

Week 5

Classification





Overview

1. Steps for KNN algorithms
2. Implementation of Confusion Matrix
3. Implementation of Naïve Bayes Classifier
4. ROC Curve



Classification

Classification problem => inference stage => decision stage

$$p(\mathcal{C}_k|\mathbf{x}) = \frac{p(\mathbf{x}|\mathcal{C}_k)p(\mathcal{C}_k)}{p(\mathbf{x})}.$$

Discriminant functions:

these approaches map each input directly on to a class label and probabilities play no role.

Discriminative models:

These models solve the posterior class probability, $p(\mathcal{C}_k|\mathbf{x})$ directly, and then assign each new \mathbf{x} to a class using a suitable loss function or other decision function. (e.g. Logistic Regression)

Generative models: Like discriminative models, these also solve for $p(\mathcal{C}_k|\mathbf{x})$, but first have to determine $p(\mathbf{x}|\mathcal{C}_k)$ and $p(\mathcal{C}_k)$ for each class individually. Afterwards, a decision function determines class membership. (e.g. Naïve Bayes)



Naïve Bayes Classifier

$$p(C_k|\mathbf{x}) = \frac{p(\mathbf{x}|C_k)p(C_k)}{p(\mathbf{x})}.$$

Assumption: features are conditionally independent given the class (hence naïve)

$P(\mathbf{x})$ is normalisation constant

Pick C_k has the largest probability as outcome => Maximum A Posteriori