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2 Susceptible host dynamics explain pathogen resilience
3
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5 **Abstract**

6 Major priority for epidemiological research in the time of anthropogenic change is
7 understanding how infectious disease dynamics respond to perturbations. Interven-
8 tions to slow the spread of COVID-19 significantly disrupted the transmission of other
9 human pathogens, providing unique opportunities to learn about pathogen charac-
10 teristics from spatiotemporal variation in re-emergence patterns. As interventions
11 lifted, a key question of whether and when respiratory pathogens would eventually
12 return to their pre-pandemic dynamics remains to be answered. To address this
13 gap, we develop a framework for estimating pathogen resilience based on how fast
14 epidemic patterns return to their pre-pandemic, endemic cycles. Our analysis re-
15 veals a possibility that some pathogens may have settled to endemic cycles that are
16 different from their pre-pandemic patterns. Finally, we show that heterogeneity in
17 pathogen resilience can be understood in terms of how fast a susceptible host popula-
18 tion becomes replenished. Our framework offers a novel perspective to characterizing
19 epidemic dynamics of endemic pathogens and measuring epidemic time scales.

Understanding how ecological systems respond to perturbations is a fundamental challenge in predicting species persistence and extinction (Bender et al., 1984; Ives and Carpenter, 2007; Scheffer et al., 2009). These responses are often characterized in terms of resilience, which captures how fast a system returns to its stable, reference state following a perturbation (Pimm, 1979; Neubert and Caswell, 1997; Gunderson, 2000; Dakos and Kéfi, 2022). Both theoretical and empirical efforts to quantify resilience of ecological systems have provided key insights for understanding the dynamics of complex systems and linking these findings to actionable strategies for species conservation. However, despite rich literature on ecological resilience, there have been limited applications to measuring the resilience of host-pathogen systems, especially for human pathogens.

Non-pharmaceutical interventions (NPIs) to slow the spread of COVID-19 disrupted the transmission of other human pathogens, providing large-scale natural experiments for understanding how various host-pathogen systems respond to perturbations (Baker et al., 2020; Gomez et al., 2021; Koltai et al., 2022; Park et al., 2024). In particular, as interventions lifted, large heterogeneities in outbreak dynamics were observed across different pathogens in different countries (Figure 1), likely reflecting differences in NPI patterns, pathogen characteristics, immigration/importation from other countries, and pre-pandemic pathogen dynamics. Even though more than four years have already passed since the emergence of COVID-19, current circulation patterns for many respiratory pathogens appear to be different from their pre-pandemic, seasonal patterns, especially in Hong Kong and Korea: some pathogens, such as human metapneumovirus and bocavirus in Korea, are circulating at lower levels, whereas other pathogens, such as RSV in Korea, seem to exhibit different seasonality (Figure 1). These observations pose two fundamental questions for current and future infectious disease dynamics: (1) can we learn about underlying pathogen characteristics, such as their transmissibility or duration of immunity, from re-emergence patterns? and (2) can we predict whether and when other respiratory pathogens will eventually return to their pre-pandemic dynamics?

To address this question, we propose a framework for characterizing the resilience of a host-pathogen system based on how fast the system recovers from perturbation. We begin by laying out a few example scenarios that represent the expected outbreak dynamics following COVID-19 interventions and illustrating how resilience can be measured by comparing the post- and pre-pandemic dynamics of susceptible and infected hosts. In practice, the dynamics of susceptible hosts are often unavailable, and traditional susceptible reconstruction approaches often require long-term endemic time series, which cannot be applied due to disruptions in epidemic patterns caused by COVID-19 NPIs. Instead, we utilize Takens' embedding theorem to reconstruct empirical attractors from data and further measure the distance from this empirical attractor, which allows us to characterize the rate at which this distance decreases. Analyses of pathogen surveillance data for a wide array of respiratory pathogens in Canada, Hong Kong, and Korea suggest ... Finally, we show that variation in resilience estimates can be understood in terms of susceptible host dynamics.

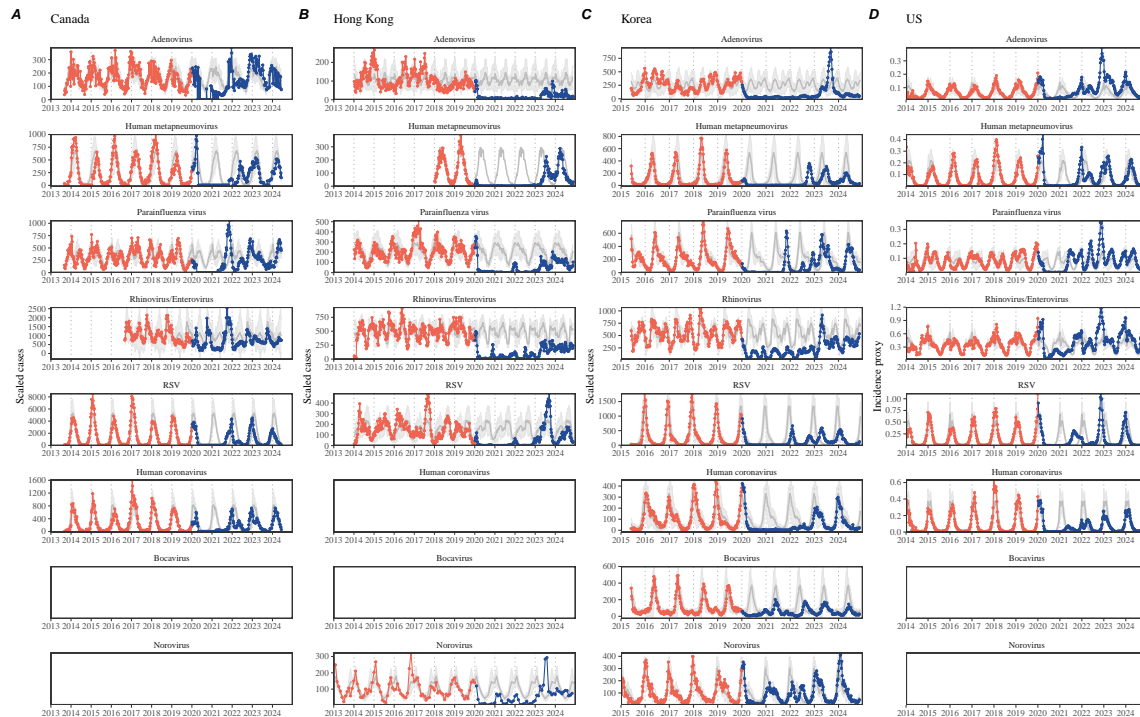


Figure 1: Observed heterogeneity in responses to COVID-19 pandemic across respiratory pathogens and norovirus in (A) Canada, (B) Hong Kong, (C) Korea, and (D) US. Red points and lines represent data before 2020. Blue points and lines represent data since 2020. Gray lines and shaded regions represent the mean seasonal patterns and corresponding 95% confidence intervals based on the observed outbreak patterns before 2020.

63 [SWP: Revisit.]

64 Conceptual introduction to pathogen resilience

65 In classical ecological literature, resilience of an ecological system is measured by the
 66 rate at which the system returns to its reference state following a perturbation. This
 67 rate corresponds to the largest real part of the eigenvalues of the linearized system
 68 near equilibrium—here, we refer to this value as the *intrinsic* resilience of the system,
 69 which represents the expected rate of return from perturbed states. However, res-
 70 piratory pathogens often exhibit seasonal variation in transmission, meaning that the
 71 intrinsic resilience of a host-pathogen system varies across season. Nonetheless, we
 72 can still measure the *empirical* resilience of a host-pathogen system by looking at how
 73 fast the system returns to the pre-pandemic, endemic dynamics after interventions
 74 are lifted.

75 As an example, consider an intervention that reduce transmission by 50% for 6
 76 months starting in 2020, which causes epidemic patterns to deviate from its original

stable annual cycle for a short period of time and eventually come back (Figure 2A). To measure the empirical resilience of this system, we first need to be able to measure the distance from its pre-pandemic attractor. There are many different ways we can measure the distance from attractor, but for illustrative purposes, we choose one of the most parsimonious approach: that is, we look at how the susceptible (S) and infected (I) populations change over time and measure the distance on the SI phase plane (Figure 2B). In this simple case, the locally estimated scatterplot smoothing (LOESS) fit indicates that the distance from attractor decreases linearly on average (Figure 2C). Furthermore, the overall rate of return matches the intrinsic resilience of the seasonally unforced system (Figure 2C).

Alternatively, NPIs can permanently change our behavior and have persisting impact on the pathogen dynamics; as an example, we consider a scenario in which a 10% reduction in transmission persists even after the NPIs are lifted (Figure 2D–F). In such cases, we cannot know whether the pathogen will return to its original cycle or a different cycle until many years have passed after the NPIs are lifted, meaning that we cannot measure the distance against the new attractor that the system will eventually approach. Nonetheless, we can still measure the distance against the original, pre-pandemic attractor and ask how the distance changes over time (Figure 2E). The LOESS fit suggests that the distance from the attractor will initially decrease exponentially on average (equivalently, linearly on a log scale) and eventually plateau (Figure 2F). Here, a permanent 10% reduction in transmission rate slows down the system, which causes the distance from the attractor to decrease at a slower rate (Figure 2F) than it would have otherwise in the absence of permanent transmission reduction (Figure 2C). This example shows that resilience is not necessarily an intrinsic property of a specific pathogen. Instead, pathogen resilience is a property of a specific attractor that a host-pathogen system approaches, which depends on both pathogen and host characteristics. **[SWP: Add discussion about observation error, e.g., under-reporting.]**

Finally, transient phenomena can also complicate the picture (Figure 2G–I). For example, a stage-structured model for RSV initially exhibits a stable annual cycle, but perturbations from NPIs cause the epidemic to exhibit biennial cycles (Figure 2G). Despite this biennial cycle, we see that the system eventually approaches the original pre-pandemic attractor (Figure 2H), suggesting that this biennial cycle is a transient phenomenon. The LOESS fit indicates that the distance from the attractor will initially decrease exponentially at a rate that is consistent with the intrinsic resilience of the seasonally unforced system, but the rate of decrease slows down as the epidemic exhibits a biennial cycle (Figure 2I). In classical ecological theory, this behavior is also referred to as a ghost attractor, which causes long transient dynamics and slow transitions.

These observations indicate three possibilities. First, we can directly estimate the empirical resilience of a host-pathogen system by looking at how fast the system approaches a pre-pandemic attractor, provided that we can measure the distance from attractor. The empirical approach to estimating pathogen resilience is partic-

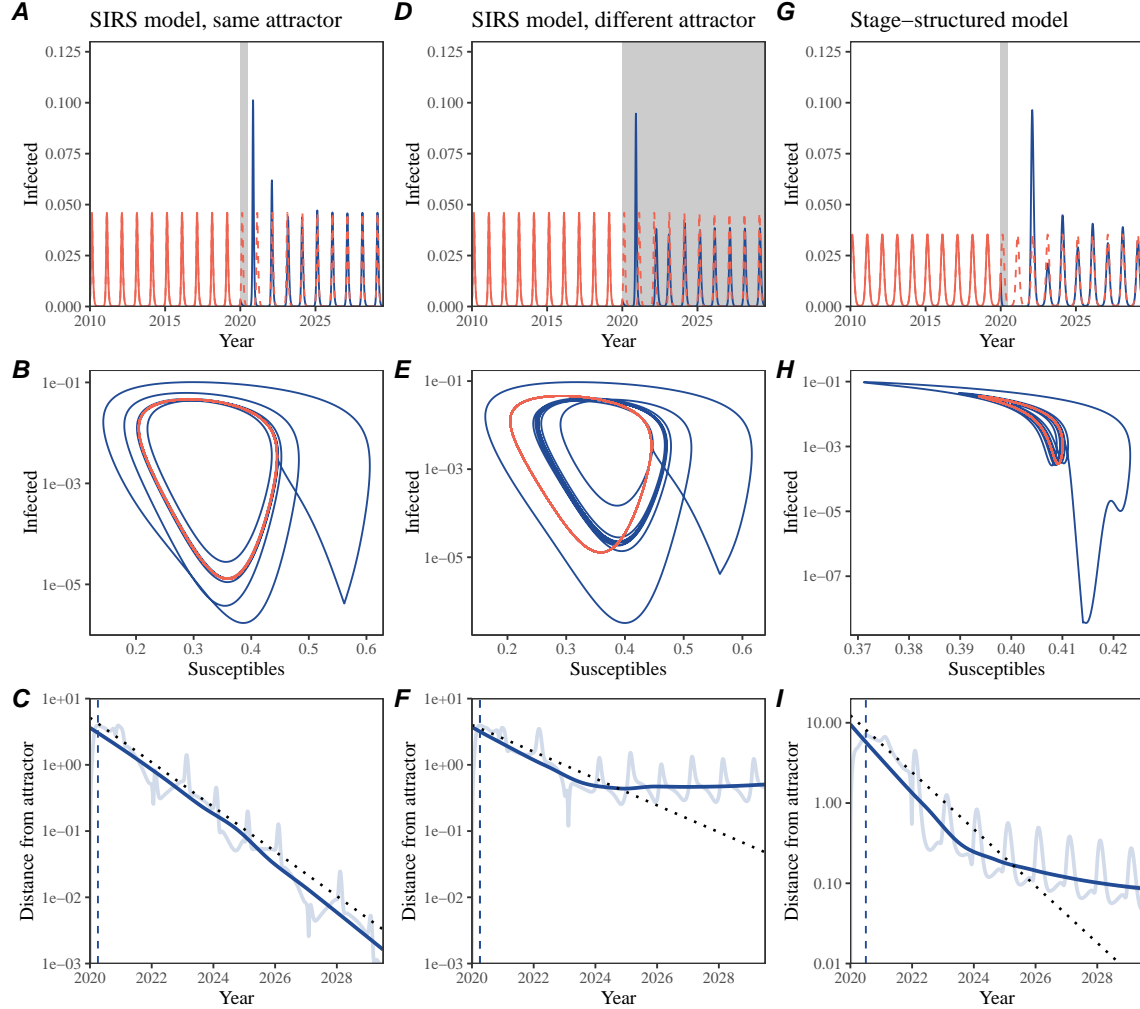


Figure 2: **Conceptual framework for measuring pathogen resilience following NPIs across different scenarios.** (A, D, G) Simulated epidemic trajectories across various models. Red and blue solid lines represent epidemic dynamics before and after interventions are introduced, respectively. Red dashed lines represent counterfactual epidemic dynamics in the absence of interventions. Gray regions indicate the duration of interventions. (B, E, H) Phase plane representation of the corresponding model. Red and blue solid lines represent epidemic trajectories on an SI phase plane before and after interventions are introduced, respectively. (C, F, I) Changes in logged distance from attractor over time. Transparent solid lines represent the logged distance from attractor. Non-transparent solid lines represent the locally estimated scatterplot smoothing (LOESS) fits to the logged distance from attractor. Dotted lines are superimposed as a comparison to have the same slope as the intrinsic resilience of the system.

120 ularly convenient because it does not require us to know the true underlying model.

121 As we show in Supplementary Materials, estimating the intrinsic resilience from fit-
 122 ting standard compartmental models can lead to biased estimates, especially under
 123 model misspecification ([SWP: *TODO*]). Second, resilience estimates allow us to
 124 make phenomenological predictions about the dynamics of a host-pathogen system
 125 following a perturbation: assuming that the distance from the attractor will decrease
 126 exponentially over time, we can obtain a ballpark estimate for when the system will
 127 reach an attractor. Finally, deviation from an exponential decrease in the distance
 128 from attractor can provide information about whether the system has reached an
 129 alternative attractor, or a ghost attractor, that is different from the original, pre-
 130 pandemic attractor. These alternative attractors may reflect continued perturbations
 131 from permanent changes in transmission patterns as well as changes in immune land-
 132 scapes.

133 [SWP: *Multi-strain system to be discussed in the supp after some more investi-*
 134 *gation.*]

135 Inferring pathogen resilience from real data

136 Based on these observations, we now set out to infer pathogen resilience from real
 137 data. Here, we briefly lay out our approach to estimating pathogen resilience from
 138 real data (Figure 3). We then test this approach against simulations and apply it to
 139 real data.

140 So far, we focused on simple examples that assume a constant transmission re-
 141 duction. However, in practice, the impact of NPIs on pathogen transmission is
 142 likely more complex (Figure 3A), reflecting introduction and relaxation of various
 143 intervention strategies. These complexities can lead to longer delays between the
 144 introduction of NPIs and pathogen re-emergence as well as temporal variation in
 145 outbreak sizes (Figure 3B): in this example, continued transmission reduction from
 146 NPIs limits the size of the first outbreak in 2021 following the emergence, allowing
 147 for a larger outbreak in 2022 when NPIs are further relaxed.

148 Previously, we relied on the dynamics of susceptible and infected hosts to compute
 149 the distance from attractor (Figure 2), but information on susceptible hosts are
 150 often not available in practice. In addition, uncertainties in case counts due to
 151 observation error as well as the possibility of complex, multiannual attractor adds
 152 challenges to measuring the distance from attractor. To address these challenges, we
 153 first reconstruct an empirical attractor by utilizing Takens' theorem, which states
 154 that an attractor of a nonlinear multidimensional system can be mapped onto a
 155 delayed embedding. Here, we use delayed copies of logged values of pre-pandemic
 156 cases $C(t)$ (Figure 3C) to reconstruct the attractor:

$$\langle \log(C(t) + 1), \log(C(t - \tau) + 1), \dots, \log(C(t - (M - 1)\tau) + 1) \rangle, \quad (1)$$

157 where the delay τ and embedding dimension M are determined based on autocor-
 158 relations and false nearest neighbors, respectively. We then apply the same delay

159 and embedding dimensions to the entire time series to determine the position on a
 160 multi-dimensional state space (Figure 3D), which allows us to measure the nearest
 161 neighbor distance between the current state of the system and the empirical attractor
 162 (Figure 3E). In principle, we can quantify how fast this distance decreases by fitting
 163 a linear regression on a log scale, where the slope of the linear regression corresponds
 164 to pathogen resilience.

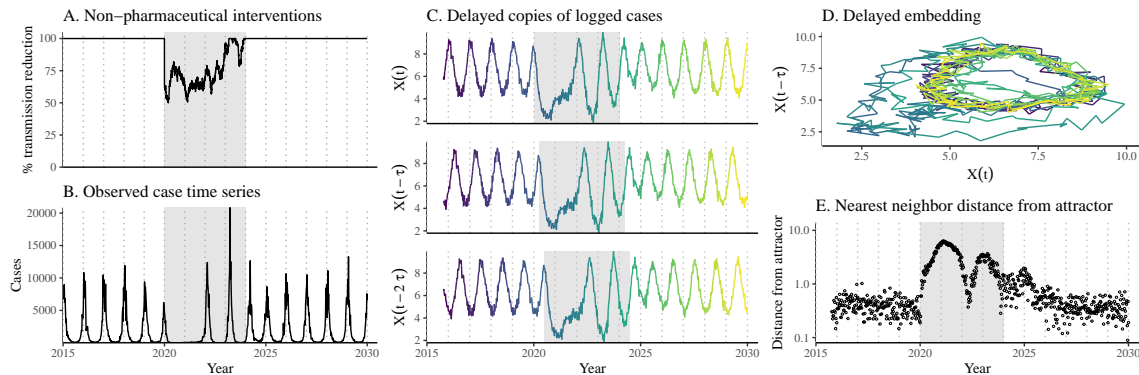


Figure 3: **A schematic diagram explaining how pathogen resilience can be inferred from real data.** (A) A realistic example of a synthetic NPI, represented by a relative reduction in transmission. (B) The impact of the synthetic NPI on epidemic dynamics simulated using a stochastic SIRS model. (C) Generating delayed copies of the logged time series allows us to obtain an embedding. (D) Two dimensional representation of an embedding. (E) Delayed embedding allows us to calculate the nearest neighbor distance from the empirical attractor, which is determined based on the pre-pandemic time series. This distance time series can be used to infer pathogen resilience by fitting a linear regression after choosing an appropriate window for regression.

165 Complex changes in the distance from attractor suggest that estimating pathogen
 166 resilience from linear regression will likely be sensitive to our choice of fitting windows
 167 for the regression. In Supplementary Materials, we explore an automated window
 168 selection criteria for linear regression and test it against randomized, stochastic sim-
 169 ulations across a wide range of realistic NPI shapes. We find that resilience estimates
 170 based on the automated window selection criteria are moderately correlated (0.54)
 171 with the intrinsic resilience of the post-NPI attractor. In contrast, a naive approach
 172 that uses the entire time series, starting from the peak distance, only gives a corre-
 173 lation of 0.21 and consistently underestimates the intrinsic resilience.

174 Now, we apply this approach to pathogen surveillance data presented in Figure
 175 1. For each time series, we apply Takens' theorem independently to reconstruct
 176 the empirical attractor and obtain the corresponding time series of distance from
 177 attractors ([SWP: Supp]). Then, we use the automated window selection criteria
 178 to fit a linear regression and estimate the empirical resilience for each pathogen
 179 in each country. For most respiratory pathogens, resilience estimates 0.5/year and

2/year (Figure 4A), with the exception of Rhinovirus in the US (0.066/year; 95% CI: 0.018/year–0.113/year) and Bocavirus in Korea (0.087/year; 95% CI: 0.023/year–0.151/year). Excluding these exceptions, the mean resilience of common respiratory pathogens is 0.974/year (95% CI: 0.784/year–1.16/year). As a reference, this is ≈ 7 times higher than the intrinsic resilience of pre-vaccination measles dynamics (≈ 0.13 /year). Finally, resilience estimates for norovirus appears to be comparable to the intrinsic resilience of measles: 0.119/year (95%CI: 0.004/year–0.233/year) for Korea and 0.385/year (95% CI: 0.167/year–0.603/year). A simple ANOVA shows that there are significant differences in resilience estimates across countries ($p < 0.036$) and pathogens ($p < 0.030$).

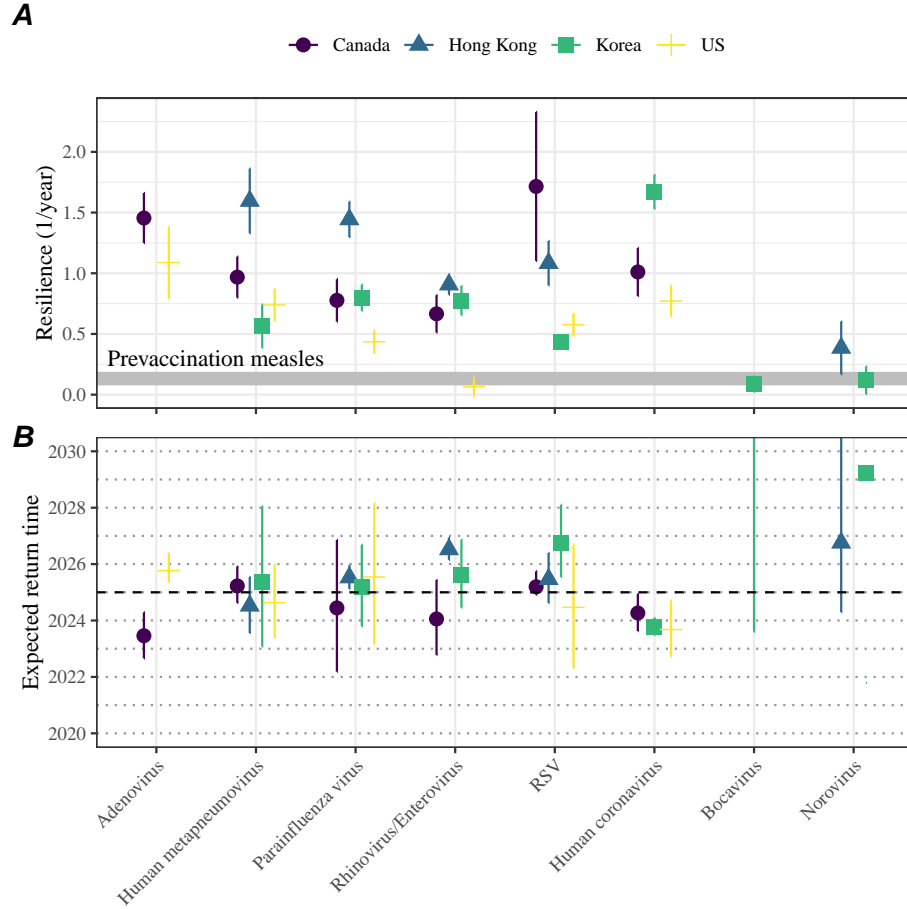


Figure 4: **Summary of resilience estimates.** (A) Estimated pathogen resilience. The gray horizontal line represents the intrinsic resilience of pre-vaccination measles dynamics. (B) Predicted timing of when each pathogen will return to their pre-pandemic cycles. The dashed line in panel B indicates the end of 2024 (current observation time). Error bars represent 95% confidence intervals.

Using resilience estimates, we now predict when each pathogen will return to

191 their original pre-pandemic cycles. Specifically, we extend our linear regression fits
 192 to distance-from-attractor time series and ask when the predicted regression line
 193 will cross a threshold value, which we set to a mean of pre-pandemic distances. We
 194 predict that a return to pre-pandemic cycles would be imminent for most pathogens
 195 (Figure 4B). In addition, we also predict that many pathogens should have already
 196 returned to their pre-pandemic dynamics by the end of 2024; but these predictions
 197 contradict some of the observed pathogen dynamics. For example, we predict that both
 198 human metapneumovirus and RSV in Korea should have returned to their attractors
 199 by now, but the magnitude and timing of recent epidemics are different from pre-
 200 pandemic patterns (Figure 1). These observations suggest the possibility that some
 201 common respiratory pathogens may have converged to different attractors.

202 **Susceptible host dynamics explain variation in pathogen** 203 **resilience**

204 So far, we focused on quantifying pathogen resilience from the observed patterns of
 205 pathogen re-emergence following COVID-19 interventions. But what factors deter-
 206 mine how resilient a host-pathogen system is? Here, we use a standard Susceptible-
 207 Infected-Recovered-Susceptible (SIRS) model to show that susceptible host dynamics
 208 are the key determinants of pathogen resilience. To do so, we vary the basic reproduc-
 209 tion number \mathcal{R}_0 , which represents the average number of secondary infections caused
 210 by a newly infected individual in a fully susceptible population, and the duration of
 211 immunity and compute intrinsic resilience for each parameter.

212 We find that pathogen resilience increases with higher \mathcal{R}_0 and shorter duration
 213 of immunity (Figure 4A). These variations can be understood in terms of the suscep-
 214 tible host dynamics, where faster per-capita susceptible replenishment rate causes
 215 the system to be more resilient (Figure 4B). This rate can be expressed as a ra-
 216 tio between absolute rate at which new susceptibles enter the population and the
 217 equilibrium number of susceptible individuals in the population, \bar{S} . Therefore, both
 218 higher \mathcal{R}_0 and shorter duration of immunity can drive faster per-capita susceptible
 219 replenishment rate (Figure 4B), especially because higher \mathcal{R}_0 leads to lower \bar{S} .

220 Finally, we can now rank different pathogens based on their empirical resilience.
 221 For simplicity, we take the average of resilience estimates across countries to de-
 222 termine the ranking, which shows that influenza B is least resilient (Figure 4A).
 223 This observation is consistent with the extinction of influenza B/Yamagata, which
 224 indicates the persistence of a pathogen should be associated with its resilience. Sim-
 225 ilarities in resilience ranking between RSV and Human metapneumovirus is also
 226 interesting, given the apparent coupling of their dynamics through cross immunity.
 227 These rankings further allow us to map each pathogen onto a set of parameters that
 228 are consistent with its empirical resilience (Figure 4A) and obtain a plausible range
 229 of susceptible replenishment rates for each pathogen (Figure 4B).

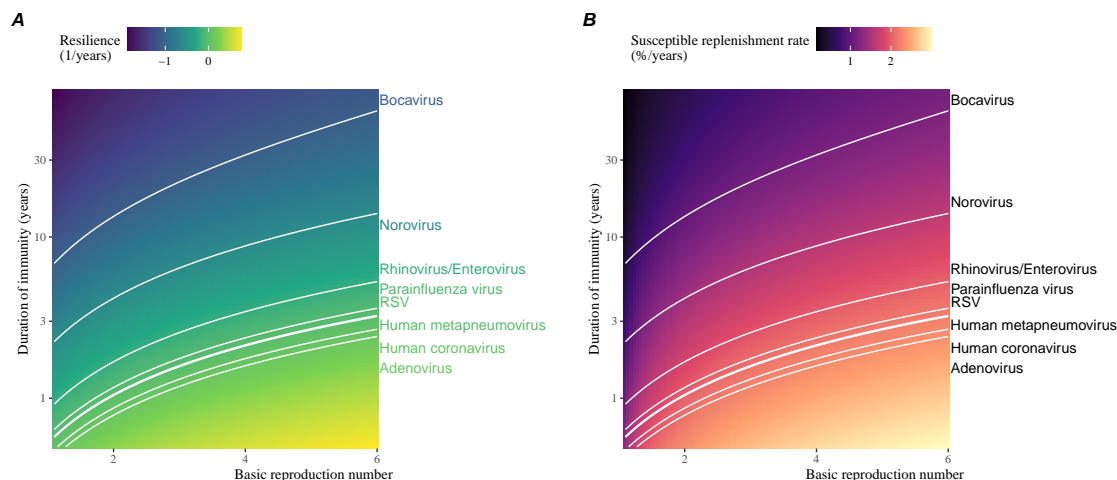


Figure 5: **Linking pathogen resilience to epidemiological parameters and susceptible host dynamics.** (A) The heat map represents intrinsic resilience as a function of the basic reproduction number \mathcal{R}_0 and the duration of immunity. (B) The heat map represents per-capita susceptible replenishment rate as a function of the basic reproduction number \mathcal{R}_0 and the duration of immunity. The standard SIRS model is used to compute intrinsic resilience and per-capita susceptible replenishment rate. Lines correspond to a set of parameters that are consistent with mean resilience estimates for each pathogen. Pathogens are ranked based on their mean resilience estimates, averaged across different countries.

Discussion

The COVID-19 interventions have caused major disruptions to circulation patterns of both respiratory and non-respiratory pathogens, adding challenges to predicting their future dynamics. On the other hand, these interventions offer large-scale natural experiments for understanding how different pathogens respond to perturbations. In this study, we show that pathogen re-emergence patterns following COVID-19 interventions can be characterized through the lens of ecological resilience. Traditionally, ecological resilience measures how fast a system returns to a reference state following a perturbation. In the context of respiratory pathogens, resilience measures how fast epidemics return to their endemic cycles after interventions are lifted.

We use an attractor reconstruction approach to quantify how distance from attractor changes over time for each pathogen. By fitting a linear regression to log distances, we can estimate pathogen resilience and further predict when each pathogen will return to their endemic cycles. Consistency in resilience estimates across countries is particularly surprising given that each country imposed different intervention measures; this consistency provides robustness to our estimates. The ability to predict future epidemic patterns from resilience estimates also offers a new paradigm for epidemic forecasting. While this approach cannot predict the exact timing of out-

breaks or epidemic patterns, it is nonetheless useful for predicting when epidemics will settle down to regular cycles after a large perturbation, such as COVID-19 interventions.

Our analyses suggest a possibility that several pathogens may have converged to different endemic cycles compared to their pre-pandemic epidemic patterns. Key examples include human metapneumovirus, RSV, and bocavirus in Korea as well as RSV in Hong Kong. These changes may reflect permanent changes in behavior since 2020 or a shift in population-level immunity. However, it seems unlikely that permanent changes in behavior would only affect a few pathogens and not others. A shift in population-level immunity is plausible, as the emergence of SARS-CoV-2 and extinction of influenza B/Yamagata likely caused major changes in immune landscapes; however, we currently do not know how immunity, or lack thereof, from these pathogens would affect infection from other pathogens. Future studies should use detailed mechanistic models, coupled with behavioral and immunological data, to test these hypotheses and better understand post-pandemic dynamics of endemic pathogens.

We show that susceptible host dynamics shape pathogen resilience, where faster replenishment of the susceptible population causes the pathogen to be more resilient. For simplicity, we focus on waning immunity and birth as a main driver of the susceptible host dynamics but other mechanisms can also contribute to the replenishment of the susceptible population. In particular, pathogen evolution, especially the emergence of antigenically novel strains, can cause effective waning of immunity in the population; therefore, we tentatively hypothesize that faster rates of antigenic evolution can also cause a pathogen to be more resilient. Future studies should explore the relationship between the rate of evolution and resilience for antigenically evolving pathogens.

Quantifying pathogen resilience also offers novel approaches to validating epidemiological models. So far, the majority of model validation in epidemiology is based on the ability of a model to reproduce the observed epidemic dynamics and to predict future dynamics. However, there can be plethora of models that meet these criteria. For example, two major RSV models have been proposed so far to explain biennial epidemic patterns: (1) a stage- and age-structured model that allows for disease severity to vary with number of past infections and age of infection and (2) a pathogen-interaction model that accounts for cross immunity between RSV and human metapneumovirus. Since both models can accurately reproduce the observed epidemic patterns, standard criteria for model validation do not allow us to distinguish between these two models. Instead, we can measure the empirical resilience of each model by simulating various perturbations and compare them to estimates of empirical resilience from data, using COVID-19 interventions as an opportunity. Future studies should further investigate using pathogen resilience for validating epidemic models.

There are several limitations to our work. In particular, our estimates of pathogen resilience and the associated ranking are necessarily crude. **[SWP: *Limitation TBD.*]**

291 Nonetheless, our study illustrates the utility of quantifying pathogen resilience for
292 understanding how different pathogens respond to perturbations.
293 [SWP: Conclusion paragraph TBD.]

294 Materials and Methods

295 Data

296 We gathered time series on respiratory infections from four different countries: Canada,
297 Hong Kong, Korea, and United States (US). As a reference, we also included time
298 series data on norovirus infections for available countries—in contrast to respiratory
299 pathogens, we expect gastrointestinal viruses, such as norovirus, to be less affected
300 by COVID-19 intervention measures.

301 Weekly time series of respiratory infection cases in Canada come from the Res-
302 piratory Virus Detection Surveillance System, which collect data from select labo-
303 ratories across Canada. We extracted the data from [https://www.canada.ca/en/
304 public-health/services/surveillance/respiratory-virus-detections-canada.
305 html](https://www.canada.ca/en/public-health/services/surveillance/respiratory-virus-detections-canada.html).

306 Weekly time series of respiratory infection cases in Hong Kong came from the
307 Centre for Health Protection, Department of Health. We extracted the data from
308 <https://www.chp.gov.hk/en/statistics/data/10/641/642/2274.html>.

309 Weekly time series of respiratory infection cases in Korea came from Korea Dis-
310 ease Control and Prevention Agency. We extracted the data from [https://dportal.
311 kdca.go.kr/pot/is/st/ari.do](https://dportal.kdca.go.kr/pot/is/st/ari.do).

312 Finally, weekly time series of respiratory infection cases in the US comes from
313 the National Respiratory and Enteric Virus Surveillance System.

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