

Symbols You Must Know		
Population		Sample
<b>N</b>	<b>Size</b>	<b>n</b>
<b>μ</b>	<b>Mean</b>	<b><math>\bar{x}</math></b>
<b>σ<sup>2</sup></b>	<b>Variance</b>	<b>s<sup>2</sup></b>
<b>σ</b>	<b>Standard Deviation</b>	<b>s</b>
<b>p</b>	<b>Proportion</b>	<b>p'</b>
Single Data Set Formulae		
Population		Sample
$\mu = E(x) = \frac{1}{N} \sum_{i=1}^N (x_i)$	<b>Arithmetic Mean</b>	$\bar{x} = \frac{1}{n} \sum_{i=1}^n (x_i)$
$Q_3 = \frac{3(n+1)}{4}, Q_1 = \frac{(n+1)}{4}$	<b>Inter-Quartile Range</b> <b><math>IQR = Q_3 - Q_1</math></b>	$Q_3 = \frac{3(n+1)}{4}, Q_1 = \frac{(n+1)}{4}$
$\sigma^2 = \frac{1}{N} \sum_{i=1}^N (x_i - \mu)^2$	<b>Variance</b>	$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$
Grouped Data Set Formulae		
Population		Sample
$\mu = E(x) = \frac{1}{N} \sum_{i=1}^k (m_i * f_i)$	<b>Arithmetic Mean</b>	$\bar{x} = \frac{1}{n} \sum_{i=1}^k (m_i * f_i)$
$\sigma^2 = \frac{1}{N} \sum_{i=1}^k (m_i - \mu)^2 * f_i$	<b>Variance</b>	$s^2 = \frac{1}{n-1} \sum_{i=1}^k (m_i - \bar{x})^2 * f_i$
$CV = \frac{\sigma}{\mu} * 100$	<b>Coefficient of Variation</b>	$CV = \frac{s}{\bar{x}} * 100$
Basic Probability Rules		
$P(A \cap B) = P(A   B) * P(B)$		<b>Multiplication Rule</b>
$P(A \cup B) = P(A) + P(B) - P(A \cap B)$		<b>Addition Rule</b>
$P(A \cap B) = P(A) * P(B)$ or $P(A B) = P(A)$		<b>Independence Test</b>

Hypergeometric Distribution Formulae	
$nCx = \binom{n}{x} = \frac{n!}{x!(n-x)!}$	Combinatorial Equation
$P(x) = \frac{\binom{N_1}{x} \binom{N-N_1}{n-x}}{\binom{N}{n}}$	Probability Equation
$E(X) = \mu = np$	Mean
$\sigma^2 = \left(\frac{N-n}{N-1}\right) np(q)$	Variance
Binomial Distribution Formulae	
$P(x) = \frac{n!}{x!(n-x)!} p^x (q)^{n-x}$	Probability Density Function
$E(X) = \mu = np$	Arithmetic Mean
$\sigma^2 = np(q)$	Variance
Geometric Distribution Formulae	
$P(X = x) = (1-p)^{x-1}(p)$	Probability when x is the first success
$\mu = \frac{1}{p}$	Mean
$\sigma^2 = \frac{(1-p)}{p^2}$	Variance
Poisson Distribution Formulae	
$P(x) = \frac{e^{-\mu} \mu^x}{x!}$	Probability Equation
$E(X) = \mu$	Mean
$\sigma^2 = \mu$	Variance
Uniform Distribution Formulae	
$f(x) = \frac{1}{b-a} \text{ for } a \leq x \leq b$	PDF
$E(X) = \mu = \frac{a+b}{2}$	Mean
$\sigma^2 = \frac{(b-a)^2}{12}$	Variance
Exponential Distribution Formulae	
$P(X \leq x) = 1 - e^{-mx}$	Cumulative Probability
$E(X) = \mu = \frac{1}{m} \text{ or } m = \frac{1}{\mu}$	Mean and Decay Factor
$\sigma^2 = \frac{1}{m^2} = \mu^2$	Variance

The following page of formulae require the use of the “Z”, “t”, and “ $\chi^2$ ” tables.

$Z = \frac{x - \mu}{\sigma}$	<b>Z-transformation for Normal Distribution</b>	
$Z = \frac{x - np'}{\sqrt{np'(q')}}}$	<b>Normal Approximation to the Binomial</b>	
<b>Probability (ignore subscripts) Hypothesis Testing</b>	<b>Confidence Intervals</b> [bracketed symbols equal margin of error] (subscripts denote locations on respective distribution tables)	
$Z_c = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$	Interval for the population mean when sigma is known $\bar{x} \pm \left[ Z_{(\alpha/2)} \frac{\sigma}{\sqrt{n}} \right]$	
$t_c = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$	Interval for the population mean when sigma is unknown $\bar{x} \pm \left[ t_{(n-1),(\alpha/2)} \frac{s}{\sqrt{n}} \right]$	
$Z_c = \frac{p' - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$	Interval for the population proportion $p' \pm \left[ Z_{(\alpha/2)} \sqrt{\frac{p' q'}{n}} \right]$	
$t_c = \frac{\bar{d} - \delta_0}{\frac{s_d}{\sqrt{n}}}$	Interval for difference between two means with matched pairs $\bar{d} \pm \left[ t_{(n-1),(\alpha/2)} \frac{s_d}{\sqrt{n}} \right]$ where $S_d$ is the deviation of the differences	
$Z_c = \frac{(\bar{x}_1 - \bar{x}_2) - \delta_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$	Interval for difference between two means when sigmas are known $(\bar{x}_1 - \bar{x}_2) \pm \left[ Z_{(\alpha/2)} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \right]$	
$t_c = \frac{(\bar{x}_1 - \bar{x}_2) - \delta_0}{\sqrt{\left(\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2}\right)}}$	Interval for difference between two means with equal variances when sigmas are unknown $(\bar{x}_1 - \bar{x}_2) \pm \left[ t_{df,(\alpha/2)} \sqrt{\left(\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2}\right)} \right]$ where $df = \frac{\left(\frac{(s_1)^2}{n_1} + \frac{(s_2)^2}{n_2}\right)^2}{\left(\frac{1}{n_1-1}\right)\left(\frac{(s_1)^2}{n_1}\right)^2 + \left(\frac{1}{n_2-1}\right)\left(\frac{(s_2)^2}{n_2}\right)^2}$	
$Z_c = \frac{(p'_1 - p'_2) - \delta_0}{\sqrt{\frac{p'_1(q'_1)}{n_1} + \frac{p'_2(q'_2)}{n_2}}}$	Interval for the difference between two population proportions $(p'_1 - p'_2) \pm \left[ Z_{(\alpha/2)} \sqrt{\frac{p'_1(q'_1)}{n_1} + \frac{p'_2(q'_2)}{n_2}} \right]$	
$\chi^2_c = \frac{(n - 1)s^2}{\sigma_0^2}$	Tests for GOF, Independence, and Homogeneity $\chi^2_c = \sum \frac{(O - E)^2}{E}$ where $O$ = observed values and $E$ = expected values	
<b>The Next 3 Formulae are for Determining Sample Size with Confidence Intervals</b> (note: E represents the margin of error)		
$n = \frac{Z^2_{\left(\frac{\alpha}{2}\right)} \sigma^2}{E^2}$  <i>Use when sigma is known</i>	$n = \frac{Z^2_{\left(\frac{\alpha}{2}\right)} (0.25)}{E^2}$  <i>Use when p' is unknown</i>	$n = \frac{Z^2_{\left(\frac{\alpha}{2}\right)} [p'(q')]}{E^2}$  <i>Use when p' is known</i>

Simple Linear Regression Formulae for $y = a + b(x)$				
$r = \frac{\sum[(x - \bar{x})(y - \bar{y})]}{\sqrt{\sum(x - \bar{x})^2 * \sum(y - \bar{y})^2}} = \frac{S_{xy}}{S_x S_y} = \sqrt{\frac{SSR}{SST}}$	Correlation Coefficient			
$b = \frac{\sum[(x - \bar{x})(y - \bar{y})]}{\sum(x - \bar{x})^2} = \frac{S_{xy}}{SS_x} = r_{y,x} \left( \frac{s_y}{s_x} \right)$	Coefficient $b$ (slope)			
$a = \bar{y} - b(\bar{x})$	y-intercept			
$s_e^2 = \frac{\sum(y_i - \hat{y}_i)^2}{n - k} = \frac{\sum_{i=1}^n e_i^2}{n - k}$	Estimate of the Error Variance			
$S_b = \frac{s_e^2}{\sqrt{\sum(x_i - \bar{x})^2}} = \frac{s_e^2}{(n - 1)S_x^2}$	Standard Error for Coefficient $b$			
$t_c = \frac{b - \beta_0}{s_b}$	Hypothesis Test for Coefficient $\beta$			
$b \pm [t_{n-2, \alpha/2} S_b]$	Interval for Coefficient $\beta$			
$\hat{y} \pm \left[ t_{\alpha/2} * s_e \left( \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{s_x^2}} \right) \right]$	Interval for Expected Value of y			
$\hat{y} \pm \left[ t_{\alpha/2} * s_e \left( \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{s_x^2}} \right) \right]$	Prediction Interval for an Individual y			
ANOVA Formulae				
$SSR = \sum_{i=1}^n (\hat{y}_i - \bar{y})^2$	Sum of Squares Regression			
$SSE = \sum_{i=1}^n (y_i - \hat{y}_i)^2$	Sum of Squares Error			
$SST = \sum_{i=1}^n (y_i - \bar{y})^2$	Sum of Squares Total			
The Following is the breakdown of a one-way ANOVA table for linear regression				
Source of Variation	Sum of Squares	Degrees of Freedom	Mean Squares	F – Ratio
Regression	SSR	1 or $k - 1$	$MSR = \frac{SSR}{df_R}$	$F = \frac{MSR}{MSE}$
Error	SSE	$n - k$	$MSE = \frac{SSE}{df_E}$	
Total	SST	$n - 1$		