

# Modelo

## 1. Definir ecuaciones para el modelo y cargar los datos de la serie de tiempo

```
syms Ms(t) Me(t) Mi(t) Hs(t) He(t) Hi(t) Hr(t) Hit(t)

syms lambda beta_m mu_m theta_m mu_h beta_h theta_h...
gamma_h

H=Hs+He+Hr;
M=Ms+Me+Mi;
ode1 = diff(Ms) == lambda - beta_m*Hi*Ms/H - (mu_m)*Ms;
ode2 = diff(Me) == beta_m*Hi*Ms/H - (theta_m+mu_m)*Me;
ode3 = diff(Mi) == theta_m*Me - mu_m*Mi;
ode4 = diff(Hs) == -beta_h*Mi*Hs/M + (He+Hi+Hr)*mu_h;
ode5 = diff(He) == beta_h*Mi*Hs/M - (theta_h+mu_h)*He;
ode6 = diff(Hi) == theta_h*He - (gamma_h+mu_h)*Hi;
ode7 = diff(Hr) == gamma_h*Hi - mu_h*Hr;
ode8 = diff(Hit) == theta_h*He;
odes=[ode1; ode2 ;ode3; ode4; ode5 ;ode6; ode7; ode8];
vars=[Hit Hi Me Hr Hs He Ms Mi];
opts = odeset('NonNegative',1:8);
```

## 2. Preparar los datos:

Escogimos la ventana de tiempo (entre la semana 153 y la semana 233).

```
load Range7.mat
[T,~]=gsua_dpmat(odes,vars,[0 150], '7m', 'output',1, 'opt',opts, 'Range',Range);
```

Introduce ranges in the following order:

$\text{ans}(t) = (\text{Hit}(t) \quad \text{Hi}(t) \quad \text{Me}(t) \quad \text{Hr}(t) \quad \text{Hs}(t) \quad \text{He}(t) \quad \text{Ms}(t) \quad \text{Mi}(t) \quad \beta_h \quad \beta_m \quad \gamma_h \quad \lambda \quad \mu_h \quad \mu_m \quad \theta_h \quad \theta_m)$

```
load('DataBello_full.mat');
ydata=DataBello.cases(153:233)';
xdata=linspace(0,length(ydata)-1,length(ydata));
ydata2=ydata;
for i=1:length(ydata)
ydata2(i)=sum(ydata(1:i));
end
```

## 3. Análisis de sensibilidad

### 3.1. Preparamos los datos: usamos la tabla con los rangos y los valores nominales de los parámetros y

preparamos la matriz de diseño experimental.

```
[T,~]=gsua_dpmat(odes,vars,[0 80], '7m', 'output',1,'opt',opts,'Range',Range);
```

Introduce ranges in the following order:

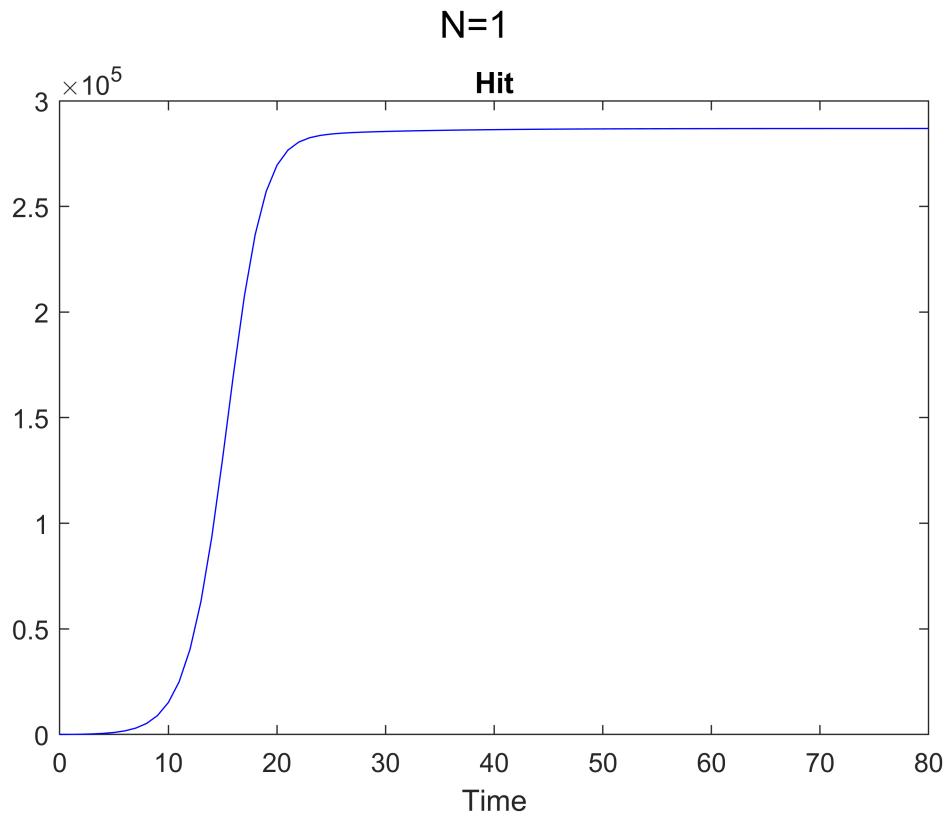
```
ans(t) = (Hit(t) Hi(t) Me(t) Hr(t) Hs(t) He(t) Ms(t) Mi(t) βh βm γh λ μh μm θh θm)
```

```
T.Properties.CustomProperties.output = 1;  
M = gsua_dmatrix(T,100);
```

### 3.2. Análisis de sensibilidad

Usamos el toolbox para realizar el análisis de sensibilidad variando los parámetros según los rangos que nos dieron.

```
ynom = gsua_eval(T.Nominal,T);
```



```
plot(cumsum(ydata),'b')  
title('Original Acumulated Human Infections (Hit)')  
xlabel('Weeks')  
ylabel('Cases')  
%savefig('iteration1/figures/NominalValues.fig')
```

```
Tsa = gsua_sa(M,T,'parallel', false, 'SensMethod', 'Xiao', 'ynom', ynom);
```

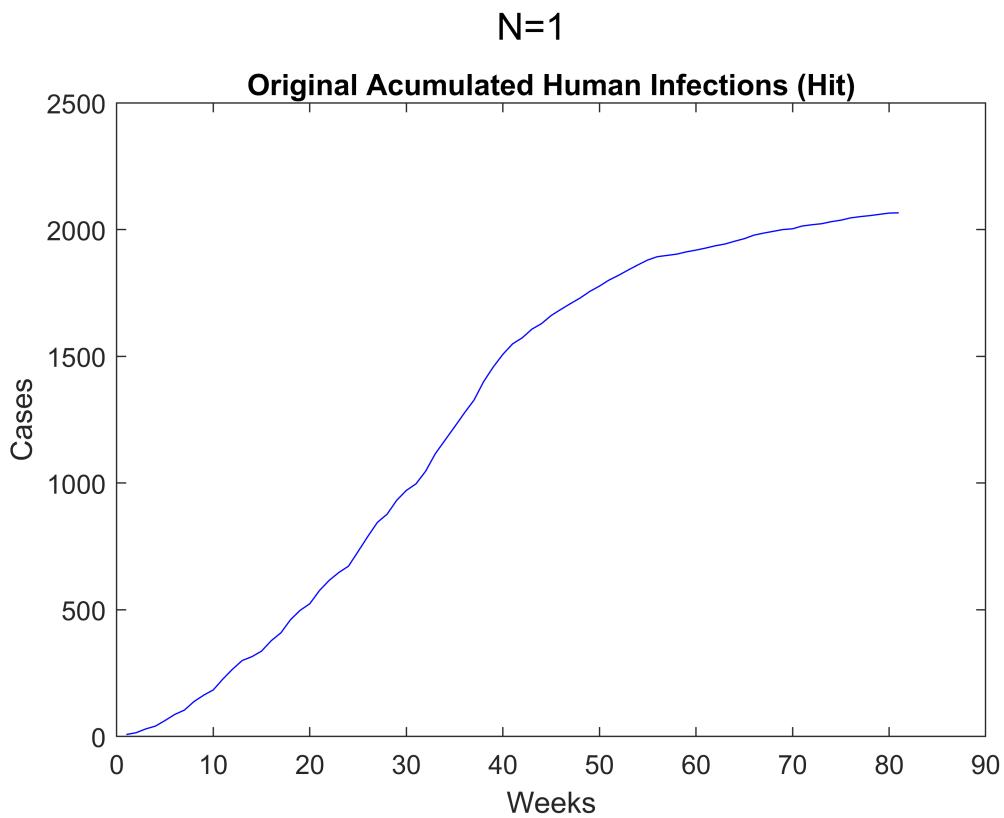
```
Progress: 7%
Estimated processing time (h:m:s): 0:0:8
Remaining time (h:m:s): 0:0:8
Elapsed time (h:m:s): 0:0:0
Estimated stop time (h:m:s): 22:4:20
Number of simulations: 750
Progress: 14%
Estimated processing time (h:m:s): 0:0:8
Remaining time (h:m:s): 0:0:7
Elapsed time (h:m:s): 0:0:1
Estimated stop time (h:m:s): 22:4:20
Number of simulations: 750
Progress: 20%
Estimated processing time (h:m:s): 0:0:8
Remaining time (h:m:s): 0:0:6
Elapsed time (h:m:s): 0:0:1
Estimated stop time (h:m:s): 22:4:19
Number of simulations: 750
Progress: 27%
Estimated processing time (h:m:s): 0:0:8
Remaining time (h:m:s): 0:0:6
Elapsed time (h:m:s): 0:0:2
Estimated stop time (h:m:s): 22:4:19
Number of simulations: 750
Progress: 34%
Estimated processing time (h:m:s): 0:0:8
Remaining time (h:m:s): 0:0:5
Elapsed time (h:m:s): 0:0:2
Estimated stop time (h:m:s): 22:4:19
Number of simulations: 750
Progress: 40%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:4
Elapsed time (h:m:s): 0:0:3
Estimated stop time (h:m:s): 22:4:19
Number of simulations: 750
Progress: 47%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:4
Elapsed time (h:m:s): 0:0:3
Estimated stop time (h:m:s): 22:4:19
Number of simulations: 750
Progress: 54%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:3
Elapsed time (h:m:s): 0:0:4
Estimated stop time (h:m:s): 22:4:19
Number of simulations: 750
Progress: 60%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:3
Elapsed time (h:m:s): 0:0:4
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750
Progress: 67%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:2
Elapsed time (h:m:s): 0:0:4
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750
Progress: 74%
```

```

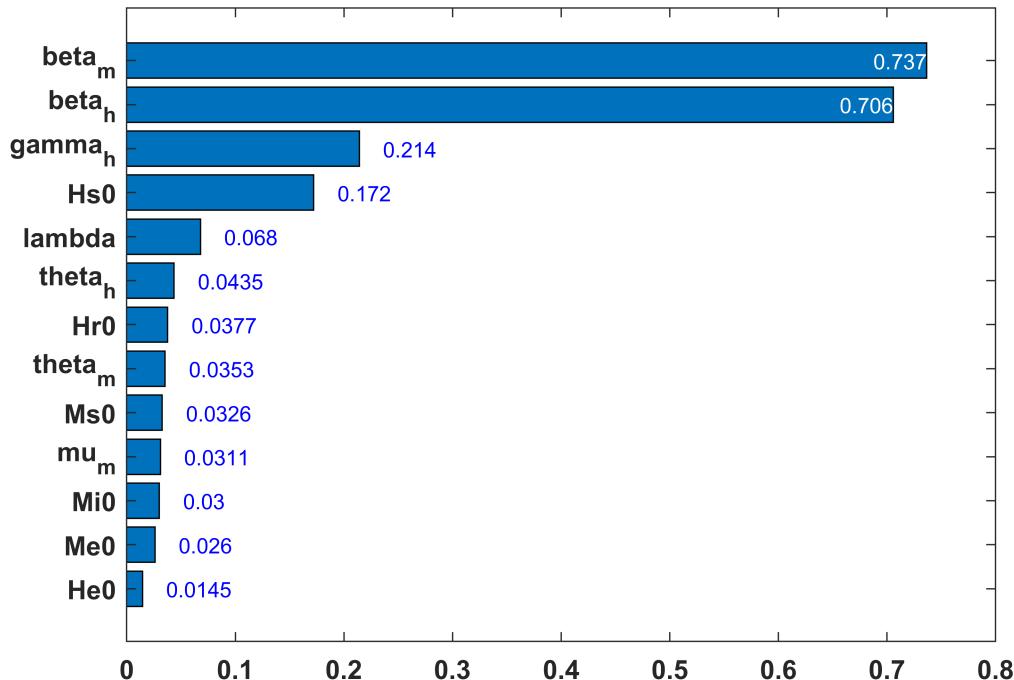
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:1
Elapsed time (h:m:s): 0:0:5
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750
Progress: 81%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:1
Elapsed time (h:m:s): 0:0:5
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750
Progress: 87%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:0
Elapsed time (h:m:s): 0:0:6
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750
Progress: 94%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:0
Elapsed time (h:m:s): 0:0:6
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750
Progress: 100%
Estimated processing time (h:m:s): 0:0:7
Remaining time (h:m:s): 0:0:0
Elapsed time (h:m:s): 0:0:7
Estimated stop time (h:m:s): 22:4:18
Number of simulations: 750

```

```
gsua_plot('Bar',Tsa,Tsa.STi)
```



## N=1 Bar chart of sensitivity indices for MSE function using Xiao method



```
%>>> %%savefig('iteration1/figures/SensibilityAnalisis.fig')
```

### 3.3. Confiabilidad

Mientras mayor sea c, mayor confianza tenemos en los resultados del análisis.

```
c = sum(Tsa.Si)/sum(abs(Tsa.Si))
```

```
c = 0.9793
```

### 3.4 Fijar parámetros

Según el análisis previo, el último parámetro es insensible, entonces lo podemos fijar ya que no es identificable.

Este parámetros son  $H_{e0}$

Para esto usamos los valores nominales de la tabla T.

```
vars=[Hit Hi He Me Hr Hs Ms Mi];  
  
He0 = T.Nominal('He0');  
  
RangeTemp = Range;
```

```

Range(3,:) = He0;
Range(4:6,:) = [RangeTemp(3,:); RangeTemp(4,:); RangeTemp(5,:)];
[T,~]=gsua_dpmat(odes,vars,[0 80], '7m','output',1,'opt',opts,'Range',Range);

```

Introduce ranges in the following order:

$\text{ans}(t) = (\text{Hit}(t) \quad \text{Hi}(t) \quad \text{He}(t) \quad \text{Me}(t) \quad \text{Hr}(t) \quad \text{Hs}(t) \quad \text{Ms}(t) \quad \text{Mi}(t) \quad \beta_h \quad \beta_m \quad \gamma_h \quad \lambda \quad \mu_h \quad \mu_m \quad \theta_h \quad \theta_m)$

```

T.Properties.CustomProperties.output = 1;
M = gsua_dmatrix(T,100);

```

#### 4. Estimación de parámetros.

```

opt = optimoptions('lsqcurvefit','UseParallel',true,'Display','iter');
[T7,res] = gsua_pe(T,xdata,ydata2,'N',100,'opt',opt); %mover N ( 100 buena, 50 aceptable, 10 :)
%save('iteration1/values/Results7.mat','T7','res','xdata','ydata2')

```

#### 5. Análisis de identificabilidad

Escogemos las curvas que estén más cercanas a la mejor.

```
th = sum(res<res(1)*1.01)
```

```
th = 3
```

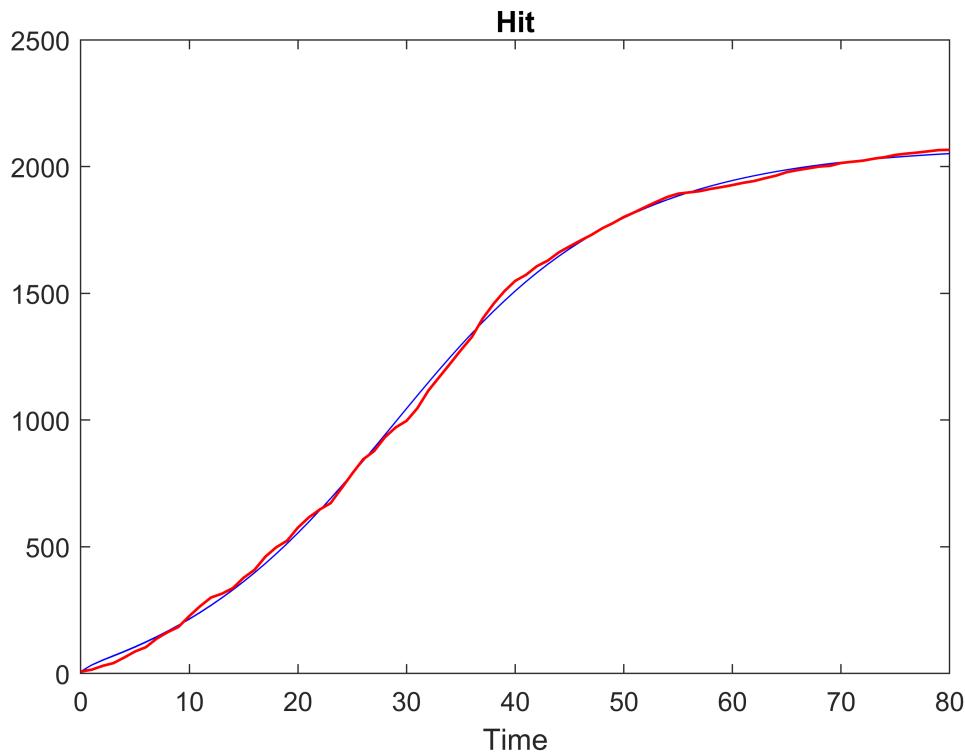
```
y7 = gsua_eval(T7.Estlsc(1:th),T7,xdata,ydata2);
```

```

Sim3 Done
Sim2 Done
Sim1 Done

```

N=3

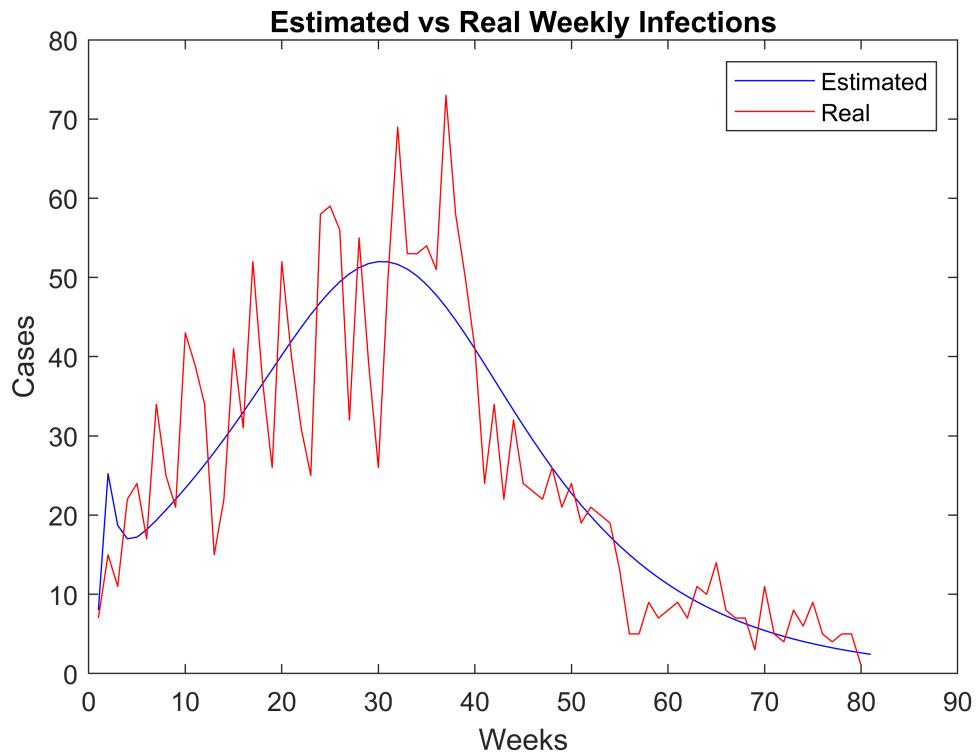


```
%savefig('iteration1/figures/curves.fig')
```

Comparamos la mejor curva con los valores reales para ver que tan bien ajusta.

```
bestest = y7(1,:);
trend = [bestest(1),bestest(2:end)-bestest(1:end-1)];
plot(trend,'b')
hold on
plot(diff(ydata2),'r')
title('Estimated vs Real Weekly Infections')
xlabel('Weeks')
ylabel('Cases')
legend({'Estimated','Real'})
```

N=3



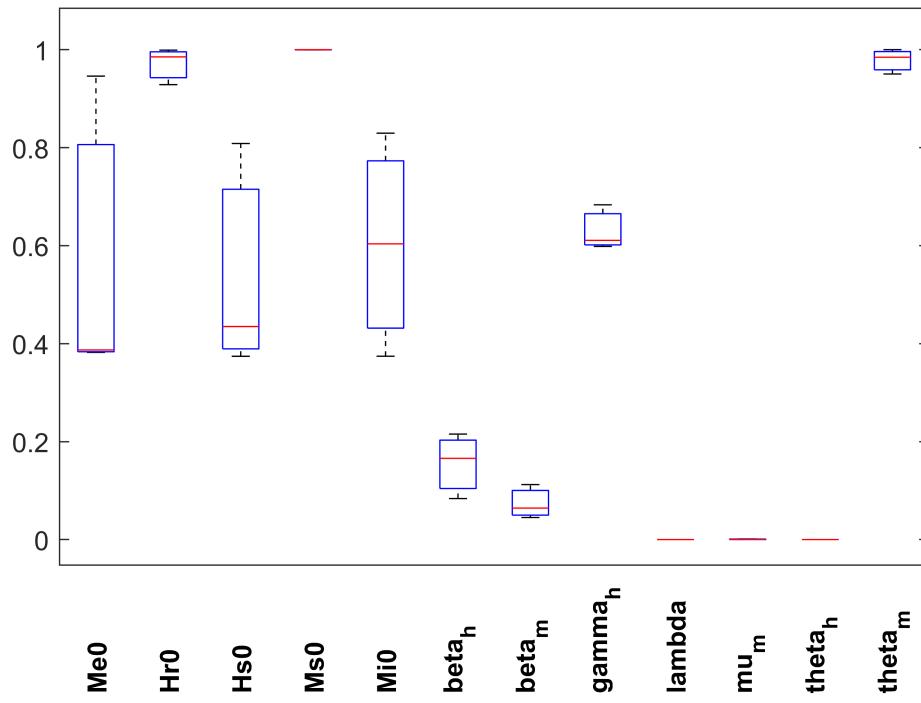
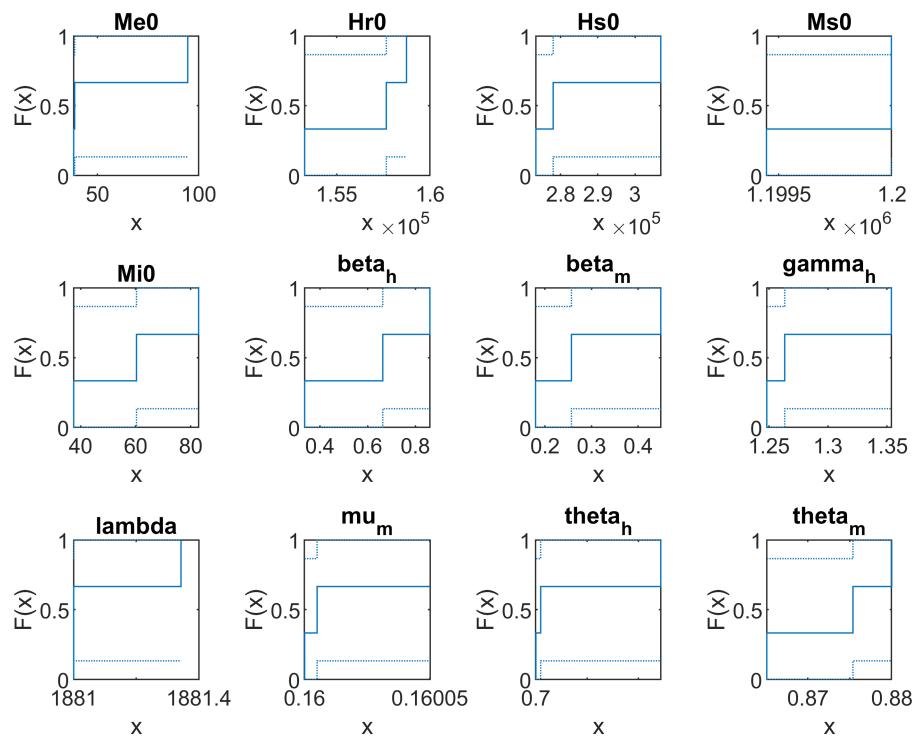
```
%savefig('iteration1/figures/EstimatedvsReal.fig')
```

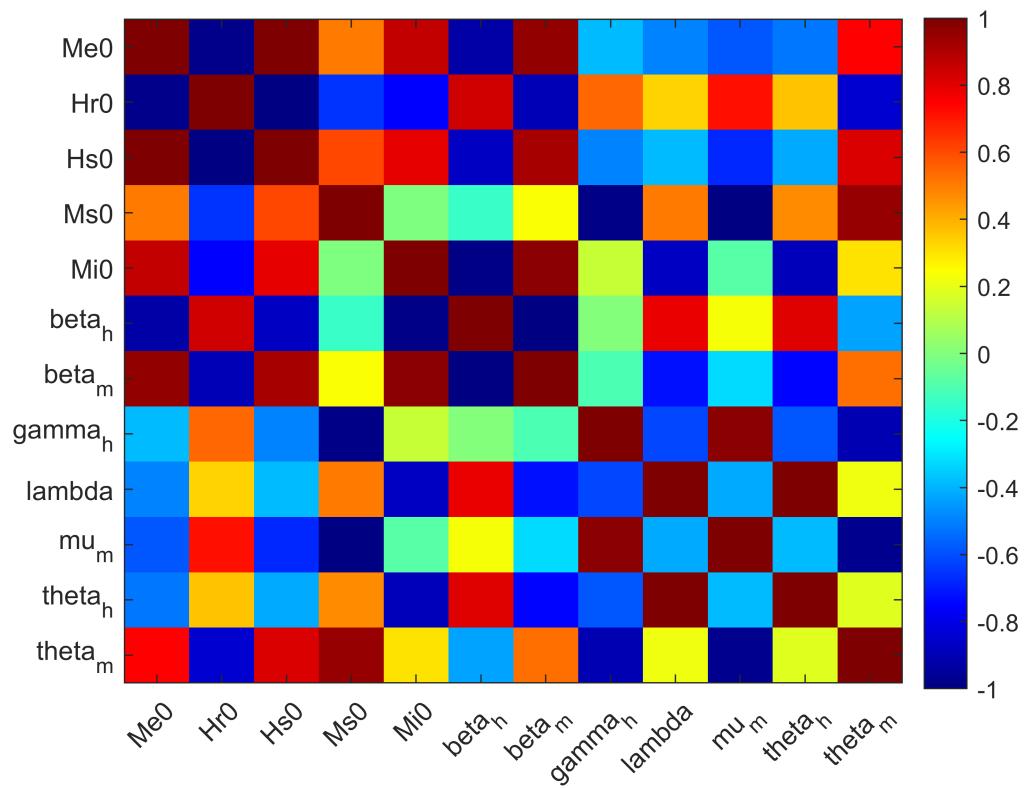
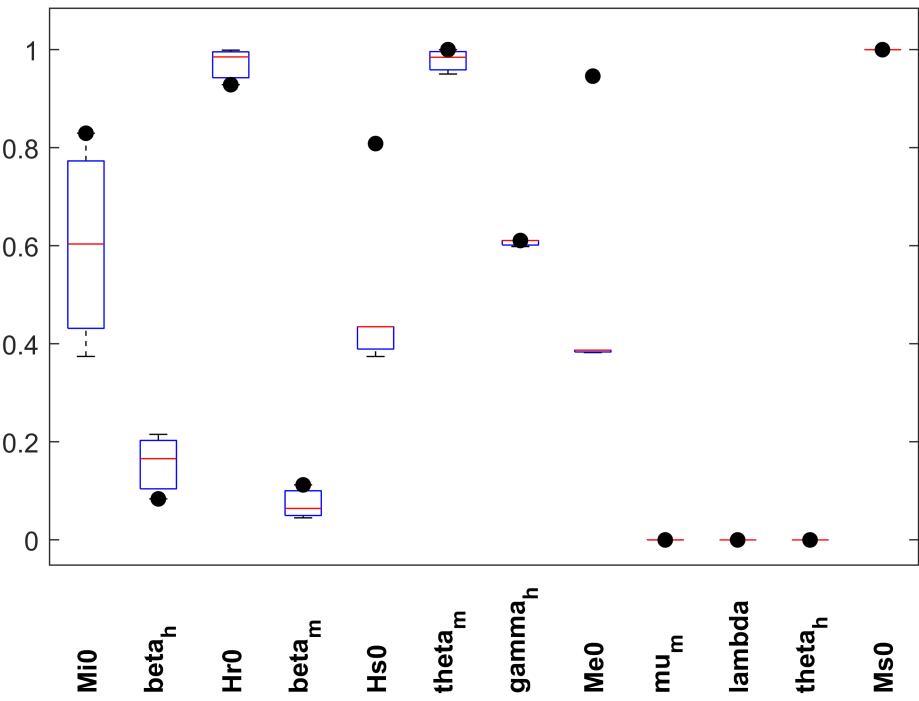
Ahora visualizamos el análisis de identificabilidad para asegurarnos de la fiabilidad del modelo ajustado.

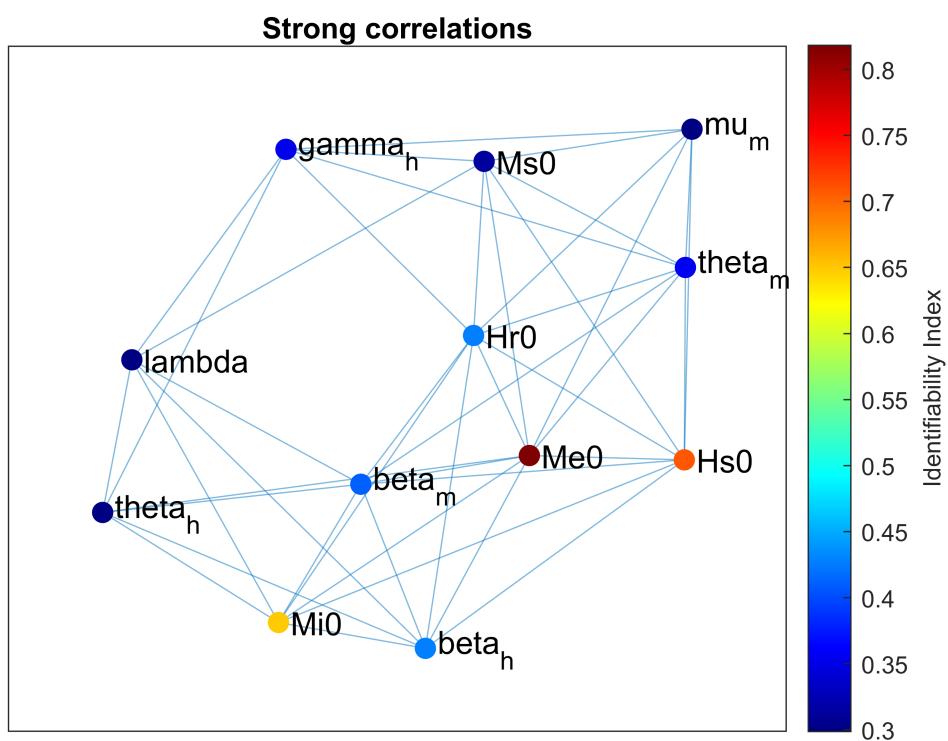
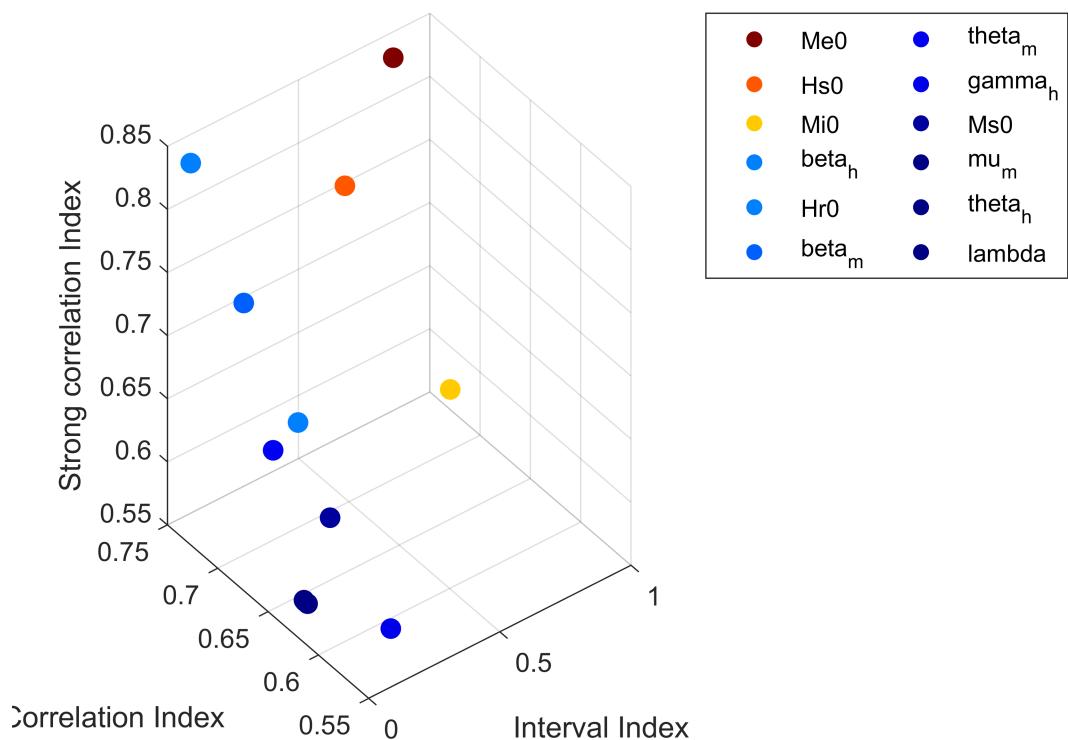
```
T7.Nominal = T7.Estlsqc(:,1);  
%res : funciones de costo  
th = sum(res<res(1)*1.01)
```

```
th = 3
```

```
T7 = gsua_ia(T7,T7.Estlsqc(:,1:th), false, true);
```







T = 11x2 table | Reduced from 12 rows

	Range		Nominal
1 Me0	81405	158809	120107

	Range		Nominal
2 Hs0	244402	321734	283068
3 Ms0	0	1200000	600000
4 Mi0	0	100	50
5 beta_h	0	4	2
6 beta_m	0	4	2
7 gamma_h	0.5000	1.7500	1.1250
8 lambda	1881	42694	2.2288e+04
9 mu_m	0.1600	0.2000	0.1800
10 theta_h	0.7000	1.7500	1.2250
11 theta_m	0.5800	0.8800	0.7300

```
%savefig('iteration1/figures/CorrelationsDiag.fig')
```

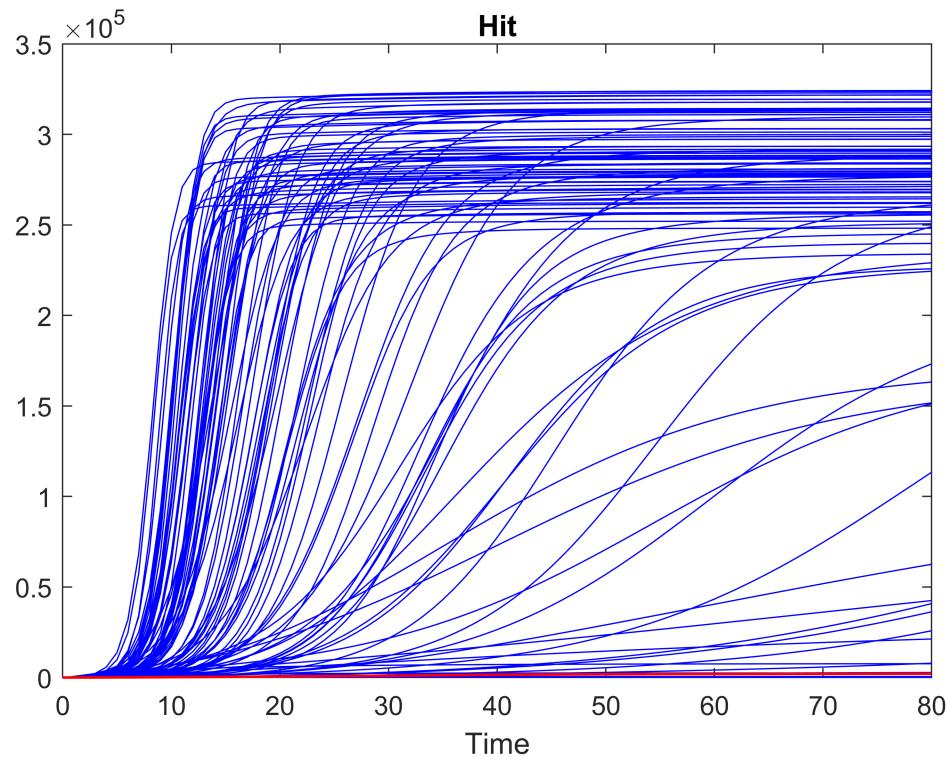
## 6. Análisis de incertidumbre

Veamos que las curvas hagan una banda al lado de los datos que estamos estimando. Si la banda es chevere, (visualmente) terminamos, si no, debemos fijar algún parámetro.

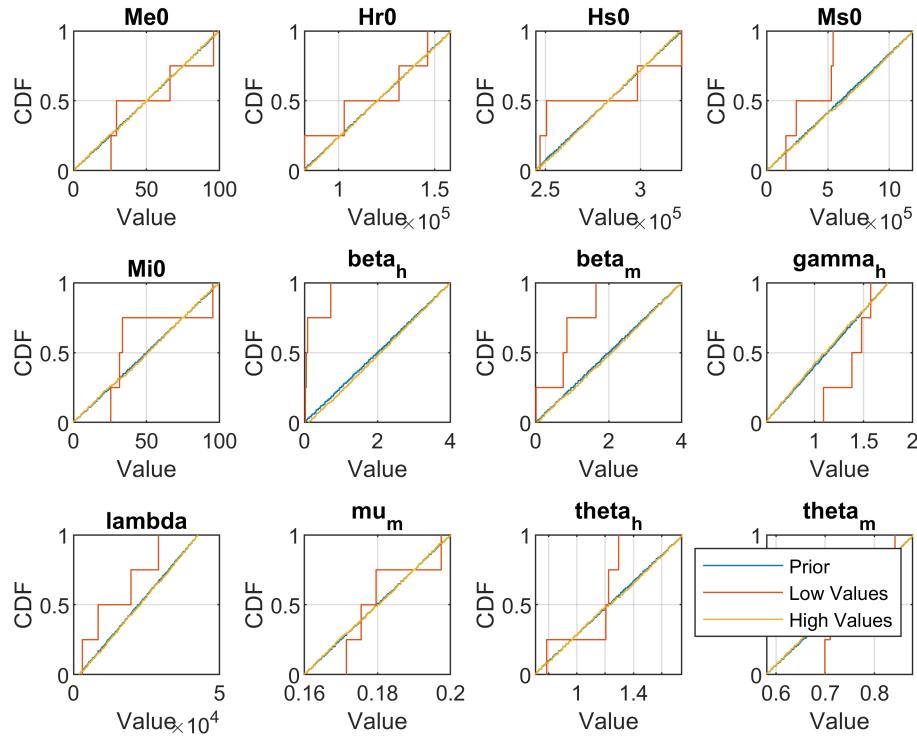
```
Ua = gsua_ua(M, T7, 'parallel', false, 'ynom',ydata2);
```

```
Progress: 100%
Estimated processing time (h:m:s): 0:0:0
Remaining time (h:m:s): 0:0:0
Elapsed time (h:m:s): 0:0:0
Estimated stop time (h:m:s): 22:18:21
Number of simulations: 100
```

N=100



Montecarlo Filtering for escalar Y with N: 100



```
%savefig('iteration1/figures/Montecarlo.fig')
```

## Segunda iteracion de los calculos

Debemos de repetir todo desde el paso 3 (el análisis de sensibilidad) pero habiendo aumentado los rangos de las

variables que se observan desde el boxplot de identificabilidad.

Aumentamos los rangos de theta\_h, theta\_m, lambda, mu\_m, Ms0 .

```
T.Range('theta_h',1) = 0.5;
T.Range('lambda',1) = 1500;
T.Range('mu_m',1) = 0.12;
T.Range('Ms0',2) = 1.5e6;
T.Range('theta_m',2) = 1.2;
%save('iteration1/values/T.mat','T')
```

### 4. Estimación de parámetros

```
opt = optimoptions('lsqcurvefit','UseParallel',true,'Display','iter');
[T7_1,res_1] = gsua_pe(T,xdata,ydata2,'N',100,'opt',opt);
%save('iteration2/values/Results7.mat','T7_1','res_1','xdata','ydata2')
```

### 5. Análisis de identificabilidad

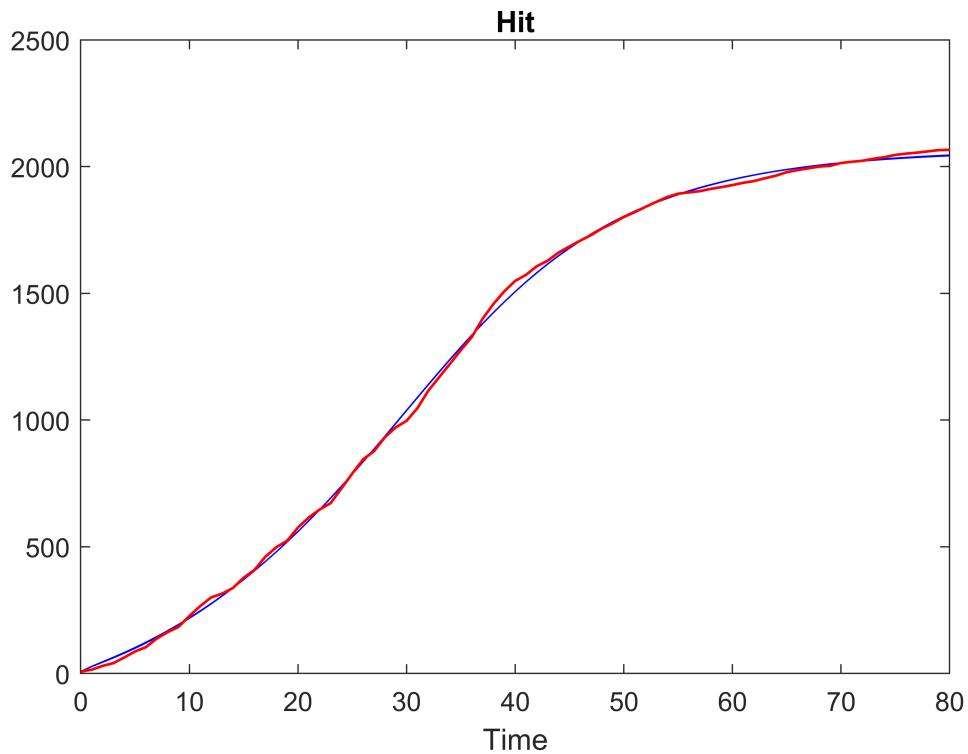
```
th_1 = sum(res_1<res_1(1)*1.01)
```

```
th_1 = 9
```

```
y7_1 = gsua_eval(T7_1.Estlsqlc(:,1:th_1),T7_1,xdata,ydata2);
```

```
Sim9 Done
Sim8 Done
Sim7 Done
Sim6 Done
Sim5 Done
Sim4 Done
Sim3 Done
Sim2 Done
Sim1 Done
```

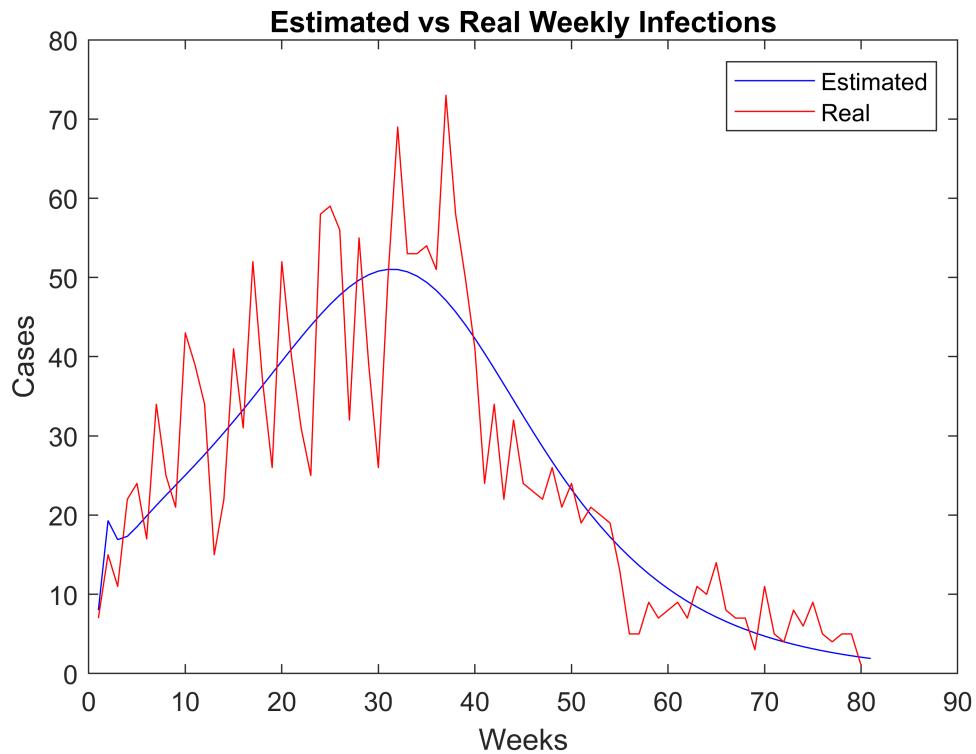
N=9



```
%savefig('iteration2/figures/curves.fig')
```

```
bestest_1 = y7_1(1,:);
trend = [bestest_1(1),bestest_1(2:end)-bestest_1(1:end-1)];
plot(trend,'b')
hold on
plot(diff(ydata2),'r')
title('Estimated vs Real Weekly Infections')
xlabel('Weeks')
ylabel('Cases')
legend({'Estimated','Real'})
```

N=9



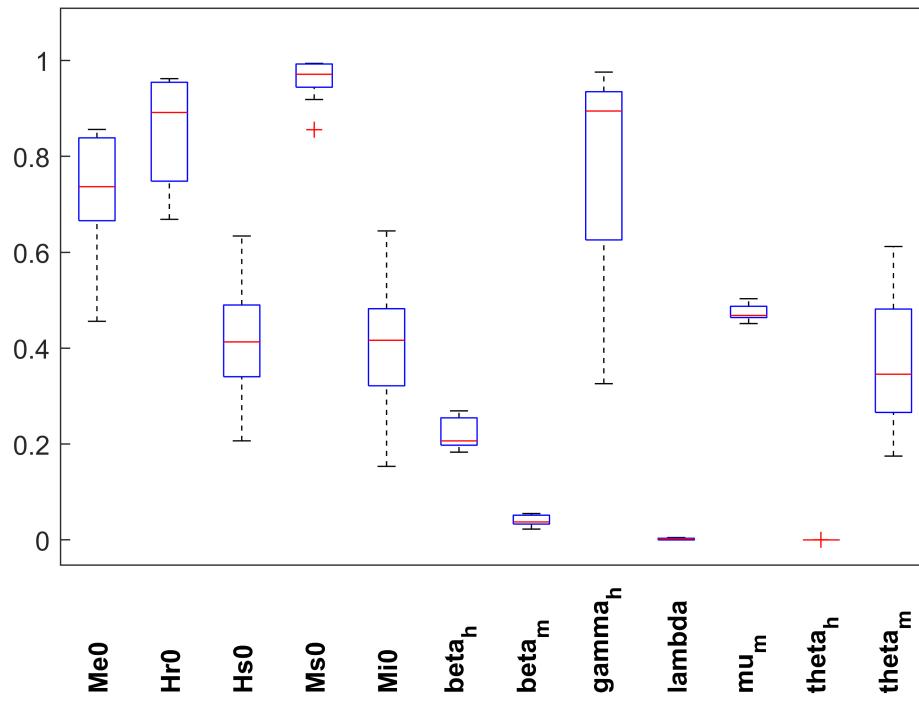
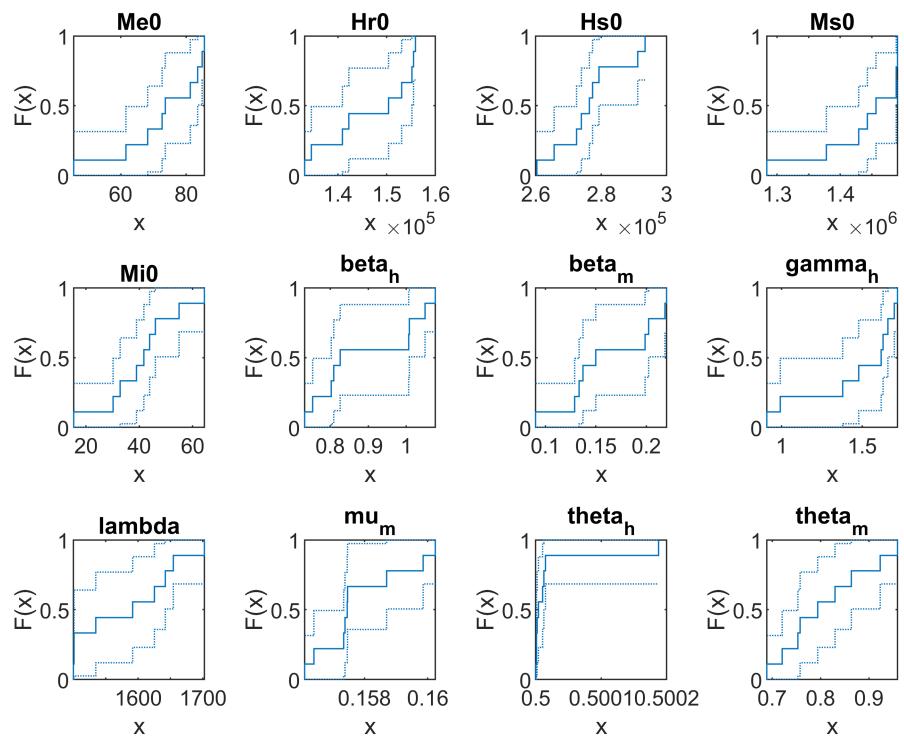
```
%savefig('iteration2/figures1/EstimatedvsReal.fig')
```

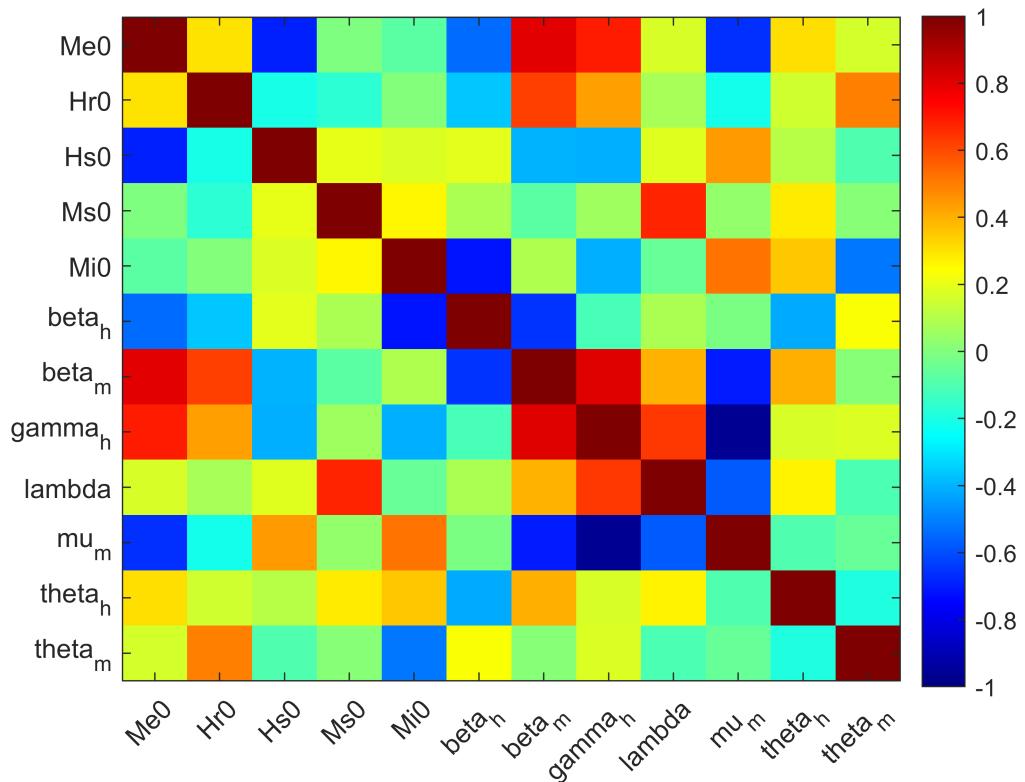
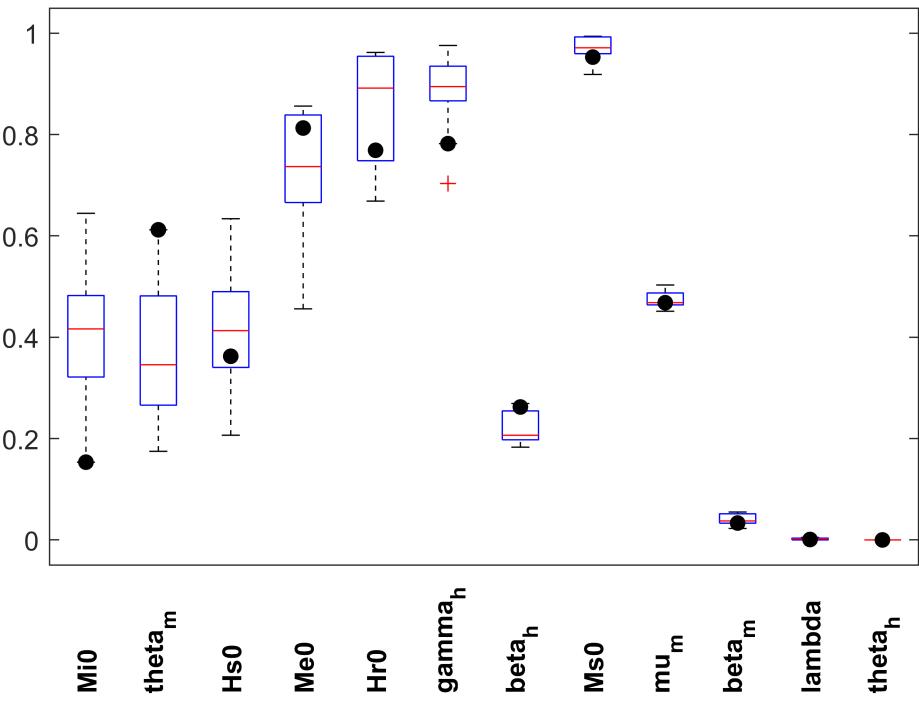
```
T7_1.Nominal = T7_1.Estlscqc(:,1);
%res : funciones de costo
th_1 = sum(res_1<res_1(1)*1.01) % threshold, cambiar el 1.01
```

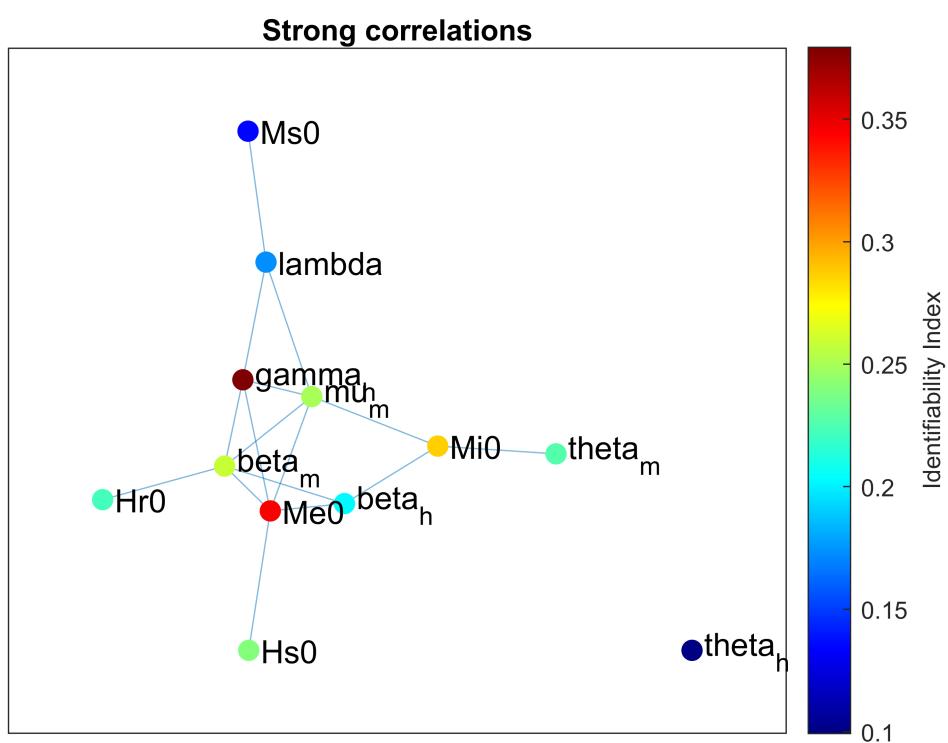
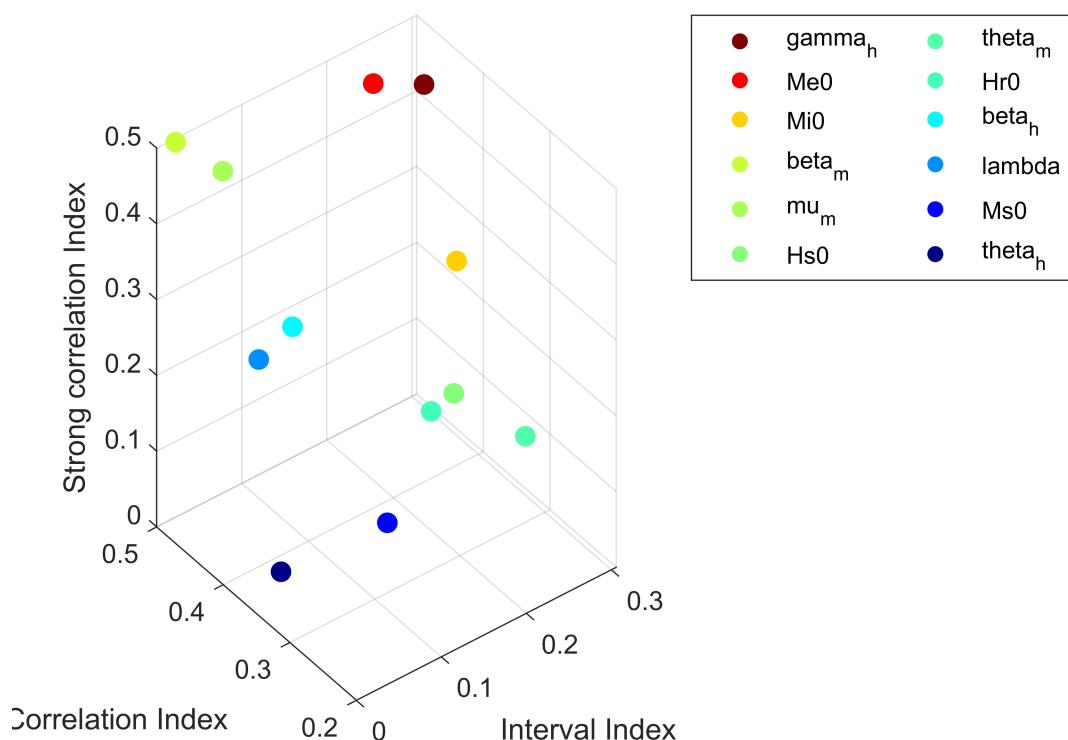
```
th_1 = 9
```

```
%th = 476 %el parametro que habia dado el profe, a nosotros nos da 1????
```

```
T7_1 = gsua_ia(T7_1,T7_1.Estlscqc(:,1:th_1), false, true);
```







T = 11x2 table | Reduced from 12 rows

	Range		Nominal
1 Me0	81405	158809	120107

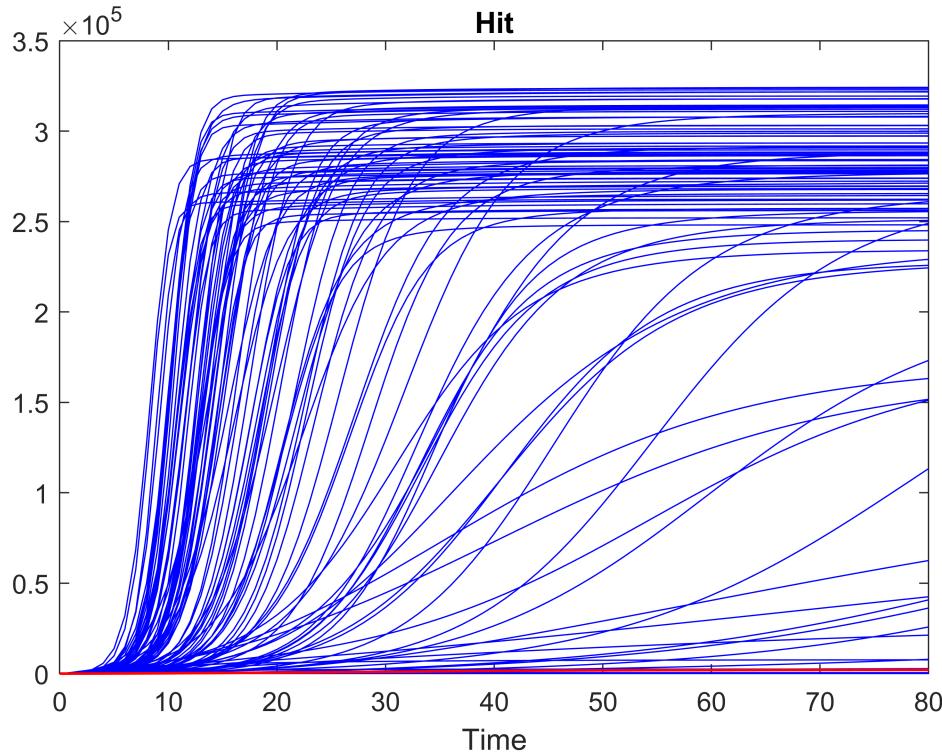
	Range		Nominal
2 Hs0	244402	321734	283068
3 Ms0	0	1200000	600000
4 Mi0	0	100	50
5 beta_h	0	4	2
6 beta_m	0	4	2
7 gamma_h	0.5000	1.7500	1.1250
8 lambda	1881	42694	2.2288e+04
9 mu_m	0.1600	0.2000	0.1800
10 theta_h	0.7000	1.7500	1.2250
11 theta_m	0.5800	0.8800	0.7300

```
%savefig('iteration2/figures/Correlations.fig')
```

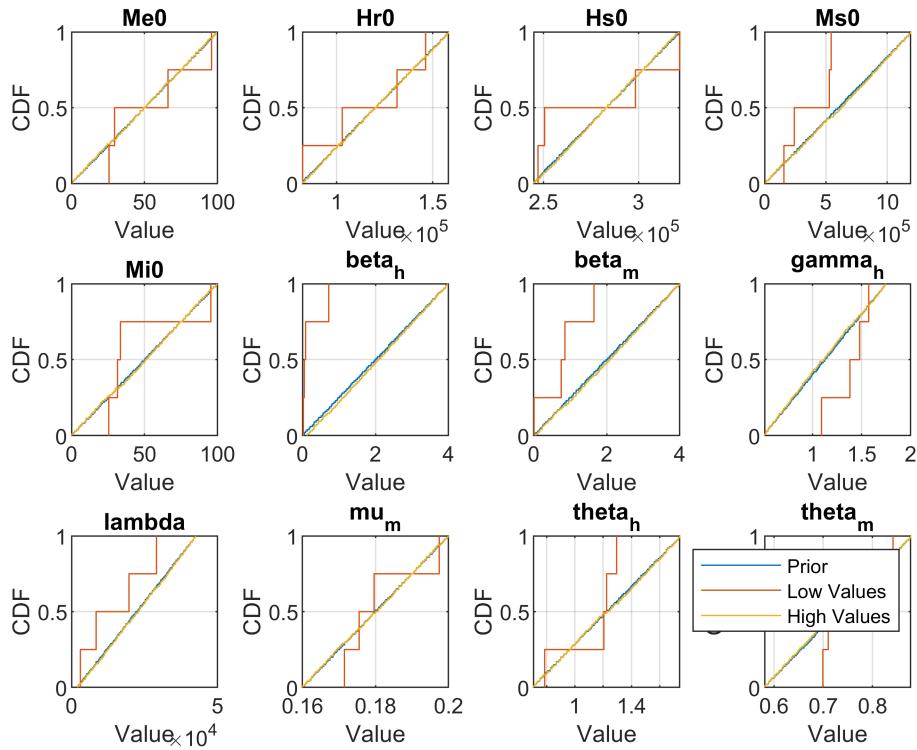
```
gsua_ua(M, T7_1, 'parallel', false, 'ynom',ydata2);
```

Progress: 100%  
 Estimated processing time (h:m:s): 0:0:0  
 Remaining time (h:m:s): 0:0:0  
 Elapsed time (h:m:s): 0:0:0  
 Estimated stop time (h:m:s): 22:32:17  
 Number of simulations: 100

N=100



### Montecarlo Filtering for escalar Y with N: 100



## Tercera Iteracion

Vemos que todavia debemos aumentar los rangos de lambda, theta\_h, Ms0 y theta\_m

```
T.Range('lambda',1) = 1100;
T.Range('theta_h',1) = 0.2;
T.Range('Ms0',2) = 1.6e6;
T.Range('theta_m',2) = 1.2;
```

#### 4. Estimamos los parámetros

```
opt = optimoptions('lsqcurvefit','UseParallel',false,'Display','iter');
[T7_2,res_2] = gsua_pe(T,xdata,ydata2,'N',100,'opt',opt);
%save('iteration3/values/Results7.mat','T7_2','res_2','xdata','ydata2')
```

#### 5. Análisis de identificabilidad

```
th_2 = sum(res_2<res_2(1)*1.03)
```

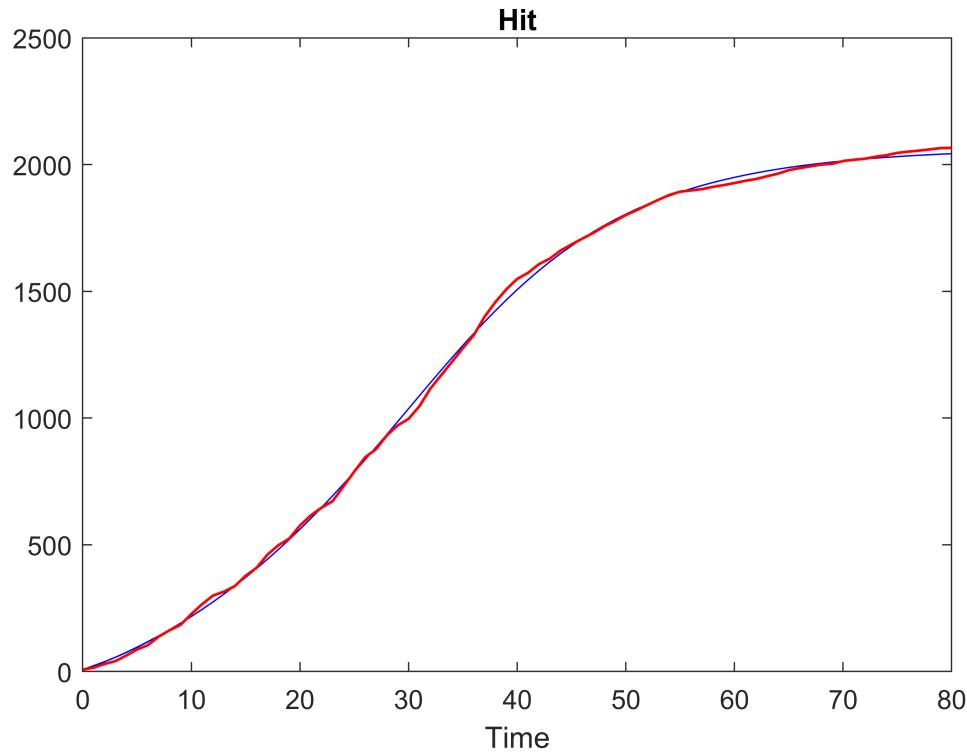
```
th_2 = 10
```

```
y7_2 = gsua_eval(T7_2.Estlscqc(:,1:th_2),T7_2,xdata,ydata2);
```

```
Sim10 Done
Sim9 Done
Sim8 Done
```

```
Sim7 Done
Sim6 Done
Sim5 Done
Sim4 Done
Sim3 Done
Sim2 Done
Sim1 Done
```

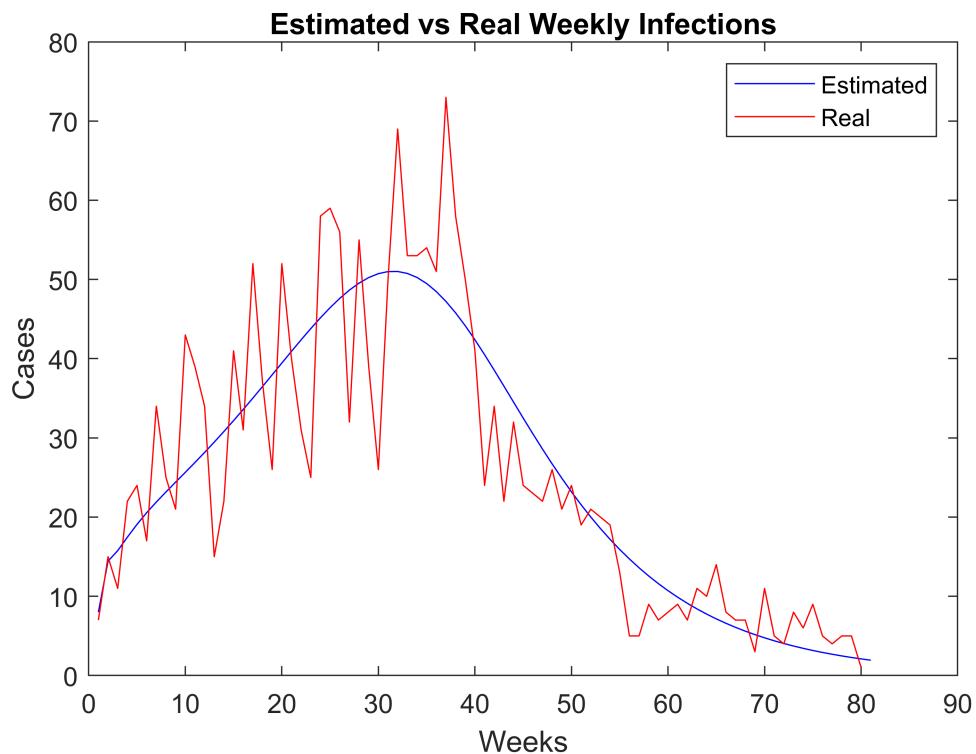
N=10



```
%savefig('iteration3/figures/circles.fig')
```

```
bestest_2 = y7_2(1,:);
trend = [bestest_2(1),bestest_2(2:end)-bestest_2(1:end-1)];
plot(trend,'b')
hold on
plot(diff(ydata2),'r')
title('Estimated vs Real Weekly Infections')
xlabel('Weeks')
ylabel('Cases')
legend({'Estimated','Real'})
```

N=10

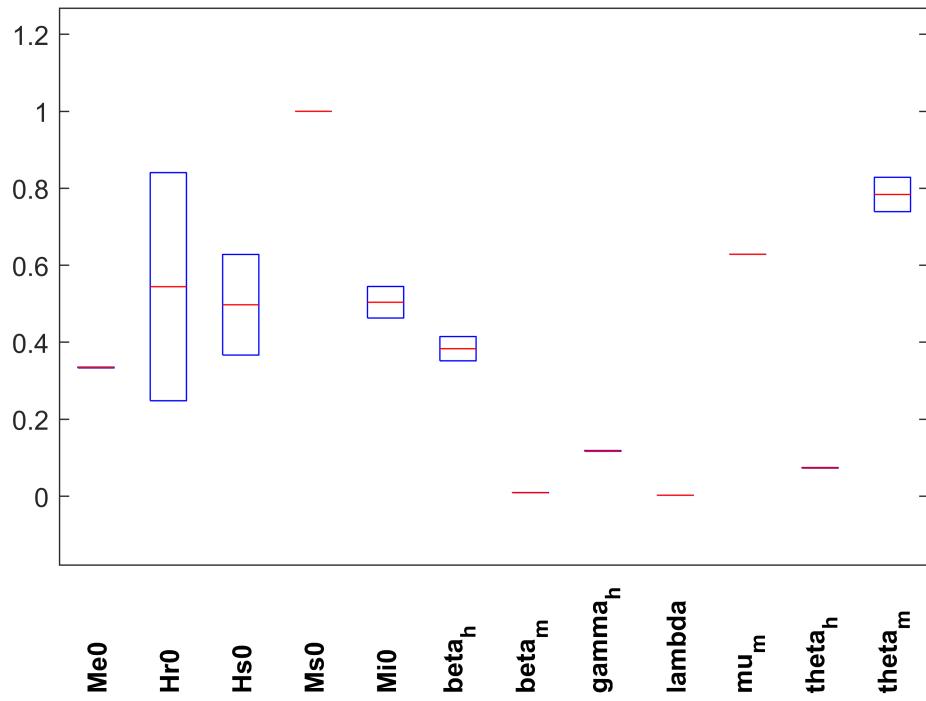
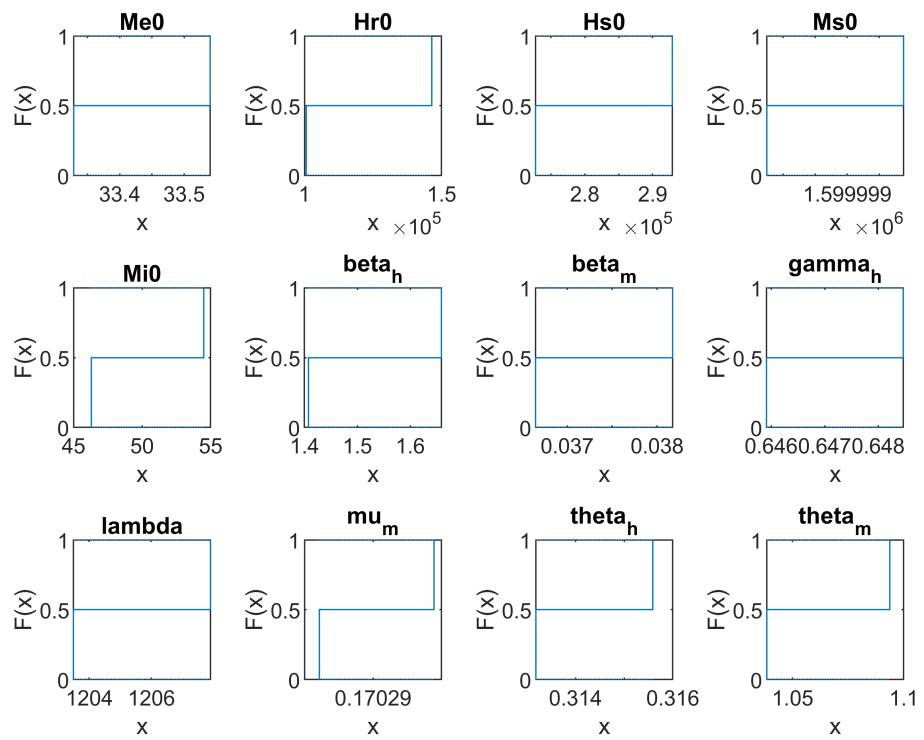


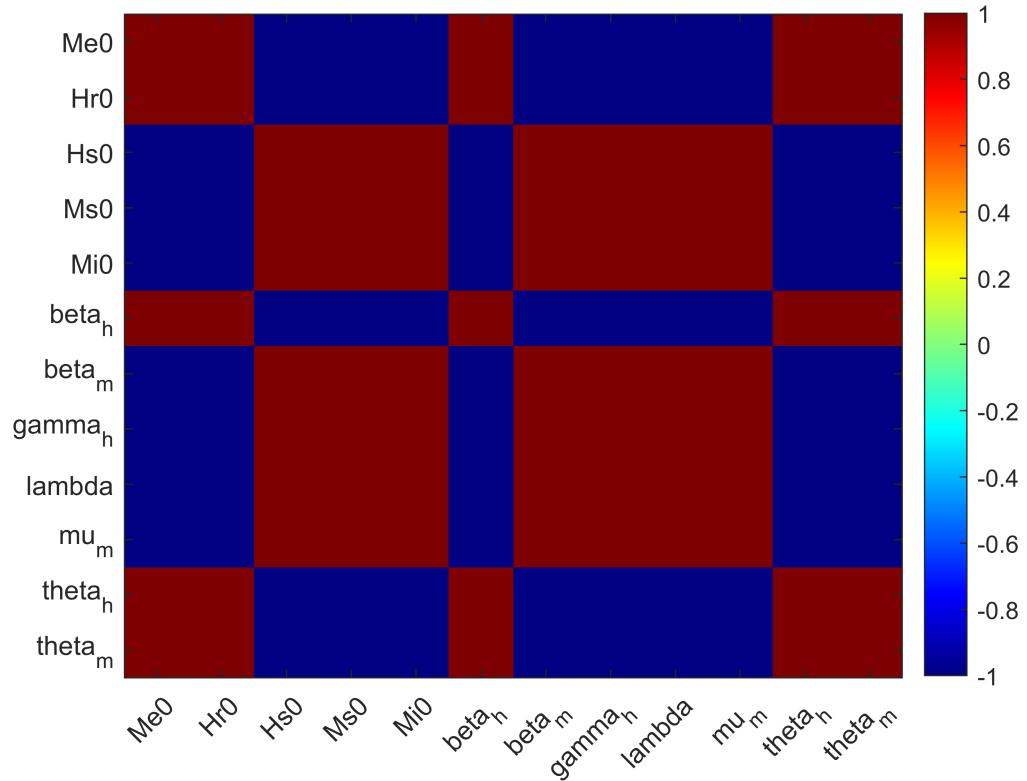
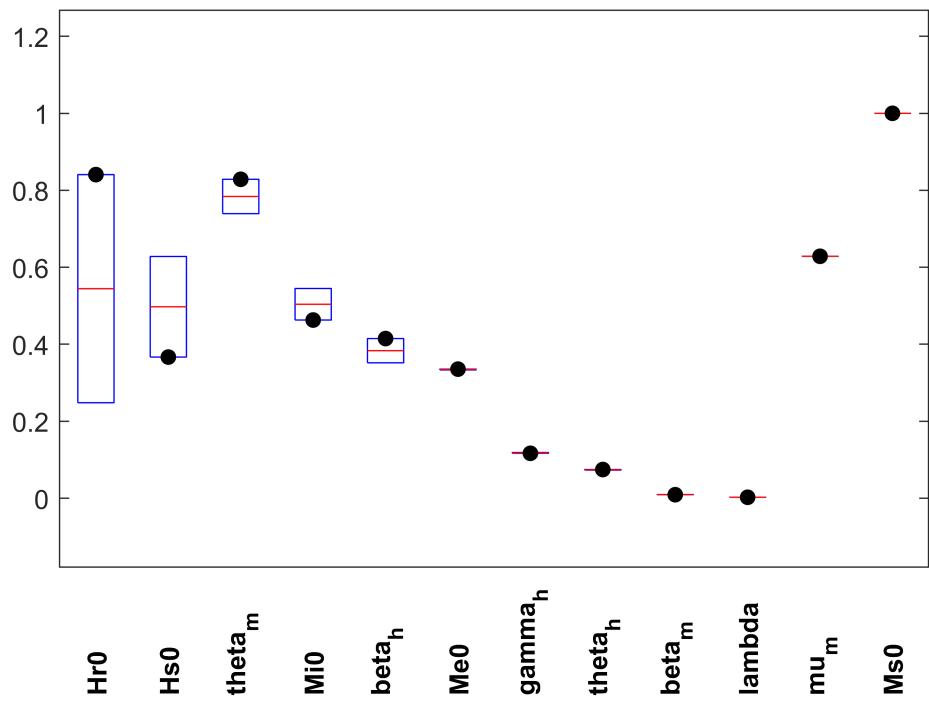
```
%savefig('iteration3/figures1/EstimatedvsReal.fig')
```

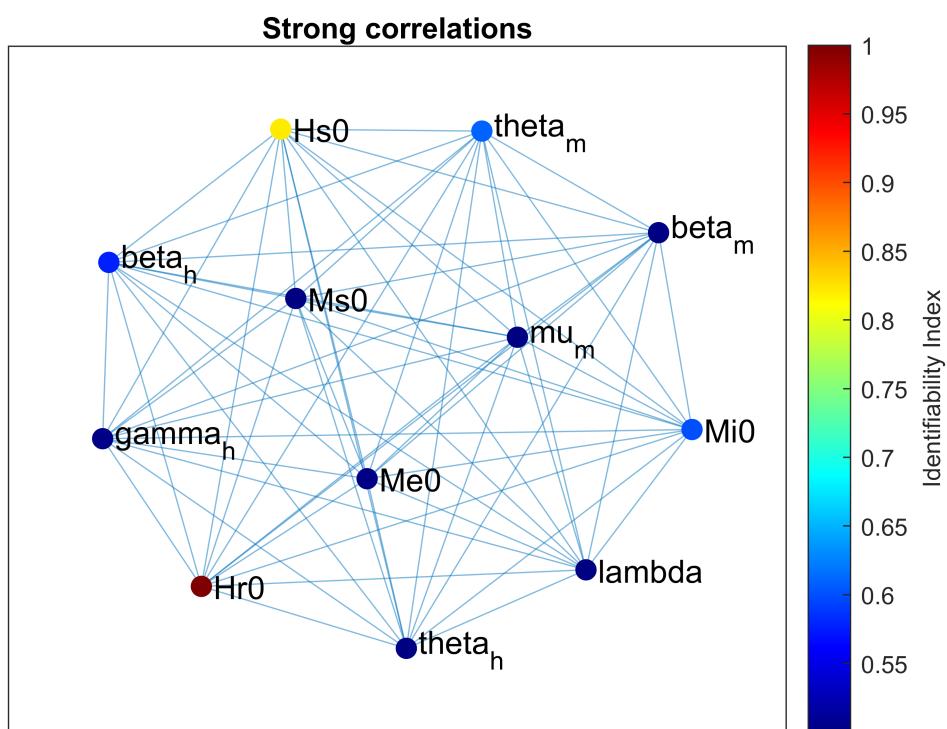
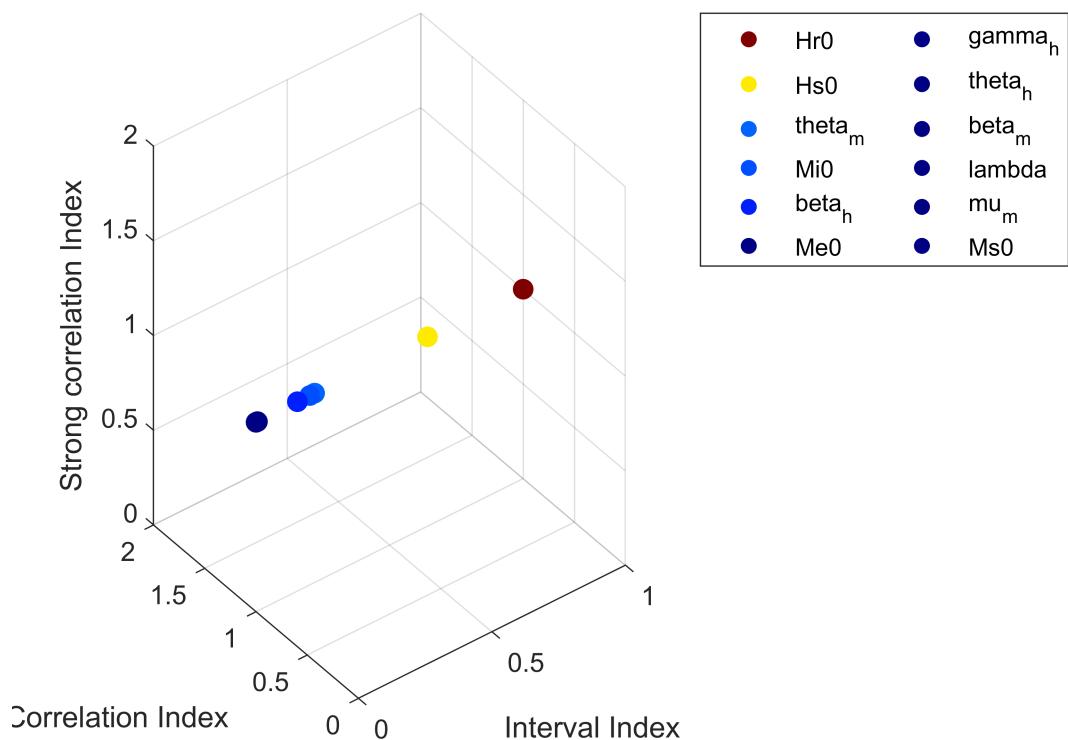
```
T7_2.Nominal = T7_2.Estlsqc(:,1);  
th_2 = sum(res_2<res_2(1)*1.01)
```

```
th_2 = 2
```

```
T7_2 = gsua_ia(T7_2,T7_2.Estlsqc(:,1:th_2), false, true);
```







T = 11×2 table | Reduced from 12 rows

	Range		Nominal
1 Me0	81405	158809	120107

	Range		Nominal
2 Hs0	244402	321734	283068
3 Ms0	0	1200000	600000
4 Mi0	0	100	50
5 beta_h	0	4	2
6 beta_m	0	4	2
7 gamma_h	0.5000	1.7500	1.1250
8 lambda	1881	42694	2.2288e+04
9 mu_m	0.1600	0.2000	0.1800
10 theta_h	0.7000	1.7500	1.2250
11 theta_m	0.5800	0.8800	0.7300

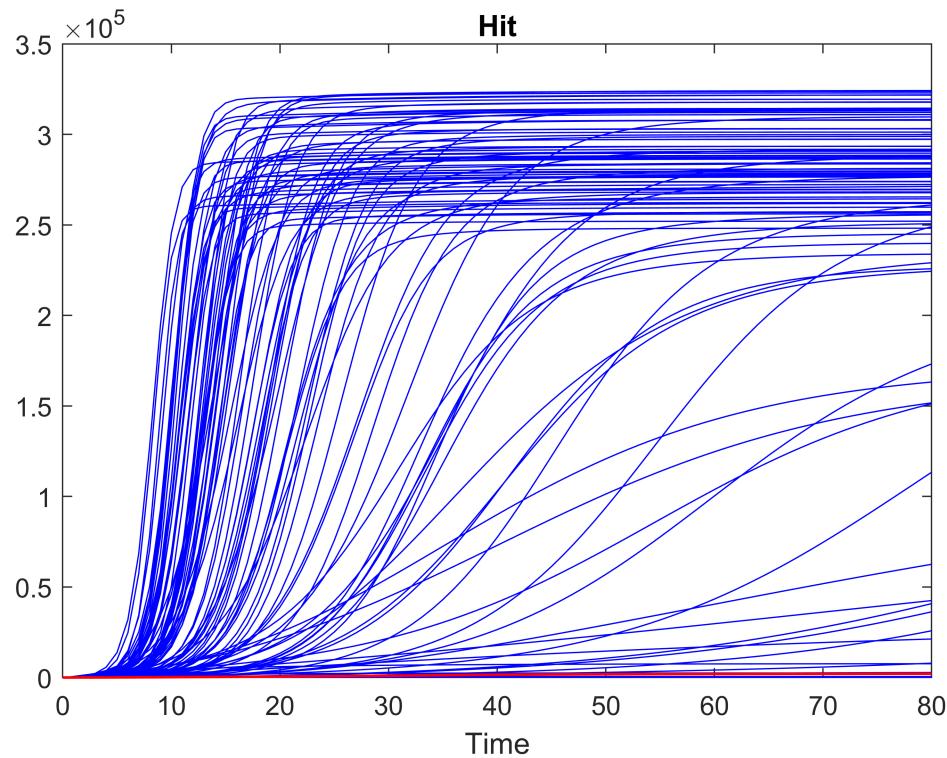
```
%savefig('iteration3/figures/Correlations.fig')
```

## 6. Análisis de incertidumbre

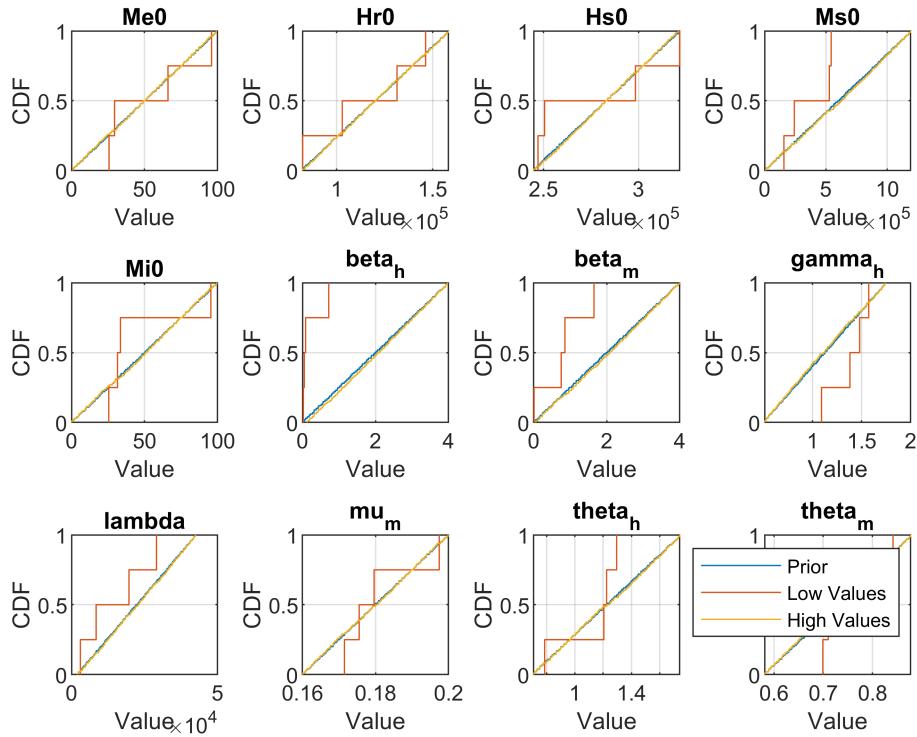
```
gsua_ua(M, T7_2, 'parallel', false, 'ynom',ydata2);
```

```
Progress: 100%
Estimated processing time (h:m:s): 0:0:0
Remaining time (h:m:s): 0:0:0
Elapsed time (h:m:s): 0:0:0
Estimated stop time (h:m:s): 22:51:15
Number of simulations: 100
```

N=100



Montecarlo Filtering for escalar Y with N: 100



```
%savefig('iteration3/figures/Montecarlo.fig')
```

## Cuarta Iteracion

Fijamos Hr) dado que este esta muy correlacionado a las otras variables

```
vars=[Hit Hi He Hr Me Hs Ms Mi];  
  
Hr0 = T7_2.Estlsqc('Hr0',1);  
  
RangeTemp = Range;  
Range(4,:) = He0;  
  
[T,~]=gsua_dpmat(odes,vars,[0 80], '7m', 'output',1,'opt',opts,'Range',Range);
```

Introduce ranges in the following order:

$\text{ans}(t) = (\text{Hit}(t) \quad \text{Hi}(t) \quad \text{He}(t) \quad \text{Hr}(t) \quad \text{Me}(t) \quad \text{Hs}(t) \quad \text{Ms}(t) \quad \text{Mi}(t) \quad \beta_h \quad \beta_m \quad \gamma_h \quad \lambda \quad \mu_h \quad \mu_m \quad \theta_h \quad \theta_m)$

```
T.Properties.CustomProperties.output = 1;  
M = gsua_dmatrix(T,100);
```

### 4. Estimamos los parámetros

```
opt = optimoptions('lsqcurvefit','UseParallel',true,'Display','iter');  
[T7_3,res_3] = gsua_pe(T,xdata,ydata2,'N',100,'opt',opt);  
%save('iteration3/values/Results7.mat','T7_2','res_2','xdata','ydata2')
```

### 5. Análisis de identificabilidad

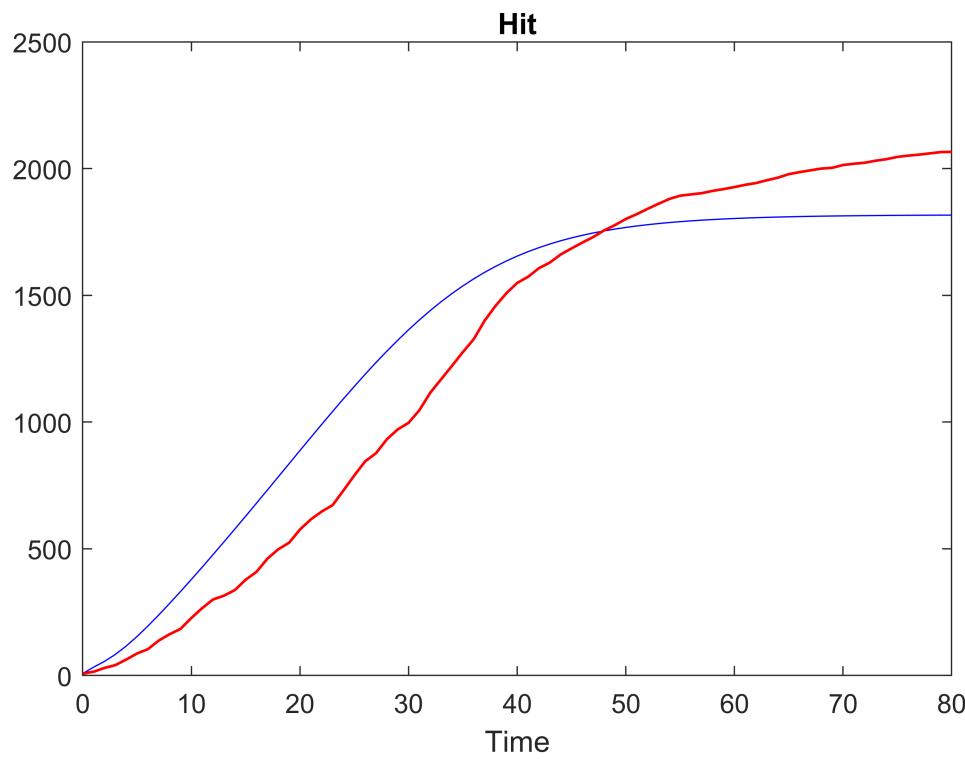
```
th_3 = sum(res_3<res_3(1)*1.01)  
  
th_3 = 100  
  
y7_3 = gsua_eval(T7_3.Estlsqc(:,1:th_3),T7_3,xdata,ydata2);
```

```
Sim100 Done  
Sim99 Done  
Sim98 Done  
Sim97 Done  
Sim96 Done  
Sim95 Done  
Sim94 Done  
Sim93 Done  
Sim92 Done  
Sim91 Done  
Sim90 Done  
Sim89 Done  
Sim88 Done  
Sim87 Done  
Sim86 Done  
Sim85 Done  
Sim84 Done  
Sim83 Done  
Sim82 Done  
Sim81 Done  
Sim80 Done  
Sim79 Done
```

Sim78 Done  
Sim77 Done  
Sim76 Done  
Sim75 Done  
Sim74 Done  
Sim73 Done  
Sim72 Done  
Sim71 Done  
Sim70 Done  
Sim69 Done  
Sim68 Done  
Sim67 Done  
Sim66 Done  
Sim65 Done  
Sim64 Done  
Sim63 Done  
Sim62 Done  
Sim61 Done  
Sim60 Done  
Sim59 Done  
Sim58 Done  
Sim57 Done  
Sim56 Done  
Sim55 Done  
Sim54 Done  
Sim53 Done  
Sim52 Done  
Sim51 Done  
Sim50 Done  
Sim49 Done  
Sim48 Done  
Sim47 Done  
Sim46 Done  
Sim45 Done  
Sim44 Done  
Sim43 Done  
Sim42 Done  
Sim41 Done  
Sim40 Done  
Sim39 Done  
Sim38 Done  
Sim37 Done  
Sim36 Done  
Sim35 Done  
Sim34 Done  
Sim33 Done  
Sim32 Done  
Sim31 Done  
Sim30 Done  
Sim29 Done  
Sim28 Done  
Sim27 Done  
Sim26 Done  
Sim25 Done  
Sim24 Done  
Sim23 Done  
Sim22 Done  
Sim21 Done  
Sim20 Done  
Sim19 Done  
Sim18 Done  
Sim17 Done  
Sim16 Done  
Sim15 Done

```
Sim14 Done
Sim13 Done
Sim12 Done
Sim11 Done
Sim10 Done
Sim9 Done
Sim8 Done
Sim7 Done
Sim6 Done
Sim5 Done
Sim4 Done
Sim3 Done
Sim2 Done
Sim1 Done
```

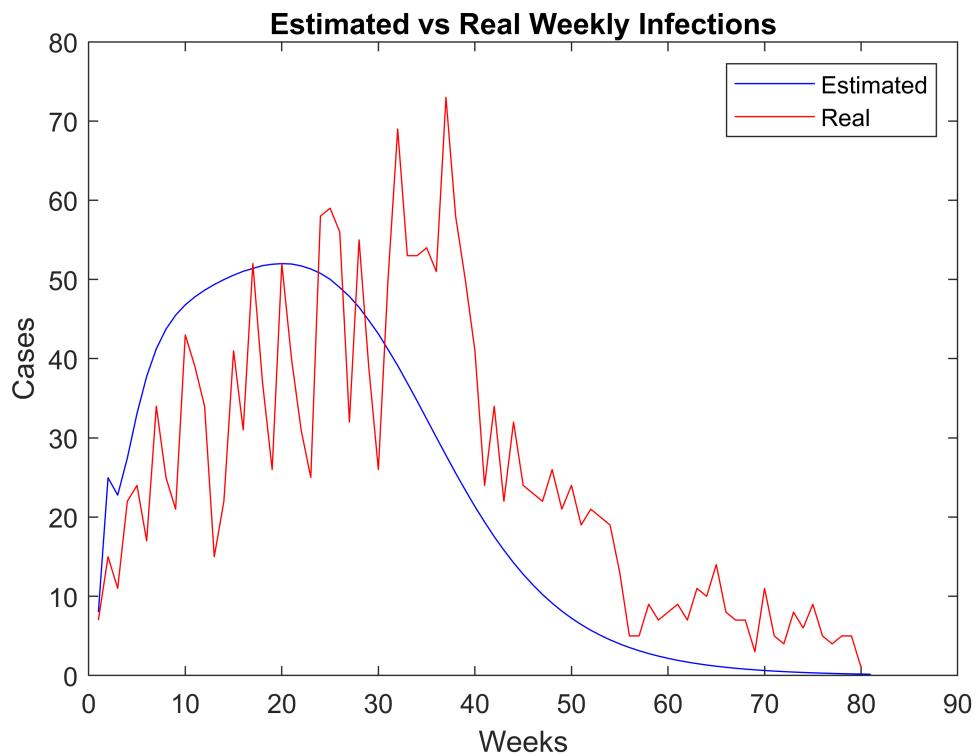
N=100



```
%savefig('iteration3/figures/circles.fig')
```

```
bestest_3 = y7_3(1,:);
trend = [bestest_3(1),bestest_3(2:end)-bestest_3(1:end-1)];
plot(trend,'b')
hold on
plot(diff(ydata2),'r')
title('Estimated vs Real Weekly Infections')
xlabel('Weeks')
ylabel('Cases')
legend({'Estimated','Real'})
```

N=100



```
%savefig('iteration3/figures1/EstimatedvsReal.fig')
```

Al fijar  $H_r$  las estimaciones dejan de funcionar y el modelo deja de ajustar correctamente, esto tiene multiples distintas razones por las que puede ser, no se ampliaron los rangos lo suficiente en las iteraciones anteriores, el parametro que se fijo, tenia mucha incertidumbre sobre su valor, esto se observa en el boxplot de la iteracion anterior, donde  $H_r$ , es el parametro con mayor caja, por lo que aunque afectaba mucho a los otros parametros, habia muy poca certeza sobre su valor real. O que posiblemente el threshold que se tomo fue muy restrictivo, lo cual afecto mucho los analisis de identificabilidad, por tanto se termino eligiendo el parametro incorrecto, con un valor posiblemente inadecuado. Tambien se observa como al realizar el analisis de identificabilidad, el parametro  $\mu$  quedo con un rango basicamente nulo, por lo que esto tambien pudo haber afectado el analisis y la estimacion de parametros en la siguiente iteracion.