Name:	
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Student Workbook



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The Math Inside Video Games

- Video games are all about *change*: How fast is this character moving? How does the score change if the player collects a coin? Where on the screen should we draw a castle?
- We can break down a game into parts, and figure out which parts change and which ones stay the same. For example:
 - Computers use coordinates to position a character on the screen. These coordinates specify how far from the left (x-coordinate) and the bottom (y-coordinate) a character should be. Negative values can be used to "hide" a character, by positioning them somewhere off the screen.
 - When a character moves, those coordinates change by some amount. When the score goes up or down, it *also* changes by some amount.
- From the computer's point of view, the whole game is just a bunch of numbers that are changing according to some equations. We might not be able to see those equations, but we can definitely see the effect they have when a character jumps on a mushroom, flies on a dragon, or mines for rocks!
- Modern video games are *incredibly* complex, costing millions of dollars and several years to make, and relying on hundreds of programmers and digital artists to build them. But building even a simple game can give us a good idea of how the complex ones work!

Notice and Wonder

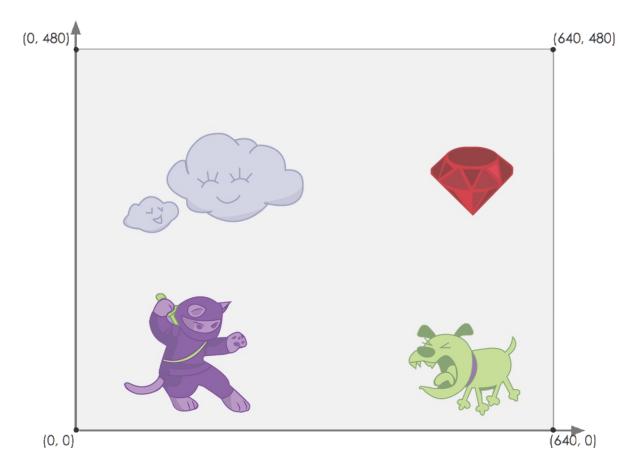
Write down what you notice and wonder about the Ninja Cat game screenshot.

"Notices" should be statements, not questions. What stood out to you? What do you remember?

What do you Notice?	What do you Wonder?

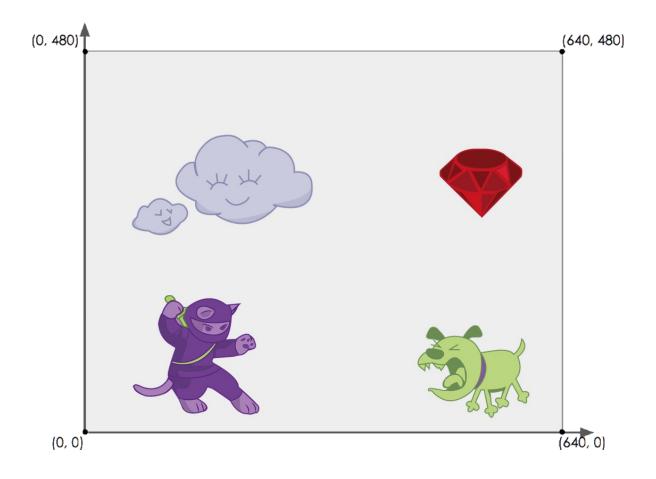
Reverse Engineer a Video Game

What is changing in the game? The first example is filled in for you.



Thing in the Game	What Changes About It?	More Specifically?
Dog	Position	x-coordinate

Estimating Coordinates



Brainstorm Your Own Game

Created by:	
Background	
Our game takes place: In space? The desert? A mall?	
inspace: The desert: A mail:	
Player	
The Player is a	<u>—</u>
The Player moves only up and down.	
Target	
Your Player GAINS points when they hit The Target.	
The Target is a	
The Target moves only to the left or right.	
Danger	
Danger	
Your Player LOSES points when they hit The Danger.	
The Danger is a	
The Danger moves only to the left or right.	
Artwork/Sketches/Proof of Concept	
Draw a rectangle representing your game screen, and label the bottom-left corner	as the coordinate (0,0). Then label the
other four corners. Then, in the rectangle, sketch a picture of your game!	

Order of Operations

Order of Operations is incredibly important when programming. To help us organize our math into something we can trust, we can $\emph{diagram}$ a math expression using the $\emph{Circles}$ of Evaluation . For example, the expression $1-4\div 10~\times~7$ can be diagrammed as shown below.



To convert a **Circle of Evaluation** into code, we walk through the circle from outside-in, moving left-to-right. We type an open parenthesis when we *start* a circle, and a close parenthesis when we *end* one. Once we're in a circle, we write whatever is on the left of the circle, then the **operation** at the top, and then whatever is on the right. The circle above, for example, would be programmed as ((1 - 4) / (10 * 7)).

Completing Circles of Evaluation from Arithmetic Expressions

For each expression on the left, finish the Circle of Evaluation on the right by filling in the blanks.

	Arithmetic Expression	Circle of Evaluation Circle of Evaluation
1	$4+2-\frac{10}{5}$	4 2 5
2	$7-1+5 \; imes \; 8$	+
3	$\frac{-15}{5+-8}$	/ + 5
4	(4+(9-8)) imes 5	* 4 9 8
5	$6 \times 4 + \frac{96}{5}$	4
*	$rac{20}{6+4} - rac{5 imes 9}{-12-3}$	20 + 4

Matching Circles of Evaluation and Arithmetic Expressions

Draw a line from each Circle of Evaluation on the left to the corresponding arithmetic expression on the right.

Circle of Evaluation

Arithmetic Expression



1

A
$$1 \div (1 \times 1)$$



2

B
$$(1+1)-1$$

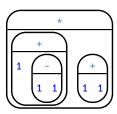


3

c
$$(1 \times 1) \div 1$$



$$\mathsf{D} \qquad \ \, \left(1+(1-1)\right) \, \times \, \left(1+1\right) \\$$



5

E
$$(1-1) \times (1+1)$$

Translate Arithmetic to Circles of Evaluation & Code (Intro)

Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

	Arithmetic	Circle of Evaluation	Code
1	(3 imes 7) - (1+2)		
2	3-(1+2)		
3	$3-(1+(5 \ imes 6))$		
4	$(1+(5 \ imes 6))-3$		

Completing Partial Code from Circles of Evaluation

For each Circle of Evaluation on the left, finish the Code on the right by filling in the blanks.

	Circle of Evaluation	Code
1	+ 16	(+ (6 *))
2	+ 25 13 (2 4)	((+ 13) (4))
3	* + 28 10 4	(() + 4))
4	* 13 / 7 + 2 -4	(13 (7 (24)))
5	+ - - - - - - - - - - - - -	(((8 1) 3) (5 3))
6	/ + 7 9 x 2 4	((+) / (*))

Matching Circles of Evaluation & Code

Draw a line from each Circle of Evaluation on the left to the corresponding Code on the right.

Circle of Evaluation

Code



1

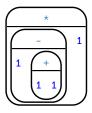
((1 - (1 + 1)) * 1)



2

В

((1-1)*(1+1))



3

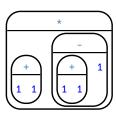
C ((1 + 1) * ((1 + 1) - 1))



4

D

((1 + 1) - 1)



5

E

((1 - 1) + 1)

Translate Arithmetic to Circles of Evaluation & Code 2

Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

	Arithmetic	Circle of Evaluation	Code
1	6 imes 8 + (7 - 23)		
2	$18 \div 2 + 24 imes 4 - 2$		
3	$22-7\div 3+2$		
4	$24 \div 4 \hspace{0.1cm} \times \hspace{0.1cm} 2 - 6 + 20 \hspace{0.1cm} \times \hspace{0.1cm} 2$		

Arithmetic Expressions to Circles of Evaluation & Code - Challenge

Translate each of the arithmetic expressions below into Circles of Evaluation, then translate them to Code.

Code			
Circle of Evaluation			
Arithmetic	$\frac{16+3^2}{\sqrt{49}-2}$	45-9 imes (3+(2-4))-7	$50 \div 5 imes 2 - ((3+4) imes 2 - 5)$
	7	7	м

Introduction to Programming

The **Editor** is a software program we use to write Code. Our Editor allows us to experiment with Code on the right-hand side, in the **Interactions Area**. For Code that we want to *keep*, we can put it on the left-hand side in the **Definitions Area**. Clicking the "Run" button causes the computer to re-read everything in the Definitions Area and erase anything that was typed into the Interactions Area.

Data Types

Programming languages involve different data types, such as Numbers, Strings, Booleans, and even Images.

- Numbers are values like 1, 0.4, 1/3, and -8261.003.
 - Numbers are usually used for quantitative data and other values are usually used as categorical data.
 - o In Pyret, any decimal must start with a 0. For example, 0.22 is valid, but .22 is not.
- Strings are values like "Emma", "Rosanna", "Jen and Ed", or even "08/28/1980".
 - All strings *must* be surrounded in quotation marks.
- Booleans are either true or false.

All values evaluate to themselves. The program 42 will evaluate to 42, the String "Hello" will evaluate to "Hello", and the Boolean false will evaluate to false.

Operators

Operators (like +, -, *, <, etc.) work the same way in Pyret that they do in math.

- Operators are written between values, for example: 4 + 2.
- In Pyret, operators must always have a space around them. 4 + 2 is valid, but 4+2 is not.
- If an expression has different operators, parentheses must be used to show order of operations. 4 + 2 + 6 and 4 + (2 * 6) are valid, but 4 + 2 * 6 is not.

Applying Functions

Applying functions works much the way it does in math. Every function has a name, takes some inputs, and produces some output. The function name is written first, followed by a list of *arguments* in parentheses.

- In math this could look like f(5) or g(10,4).
- In Pyret, these examples would be written as f(5) and g(10, 4).
- Applying a function to make images would look like star(50, "solid", "red").
- There are many other functions, for example num-sqr, num-sqrt, triangle, square, string-repeat, etc.

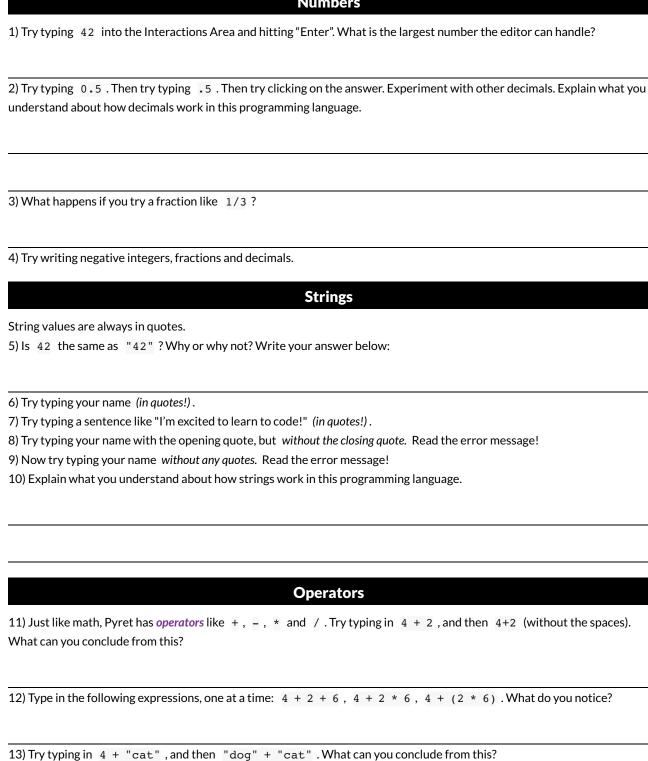
Functions have contracts, which help explain how a function should be used. Every contract has three parts:

- The Name of the function literally, what it's called.
- The Domain of the function what types of values the function consumes, and in what order.
- The Range of the function what type of value the function produces.

Numbers and Strings

Make sure you've loaded the code.pyret.org, (CPO) editor, clicked "Run", and are working in the Interactions Area.





Booleans

Boolean-producing expressions are yes-or-no questions and will always evaluate to either true ("yes") or false ("no"). What will each of the expressions below evaluate to? Write down your prediction in the blanks provided and then type the code into the interactions area to see what it returns.

	Prediction:	Computer Returns:		Prediction:	Computer Returns:
1) 3 <= 4			2)"a" > "b"		
3) 3 == 2			4)"a" < "b"		
5) 2 < 4			6)"a" == "b"		
7) 5 >= 5			8)"a" <> "a"		
9) 4 >= 6			10)"a" >= "a"		
11) 3 <> 3			12)"a" <> "b"		
13) In your own words	, describe what	< does.			
14) In your own words	, describe what	>= does.			
15) In your own words	, describe what	<> does.			
			Prediction:	Compute	r Returns:
16) string-contain	ins("catnap'	', "cat")			
17) string-contain	ins("cat", '	'catnap")			
18) How many Numb	ers are there in	the entire uni	verse?		
19) How many String	s are there in th	ne entire unive	rse?		
20) How many Image	es are there in th	ne entire unive	rse?		
21) How many Boole	ans are there in	the entire uni	verse?		

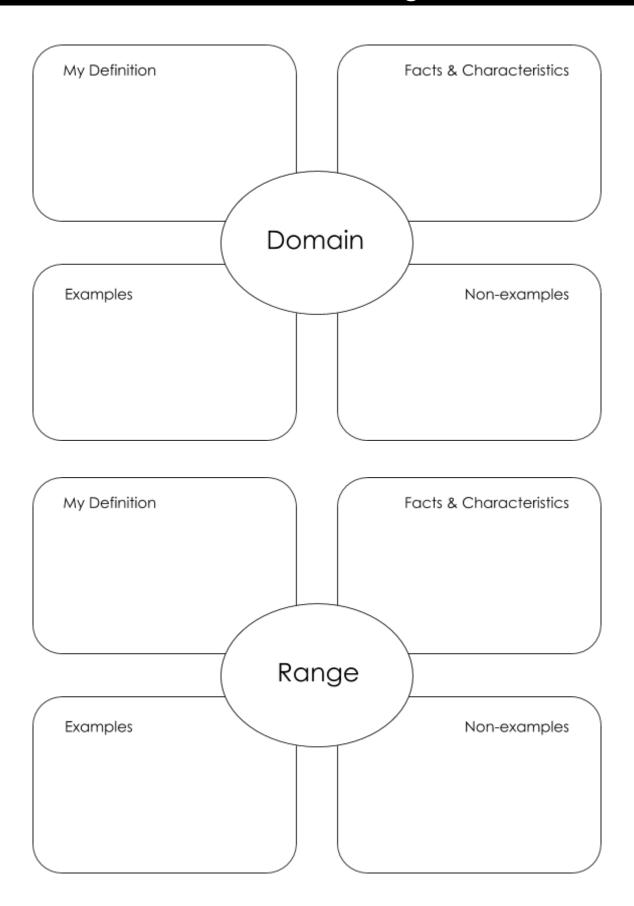
Applying Functions

Type this line of code into the interactions area and hit "Enter":

triangle(50, "solid", "red")

1	What is the name of this function?
2	What did the expression evaluate to?
3	How many arguments does triangle expect?
4	What data type does the triangle function produce? (Numbers? Strings? Booleans?)
	Catching Bugs
	following lines of code are all BUGGY! Read the code and the error messages to identify the mistake. riangle(20, "solid" "red") Pyret didn't understand your program around triangle(20, "solid" "red")
Can	you spot the mistake?
6) t	This application expression errored: triangle (20, "solid") 2 arguments were passed to the operator. The operator evaluated to a function accepting 3 parameters. An application expression expects the number of parameters and arguments to be the same.
Can	you spot the mistake?
7) t	riangle (20, 10, "solid", "red") This <u>application expression</u> errored: triangle (20, 10, "solid", "red")` <u>4 arguments</u> were passed to the <u>operator</u> . The <u>operator</u> evaluated to a function accepting 3 parameters. An <u>application expression</u> expects the number of parameters and <u>arguments</u> to be the same.
Can	you spot the mistake?
8) t	riangle (20, "solid", "red") Pyret thinks this code is probably a function call: triangle (20, "solid", "red") Function calls must not have space between the function expression and the arguments.
Can	you spot the mistake?

Domain and Range



Practicing Contracts: Domain & Range

Consider	the fol	lowing	contract
COMBIGCI			continue

is-beach-weather :: Number, String -> Boolean 1) What is the **Name** of this function? 2) How many arguments are in this function's **Domain**? 3) What is the **type** of this function's **first argument**? 4) What is the **type** of this function's **second argument**? 5) What is the **Range** of this function? 6) Circle the expression below that shows the correct application of this function, based on its contract. A. is-beach-weather(70, 90) B. is-beach-weather(80, 100, "cloudy") C. is-beach-weather("sunny", 90) D. is-beach-weather(90, "stormy weather") Consider the following contract: cylinder :: Number, Number, String -> Image 7) What is the **Name** of this function? 8) How may arguments are in this function's **Domain**? 9) What is the **type** of this function's **first argument**? 10) What is the **type** of this function's **second argument**? 11) What is the **type** of this function's **third argument**? 12) What is the **Range** of this function? 13) Circle the expression below that shows the correct application of this function, based on its contract.

- B. cylinder(30, "green")
- C. cylinder(10, 25, "blue")
- D. cylinder(14, "orange", 25)

Matching Expressions and Contracts

Match the contract (left) with the expression described by the function being used (right).

Contract		Expression
<pre># make-id :: String, Number -> Image</pre>	1	A make-id("Savannah", "Lopez", 32)
<pre># make-id :: String, Number, String -> Image</pre>	2	B make-id("Pilar", 17)
<pre># make-id :: String -> Image</pre>	3	C make-id("Akemi", 39, "red")
<pre># make-id :: String, String -> Image</pre>	4	D make-id("Raïssa", "McCracken")
<pre># make-id :: String, String, Number -> Image</pre>	5	<pre>E make-id("von Einsiedel")</pre>

Contract		Expression
# is-capital :: String, String -> Boolean	6	A show-pop("Juneau", "AK", 31848)
# is-capital :: String, String, String -> Boolean	7	B show-pop("San Juan", 395426)
<pre># show-pop :: String, Number -> Image</pre>	8	C is-capital("Accra", "Ghana")
<pre># show-pop :: String, String, Number -> Image</pre>	9	D show-pop(3751351, "Oklahoma")
# show-pop :: Number, String -> Number	10	E is-capital("Albany", "NY", "USA")

Using Contracts

Use the contracts to write expressions to generate images similar to those pictured.

ellipse :: Number, Number, String, String -> Image

What changes with the first number?	
What about the shape changes with the second Number?	
Write an expression using ellipse to produce a circle.	

regular-polygon :: Number, Number, String, String -> Image

What changes with the first Number?	
What about the shape changes with the second Number?	
Use regular-polygon to write an expression for a square!	
How would you describe a regular polygon to a friend?	

Using Contracts (continued)

Use the contracts to write expressions to generate images similar to those pictured.

rhombus :: Number, Number, String, String -> Image

Write an expression for a square (rotated) using rhombus!	
What variable changes with the first Number?	
What variable changes with the second Number?	

Triangle Contracts

1) What kind of triangle does the triangle function produce?		
There are lots of other kinds of triangles! And Pyret has lots of other functions that make triangles!		
triangle :: (size:: Number, style :: String, color :: String) -> Image		
right-triangle :: (base::Number, height::Number, style::String, color::String) -> Image		
isosceles-triangle:: (leg::Number, angle::Number, style::String, color::String) -> Image		
2) Why do you think triangle only needs one number, while right-triangle and isosceles-triangle need two		
numbers and triangle-sas needs three?		
3) Write right-triangle expressions for the images below. One argument for each should be 100.		
4) What do you think the numbers in right-triangle represent?		
5) Write isosceles-triangle expressions for the images below. 1 argument for each should be 100.		
6) What do you think the numbers in isosceles-triangle represent?		
7) Write 2 expressions that would build right-isosceles triangles. Use right-triangle for one expression and		
isosceles-triangle for the other expression.		

Radial Star

```
radial-star :: (

points :: Number,
 inner-radius :: Number,
 full-radius :: Number,
 style :: String,
 color :: String
) -> Image
```

Using the detailed contract above, match each image to the expression that describes it.

Image			Expression
*	1	А	radial-star(5, 50, 200, "solid", "black")
*	2	В	radial-star(7, 100, 200, "solid", "black")
	3	С	radial-star(7, 100, 200, "outline", "black")
	4	D	radial-star(10, 150, 200, "solid", "black")
M	5	E	radial-star(10, 20, 200, "solid", "black")
*	6	F	radial-star(100, 20, 200, "solid", "black")
*	7	G	radial-star(100, 100, 200, "outline", "black")

What's on your mind?

For each function composition diagrammed below, translate it into the equivalent Circle of Evaluation for Order of Operations. Then write expressions for both versions of the Circles of Evaluation, and evaluate them for x=4. The first one has been completed for you.

Function Composition	Order of Operations	Trans	slate & Evaluate
1)	- 1	Composition:	h(g(f(x)))
g	* 6	Operations:	((3 * x) + 6) - 1
(F) X	3 x	Evaluate for x = 4	h(g(f(4)))=17
2)		Composition:	
g f		Operations:	
		Evaluate for x = 4	
3)		Composition:	
f		Operations:	
		Evaluate for x = 4	
4) f		Composition:	
h	Operations:		
(g) X		Evaluate for x = 4	

Function Composition — Green Star

1) Draw a Circle of Evaluation and write the Code for a $\,$ solid, green $\,$ star, size $\,$ 50 $\,$.

Circle of Evaluation:

Code: Using the star described above as the original , draw the Circl	es of Evaluation and write the Code for each exercise below.
2 A solid, green star, that is triple the size of the original (using scale) Circle of Evaluation:	3 A solid, green star, that is half the size of the original (using scale) Circle of Evaluation:
Code:	Code:
4 A solid, green star of size 50 that has been rotated 45 degrees counter-clockwise Circle of Evaluation:	5 A solid, green star that is 3 times the size of the original and has been rotated 45 degrees Circle of Evaluation:
Code:	Code:

Function Composition — Your Name

You'll be investigating these functions with your partner:

```
# text :: String, Number, String -> Image  # frame :: Image -> Image
# flip-horizontal :: Image -> Image  # above :: Image, Image -> Image
# flip-vertical :: Image -> Image  # beside :: Image, Image -> Image
```

1) In the editor, write the code to make an image of your name in big letters in a color of your choosing using text. Then draw the Circle of Evaluation and write the Code that will create the image.

Circle of Evaluation:

Code: Using the "image of your name" described above as the original, draw the Circles of Evaluation and write the Code for each exercise below. Test your ideas in the editor to make sure they work.			
Code:	Code:		
4 The "image of your name" above "the image of your name" flipped vertically. Circle of Evaluation:	5 The "image of your name" flipped horizontally beside "the image of your name". Circle of Evaluation:		
Code:	Code:		

Function Composition — scale-xy

You'll be investigating these two functions with your partner:

scale-xy :: Number, Number, Image -> Image

overlay :: Image, Images -> Image

The Ir	nage:	Circle of Evaluation:	Code:
		rhombus 40 90 "solid" "purple"	rhombus(40, 90, "solid", "purple")

Starting with the image described above, write the Circles of Evaluation and Code for each exercise below. Be sure to test your code in the editor!

1 A purple rhombus that is stretched 4 times as wide. Circle of Evaluation:	2 A purple rhombus that is stretched 4 times as tall Circle of Evaluation:
Code:	Code:
3 The tall rhombus overlayed on the wide rhombus. Circle of Evaluation:	★: Overlay a red rhombus onto the last image you made. Circle of Evaluation:
Code:	Code:

More than one way to Compose an Image!

Read through these 4 expressions and try to picture the images they are composing. If you're not sure what they'll look like, type them into the interactions area of your editor and see if you can figure out how the code connects to the image.

```
beside(rectangle(200, 100, "solid", "black"), square(100, "solid", "black"))
scale-xy(1, 2, square(100, "solid", "black"))
                                                                                        scale(2, rectangle(100, 100, "solid", "black"))
                                                                                                                                                                                                                                                                     rectangle(200, 100, "solid", "black"),
rectangle(100, 50, "solid", "black")))
                                                                                                                                                                               rectangle(100, 50, "solid", "black"),
```

For each image below, identify 2 expressions that could be used to compose it. The bank of expressions at the top of the page includes one possible option for each image.



Defining Values

In math, we use values like -98.1, 2/3 amd 42. In math, we also use expressions like 1×3 , $\sqrt{16}$, and 5-2. These evaluate to results, and typing any of them in as code produces some answer.

Math also has **definitions**. These are different from values and expressions, because they *they do not produce results*. Instead, they simply create names for values, so that those names can be re-used to make the Math simpler and more efficient.

Definitions always have both a name and an expression. The name goes on the left and the value-producing expression goes on the right, separated by an equals sign:

$$x = 4$$
$$y = 9 + x$$

The name is defined to be the result of evaluating the expression. Using the above examples, we get "x is defined to be 4, and y is defined to be 13". **Important: there is no "answer" to a definition**, and typing in a definition as code will produce no result.

Notice that definitions can refer to previous definitions. In the example above, the definition of y refers to x. But x, on the other hand, cannot refer to y. Once a value has been defined, it can be used in later expressions.

In Pyret, these definitions are written the exact same way:

Try typing these definitions into the Definitions Area on the left, clicking "Run", and then using them in the Interactions Area on the right.

```
x = 4
y = 9 + x
```

Just like in math, definitions in our programming language can only refer to previously-defined values.

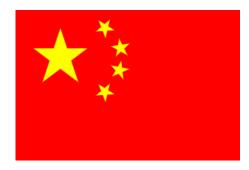
Here are a few more value definitions. Feel free to type them in, and make sure you understand them.

```
x = 5 + 1
y = x * 7
food = "Pizza!"
dot = circle(y, "solid", "red")
```

Defining Values - Explore

Open the <u>Defining Values Starter File</u> and click run.
1) What do you notice?
2) What do you wonder?
Look at the expressions listed below. Think about what you expect each of them to produce. Then, test them out one at a
time in the Interactions Area.
• <u>x</u>
• x + 5
• y - 9
• x * y
• z
• t
• gold-star
• my-name
• swamp
• c
3) What have you learned about defining values?
4) Define at least 2 more variables in the definitions area, click run and test them out. Once you know they're working,
record the code you used below.

Defining Values - Chinese Flag



- 1) What image do you see repeated in the flag?
- 2) Highlight or circle all instances of the structure that makes the repeated image in the code below.
- 3) In the code below, highlight or circle all instances of the expression for that image.

```
put-image(
  rotate(40, star(15, "solid", "yellow")),
  120, 175,
  put-image(
    rotate(80, star(15, "solid", "yellow")),
    140, 150,
    put-image(
       rotate(60, star(15, "solid", "yellow")),
       140, 120,
       put-image(
          rotate(40, star(15, "solid", "yellow")),
       120, 90,
          put-image(scale(3, star(15, "solid", "yellow")),
          60, 140,
          rectangle(300, 200, "solid", "red")))))))
```

4) Write the code to define a value for the repeated expression.

5) Open the Chinese flag starter file (Pyret) and click Run.

Then type china into the interactions area and click Enter.

- 6) Save a copy of the file, and simplify the flag code using the value you defined. Click Run, and confirm that you still get the same image as the original.
- 7) Now change the color of all of the stars to black, in both files. Then change the size of the stars.
- 8) Why is it helpful to define values for repeated images?

Challenge:

- This file uses a function we haven't seen before! What is it?
- Can you figure out its contract? Hint: Focus on the last instance of the function.

Why Define Values?

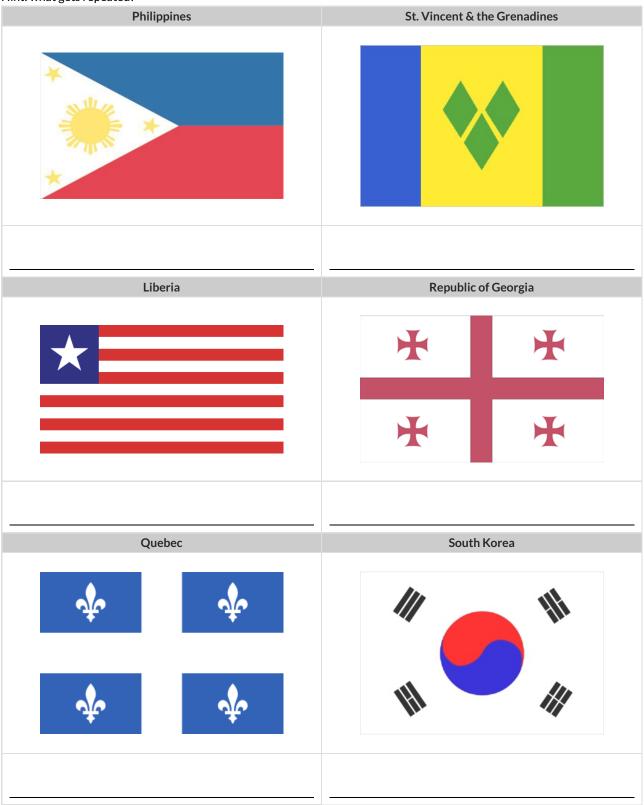
- 1) Complete the table using the first row as an example.
- 2) Write the code to define the value of sunny.

→ Use the defined value sunny to simplify!	scale 3 sunny	Code: ⇒ scale(3, sunny)	†	Code:	†	
Original Circle of Evaluation & Code	3 radial-star 30 20 50 "solid" "yellow"	Code: scale(3, radial-star(30, 20, 50, "solid", "yellow"))	frame radial-star 30 20 50 "solid" "yellow"	<pre>Code: frame(radial-star(30, 20, 50, "solid", "yellow"))</pre>	text radial-star sun" 30 "black" 30 20 50 "solid" "yellow"	

3) Test your code in the editor and make sure it produces what you would expect it to.

Which Value(s) Would it Make Sense to Define?

For each of the images below, identify which element(s) you would want to define before writing code to compose the image. Hint: what gets repeated?



Writing Code using Defined Values

1) On the line below, write the Code to define PRIZE-STAR as a pink, outline star of size 65.

Using the PRIZE-STAR definition from above, draw the Circle of Evaluation and write the Code for each of the exercises. One Circle of Evaluation has been done for you.

2 The outline of a pink star that is three times the size of the original (using scale)	3 The outline of a pink star that is half the size of the original (using scale)
Circle of Evaluation:	Circle of Evaluation:
scale 3 PRIZE-STAR	
Code:	Code:
4 The outline of a pink star that is rotated 45 degrees (It should be the same size as the original.)	5 The outline of a pink star that is three times as big as the original and has been rotated 45 degrees
Circle of Evaluation:	Circle of Evaluation:
Code:	Code:
6) How does defining values help you as a programmer?	

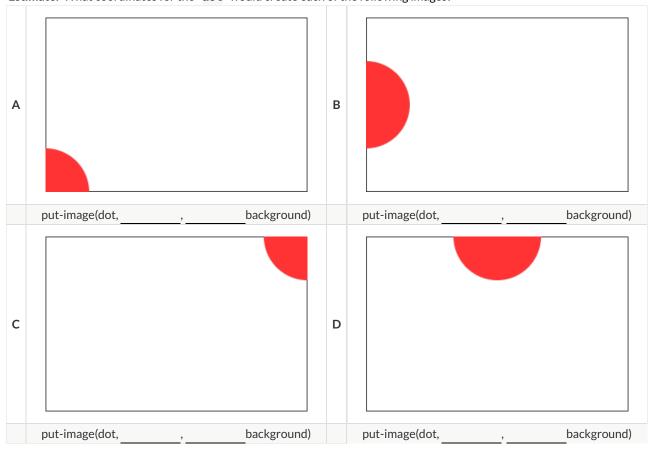
Estimating Coordinates

Think of the background image as a sheet of graph paper with the origin (0,0) in the bottom left corner.

The numbers in put-image specify a point on that graph paper, where the center of the top image should be placed.

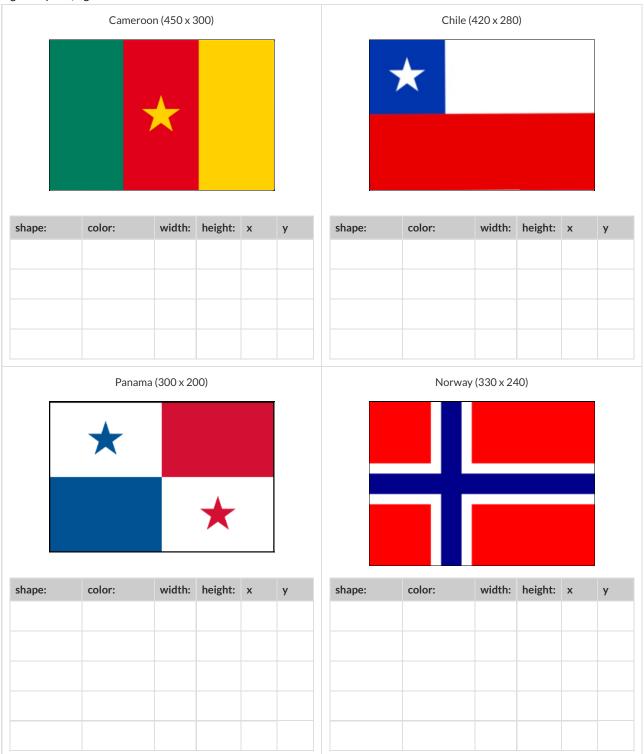
The width of the rectangle is 300 and the height is 200. The definitions for dot and background are: dot = circle(50, "solid", "red")
background = rectangle(300, 200, "outline", "black")

Estimate: What coordinates for the dot would create each of the following images?



Decomposing Flags

Each of the flags below is shown with their width and height. Identify the shapes that make up each flag. Use the flag's dimensions to estimate the dimensions of the different shapes. Then estimate the x and y coordinates for the point at which the center of each shape should be located on the flag. Hint: The bottom left corner of each flag is at (0,0) and the top right corner is given by the flags dimensions.



Notice and Wonder

As you investigate the Game Starter File with your partner, record what you Notice, and then what you Wonder. Remember, "Notices" are statements, not questions.

What do you Notice?	What do you Wonder?

Defining Functions

Functions can be viewed in *multiple representations*. You already know one of them: *Contracts*, which specify the Name, Domain, and Range of a function. Contracts are a way of thinking of functions as a *mapping* between one set of data and another. For example, a mapping from Numbers to Strings:

```
f :: Number -> String
```

Another way to view functions is with *Examples*. Examples are essentially input-output tables, showing what the function would do for a specific input:

In our programming langauge, we focus on the last two columns and write them as code:

```
examples:
    f(1) is 1 + 2
    f(2) is 2 + 2
    f(3) is 3 + 2
    f(4) is 4 + 2
end
```

Finally, we write a formal **function definition** ourselves. The pattern in the Examples becomes *abstract* (or "general"), replacing the inputs with *variables*. In the example below, the same definition is written in both math and code:

```
f(x) = x + 2 fun f(x): x + 2 end
```

Look for connections between these three representations!

- The function name is always the same, whether looking at the Contract, Examples, or Definition.
- The number of inputs in the Examples is always the same as the number of types in the Domain, which is always the same as the number of variables in the Definition.
- The "what the function does" pattern in the Examples is almost the same in the Definition, but with specific inputs replaced by variables.

Matching Examples and Definitions (Math)

Look at each set of examples on the left and circle what is changing from one example to the next.

Then, *match* the examples on the left to the definitions on the right.

Example	es:		Functions:
x	f(x)		
1	2 imes 1		
2	2 imes 2	1 A	f(x)=x-3
3	2 imes 3		
m	f(x)		
<i>x</i>	$\frac{f(x)}{15-3}$		
25	25 - 3	2 B	f(x)=2x
35	35 - 3		
33	33 – 3		
x	f(x)		
10	10 + 2		
15	15 + 2	3 C	f(x)=2x+1
20	20 + 2		
x	f(x)		
0	3(0)-2		
1	3(1) - 2	4 D	f(x)=3x-2
2	3(2) - 2		
\boldsymbol{x}	f(x)		
10	2(10) + 1	5 E	f(x) = x + 2
20	2(20) + 1		$J(\omega) = \omega + 2$
30	2(30) + 1		

Matching Examples and Function Definitions

Highlight the variables in gt and label them with the word "size".

```
examples:
   gt(20) is
     triangle(20, "solid", "green")
   gt(45) is
     triangle(45, "solid", "green")
end
fun gt(size): triangle(size, "solid", "green") end
```

Highlight and label the variables in the example lists below. Then, using gt as a model, match the examples to their corresponding function definitions.

Examples		Definition
<pre>examples: f("solid") is circle(8, "solid", "red") f("outline") is circle(8, "outline", "red") end</pre>	1	A fun f(s): star(s, "outline", "red") end
examples: f(2) is 2 + 2 f(4) is 4 + 4 f(5) is 5 + 5 end	2	B fun f(num): num + num end
<pre>examples: f("red") is circle(7, "solid", "red") f("teal") is circle(7, "solid", "teal") end</pre>	3	C fun f(c): star(9, "solid", c) end
<pre>examples: f("red") is star(9, "solid", "red") f("grey") is star(9, "solid", "grey") f("pink") is star(9, "solid", "pink") end</pre>	4	D fun f(s): circle(8, s, "red") end
<pre>examples: f(3) is star(3, "outline", "red") f(8) is star(8, "outline", "red") end</pre>	5	<pre>E fun f(c): circle(7, "solid", c) end</pre>

Match each set of examples (left) with the contract that best describes it(right).

Examples			Contract
examples: f(5) is 5 / 2 f(9) is 9 / 2 f(24) is 24 / 2 end	Ħ	∢	# f :: Number -> Number
<pre>examples: f(1) is rectangle(1, 1, "outline", "red") f(6) is rectangle(6, 6, "outline", "red") end</pre>	2	æ	# f :: String -> Image
<pre>examples: f("pink", 5) is star(5, "solid", "pink") f("blue", 8) is star(8, "solid", "blue") end</pre>	ო	U	# f :: Number -> Image
<pre>examples: f("Hi!") is text("Hi!", 50, "red") f("Ciao!") is text("Ciao!", 50, "red") end</pre>	4	۵	# f :: Number, String -> Image
<pre>examples: f(5, "outline") is star(5, "outline", "yellow") f(5, "solid") is star(5, "solid", "yellow") end</pre>	ιn	ш	# f :: String, Number -> Image

Contracts, Examples & Definitions

ery contract has t l gt								
9 -	::			Nun	mber		->	Image
function name					omain			range
rite some example	s, then cin	cle and label w	hat chan	ges.				
amples:								
gt	(10)	is	triangle(10	, "solid",	"greer	า")
function name		input(s)				at the function prod		
gt	(20)	is	triangle(20			า")
function name		input(s)			wh	at the function prod	uces	
rite the definition,	giving va	riable names t	o all vour	innı	ut values			
	givilig val	size):	пр	ut values			
function nam	\	variable(s)						
	ze, "so			nction	n does with those varia	ble(s)		
triangle(siz	a functio	n called be ,	what the fun		bc		adius we v	want.
ad	a functio	n called be ,	what the fun		bc		adius we v	want.
d rections : Define	a functio	n called be ,	what the fun	akes	bc			want.
irections : Define ery contract has th	a function hree parts.	n called bc ,	what the fun	akes	bc s solid blue circle			
irections : Define ery contract has the function name	a function hree parts.	n called bc ,	what the fun	akes	bc s solid blue circle			
irections : Define ery contract has the function name rite some example	a function hree parts.	n called bc ,	what the fun which ma	akes	bc s solid blue circle			
rections : Define ery contract has the function name ite some example	a function hree parts.	n called bc ,	what the fun which ma	doi doi ges	bc s solid blue circle		->	
rections: Define ery contract has the function name ite some example amples:	a function hree parts.	n called be,	what the fun	doi doi ges	bc s solid blue circle	s of whatever r	->	
e ctions : Define	a functio	n called be ,	what the fun		bc			want.
irections: Define ery contract has the function name rite some example camples:	a function hree parts.	n called bc , ' cle and label w	what the fun which ma	doi doi ges	bc s solid blue circle			
rections: Define ery contract has the function name ite some example amples:	a function hree parts.	n called bc , ' cle and label w	what the fun which ma	doi doi ges	bc s solid blue circle	s of whatever r	->	
rections: Define ry contract has to function name ite some example amples:	a function hree parts.	n called bc , ' cle and label w	what the fun	don ges.	bc s solid blue circle	s of whatever r	->	
rections: Define ry contract has to function name ite some example amples:	a function hree parts.	n called bc , ' cle and label w	what the fun	don ges.	bc s solid blue circle	s of whatever r	->	
rections: Define ery contract has the function name rite some example amples:	a function hree parts.	n called bc , ' cle and label w	what the fun	don ges.	bc s solid blue circle	s of whatever r	->	

what the function does with those variable(s)

end

What's on your mind?

Solving Word Problems

Being able to see functions as Contracts, Examples or Definitions is like having three powerful tools. These representations can be used together to solve word problems!

- 1) When reading a word problem, the first step is to figure out the **Contract** for the function you want to build. Remember, a Contract must include the Name, Domain and Range for the function!
- 2) Then we write a **Purpose Statement**, which is a short note that tells us what the function *should do*. Professional programmers work hard to write good purpose statements, so that other people can understand the code they wrote!
- 3) Next, we write at least two **Examples**. These are lines of code that show what the function should do for a *specific* input. Once we see examples of at least two inputs, we can *find a pattern* and see which parts are changing and which parts aren't.
- 4) To finish the Examples, we circle the parts that are changing, and label them with a short variable name that explains what they do.
- 5) Finally, we define the function itself! This is pretty easy after you have some examples to work from: we copy everything that didn't change, and replace the changeable stuff with the variable name!

Creating Contracts From Examples

Write the contracts used to create each of the following collections of examples.

```
1)
  examples:
   big-triangle(100, "red") is
     triangle(100, "solid", "red")
   big-triangle(200, "orange") is
     triangle(200, "solid", "orange")
+ end
2)
  examples:
   purple-square(15) is
     rectangle(15, 15, "outline", "purple")
   purple-square(6) is
     rectangle(6, 6, "outline", "purple")
+ end
3)
  examples:
   banner("Game Today!") is
    text("Game Today!", 50, "red")
   banner("Go Team!") is
     text("Go Team!", 50, "red")
   banner("Exit") is
     text("Exit", 50, "red")
+ end
4)
  examples:
   twinkle("outline", "red") is
     star(5, "outline", "red")
   twinkle("solid", "pink") is
     star(5, "solid", "pink")
   twinkle("outline", "grey") is
     star(5, "outline", "grey")
+ end
5)
  examples:
   half(5) is 5/2
   half(8) is 8 / 2
   half(900) is 900 / 2
+ end
```

Writing Examples from Purpose Statements

We've provided contracts and purpose statements to describe two different functions. Write examples for each of those functions.

Contract and Purpose Statement		
Every contract has three parts		
<pre># upside-down::</pre>	Image	-> Image
function name	domain	range
#Consumes an image, and flips	it upside down by rotating it 180 de	grees.
	what does the function do?	
Examples		
Write some examples, then circle and label w	rhat changes	
examples:		
() is	
function name	input(s)	
,	what the function produces	
function name	input(s) is	
Tonchormanie	11 (ports)	
	what the function produces	<u> </u>
end		
Contract and Purpose Statement		
Every contract has three parts		
#product-squared::	Number, Number	-> Number
function name	domain	range
#Consumes two numbers and so	quares their product	
	what does the function do?	
Examples		
Write some examples, then circle and label w	/hat changes	
examples:		
() is	
function name	input(s) what the	the function produces
() is	
function name	input(s) what the	the function produces

end

Word Problem: rocket-height

Directions: A rocket blasts off, and is now traveling at a constant velocity of 7 meters per second. Use the Design Recipe to write a function rocket-height, which takes in a number of seconds and calculates the height.

Contract and Purp	oose Stat	ement				
Every contract has three	parts					
#	::				->	
function name	· ·		domain		range	
#						
			what does the	e function do?		
Examples						
Write some examples, th	en circle an	d label what chan	ges			
examples:						
	() is			
function name		input(s)		what the function p	roduces	
	() is			
function name		input(s)		what the function p	roduces	
end						
Definition						
Write the definition, givin	ng variable i	names to all your	input values			
fun	():			
function name	e	variable(s)				
-		wh	at the function does	with those variable(s)		
end						

Writing Quality Purpos	Quality Purpose Statements 3 Reads
1st Read: What is this problem about?	2nd Read: What are the Quantities?
3rd Read: What is a good Purpose Statement?	
Stronger & Clearer Purpose Statement 1st Revision:	Clearer
Purpose Statement 2nd Revision:	

The Design Recipe - Direct Variation

 $\textbf{Directions}: Write a function \ \ wage \ , that takes in a number of hours worked and returns the amount a worker will get paid if their rate is $10.25/hr.$

Contract and Pur	pose State	ement				
Every contract has three	e parts					
#	::				->	
function name			domain		range	
#						
			what does the	e function do?		
Examples						
Write some examples, tl	hen circle and	d label what change	5			
examples:						
	() is			
function name		input(s)		what the function prod	duces	
	() is			
function name		input(s)		what the function prod	duces	
end 						
Definition						
Write the definition, giv	ing variable r	names to all your inp	ut values			
fun	():			
function nam	ne	variable(s)	_			
-		who	t the function does	with those variable(s)		
end						
Contract and Pur				mber of calories burned		
Every contract has three	e parts					
#	::				->	
function name			domo	nin	rang	ge
#						
_			what does the	e function do?		
Examples						
Write some examples, tl	hen circle and	d label what change:	5			
examples:						
	() is			
function name	— `—	input(s)		what the function p	produces	
	() is			
function name	— `—	input(s)		what the function p	produces	
end						
Definition						
Write the definition, giv	ing variable r	names to all your inp	ut values			
fun	():			
function na	me	variable(s)	<u> </u>			
-		who	t the function does	with those variable(s)		
end						

The Design Recipe (Practice 1)

Directions: Write a function marquee that takes in a message and returns that message in large gold letters.

Cor	ntract and Purp	ose State	ement					
Every	contract has three p	oarts						
#		::				->		
	function name				domain		range	
#								
				wh	at does the f	function do?		
Exa	amples							ш
Write	some examples, the	n circle and	d label what chan	iges				
exan	mples:							
		()	is			
_	function name	_	input(s)			what the function produces		
		()	is			
_	function name	_	input(s)			what the function produces		
end								
Def	finition							
Write	the definition, givin	g variable ı	names to all your	input value	?s			
fun		():				
	function name		variable(s)					
			W	vhat the fund	ction does w	rith those variable(s)	_	
end								
-							ı	
Dire	ections : vvrite a	Tunction	num-cube	tnat take	es in a nur	mber and returns the cube of that n	umber.	
Cor	ntract and Purp	ose State	ement					
Every	contract has three p	oarts						
#		::				->		
	function name	-			domain		range	
#								
				wh	at does the f	function do?		_
Exa	amples							
Write	some examples, the	n circle and	d label what chan	iges				
exan	mples:							
		()	is			
_	function name	- `	input(s)			what the function produces		
		()	is			
_	function name	- `	input(s)			what the function produces		
end								
Def	finition							
	the definition, givin	g variable ı	names to all your	input value	?S			
fun	, , , , , ,	(,):				
	function name	`	variable(s)					
			W	vhat the fund	ction does w	rith those variable(s)		
end								

The Design Recipe (Practice 2)

Directions: Write a function split-tab that takes in a cost and the number of people sharing the bill and splits the cost equally.

Cor	ntract and Purpos	e State	ement			
Every	contract has three par	ts				
#	::					->
	function name				domain	range
#						
				who	at does the	e function do?
Exa	amples					
Write	some examples, then o	ircle and	l label what chang	ges		
exar	mples:					
		()	is	
_	function name	`	input(s)		-	what the function produces
		() :	is	
	function name	`	input(s)			what the function produces
end						
Def	finition					
	the definition, giving v	ariable r	names to all your i	nput value	S	_
fun	, , , , ,	(,):		
	function name	_`—	variable(s)	— ′		
			W	hat the fund	tion does	with those variable(s)
end						
Dire	ections : Write a fu	nction	tip-calcul	lator t	hat take	es in the cost of a meal and returns the 15% tip for that meal.
Cor	ntract and Purpos	e State	ement			
	contract has three par					_
#	•••					->
<i>"</i> —	function name				domain	
#						, and the second
"-				who	at does the	e function do?
Eva	amples					
		irolo ano	llabal what abana	700		
	some examples, then o	ircie and	i label what chang	ges		
exar	mples:	,				
		()	is	
	function name		input(s)			what the function produces
		()	is	
end	function name		input(s)			what the function produces
	finition					
Write	the definition, giving v	ariable n	names to all your i	nput value	S	
fun		():		
	function name		variable(s)			
			W	hat the fund	tion does	with those variable(s)
end						

The Design Recipe (Practice 3)

Directions: The Swamp in the City Festival is ordering t-shirts. The production cost is \$75 to set up the silk screen and \$9 per shirt. Write a function $\min_{shirt-price}$ that takes in the number of shirts to be ordered, n, and returns the minimum amount the festival should charge for the shirts in order to break even. (Assume that they will sell all of the shirts.)

Contract	and Purpose Stater	nent					Ш
Every contrac	t has three parts						
#	::				->		
function	on name		C	domain		range	
#							
			what doe	es the functio	n do?	_	
Examples	;						
Write some ex	kamples, then circle and l	abel what changes					
examples	:						
	() i:	s			
func	tion name	input(s)			what the function produces		
	() i:	s			
	tion name	input(s)			what the function produces		
end							
Definition	n						
Write the defi	nition, giving variable no	mes to all your inp	ut values				
fun	():				
f	unction name	variable(s)					
		what	t the function (does with tho	se variable(s)		
end							

The Design Recipe (Slope/Intercept 1)

Directions: For his birthday, James' family decided to open a savings account for him. He started with \$50 and committed to adding \$10 a week from his afterschool job teaching basketball to kindergartners. Write a function savings that takes in the number of weeks since his birthday and calculates how much money he has saved.

Contract and Purp	ose State	illelit						
very contract has three p	arts							
<u> </u>	::					->		
function name	_			domain			range	
			wha	t does the fund	ction do?			
Examples								
rite some examples, the	n circle and	l label what char	nges					
xamples:								
	() i	s				
function name	- `	input(s)			what the function pr	oduces		
	() i	s				
function name	- `	input(s)			what the function pr	oduces		
nd								
Definition								
rite the definition, giving	g variable =	names to all your	innut values					
un	3 variable 11	idines to un your):	•••				
function name	'	variable(s)						
ronononnamo		, a., a., a., a., a., a., a., a., a., a.						
			ub out the frame	tion door with	th and waviable (a)			
		V	what the funct	non does wiin	those variable(s)			
Pirections : Write a					nd number of miles d	riven and re	eturns the co	st of renting
Directions : Write a ruck. The truck is \$4	15 per da	y and each dr			nd number of miles d	riven and re	eturns the co	st of renting
Directions: Write a ruck. The truck is \$4	15 per da ose State	y and each dr			nd number of miles d	riven and re	eturns the co	st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three p	15 per da ose State	y and each dr			nd number of miles d	riven and re	eturns the co	st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purp	15 per da ose State	y and each dr	iven mile i		nd number of miles d		eturns the cos	st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three professions function name	15 per da ose State	y and each dr	iven mile i	s 15¢.	nd number of miles d			st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three professions function name	15 per da ose State	y and each dr	iven mile i	s 15¢.				st of renting
Pirections: Write a ruck. The truck is \$4 Contract and Purpovery contract has three production name	15 per da ose State	y and each dr	iven mile i	s 15¢.				st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three purpovery contract	45 per da ose State oarts	y and each dr	iven mile i	s 15¢.				st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three purposes function name Examples Virite some examples, the	45 per da ose State oarts	y and each dr	iven mile i	s 15¢.				st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three purpovery contract	45 per da ose State oarts :: n circle and	y and each dr	wha	s 15¢.				st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpovery contract has three purpovery contract	45 per da ose State oarts	y and each dr ement	iven mile i	s 15¢.	ction do?	->		st of renting
Pirections: Write a uck. The truck is \$4 Contract and Purporery contract has three production name Examples Trite some examples, the	45 per da ose State oarts :: n circle and	y and each dr	wha	domain		->		st of renting
Pirections: Write a ruck. The truck is \$4 Contract and Purper very contract has three production name Examples Trite some examples, the examples:	45 per da ose State oarts :: n circle and	y and each dr	wha	s 15¢.	ction do? what the function pr	->_		st of renting
Pirections: Write a ruck. The truck is \$4 Contract and Purporery contract has three property contract has three pr	45 per da ose State oarts :: n circle and	y and each dr ement	wha	domain	ction do?	->_		st of renting
Contract and Purpovery contract has three process function name Examples function name function name function name	45 per da ose State oarts :: n circle and	y and each dr	wha	domain	ction do? what the function pr	->_		st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpowery contract has three purpowery contract has three purpowers contract has three purpowers with the some examples, the examples:	15 per da ose State parts :: n circle and	y and each driement I label what chan input(s)	wha	domain t does the fund	ction do? what the function pr	->_		st of renting
Contract and Purpovery contract has three position name Examples Vite some examples, the examples: function name function name function name function name function name function name function name function name function name function name function name function name function name function name function name function name function name function name function name	15 per da ose State parts :: n circle and	y and each driement I label what chan input(s)	wha nges) i input values	domain t does the fund	ction do? what the function pr	->_		st of renting
Contract and Purpovery contract has three provery contract has three proves	15 per da ose State parts :: n circle and	y and each driement I label what chan input(s) input(s)	wha	domain t does the fund	ction do? what the function pr	->_		st of renting
Directions: Write a ruck. The truck is \$4 Contract and Purpowery contract has three production name Examples Virte some examples, the examples: function name function name Tunction name Definition Virte the definition, giving	15 per da ose State parts :: n circle and	y and each driement I label what chan input(s)	wha nges) i input values	domain t does the fund	ction do? what the function pr	->_		st of renting

The Design Recipe (Negative Slope/Intercept)

Directions: An Olympic pool holds 660,000 gallons of water. A fire hose can spray about 250 gallons per minute. Write a function pool that takes in the number of minutes that have passed and calculates how much water is still needed to fill it.

Contract and Purpo	nse Statem	ent				
Every contract has three p		icrit -				
	:			->	•	
function name	•		domain		range	
#						
			what does the func	tion do?		
Examples						
Write some examples, the	n circle and la	hel what changes				
examples:	ii circie ana ia	bei what changes.	····			
examples:	,		\ .			
function name	_ (input(s)) is	what the function produces		
ionclion name	,	inpui(s)		what the folicilon produces		
	_ () is			
function name end		input(s)		what the function produces		
Definition						ш
Write the definition, giving	g variable nan					
fun	():			
function name		variable(s)				
end		what	the function does with t	hose variable(s)		
Ciiu						
money they have left				kes in the number of months		
Contract and Purpo	ose Statem	ent				
Every contract has three p	arts					
#	::				->	
function name			domain		range	
#						
			what does the func	tion do?		
Examples						
Write some examples, the	n circle and la	bel what changes.				
examples:						
	() is			
function name	_ `	input(s)		what the function produces	3	
	() is			
function name	`	input(s)		what the function produces	<u> </u>	
end		7 (-)		, , , , , , , , , , , , , , , , , , , ,		
Definition						
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fun	1	nes to an your mpt	_			
function name	() :			
function name	e (variable(s)	_			
	(<u> </u>	variable(s)	_	hose variable(s)		

The Design Recipe (Geometry - Rectangles)

Directions: Write a function lawn-area that takes in the length and width of a rectangular lawn and returns its area.

Contract and Purp	ose Stater	ment						
ery contract has three p	parts							
	::					->		
function name			don	nain			range	
			what do	es the function	403			
vemonles	_	_	what do	es me ionclior	409	_	_	_
xamples	. , , ,							
ite some examples, the	en circle and i	abel what chan	ges					
camples:	,		, .					
function name	_ (input(s)) is		what the function pro	ducos		
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function name	_ (input(s)) is		what the function pro	nduces		
n d		πιροτίο			what the follellost pre	doces		
Definition								
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ne the definition, givin	ig variable na (iiiles to ali your i) :					
function name	'	variable(s)						
		.,						
		W	hat the function	does with thos	e variable(s)			
nd			riai ilie ronellori	aces will mos	e vanable (9)			
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erimeter of that red Contract and Purp	ctangle. ose Stater parts			takes in th	e length and width		gle and return	ns the
erimeter of that red Contract and Purp ery contract has three	ctangle. ose Stater parts		do	main				ns the
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Contract and Purpery contract has three process function name Examples rite some examples, the camples:	ctangle. ose Stater oarts ::	nent label what chang input(s)	do what doo ges	main	do? what the function p	->roduces		ns the
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Contract and Purp very contract has three p function name Examples frite some examples, the xamples: function name function name function name function name nd Definition frite the definition, givin	ctangle. cose Stater coarts :: en circle and l	input(s) input(s) input(s)	what do	main	do? what the function p	->roduces		ns the

The Design Recipe (Geometry - Rectangular Prisms)

Directions: Write a function rectprism-vol that takes in the length, width, and height of a rectangular prism and returns the Volume of a rectangular prism.

Contract and Purpose Statement				
Every contract has three parts				
# ::		->		
function name	domain		range	
#				
	what does the fun	ction do?		_
Examples				
Write some examples, then circle and label what change	es			
examples:				
() is			
function name input(s)		what the function produces		
() is			
function name input(s) end		what the function produces		
Definition				
Write the definition, giving variable names to all your in	put values			
fun ():			
function name variable(s)				
end wh	at the function does with	those variable(s)	<u>.</u>	
Contract and Purpose Statement Every contract has three parts # ::	505 61 60611 61 165 51	->		_
function name	domain		range	
#				
	what does the fun	action do?	_	
Examples				
Write some examples, then circle and label what change	es			
examples:				
() is			
function name input(s)				
(what the function	on produces		
function name input(s)) is			
To T				
	what the function	on produces		
end				
Definition				
Write the definition, giving variable names to all your in	put values			
fun ():			
function name variable(s)	_			
end	at the function does with	those variable(s)		

The Design Recipe (Geometry - Circles)

Directions: Write a function circle-area-dec that takes in a radius and uses the decimal approximation of pi (3.14) to return the area of the circle.

Contract and Purpose Statement			
Every contract has three parts			
# ::		->	
function name	domain		range
#			
	what does the function do?		
Examples			
Write some examples, then circle and label who	t changes		
examples:			
() is		
function name in	out(s)	what the function produces	
() is		
_	out(s)	what the function produces	
end			
Definition			
Write the definition, giving variable names to a	l your input values		
fun ():		
function name varia	ble(s)		
3	what the function does with those var	iable(s)	
end			
return the circumference of the circle Contract and Purpose Statement			
Every contract has three parts			
# ::		->	
function name	domain		range
#			
	what does the function do?		_
Examples			
Write some examples, then circle and label who	t changes		
examples:			
() is		
function name input		hat the function produces	<u></u>
() is		
function name input		hat the function produces	
end			
Definition			
Write the definition, giving variable names to a	ll your input values		
fun ():		
function name variable			
-	what the function does with those var	iable(s)	
end			

The Design Recipe (Geometry - Cylinders)

Contract and Purp	ose State	ement								
Every contract has three p	arts									
#	··						->			
function name				domain				range		
#										
			wh	at does the	function do?					
Examples										Ш
Write some examples, the	n circle and	l label what chan	nges							
examples:										
	()	is						
function name		input(s)			what	the function prod	uces			
	()	is						
function name end		input(s)			what	the function prod	uces			
Definition										Ш
Write the definition, givin	g variable n	ames to all your	input value	es						
fun	(<u> </u>							
function name		variable(s)								
end		V	vnat tne tun	ction does v	vith those variabl	ie(s)				
of the function <i>circle</i> Contract and Purp	ose State	ement								
Every contract has three p	arts									
#				-1			> 			
function name				domain				range		
#			wh	at door tho	function do?					
Evennelee			****	ar aces inc	TOTICIIOTT GO F		-		-	
Examples	u sinala su	Halada da akada a								
Write some examples, the	n circie ana	i label what char	iges							
examples:	,		,							
function name	_ (input(s))	is	what	the function prod	ucos			
Toriclion name	,	процз	,	•	what	ine fonction produ	oces			
function name	_ (input(s))	is	what	the function prod	UCAS			
end		IIIpor(3)			wildi	ine folicilon prod	0003			
Definition										
Write the definition, givin,	g variable r	names to all vour	innut valu	25						
fun	3 variable 11	idilicə to dii yodi) :	J						
function name	'	variable(s)	′·							
		.,								
		V	what the fun	ction does v	vith those variabl	le(s)				
end						•				

Danger and Target Movement

 $\begin{tabular}{ll} \textbf{Directions}: Use the Design Recipe to write a function $$ update-danger $, which takes in the danger's x- and y-coordinate and produces the next x-coordinate, which is 50 pixels to the left. \\ \end{tabular}$

Contract and Pu	rpose Sta	tement				
Every contract has thre	ee parts					
#	::			->		
function name			domain		range	_
#						
			what does the f	unction do?		_
Examples						
Write some examples,	then circle ai	nd label what chan	ges			
examples:						
	() is			
function name		input(s)		what the function produces		
function name	(iont/al) is	what the fire ties produces		
function name end		input(s)		what the function produces		
Defuition	-	_	_		_	
Definition						
Write the definition, gi	ving variable 1	names to an your				
function nai	me (variable(s)):			
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-		W	rhat the function does w	ith those variable(s)		
end						
Contract and Pu		tement				
Every contract has thre	ee parts					
# function name	_::		domain	->	range	_
#			domain		range	
#			what does the f	unction do?		
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Write some examples,	then circle a	nd lahel what chan	aps			
examples:	trieri en ele ul	ia iaser what chan	ges			
onump205.	1) is			
function name	'	input(s)	/ IS	what the function produces		
	(,) is	,		
function name	`	input(s)		what the function produces		
end						
Definition						
Write the definition, gi	ving variable	names to all your	input values			
fun	(,):			
function na	me `	variable(s)	^			
-		W	rhat the function does w	ith those variable(s)		
end						

Problem Decomposition

- Sometimes a problem is too complicated to solve all at once. Maybe there are too many variables, or there is just so much information that we can't get a handle on it!
- We can use **Problem Decomposition** to break those problems down into simpler pieces, and then work with the pieces to solve the whole. There are two strategies we can use for decomposition:
 - **Top-Down** Start with the "big picture", writing functions or equations that describe the connections between parts of the problem. Then, work on defining those parts.
 - **Bottom-Up** Start with the smaller parts, writing functions or equations that describe the parts we understand. Then, connect those parts together to solve the whole problem.
- You may find that one strategy works better for some types of problems than another, so make sure you're comfortable using either one!

The Design Recipe: Revenue & Cost

Directions: Use the Design Recipe to write a function revenue, which takes in the number of glasses sold at \$1.75 apiece and calculates the total revenue.

Contract and Purp	ose Stateme	ent				
Every contract has three	parts					
#	::				->	
function name			domain		range	
#						
			what does the fo	unction do?		
Examples						
Vrite some examples, the	en circle and lab	el what chang	es			
examples:						
	() is			
function name		input(s)		what the function prod	duces	
	() is			
function name end		input(s)		what the function prod	duces	
Definition						
Write the definition, givir	ng variable nam ,	es to all your in				
fun	(_):			
function name	·	rariable(s)				
end		wn	nat the function does wi	tn tnose variable(s)		
Contract and Purp		ent				
very contract has three	parts					
#	:				-> <u></u>	
function name			domain		range	
<u> </u>			unbart along the f	ination do 2		
			what does the fo	uncilori do e		
Examples						
Vrite some examples, the	en circle and lab	el what chang	es			
examples:						
-	_ () is			
function name	,	input(s)		what the function prod	duces	
function name	_ (in must/al) is	what the function are	duas	
function name		input(s)		what the function prod	uces	
Dofinition						
Definition	and all to the		anut values			
Nrite the definition, givir	ig variable nam '	es to all your in				
fun function name	<u> </u>	rariable(s)	_):			
ronchon name	. v	andbic (3)				
		uh	nat the function does wi	th those variable/sl		
end		WII	iai ine ionclion does wi	m mose vanabie(s)		

Word Problem: profit

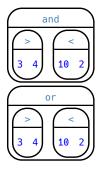
Directions: Use the Design Recipe to write a function <code>profit</code> that calculates total profit from glasses sold, which is computed by subtracting the total cost from the total revenue.

Contract and Purp	ose State	ement						
Every contract has three	parts							
#	::					->		
function name				domain			range	_
#								
			W	hat does the fo	unction do?			
Examples								
Write some examples, the	en circle and	d label what chan	ges					
examples:								
	()	is				
function name		input(s)		-	what the function	produces		
	()	is				
function name		input(s)			what the function	produces		
end								
Definition								
Write the definition, givin	ng variable i	names to all your	input val	ues				
fun	():					
function name	e	variable(s)						
		wh	nat the fu	nction does wi	ith those variable(s)			_
end								

Inequalities

- Sometimes we want to *ask questions* about data. For example, is x greater than y? Is one string equal to another?

 These questions can't be answered with a Numbers. Instead, they are answered with a new data type called a **Boolean**.
- Video games use Booleans for many things: asking when a player's health is equal to zero, whether two characters are close enough to bump into one another, or if a character's coordinates put it off the edge of the screen.
- A Boolean value is either true or false. Unlike Numbers, Strings, and Images, Booleans have only two possible values.
- You already know some functions that produce Booleans, such as < and > ! Our programming language has them, too: 3 < 4, 10 > 2, and -10 == 19.
- We also have ways of writing **Compound Inequalities**, so we can ask more complicated questions using the and and or functions.
 - o (3 > 4) and (10 < 2) translates to "three is greater than four *and* ten is less than two". This will evaluate to false, since the and function requires that both sub-expressions be true.
 - \circ (3 > 4) or (10 < 2), which translates to "three is greater than four or ten is less than two". This will evaluate to true, since the or function only requires that one sub-expression be true.
- The Circles of Evaluation work the same way with Booleans that they do with Numbers, Strings and Images:



Boolean Functions

Boolean Tunctions
Explore the functions in the Booleans Starter File . What characteristics define them as Booleans?
Fill in the blanks below so that each of the five functions returns true 1) is-odd()
2)is-even()
3) is-less-than-one()
4) is-continent()
5) is-primary-color()
Fill in the blanks below so that each of the five functions returns false 6) is-odd()
7)is-even()
8) is-less-than-one()
9) is-continent()
10) is-primary-color()

Simple Inequalities

Each inequality expression in the first column contains a number.

Decide whether or not that number is a solution to the expression and place it in the appropriate column.

Then identify 4 solution and 4 non-solution values for x.

- Solutions will make the expression true .
- Non-Solutions will make the expression false .

Challenge yourself to use negatives, positives, fractions, decimals, etc. for your \bar{x} values.

Expression	4 solutions that evaluate to true	4 non-solutions that evaluate to false
x > 2		
x <= -2		
x < 3.5		
x >= -1		
x > -4		
x <> 2		

X 💝 Z		
1) For which inequalities was	the number from the expression part of the	solution?
2) For which inequalities was	the number from the expression not part of	the solution?
3) For which inequalities were	the solutions on the left end of the number	line?
4) For which inequalities were	the solutions on the right end of the numbe	r line?

Converting Circles of Evaluation to Code

For each Circle of Evaluation on the left-hand side, write the code for the Circle on the right-hand side

	Circle of Evaluation	Code
1	> + + 9 4 5	
2	and <	
3	or == == yum "apple" yum "banana"	
4	>= String-length "My Game"	
5	and and c c c x 10	

Compound Inequalities — Practice

Create the Circles of Evaluation, then convert the expressions into code in the space provided.			
1) 2 is less than 5, and 0 is equal to 6			
What will this evaluate to?			
2) 6 is greater than 8, or -4 is less than 1			
What will this evaluate to?			
3) The String "purple" is the same as the String "blue", and 3 plus 5 equals 8			
What will this evaluate to?			

4) Write the contracts for and & or in your Contracts page.

Compound Inequalities: Solutions & Non-Solutions

For each Compound Inequality listed below, identify 4 solutions and 4 non-solutions. If there are **no solutions** or the solution set includes **all real numbers** you can write that instead of making a list.

- Solutions for intersections, which use and will make both of the expressions true.
- Solutions for *unions*, which use **or** will make at least one of the expressions true.

Pay special attention to the numbers in the sample expression! Challenge yourself to use negatives, positives, fractions, decimals, etc. for your \mathbf{x} values.

The first two have been done for you - Answers will vary!

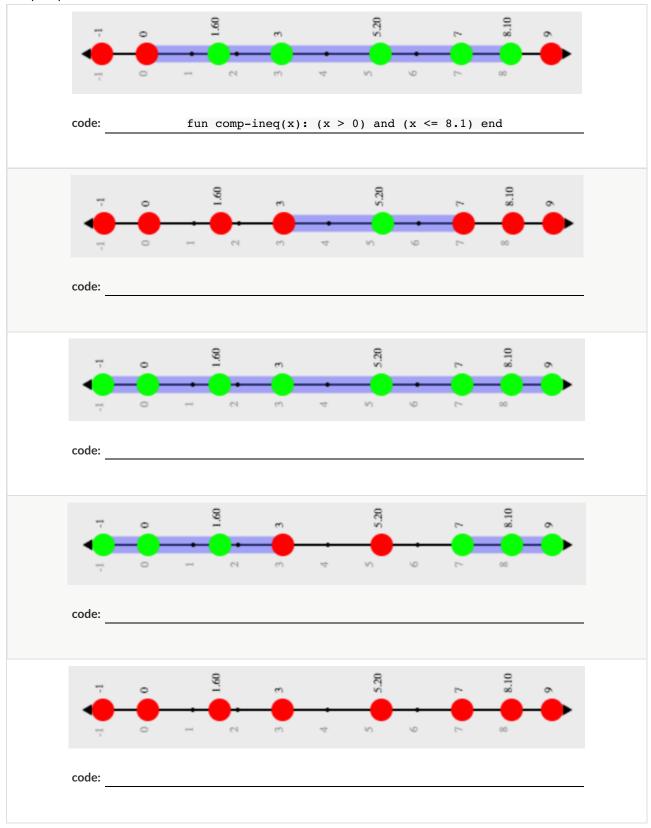
Expression	4 solutions that evaluate to true	4 non-solutions that evaluate to false		
x > 5 and $x < 15$	6, 9.5, 12, 14.9	-2, 5, 15, 16.1		
x > 5 or $x < 15$	All real numbers	No non-solutions		
$x \le -2$ and $x > 7$				
$x \le -2 \text{ or } x > 7$				
x < 3.5 and $x > -4$				
x < 3.5 or x > -4				
$x \ge -1$ and $x \ge -5$				
$x \ge -1 \text{ or } x \ge -5$				
x < -4 and $x > 2$				

2) Could there ever be an intersection whose solution is <i>all real numbers</i> ? Explain your thinking.			
1) Could there ever be a unior	with no solutions? Explain yo	ur thinking.	
x < -4 and $x > 2$			
$x \ge -1 \text{ or } x \ge -5$			
x >= -1 and $x > -5$			

Compound Inequality Functions

Each of the plots below was generated using the code

inequality(comp-ineq, [list: -1, 0, 1.6, 3, 5.2, 7, 8.1, 9]). With the exception of the example, each plot below was defined using the numbers 3 and 7. Write the code for how comp-ineq was defined for each plot in the space provided.



Sam the Butterfly

Open the "Sam the Butterfly" starter file and press "Run". (Hi, Sam!)
Move Sam around the screen using the arrow keys.
1) What do you notice about the program?
2) What do you wonder?
3) What do you see when Sam is at (0,0)? Why is that?
4) What changes as the butterfly moves left and right?
Sam is in a 640×480 yard. Sam's mom wants Sam to stay in sight.
How far to the left and right can Sam go and still remain visible?
Use the new inequality functions to answer the following questions with code:
5) Sam hasn't gone off the left edge of the screen as long as
6) Sam hasn't gone off the right edge of the screen as long as
7) Use the space below to draw Circles of Evaluation for these two expressions:

Left and Right

Directions: Use the Design Recipe to write a function <code>is-safe-left</code>, which takes in an x-coordinate and checks to see if it is greater than -50.

Contract and Pu		ment				
ery contract has thre					- >	
function name	_::		domain		-> range	
			what does the	function do?		
xamples						
ite some examples, t	hen circle and	label what char	nges			
camples:						
_	() is			
function name	_ `	input(s)		what the function prod	luces	
	() is			
function name		input(s)	·	what the function prod	duces	
ıd						
Definition						
rite the definition, giv	ing variable no	ames to all your	input values			
ın	():			
function nan	ne	variable(s)	<u></u>			
it is less than 690						
Contract and Pu		ment				
ery contract has thre	e parts					
function name	_::		domain		-> range	
Tonenonname			domain		range	
			what does the	function do?		
Examples						
rite some examples, t	hen circle and	l lahel what char	1985			
xamples:			.900			
	() is			
function name	_ '	input(s)		what the function prod	luces	
	() is			
function name	_ `	input(s)		what the function prod	duces	
nd						
Definition						
rite the definition, giv	ing variable no	ames to all your				
. •			input values			
un	(annes to an your	input values):			
function name	(variable(s)				
	ne (
	ne (variable(s)		vith those variable(s)		

Word Problem: is-onscreen

Directions: Use the Design Recipe to write a function is-onscreen, which takes in an x-coordinate and checks to see if Sam is safe on the left while also being safe on the right.

Con	itract and Purp	ose Sta	tement						
Every	contract has three	parts							
#		::					->		
	function name			(domain			range	_
#									
				what	does the function	do?			
Exa	mples								
Write	some examples, the	en circle ar	nd label what chan	iges					
exam	ples:								
		() i	.s				
-	function name	- `	input(s)						
				who	at the function pro	duces			
		() i	.s				
	function name		input(s)						
end				wn	at the function pro	auces			
Def	inition								
Write t	the definition, givin	g variable	names to all your	input values.					
fun		():					
	function name		variable(s)	 '					
_			wł	hat the function	ion does with those	variable(s)			
end						(-)			

Piecewise Functions

- Sometimes we want to build functions that act differently for different inputs. For example, suppose a business charges \$10/pizza, but only \$5 for orders of six or more. How could we write a function that computes the total price based on the number of pizzas?
- In math, **Piecewise Functions** are functions that can behave one way for part of their Domain, and another way for a different part. In our pizza example, our function would act like cost(pizzas) = 10 * pizzas for anywhere from 1-5 pizzas. But after 5, it acts like cost(pizzas) = 5 * pizzas.
- Piecewise functions are divided into "pieces". Each piece is divided into two parts:
 - 1. How the function should behave
 - 2. The domain where it behaves that way
- Our programming language can be used to write piecewise functions, too! Just as in math, each piece has two parts:

Piecewise functions are powerful, and let us solve more complex problems. We can use piecewise functions in a video game to add or subtract from a character's x-coordinate, moving it left or right depending on which key was pressed.

Welcome to Alice's Restaurant!

Alice has hired you to improve some code used at the restaurant. The code we'll be improving on is shown below.

Read through the code line-by-line with your partner before writing down your observations in the tables below.

```
# cost :: String -> Number
# given a item, produce the cost of that item
fun cost(item):
    ask:
        | item == "hamburger" then: 6.0
        | item == "onion rings" then: 3.5
        | item == "fried tofu" then: 5.25
        | item == "pie" then: 2.25
        | otherwise: "Sorry, that's not on the menu!"
    end
end
```

1 I notice	2 I wonder
3 Familiar things I see in the code	4) Unfamiliar things I see in the code
3 Familiar things I see in the code	4) Unfamiliar things I see in the code
3 Familiar things I see in the code	4) Unfamiliar things I see in the code
3 Familiar things I see in the code	4) Unfamiliar things I see in the code
3 Familiar things I see in the code	4) Unfamiliar things I see in the code

Alice's Restaurant - Explore

Alice's code has some new elements we haven't seen before, so let's experiment a bit to figure out how it works! **Open the** "Alice's Restaurant starter file, click "Run", and try using the cost function in the Interactions window.

1) What does cost("hamburger") evalua	ate to?		
2) What does cost("pie") evaluate to?_			
3) What if you ask for cost("fries")?			
4) Explain what the function is doing in your	own words.		
5) What is the function's name?	Domain	?Range?_	
6) What is the name of its variable?			
7) Alice says onion rings have gone up to \$3.	75. Change the cos	st function to reflect this.	
8) Try adding menu items of your own. What	s's your favorite?		
9) For an unknown food item, the function powhy not?	roduces the String	"That's not on the menu!"	Is this a problem? Why or

10) Suppose Alice wants to calculate the price of a hamburger, including a 5% sales tax. Draw a Circle of Evaluation for the

expression below.

Word Problem: order

Directions: Alice's Restaurant has hired you as a programmer. They offer the following menu items: hamburger (\$6.00), onion rings (\$3.50), fried tofu (\$5.25) and pie (\$2.25). Write a function called order which takes in the name of a menu item and outputs the price of that item.

Contract and Purp	oose Stat	tement							
Every contract has three	parts								
#	::						->		
function name				do	main			range	_
#									
			wł	nat do	es the funct	ion do?			
Examples									
Write some examples, th	en circle ar	nd label what chan	ges						
examples:									
_	()	is					
function name	_ `—	input(s)	′	-5		what the function p	roduces		
	(,	١	is		·			
function name	_ `—	input(s)	′	13		what the function p	roduces		
	1	1 (-)	١	is		,			
function name	_ '	input(s)		12		what the function p	roduces		
	1	1 (-)	١	is		,			
function name	_ '	input(s)	′	15		what the function p	roduces		
end		111001(3)				what the folicitor p	1000003		
Definition		_							
Write the definition, givi	ng variable ,	names to all your		ıes					
fun	(2.61.63):						
function nam	е	variable(s)							
ask:									
<u> </u>					then:				
					then:				
-					_				
					then:				
					_				
					then:				
					-				
otherwise:									
	-								
end									

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end

Word Problem: update-player

Directions: The player moves up and down by 20 pixels each time. Write a function called update-player, which takes in the player's x- and y-coordinate and the name of the key pressed ("up" or "down"), and returns the new y-coordinate.

Contract and Purpose Statement	
Every contract has three parts	
# ::	->
function name de	omain range
#	
what a	loes the function do?
Examples	
Write some examples, then circle and label what changes	
examples:	
() is	1
function name input(s)	what the function produces
() is	
function name input(s)	what the function produces
() is	
function name input(s)	what the function produces
() is	
function name input(s) end	what the function produces
B 6 33	
Definition	
Write the definition, giving variable names to all your input values	
fun (): function name variable(s)	
ask:	
ask:	
1	then:
l	then:
1	then:
·	
otherwise:	
end	

end

Challenges for update-player

For each of the challenges below, see if you can come up with two EXAMPLEs of how it should work!

1) Warping - Program one key to "warp" the player to a set location, such as the center of the screen.

2) Boundaries - Change update-player such that PLAYER cannot move off the top or bottom of the screen.

```
examples:
update-player( ) is

update-player( ) is
end
```

3) **Wrapping** - Add code to update-player such that when PLAYER moves to the top of the screen, it reappears at the bottom, and vice versa.

```
examples:
   update-player( ) is
   update-player( ) is
end
```

4) Hiding - Add a key that will make PLAYER seem to disappear, and reappear when the same key is pressed again.

```
examples:
   update-player( ) is
   update-player( ) is
end
```

Word Problem: line-length

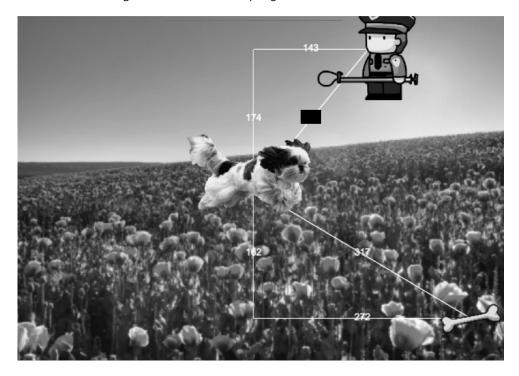
Directions: Write a function called 'line-length', which takes in two numbers and returns the **positive difference** between them. It should always subtract the smaller number from the bigger one. If they are equal, it should return zero.

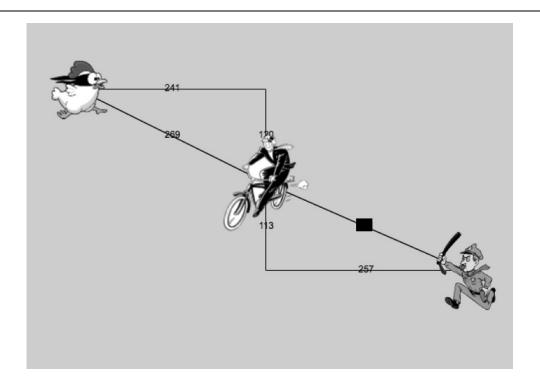
Co	ontract and Purpo	se Stat	ement					
Every	y contract has three pa	ırts						
#	::						->	
	function name			do	main		range	
#								
				what d	oes the function	qo\$		
Ex	amples							
Write	e some examples, then	circle an	d label what change	es				
exa	mples:							
	line-length	(10, 5) is	10 - 5			
_	function name	`	input(s)			what the function produces	;	
	line-length	(2, 8) is	8 - 2			
_	function name		input(s)			what the function produces	;	
end								
De	efinition							
Write	e the definition, giving	variable i	names to all your in	put values				
fun	ı	():				
	function name		variable(s)	_				
а	sk:							
- 1					then:			
- 1					then:			
е	end							

end

Writing Code to Calculate Missing Lengths

In each of the game screenshots below, one of the distance labels has been hidden. Write the code to generate the missing distance on the line below each image. Hint: Remember the Pythagorean Theorem!

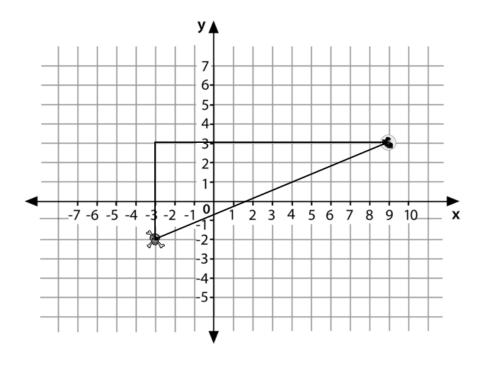




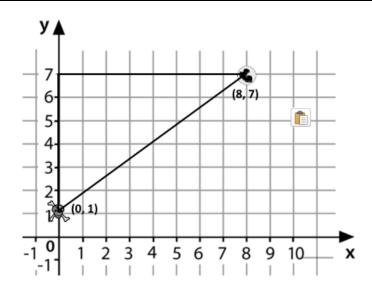
Distance on the Coordinate Plane

Distance between the pyret and the boot:

num-sqrt(num-sqr(line-length(9, -3)) + num-sqr(line-length(3, -2)))



Explain how the code works.



Now write the code to find the distance between this boot and pyret.

The Distance Between (0, 2) and (4, 5)

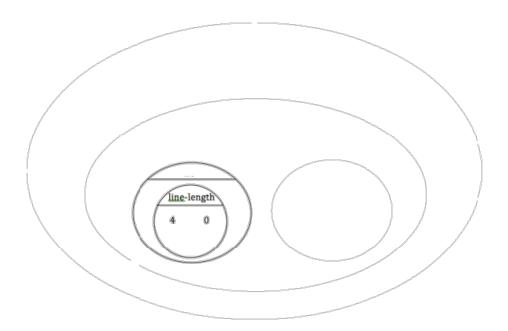
The distance between x_1 and x_2 is computed by line-length(x1, x2). The distance between y_1 and y_2 is computed by line-length(y1, y2). Below is the equation to compute the hypotenuse of a right triangle with those amount for legs:

$$\sqrt{line ext{-}length(x_2,x_1)^2+line ext{-}length(y_2,y_1)^2}$$

Suppose your player is at (0, 2) and a character is at (4, 5). What is the distance between them? With your pencil, label which numbers represent x_1, y_1, x_2 and y_2 . The equation to compute the distance between these points is:

$$\sqrt{line\text{-}length(4,0)^2 + line\text{-}length(5,2)^2}$$

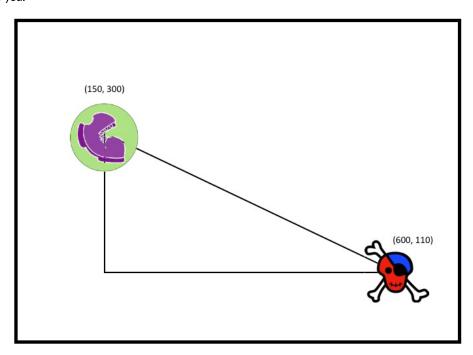
1. Translate the expression above, for (0,2) and (4,5) into a Circle of Evaluation below.



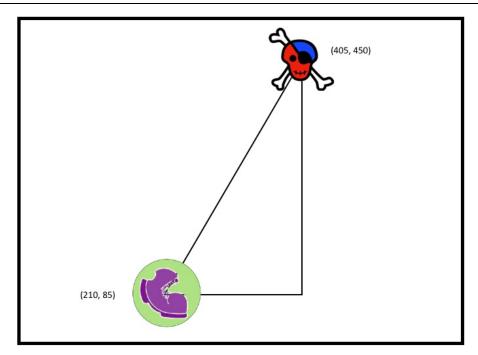
2. Convert the Circle of Evaluation to Code below.

Distance From Game Coordinates

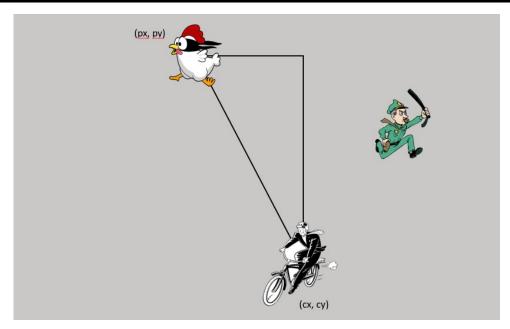
For each of the game screenshots, write the code to calculate the distance between the indicated characters. *The first one has been done for you.*



num-sqrt(num-sqr(line-length(600, 150)) + num-sqr(line-length(110, 300)))



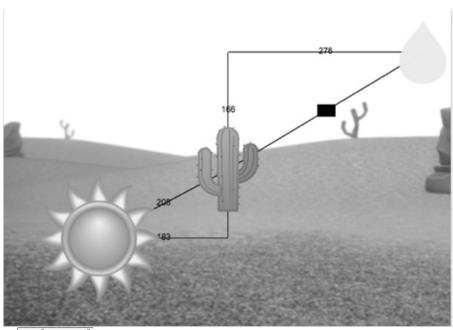
Distance (px, py) to (cx, cy)



Cor	ntract and Purpose Stateme	nt		
Every	contract has three parts			
#	::		->	
	function name	domain	range	
#				
		what does the function do?		_
Exa	mples			
Write	some examples, then circle and labe	l what changes		
exam	mples:			
	() is		
-	function name	input(s)		
		what the function produces		_
	() is		
	function name	input(s)		
		what the function produces		_
end				
Def	finition			
Write	the definition, giving variable name	s to all your input values		
fun	():		
	function name vo	riable(s)		
_		what the function does with those variable(s,		
and				

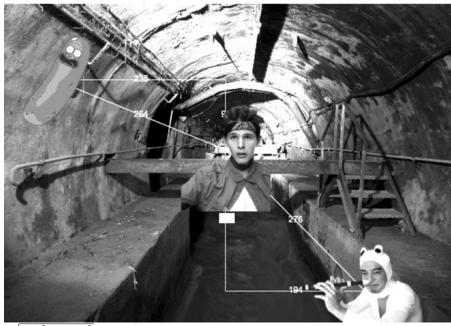
Comparing Code: Finding Missing Distances

For each of the game screenshots below, the math and the code for computing the covered distance is shown. Notice what is similar and what is different about how the top and bottom distances are calculated. Think about why those similarities and differences exist and record your thinking.



 $\sqrt{166^2+276^2}$

num-sqrt(num-sqr(166) + num-sqr(276))

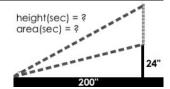


 $\sqrt{276^2-194^2}$

num-sqrt(num-sqr(276) - num-sqr(194))

Top Down/Bottom Up

A retractable flag pole starts out 24 inches tall, and grows taller at a rate of 0.6 in/sec. An elastic is anchored 200 inches from the base and attached to the top of the pole, forming a right triangle. Using a top-down or bottom-up strategy, define functions that compute the *height* of the pole and the *area* of the triangle after a given number of seconds.



Directions: Define your first function (height or area) here.

Со	ntract and Purp	ose Stat	tement					
Every	contract has three	parts						
#		::				->		
	function name				domain		range	
#								
_				wl	hat does the fur	nction do?		
Ex	amples							
Write	some examples, th	en circle ar	nd label what cha	nges				
exa	mples:							
		()	is			
_	function name		input(s)			what the function produces		
		()	is			
	function name		input(s)			what the function produces		
end								
De	finition							
Write	the definition, givi	ng variable	names to all you	r input valu	es			
fun		():				
	function name	9	variable(s)					
end				what the fur	nction does with	those variable(s)		<u> </u>
<u> </u>								
Dire	ections : Define	your sec	ond function (height	or area) here.		
	ntract and Purp							
	contract has three							
#						->		
<i>"</i> —	function name	-"			domain		range	
#								
_				wi	hat does the fur	action do?		
Ex	amples							
	some examples, th	en circle ar	nd lahel what cha	nges				
	mples:	en en ele al	ia label What cha	1,903				
	<u></u>	1)	is			
_	function name	_ '	input(s)			what the function produces		
	iononominamo	1	,20.(0))	is	ae renenen predeces		
_	function name	_ '	input(s)			what the function produces		
end			7 (-)			, , , , , , , , , , , , , , , , , , , ,		
De	finition							
	the definition, givi	ng variahle	names to all vous	r innut valu	IPS			
fun		is variable	names to an you) :				
Luii	function name	'	variable(s)					
			(-/					
_				what the fur	nction does with	those variable(s)		_
end						• •		

Word Problem: is-collide

Directions: Use the Design Recipe to write a function is-collide, which takes in the coordinates of two objects and checks if they are close enough to collide.

Contract ar	nd Purpose Statemer	nt	
Every contract h	nas three parts		
#	::		->
function n	name	domain	range
#			
		what does the function do	98
Examples			
Write some exan	mples, then circle and label	what changes	
examples:			
	() is	
function	name	nput(s) w	vhat the function produces
	() is	
function	name	nput(s)	
		what the function produ	1000
end		what the function produ	uces
Definition			
Write the definit	tion, giving variable names	to all your input values	
fun	():	
funct	tion name var	iable(s)	
		what the function does with those v	ariable(s)

end

Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String, String) -> Image tells us that the name of the function is ellipse, it takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (100, 50, "outline", "red") will evaluate to an

Image.				
Name		Domain		Range
# num-sqr	••	Number	^	Number
num-sqr(9)				
# num-sqrt	::	${\tt Numbe} r$	^	Number
num-sqrt(25)				
# string-length	::	String	^	Number
string-length("Rainbow"}				
# string-contains	::	String, String	^	Boolean
string-contains("catnap", "c	"cat")			
# triangle	••	Number, String, String	^	Image
triangle(80, "solid", "darkgreen")	reen")			
# star	::		^	
# circle	••		^	
# square	::		^	
# rectangle	••		^	

Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String, String) -> Image tells us that the name of the function is ellipse, it takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (50, 100, "solid", "teal") will evaluate to an

Range ۸ ۸ ${\displaystyle \mathop{\wedge}_{I}}$ ${\displaystyle \mathop{\wedge}_{I}}$ ۸ ۸ ${\displaystyle \mathop{\wedge}_{I}}$ Ŷ î Domain ••• :: :: :: isosceles-triangle # regular-polygon right-triangle ; triangle-sas star-polygon # radial-star # rhombus # ellipse # text Image. Name #

takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (100, 50, "solid", "fuchsia") will evaluate to an Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String, String) -> Image tells us that the name of the function is ellipse, it

Image.		
Name	Domain	Range
# triangle-asa	::	^1
# image-url	••	^
# scale		^-
# rotate		^-
# overlay		^
# put-image		^-
# flip-horizontal	••	^-
# flip-vertical	••	^
# above	::	^

takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (100, 50, "outline", "darkgreen") will evaluate Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String, String) -> Image tells us that the name of the function is ellipse, it to an Image.

6		
Name	Domain	Range
# beside	::	^-
# or	•	^-
# and	•	^-
#	::	^-
#		
#	::	^-
#		
#	::	<-
#		
#	::	^-
#		
#	::	^-
#		
#	::	^-
#		