.3

Multilinear Regression

data(Auto)
pairs(Auto)



```
names (Auto)
## [1] "mpg"
                     "cylinders"
                                   "displacement" "horsepower"
## [5] "weight"
                     "acceleration" "year"
                                                  "origin"
## [9] "name"
cor(Auto[1:8])
##
                      mpg cylinders displacement horsepower
                                                               weight
## mpg
                1.0000000 -0.7776175
                                     -0.8051269 -0.7784268 -0.8322442
               -0.7776175 1.0000000
                                     0.9508233 0.8429834 0.8975273
## cylinders
## displacement -0.8051269 0.9508233 1.0000000 0.8972570 0.9329944
## horsepower
               -0.7784268  0.8429834  0.8972570  1.0000000  0.8645377
## weight
               -0.8322442 0.8975273
                                     0.9329944 0.8645377 1.0000000
## acceleration 0.4233285 -0.5046834 -0.5438005 -0.6891955 -0.4168392
## year
              0.5805410 -0.3456474 -0.3698552 -0.4163615 -0.3091199
              0.5652088 -0.5689316 -0.6145351 -0.4551715 -0.5850054
## origin
##
              acceleration
                                 year
                                          origin
                0.4233285 0.5805410 0.5652088
## mpg
## cylinders
                -0.5046834 -0.3456474 -0.5689316
## displacement -0.5438005 -0.3698552 -0.6145351
## horsepower
                -0.6891955 -0.4163615 -0.4551715
## weight
                -0.4168392 -0.3091199 -0.5850054
## acceleration
                1.0000000 0.2903161 0.2127458
## year
                 0.2903161 1.0000000 0.1815277
## origin
                 0.2127458 0.1815277 1.0000000
fit2 <- lm(mpg \sim . - name, data = Auto)
summary(fit2)
##
## Call:
## lm(formula = mpg ~ . - name, data = Auto)
## Residuals:
               1Q Median
                              30
## -9.5903 -2.1565 -0.1169 1.8690 13.0604
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) -17.218435 4.644294 -3.707 0.00024 ***
                -0.493376
## cylinders
                           0.323282 -1.526 0.12780
## displacement
                 0.019896 0.007515
                                      2.647 0.00844 **
                           0.013787 -1.230 0.21963
## horsepower
                -0.016951
## weight
                -0.006474
                           0.000652 -9.929 < 2e-16 ***
## acceleration 0.080576
                           0.098845
                                      0.815 0.41548
## year
                 0.750773
                           0.050973 14.729 < 2e-16 ***
## origin
                 1.426141
                           0.278136
                                     5.127 4.67e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.328 on 384 degrees of freedom
```

```
## Multiple R-squared: 0.8215, Adjusted R-squared: 0.8182
## F-statistic: 252.4 on 7 and 384 DF, p-value: < 2.2e-16
par(mfrow = c(2, 2))
plot(fit2)
                                                     Standardized residuals
                                                                          Normal Q-Q
                 Residuals vs Fitted
      15
Residuals
                                                          ^{\circ}
      2
     -10
               10
                    15
                          20
                               25
                                     30
                                          35
                                                                -3
                                                                     -2
                                                                                            2
                                                                                                  3
                      Fitted values
                                                                       Theoretical Quantiles
/Standardized residuals
                                                     Standardized residuals
                                                                    Residuals vs Leverage
                   Scale-Location
     2.0
                                                                     O<sub>2</sub> O394
     1.0
                                                                        Cook's distance
                                                                                                140
     0.0
               10
                    15
                          20
                               25
                                     30
                                          35
                                                              0.00
                                                                       0.05
                                                                                0.10
                                                                                         0.15
                      Fitted values
                                                                             Leverage
fit3 <- lm(mpg ~ cylinders * displacement+displacement * weight, data = Auto[, 1:8])
summary(fit3)
##
## Call:
## lm(formula = mpg ~ cylinders * displacement + displacement *
##
        weight, data = Auto[, 1:8])
##
##
   Residuals:
##
         Min
                     1Q
                           Median
                                                   Max
   -13.2934
              -2.5184
                         -0.3476
                                     1.8399
                                              17.7723
##
##
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               5.262e+01 2.237e+00
                                                         23.519
                                                                   < 2e-16 ***
```

7.669e-01

0.992

-0.872

0.322

0.384

-4.403 1.38e-05 ***

-7.438 6.69e-13 ***

7.606e-01

cylinders:displacement -2.986e-03 3.426e-03

-7.351e-02 1.669e-02

-9.888e-03 1.329e-03

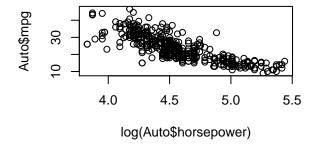
cylinders

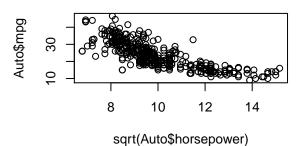
weight

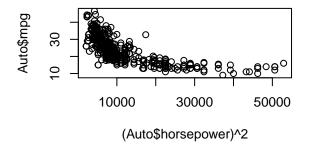
displacement

```
## displacement:weight    2.128e-05   5.002e-06    4.254   2.64e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.103 on 386 degrees of freedom
## Multiple R-squared: 0.7272, Adjusted R-squared: 0.7237
## F-statistic: 205.8 on 5 and 386 DF, p-value: < 2.2e-16

par(mfrow = c(2, 2))
plot(log(Auto$horsepower), Auto$mpg)
plot(sqrt(Auto$horsepower), Auto$mpg)
plot((Auto$horsepower)^2, Auto$mpg)</pre>
```







```
# Qualitative Predictors

fix(Carseats)
names(Carseats)

## [1] "Sales" "CompPrice" "Income" "Advertising" "Population"
## [6] "Price" "ShelveLoc" "Age" "Education" "Urban"

## [11] "US"

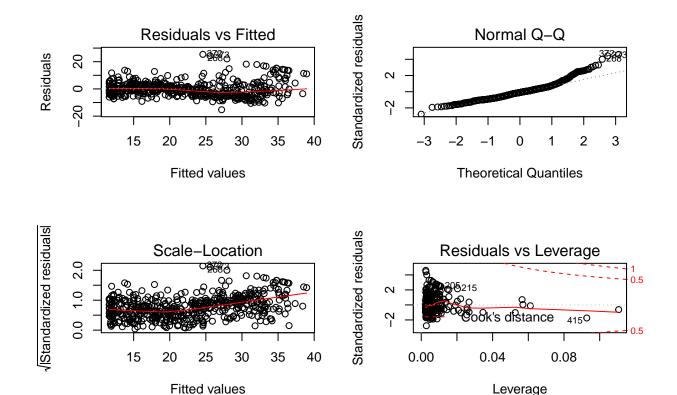
lm.fit=lm(Sales~.+Price:Urban+US,data=Carseats)
summary(lm.fit)
```

```
##
## Call:
## lm(formula = Sales ~ . + Price:Urban + US, data = Carseats)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -2.8723 -0.7011 0.0298 0.6723 3.3937
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   5.5386942 0.7371346
                                         7.514 4.02e-13 ***
## CompPrice
                   0.0928744 0.0041576 22.338 < 2e-16 ***
## Income
                   0.0157950 0.0018475
                                          8.549 2.91e-16 ***
## Advertising
                   0.1233524  0.0111724  11.041  < 2e-16 ***
## Population
                   0.0002072 0.0003709
                                          0.559
                                                   0.577
## Price
                   -0.0943707
                              0.0043411 -21.739
                                                 < 2e-16 ***
## ShelveLocGood
                   4.8492903 0.1533223 31.628 < 2e-16 ***
## ShelveLocMedium 1.9557229 0.1263016 15.485 < 2e-16 ***
                  -0.0461214  0.0031964  -14.429  < 2e-16 ***
## Age
## Education
                  -0.0206165 0.0198153 -1.040
                                                   0.299
## UrbanYes
                   0.2845509 0.5712614
                                          0.498
                                                   0.619
## USYes
                   -0.1855349 0.1501027 -1.236
                                                   0.217
## Price:UrbanYes -0.0014091 0.0048808 -0.289
                                                   0.773
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 1.02 on 387 degrees of freedom
## Multiple R-squared: 0.8734, Adjusted R-squared: 0.8695
## F-statistic: 222.6 on 12 and 387 DF, p-value: < 2.2e-16
attach(Carseats)
contrasts(ShelveLoc)
##
          Good Medium
## Bad
            0
                   0
## Good
            1
                   0
## Medium
            0
                   1
lm.fit=lm(Sales~.+Price:ShelveLoc,data=Carseats)
summary(lm.fit)
##
## Call:
## lm(formula = Sales ~ . + Price:ShelveLoc, data = Carseats)
## Residuals:
##
               1Q Median
                               3Q
      Min
                                      Max
## -2.9005 -0.6943 0.0239 0.6649
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         6.0823218 0.7901950
                                               7.697 1.18e-13 ***
                         0.0928186  0.0041874  22.166  < 2e-16 ***
## CompPrice
```

```
0.0157690 0.0018557 8.497 4.27e-16 ***
0.1232481 0.0111422 11.061 < 2e-16 ***
## Income
## Advertising
## Population
                        0.0001862 0.0003728 0.499 0.6178
## Price
                      -0.0986980 0.0046879 -21.054 < 2e-16 ***
## ShelveLocGood
                        4.1785991 0.7494181 5.576 4.64e-08 ***
## ShelveLocMedium
                        1.5344694 0.6329676 2.424 0.0158 *
                       -0.0464310 0.0032158 -14.439 < 2e-16 ***
## Age
                    -0.0221904 0.0197846 -1.122 0.2627
## Education
## UrbanYes
                        0.1247657 0.1131754 1.102 0.2710
## USYes
                        -0.1827611 0.1500758 -1.218 0.2240
## Price:ShelveLocGood 0.0057959 0.0063142 0.918 0.3592
## Price:ShelveLocMedium 0.0036944 0.0054168 0.682 0.4956
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.02 on 386 degrees of freedom
## Multiple R-squared: 0.8737, Adjusted R-squared: 0.8694
## F-statistic: 205.4 on 13 and 386 DF, p-value: < 2.2e-16
attach(Carseats)
## The following objects are masked from Carseats (pos = 3):
##
##
       Advertising, Age, CompPrice, Education, Income, Population,
##
      Price, Sales, ShelveLoc, Urban, US
contrasts(ShelveLoc)
          Good Medium
##
## Bad
            0
                   0
## Good
            1
## Medium
#install.packages("Rmisc")
library(Rmisc)
## Warning: package 'Rmisc' was built under R version 3.6.3
## Loading required package: lattice
## Loading required package: plyr
myData <- Carseats</pre>
CI(Carseats$ShevleLoc, ci=0.95)
## Warning in mean.default(x): argument is not numeric or logical: returning
## NA
## Warning in qt(ci + (1 - ci)/2, df = n - 1): NaNs produced
```

```
## upper mean lower
##
     NΑ
                 NΑ
           NΑ
confint(lm.fit)
                               2.5 %
                                            97.5 %
## (Intercept)
                        4.5286967907 7.6359468440
## CompPrice
                        0.0845856984 0.1010515389
## Income
                        0.0121203674 0.0194176506
## Advertising
                        0.1013410799 0.1451551553
## Population
                       -0.0005468093 0.0009191648
## Price
                       -0.1079149004 -0.0894810304
## ShelveLocGood
                        2.7051465912 5.6520515717
## ShelveLocMedium
                        0.2899735095 2.7789652884
## Age
                       -0.0527536069 -0.0401083721
## Education
                       -0.0610894563 0.0167085653
## UrbanYes
                       -0.0977516742 0.3472831395
## USYes
                        -0.4778295223 0.1123072528
## Price:ShelveLocGood -0.0066186981 0.0182104076
## Price:ShelveLocMedium -0.0069557012 0.0143445885
# Non Linear Regression
str(Boston)
                   506 obs. of 14 variables:
## 'data.frame':
## $ crim : num 0.00632 0.02731 0.02729 0.03237 0.06905 ...
## $ zn
            : num 18 0 0 0 0 0 12.5 12.5 12.5 12.5 ...
   $ indus : num 2.31 7.07 7.07 2.18 2.18 2.18 7.87 7.87 7.87 ...
## $ chas : int 0000000000...
           : num 0.538 0.469 0.469 0.458 0.458 0.458 0.524 0.524 0.524 0.524 ...
## $ nox
## $ rm
            : num 6.58 6.42 7.18 7 7.15 ...
          : num 65.2 78.9 61.1 45.8 54.2 58.7 66.6 96.1 100 85.9 ...
## $ age
## $ dis
          : num 4.09 4.97 4.97 6.06 6.06 ...
## $ rad
           : int 1223335555...
           : num 296 242 242 222 222 222 311 311 311 311 ...
## $ tax
## $ ptratio: num 15.3 17.8 17.8 18.7 18.7 15.2 15.2 15.2 15.2 ...
## $ black : num 397 397 393 395 397 ...
## $ lstat : num 4.98 9.14 4.03 2.94 5.33 ...
## $ medv : num 24 21.6 34.7 33.4 36.2 28.7 22.9 27.1 16.5 18.9 ...
lm.fit=lm(medv~lstat, data=Boston)
attach(Boston)
lm.fit=lm(medv~lstat)
lm.fit2=lm(medv~lstat+I(lstat^2))
summary(lm.fit2)
##
## Call:
## lm(formula = medv ~ lstat + I(lstat^2))
## Residuals:
```

```
1Q Median
                                 3Q
## -15.2834 -3.8313 -0.5295 2.3095 25.4148
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 42.862007 0.872084 49.15
                                          <2e-16 ***
## lstat
            -2.332821
                        0.123803 -18.84 <2e-16 ***
## I(lstat^2) 0.043547 0.003745 11.63 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 5.524 on 503 degrees of freedom
## Multiple R-squared: 0.6407, Adjusted R-squared: 0.6393
## F-statistic: 448.5 on 2 and 503 DF, p-value: < 2.2e-16
lm.fit=lm(medv~lstat)
anova(lm.fit,lm.fit2)
## Analysis of Variance Table
## Model 1: medv ~ lstat
## Model 2: medv ~ lstat + I(lstat^2)
## Res.Df RSS Df Sum of Sq
                              F
                                    Pr(>F)
## 1
       504 19472
## 2
       503 15347 1 4125.1 135.2 < 2.2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
par(mfrow=c(2,2))
plot(lm.fit2)
```



```
lm.fit5=lm(medv~poly(1stat,5))
summary(lm.fit5)
```

```
##
## Call:
  lm(formula = medv ~ poly(lstat, 5))
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
## -13.5433 -3.1039
                      -0.7052
                                 2.0844
                                         27.1153
##
  Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
##
                                  0.2318
                                         97.197
## (Intercept)
                     22.5328
                                                  < 2e-16
## poly(lstat, 5)1 -152.4595
                                  5.2148 -29.236
                                                  < 2e-16
## poly(lstat, 5)2
                     64.2272
                                  5.2148
                                          12.316
                                                  < 2e-16
## poly(lstat, 5)3
                    -27.0511
                                          -5.187 3.10e-07 ***
                                  5.2148
## poly(lstat, 5)4
                     25.4517
                                 5.2148
                                           4.881 1.42e-06 ***
                                          -3.692 0.000247 ***
## poly(lstat, 5)5
                    -19.2524
                                  5.2148
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 5.215 on 500 degrees of freedom
## Multiple R-squared: 0.6817, Adjusted R-squared: 0.6785
## F-statistic: 214.2 on 5 and 500 DF, p-value: < 2.2e-16
```

```
##
## Call:
## lm(formula = medv ~ log(rm), data = Boston)
##
## Residuals:
      Min 1Q Median
                             ЗQ
                                    Max
## -19.487 -2.875 -0.104 2.837 39.816
##
## Coefficients:
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -76.488 5.028 -15.21 <2e-16 ***
             54.055 2.739 19.73 <2e-16 ***
## log(rm)
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 6.915 on 504 degrees of freedom
## Multiple R-squared: 0.4358, Adjusted R-squared: 0.4347
## F-statistic: 389.3 on 1 and 504 DF, p-value: < 2.2e-16
coefficients(lm.fit2)
## (Intercept)
                   lstat I(lstat^2)
## 42.86200733 -2.33282110 0.04354689
coefficients(lm.fit5)
##
      (Intercept) poly(lstat, 5)1 poly(lstat, 5)2 poly(lstat, 5)3
                                      64.22724 -27.05110
##
         22.53281
                    -152.45955
## poly(lstat, 5)4 poly(lstat, 5)5
        25.45173
##
                  -19.25242
```

summary(lm(medv~log(rm),data=Boston))