

The Central Limit Theorem: Review

Questions 1 – 3 refer to the following:

Richard's Furniture Company delivers furniture from 10 A.M. to 2 P.M. continuously and uniformly. We are interested in how long (in hours) past the 10 A.M. start time that individuals wait for their delivery.

EXERCISE 1

$X \sim$

- A. $U(0, 4)$
- B. $U(10, 2)$
- C. $\text{Exp}(2)$
- D. $N(2, 1)$

EXERCISE 2

The average wait time is:

- A. 1 hour
- B. 2 hours
- C. 2.5 hours
- D. 4 hours

EXERCISE 3

Suppose that it is now past noon on a delivery day. The probability that a person must wait at least $1\frac{1}{2}$ more hours is:

- A. $\frac{1}{4}$
- B. $\frac{1}{2}$
- C. $\frac{3}{4}$
- D. $\frac{3}{8}$

EXERCISE 4

Given: $X \sim \text{Exp}(1/3)$.

- A. Find $P(X > 1)$
- B. Calculate the minimum value for the upper quartile.
- C. Find $P(X = 1/3)$

EXERCISE 5

- 40% of full-time students took 4 years to graduate
- 30% of full-time students took 5 years to graduate
- 20% of full-time students took 6 years to graduate
- 10% of full-time students took 7 years to graduate

The expected time for full-time students to graduate is:

- A. 4 years
- B. 4.5 years
- C. 5 years
- D. 5.5 years

EXERCISE 6

Which of the following distributions is described by the following example?

Many people can run a short distance of under 2 miles, but as the distance increases, fewer people can run that far.

- A. Binomial
- B. Uniform
- C. Exponential
- D. Normal

EXERCISE 7

The length of time to brush one's teeth is generally thought to be exponentially distributed with a mean of $\frac{3}{4}$ minutes. Find the probability that a randomly selected person brushes his/her teeth less than $\frac{3}{4}$ minutes.

- A. 0.5
- B. $\frac{3}{4}$
- C. 0.43
- D. 0.63

EXERCISE 8

Which distribution accurately describes the following situation?

The chance that a teenage boy regularly gives his mother a kiss goodnight (and he should!!) is about 20%. Fourteen teenage boys are randomly surveyed.

X = the number of teenage boys that regularly give their mother a kiss goodnight

- A. $B(14, 0.20)$
- B. $P(2.8)$
- C. $N(2.8, 2.24)$
- D. $\text{Exp}(1/0.20)$