

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$$

$x \in A \cup (B \cap C)$

$x \in A \text{ or } x \in (B \cap C)$

$\rightarrow x \in A \text{ or } [x \in B \text{ and } x \in C]$

$\Rightarrow (x \in A \text{ or } x \in B) \text{ and } (x \in A \text{ or } x \in C)$

Cardinality

$$|A \cup B| = |A| + |B| - |A \cap B|$$

$$|A - B| = |A| - |A \cap B|$$

$$|B - A| = |B| - |A \cap B|$$

$$\begin{aligned} |A \cup B \cup C| &= |A| + |B| + |C| - |A \cap B| \\ &\quad - |B \cap C| - |A \cap C| + |A \cap B \cap C| \end{aligned}$$

## LISP :-

1. Various LISP environments:

Emacs,

lispworks,

Cygwin

Eclipse w/ plugin

Power of LISP used

1. Numeric literals

2. characters - strings

3. Functions

fns  
macros

special operators

Direct numeric literals don't need parenthesis

> 1.1

> 2

> 3/2

> "abcdef"

> ( print "abc" )

## Numeric literals

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>; reduced rational #

20/2

10

>; hex

#xa  
10

for es hexadecimal

>; binary

#b1111  
15

> 123 e-3

.123

> (= 1 1)

T

> (<= 2 3)

T

its NIL also

> PI

3.141592653...

>(exp 1) => 2.7182817

## Functions:

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1. Fundamental building block for LISP programs.

→ for format

> (defun addtwo(x) see 2 page  
afterward  
(+ x 2))

> (addtwo 5)

=> 7

write a function two multiply  
two numbers

<(defun mult (x y)  
(\* x y))

<(mult 10 3)

30

① sum of 2 no./sum of 3 no.

② square of a no.

## HISTORY of LISP

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Created by John McCarthy in late 1950's

- Main idea was to study computability from a functional programming standpoint
- CLISP now supports object oriented, imperative and functional programming

<S-expression> = <atom> | <list>

<atom> = <no.> | <identifier>

<list> = (<S-expression>)

<identifier> = string of printable characters, not including parenthesis

## Fundamental data types

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1. Atom → An atom is a alphanumeric string, used either as a variable name or a data item.
  2. List → is a sequence of elements, where each element is either an atom or a list.
- A list is a left parenthesis, followed by zero or more S-expressions, followed by a right parenthesis.  
An S-expression is an atom or a list.

In 1965, McCarthy developed a fn. called "eval." used to evaluate other fn.

— literals are evaluated to themselves.  
e.g. if you type in 5, the interpreter will return 5.

Expressions that are calls to primitive fn. are evaluated as follows:

1. Each parameter is evaluated first.
2. The primitive fn. is applied to parameter values.
3. The result is displayed.

> eval 6/4  
3/2

> (eval (+ 2 3))

S

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> (eval (+ (+ 1 1) (+ 1 1)))

S

Q:

> (+ 3 2)) → error

> (if (< 2 3) (print "Yes") (print "No"))

"Yes"

> '(× 1 "foo")  
- (× 1 "foo")

> (+) → error

> (+ 1)  
1

> (dotimes (x 2) (print x))  
0  
1

< sort '< 1 2 3 > #'>  
→ for ascending  
descending  
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Define or defun\* is used to bind a name to a value

(defun (square num) (\* num num))

format:

(defun (function-name parameters)  
(expression(s)))

sqrt is the inbuilt function.

Binding names to values

(define pi 3.14)

(define two-pi (\* 2 pi))

→ Once these two expressions are typed into Lisp interpreter, typing pi will return 3.14.

→ Names consists of letters, digits and special characters (except parenthesis) but can't begin with digits.

## If statement :

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(if conditions then-form [else-form])  
— The then-form and optional else-form  
are restricted to a single Lisp form.

"cond" is a macro to handle  
multiple if statements

(cond

(test-1 form\*)

:

(test-n form\*)

① (if (= 1 1)  
      "a"  
      "b")

② (if (= 1 2)  
      (+ 0.5 0.5)  
      (- 0.5 0.5))

→ 0

③ (if (= 1 2)  
      (if (= 1 2)  
          (+ 0.5 0.5)  
          (- 0.5 0.5)))

NIL

> cond (t (print "a"))  
      (t (print "b"))  
      (t (print "c")))  
"a"

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> cond (nil (print "a"))  
      (nil (print "b"))  
      (t (print "c"))  
      (t (print "d")))

> (unless nil  
      (print "a")  
      (print "b"))

setf :- Binds a value to a  
location / variable.

(setf z '(1 2 3)) => (1 2 3)

function to reverse list:

(defun my-reverse (lis))  
  (cdr

(Pb)

(defun my-reverse (lis))

(let ((new-list nil)) ORACLE ACADEMY

(do-list (item lis))

(setf new-list (cons item newlist))  
newlist))

- NIL is the name of empty list
- As a test, NIL means false
- NIL is both an atom and a list

### Basic fn.

① CAR returns the head of a list

② CDR returns the tail of a list

③ CONS inserts a new head into a list

④ EQ compares two atoms for equality

⑤ ATOM tests if its argument is an atom

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(NULL S) tests if S is the empty list.

(LISTP S) tests if S is a list.

LIST makes a list of its evaluated arguments

- (LIST 'A' 'B' 'C' 'D') returns (A B C D)  
- (LIST (CDR '(A B)) 'C) returns ((B) C)

APPEND concatenates two lists

(APPEND '(A B) '(C X) Y))

=> (A B C X) Y)

(CAR '(a b c)) => a

Note: Not using ' will result in an error.

What is the o/p in case of CDR

(A B C)

((C X) Y) Z)

(X)

((C) C)

( )

CONS takes two arguments

- The first argument can be any sexp
- The second argument should be a list
- The result is a new list whose CAR is the first argument and whose CDR is the second.

→ obtaining the second element of a list  
 <first (rest '(a b c d))>

'first' returns the first element of a list  
 <first '(a b c d)>

'rest' returns the a list with the first element removed.

Quoted stops expression evaluation.

> (+ 1 2 3)

6

> '(+ 1 2 3)

To assign a value to a symbol (setq,  
 set, setf )

>(setq x 3.0)

3.0

>x

3.0

- setq is a special form of function (with two arguments).
- The first argument is a symbol which will not be evaluated.
- The second argument

Area of a circle:

```
(defconstant PI 3.141592)
(defun area-circle (rad)
  (terpri)
  (format t "Radius:~5f" rad)
  (format t "My Area:~10f" (* PI
                                rad
                                rad)))
(area-circle 10)
```

short hand for standard output

`~t` directive is for tabulating.  
`~10t` tells FORMAT to emit enough  
 spaces to move to the tenth column  
 before processing the next ma.

what it do?  
 ① (butlast '(a b c d e f g) 3)

② (cons 'a '(a b))  
 concatenating

(cons '(a b) '(a b))

③ Getting the length of a list  
 (length '(a b c))

④ Reversing a list  
 (reverse '(a b c))

⑤ Getting the last element of a list  
 (last '(a b c d))

⑥ creating a new list  
 (list '(a b c) '(d e f))

Expression like

'hello  
(setf n 5)

are complete stand-alone programs, not simply statements.

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> (union L1 L2) : returns the union of two lists.

) (intersection L1 L2) : returns the intersection of two lists.

) (set-difference L1 L2) : returns the difference of two lists

Some Datastructures: — ATOMS / LISTS

other data structures:

Association list, arrays, structures, dotted pairs, files, streams

1. Association lists are just list of sub-lists

(setf sarah '(("height" . 54) ("weight" . 24)))  
↑  
key value.

2. Retrieving elements from an association list

(assoc <key> <association-list>)  
(assoc 'height sarah)  
→ ans. height 54

3. Creating a lisp array:

(setf a (make-array '2 3 4))  
: initial-contents  
'((a b c d) 2 3 4)  
("this" 5 6 7)  
(#\c 8 9 10)))

4. Retrieving an array element.

(setf value (aref a 2 3))  
as 10

• Changing a value

```
(setf (aref a 2) 12)
```

- creating & manipulating a list structure

```
(
```

Program of factorial.

```
(define & factorial (n))
```

```
(if (eq n 0))
```

```
(* n (factorial (- n 1))))
```

What will be the O/P

```
(car '(this is a list of symbols))  
=> this
```

```
(cdr '(singleton))
```

```
=> () the empty list
```

```
(list 'a 'b 'c 'd 'e)
```

```
=> (a b c d e)
```

equivalent to

```
(cons 'a (cons 'b (cons 'c (cons 'd  
(cons 'e '()))))))))
```

```
(cons 'a '())
```

```
=> (a)
```