

# 1 CESK

$\varsigma \mapsto_{CESK} \varsigma'$	
$\langle x, \rho, \sigma, \kappa \rangle$	$\langle v, \rho', \sigma, \kappa \rangle$ where $\sigma(\rho(x)) = (v, \rho')$
$\langle (e_0 e_1), \rho, \sigma, \kappa \rangle$	$\langle e_0, \rho, \sigma, \mathbf{ar}(e_1, \rho, \kappa) \rangle$
$\langle v, \rho, \sigma, \mathbf{ar}(e, \rho', \kappa) \rangle$	$\langle e, \rho', \sigma, \mathbf{fn}(v, \rho, \kappa) \rangle$
$\langle v, \rho, \sigma, \mathbf{fn}(\lambda x.e), \rho', \kappa \rangle$	$\langle e, \rho'[x \mapsto a], \sigma[a \mapsto (v, \rho)], \kappa \rangle$ where $a \notin \text{dom}(\sigma)$
$\varsigma \in \Sigma$	$= \text{Exp} \times \text{Env} \times \text{Store} \times \text{Kont}$
$\rho \in \text{Env}$	$= \text{Var} \rightarrow_{\text{fin}} \text{Addr}$
$\sigma \in \text{Store}$	$= \text{Addr} \rightarrow_{\text{fin}} \text{Storable}$
$s \in \text{Storable}$	$= \text{Val} \times \text{Env}$
$a, b, c \in \text{Addr}$	an infinite set.

# 2 Lazy CESK

$\varsigma \mapsto_{\text{LazyCESK}} \varsigma'$	
$\langle x, \rho, \sigma, \kappa \rangle$	$\langle v, \rho', \sigma, \kappa \rangle$ where $\sigma(\rho(x)) = (v, \rho')$
$\langle x, \rho, \sigma, \kappa \rangle$	$\langle v, \rho', \sigma, \mathbf{st}(a, \kappa) \rangle$ where $\sigma(a = \rho(x)) = \boldsymbol{\theta}(v, \rho')$
$\langle (e_0 e_1), \rho, \sigma, \kappa \rangle$	$\langle e_0, \rho, \sigma, \mathbf{ar}(e_1, \rho, \kappa) \rangle$
$\langle x, \rho, \sigma, \mathbf{st}(a, \kappa) \rangle$	$\langle x, \rho, \sigma[a \mapsto \boldsymbol{\epsilon}(x, \rho)], \kappa \rangle$
$\langle (\lambda x.e), \rho, \sigma, \mathbf{ar}(v, \rho', \kappa) \rangle$	$\langle e, \rho[x \mapsto a], \sigma[a \mapsto \boldsymbol{\theta}(v, \rho')], \kappa \rangle$ where $a \notin \text{dom}(\sigma)$
$\varsigma \in \Sigma$	$= \text{Exp} \times \text{Env} \times \text{Store} \times \text{Kont}$
$\rho \in \text{Env}$	$= \text{Var} \rightarrow_{\text{fin}} \text{Addr}$
$\sigma \in \text{Store}$	$= \text{Addr} \rightarrow_{\text{fin}} \text{Storable}$
$s \in \text{Storable}$	$::= \boldsymbol{\theta}(v, \rho)$   $\boldsymbol{\epsilon}(v, \rho)$
$\kappa \in \text{Kont}$	$::= \mathbf{mt}$   $\mathbf{ar}(e, \rho, \kappa)$   $\mathbf{st}(a, \kappa)$
$a, b, c \in \text{Addr}$	an infinite set.

When evaluated, the thunk  $\boldsymbol{\theta}(v, \rho)$  is replaced in the store with the evaluated version  $\boldsymbol{\epsilon}(v', \rho')$ .