The goal here is to devise an algorithm creating the optimal schedule for transportation of a group of cows from other to the home planet of some alien species. Two algorithms are considered, including a greedy algorithm and a brute force solution. These solutions are compared.

To begin with, we have to read our data (initally stored in a text file) into the program. This is accomplished by load\_cows below

## Problem 1

```
In [2]:
         def load cows(filename):
             Read the contents of the given file. Assumes the file contents contain
             data in the form of comma-separated cow name, weight pairs, and return a
             dictionary containing cow names as keys and corresponding weights as values.
             Parameters:
             filename - the name of the data file as a string
             a dictionary of cow name (string), weight (int) pairs
             cow dict = {}
             file = open(filename, 'r')
             #For each line, create a list object [a,b] where a is cow name and b is the
             for line in file :
                 newline = line.split(',')
                 name = newline[0]
                 weight = int(newline[1])
                 #assigns each name as the key to a dictionary entry whose value is the d
                 cow dict[name] = weight
             return cow dict
```

The output of load\_cows is a dictionary, whose keys are the cow names and values are the weight of the cows (in come unspecified unit).

The module operator is imported to sort by values in the input dictionary.

# Problem 2:

```
import operator
def greedy_cow_transport(cows,limit=10):
    Uses a greedy heuristic to determine an allocation of cows that attempts to minimize the number of spaceship trips needed to transport all the cows. The returned allocation of cows may or may not be optimal.
    The greedy heuristic should follow the following method:
    1. As long as the current trip can fit another cow, add the largest cow that to the trip
    2. Once the trip is full, begin a new trip to transport the remaining cows
```

```
Does not mutate the given dictionary of cows.
Parameters:
cows - a dictionary of name (string), weight (int) pairs
limit - weight limit of the spaceship (an int)
Returns:
A list of lists, with each inner list containing the names of cows
transported on a particular trip and the overall list containing all the
0.00
new list = sorted(cows.items(), key=operator.itemgetter(1), reverse = True)
print(new list)
result = []
totalWeight = 0
while len(new list) > 0 :
    trip = []
    fake list = new_list[:]
    for pair in new list :
        if (totalWeight + pair[1] <= limit ) :</pre>
            trip.append(pair[0])
            totalWeight+= pair[1]
            fake list.remove(pair)
    result.append(trip)
    new list = fake list
    totalWeight = 0
return result
```

This program has a few features that are worth commenting on. Implementation-wise, new\_list is a sorted list of tuples (name, weight), which is generated from the inputed dictionary *cows*. The output *result* is a list of lists, each output of *result* being a list representing one trip.

Below the algorithm is tested on two inputs.

First, the dicitonary objects are generated from the input files using load\_cow.

```
In [4]: cows_1 = load_cows('ps1_cow_data.txt')
    cows_2 = load_cows('ps1_cow_data_2.txt')
```

Next, we run the greedy algorithm on each input:

```
In [5]:
    res_1 = greedy_cow_transport(cows_1)
    print(cows_1, ': the following trip is (greedy) optimal: ', res_1)
        [('Betsy', 9), ('Henrietta', 9), ('Herman', 7), ('Oreo', 6), ('Millie', 5), ('Maggie', 3), ('Moo Moo', 3), ('Milkshake', 2), ('Lola', 2), ('Florence', 2)]
        {'Maggie': 3, 'Herman': 7, 'Betsy': 9, 'Oreo': 6, 'Moo Moo': 3, 'Milkshake': 2, 'Millie': 5, 'Lola': 2, 'Florence': 2, 'Henrietta': 9} : the following trip is (greedy) optimal: [['Betsy'], ['Henrietta'], ['Herman', 'Maggie'], ['Oreo', 'Mo o Moo'], ['Millie', 'Milkshake', 'Lola'], ['Florence']]

Out[5]: 6

In [6]:
    res_2 = greedy_cow_transport(cows_2)
    print(cows_2, ': the following trip is (greedy) optimal: ', res_2)
```

```
len(res_2)

[('Lotus', 10), ('Horns', 9), ('Dottie', 6), ('Betsy', 5), ('Milkshake', 4), ('Miss Moo-dy', 3), ('Rose', 3), ('Miss Bella', 2)]
{'Miss Moo-dy': 3, 'Milkshake': 4, 'Lotus': 10, 'Miss Bella': 2, 'Horns': 9, 'Betsy': 5, 'Rose': 3, 'Dottie': 6}: the following trip is (greedy) optimal:
[['Lotus'], ['Horns'], ['Dottie', 'Milkshake'], ['Betsy', 'Miss Moo-dy', 'Miss Bella'], ['Rose']]

Out[6]: 5
```

#### Problem 3

Now we wish to greate a brute force solution to the transport problem, one where all possible sequences of trips, or results, are considered. Since the optimal result is sure to be among the set of possible results, examining each result will find us the optimal solution.

Just like the greedy program, this will take a dictionary as an input, again with a weight limit (default value of 2).

```
In [7]:
         import ps1 partition
         def brute force cow transport(cows,limit=10):
             Finds the allocation of cows that minimizes the number of spaceship trips
             via brute force. The brute force algorithm should follow the following meth
             1. Enumerate all possible ways that the cows can be divided into separate to
                 Use the given get partitions function in psl partition.py to help you!
             2. Select the allocation that minimizes the number of trips without making a
                 that does not obey the weight limitation
             Does not mutate the given dictionary of cows.
             Parameters:
             cows - a dictionary of name (string), weight (int) pairs
             limit - weight limit of the spaceship (an int)
             Returns:
             A list of lists, with each inner list containing the names of cows
             transported on a particular trip and the overall list containing all the
             trips
             def goodWeight(result, my dict, limit):
                 for trip in result :
                     weight = 0
                     for cow in trip:
                         if weight + my_dict[cow] <= limit :</pre>
                             weight += my dict[cow]
                         else:
                             return False
                 return True
             all_results = psl_partition.get_partitions(cows)
             best result = None
             max length = len(cows)
```

for result in all results:

```
best result = result
                         max length = len(result)
                return best_result
In [8]:
           optimal = brute_force_cow_transport(cows_1)
           print(cows 1, ': the optimal solution is ', optimal )
           len(optimal)
          {'Maggie': 3, 'Herman': 7, 'Betsy': 9, 'Oreo': 6, 'Moo Moo': 3, 'Milkshake': 2, 'Millie': 5, 'Lola': 2, 'Florence': 2, 'Henrietta': 9} : the optimal solution is
          [['Henrietta'], ['Florence', 'Lola', 'Oreo'], ['Moo Moo', 'Herman'], ['Milkshak
          e', 'Millie', 'Maggie'], ['Betsy']]
Out[8]: 5
In [9]:
           cows 3 = {'Jesse': 6, 'Maybel': 3, 'Callie': 2, 'Maggie': 5}
           print(greedy cow transport(cows 3))
           print(brute force cow transport(cows 3))
          [('Jesse', 6), ('Maggie', 5), ('Maybel', 3), ('Callie', 2)]
          [['Jesse', 'Maybel'], ['Maggie', 'Callie']]
[['Callie', 'Maggie', 'Maybel'], ['Jesse']]
```

if goodWeight(result, cows, limit) and len(result) < max length :</pre>

### Problem 4

We now wish to compare the two algorithms.

```
In [10]:
          import time
          def compare_cow_transport_algorithms():
              Using the data from psl_cow_data.txt and the specified weight limit, run you
              greedy cow transport and brute force cow transport functions here. Use the
              default weight limits of 10 for both greedy cow transport and
              brute force cow transport.
              Print out the number of trips returned by each method, and how long each
              method takes to run in seconds.
              Returns:
              Does not return anything.
              cows = load_cows('ps1_cow_data.txt')
              #greedy algorithm
              #Time that program starts running.
              start = time.time()
              #run greedy algorithm
              result_greedy = greedy_cow_transport(cows)
              #time that program finishes running, and difference.
              finish = time.time()
              time greedy = finish - start
              num_greedy = len(result_greedy)
              print('The greedy algorithm requires a minimum of ', num greedy, 'trips.')
              print('It took ', time_greedy, ' seconds to run')
              #Time that program starts running.
```

```
start = time.time()
result_brute = brute_force_cow_transport(cows)
finish = time.time()
time_brute = finish - start
num_brute = len(result_brute)
print('The brute algorithm requires a minimum of ', num_brute, 'trips.')
print('It took ', time_brute, ' seconds to run')
compare_cow_transport_algorithms()
```

```
[('Betsy', 9), ('Henrietta', 9), ('Herman', 7), ('Oreo', 6), ('Millie', 5), ('Maggie', 3), ('Moo Moo', 3), ('Milkshake', 2), ('Lola', 2), ('Florence', 2)] The greedy algorithm requires a minimum of 6 trips. It took 0.00014972686767578125 seconds to run The brute algorithm requires a minimum of 5 trips. It took 0.6065704822540283 seconds to run
```

## Write up

We see that, although the greedy algorithm runs considerably faster than the brute force algorithm (several orders of magnitude faster), it does not return an optimal solution.

Why is this? It's clear why the brute force algorithm works. It considers every possible solution (gen\_paritions effectively generating the power set of the set of cows, and hence all possible sequences of trips), so it must find the best solution. The downside is that this algorithm has an exponential order of growth, and in fact takes considerably longer to run.

Now why doesn't the greedy algorithm return the optimal solution? To see why let's analyze an example. We'll consider the set of cows below:

```
In [11]:
    print(sorted(cows_1.items(), key=operator.itemgetter(1), reverse = True))
    optimal_greedy = greedy_cow_transport(cows_1)
    print('Greedy solution: the optimal result is', optimal_greedy )
    len(optimal_greedy)

[('Betsy', 9), ('Henrietta', 9), ('Herman', 7), ('Oreo', 6), ('Millie', 5), ('Maggie', 3), ('Moo Moo', 3), ('Milkshake', 2), ('Lola', 2), ('Florence', 2)]
    [('Betsy', 9), ('Henrietta', 9), ('Herman', 7), ('Oreo', 6), ('Millie', 5), ('Maggie', 3), ('Moo Moo', 3), ('Milkshake', 2), ('Lola', 2), ('Florence', 2)]
    Greedy solution: the optimal result is [['Betsy'], ['Henrietta'], ['Herman', 'Maggie'], ['Oreo', 'Moo Moo'], ['Millie', 'Milkshake', 'Lola'], ['Florence']]

Out[11]: 6
```

In this set of cows, Betsy and Henrietta are tied for the biggest. In this case the algorithm selects the cow that comes first alphabetically (Betsy) and sends it out on a trip by itself. Now it selects the other biggest cow (Henrietta) and does the same. In general, the algorithm is designed to *always pick the biggest available cow*.

Now' let's examine the solution returned by the brute force algorithm, which (recall) is guaranteed to be the optimal solution:

```
optimal_brute = brute_force_cow_transport(cows_1)
print('Brute force solution: the optimal result is', optimal_brute)
len(optimal_brute)
```

```
Brute force solution: the optimal result is [['Henrietta'], ['Florence', 'Lola', 'Oreo'], ['Moo Moo', 'Herman'], ['Milkshake', 'Millie', 'Maggie'], ['Betsy']]
Out[12]: 5
```

Betsy and Henrietta are still sent on their own. Similarly, Herman is still going on a trip with a cow of weight 3 (in this case Moo Moo). In other words, the three heaviest cows behave similarly. The difference comes with Oreo. In the greedy algorithm, Oreo was forced to go on a trip with on of the cows of weight 3 (Moo Moo or Maggie), because the greedy algorithm could only optimize locally. It had to pick the next heaviest cow that satisfied the weight constraint. Then Millie had to shack up with Lola, leavin