



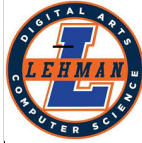
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# Fall 2021 Precalc Lesson 13.1

Dr. O'Brien  
Herbert H. Lehman High School  
13 December 2021

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VOCAB:  
nested loop

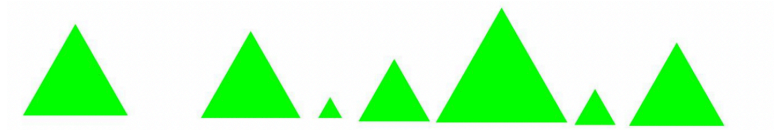


### Do now

be sure to: Get out your **binder**. Make sure you receive your **Brainstorm your own game** worksheet. Copy the **goal** and answer **do now** questions below. Write a complete sentence for each answer:

Let's say we want to make the image below in Pyret.

1. What functions would we need to use (check your contracts handout).
2. Make a **prediction**: How many lines of code would we need to run?

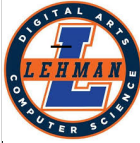


**class:** precalc **goal:** HDW define our own functions in Pyret?

1 seems more efficient, since you're only asking one question.

+How can we measure 'efficiency'? which operation is faster? One will probably take less time

+What might be some problems with situation (1)? if a lot of people share the same birthday as you, it might get confusing.



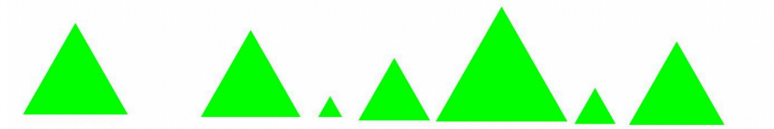
### Do now

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Copy the **goal** and answer **do now** questions below. Write a complete sentence for each answer:

Making this would get find of tedious because  
because we'd be using the triangle function over  
and over again.

There has to be a better way...

```
triangle( 50, "solid", "green")  
triangle( 80, "solid", "green")  
triangle(200, "solid", "green")  
triangle(275, "solid", "green")
```

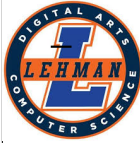


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#### framing

- **what:** define our own functions in Pyret
- **why:** Making our own functions will be useful to getting our images to move around on the screen in our game. But it will also deepen our understanding of mathematical functions.
- **where to:** using functions in Pyret to solve mathematical word problems

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## Vocab

be sure to: Keep your **notebook** open. These definitions should be in your Glossary. If not Copy each definition, in your Pyret Glossary.

### example

Shows the use of a function on specific inputs and the computation the function should perform on those inputs

### function

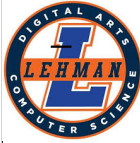
a mathematical object that takes in an input and produces a unique output

### function definition

Code that names a function, defines its arguments, and states the expression to compute when code is used

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### Coding to learn: warm up

be sure to: Answer the questions below in your **notebook**. Be prepared to share out.

1. Define a function  $f(x)$  so that it will **output** the appropriate values given the **inputs** to the right
2. Define a function  $g(x)$  so that it will give the appropriate **outputs** given the **inputs** to the right
3. How could you write a **contract** specifying the **domain** and **range** for  $f(x)$  and  $g(x)$ ?

$$\begin{aligned}f(1) &= 4 \\f(2) &= 5 \\f(3) &= 6 \\f(5) &= 8\end{aligned}$$

$$\begin{aligned}g(1) &= 3 \times 1 = 3 \\g(2) &= 3 \times 4 = 12 \\g(3) &= 3 \times 9 = 27 \\g(5) &= 3 \times 25 = 75\end{aligned}$$

**class:** precalc **goal:** HDW define our own functions in Pyret?

1.  $f(x) = x + 3$
2.  $g(x) = 3x^2$
3. the contract will be Number  $\rightarrow$  Number; in other words the domain maps any real number to another real number.

Model how to write functions in pyret (next page)



**be sure to:** Write the definitions below in your **notebook**.

$$\begin{array}{l} f(1) = 4 \\ f(2) = 5 \\ f(3) = 6 \\ f(5) = 8 \end{array}$$

$g(1) = 3 \times 1 = 3$ $g(2) = 3 \times 4 = 12$ $g(3) = 3 \times 9 = 27$ $g(5) = 3 \times 25 = 75$
--

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## #FUNCTION DEFINITIONS

+How are the function definitions in Pyret different from standard math definitions? They're written in a funny way, with fun at the beginning and end telling us where the function ends. Also instead of an '=' we have a ':'.



### Mini-lesson

be sure to: on your computer, open **Monday Examples pyret file** in Google classroom.  
Examine the code with Dr. O'Brien

Dr. O'Brien 12/13

```
#1 WARM UP EXAMPLES
#CONTRACT
#f :: Number -> Number
#g :: Number -> Number

#EXAMPLES
examples:
  f(1) is 4
  f(2) is 5
  f(3) is 6
  f(5) is 8
end

examples:
  g(1) is 3 * 1
  g(2) is 3 * 4
  g(3) is 3 * 9
  g(5) is 3 * 25
end

#FUNCTION DEFINITIONS
fun f(x): x + 3 end
fun g(x): 3 * num-sqr(x) end
```

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The examples block creates a set of examples which are test on the function. If the function returns the correct output for each input, they pass.

Illustrate by changing def. of  $f(x)$  to  $x + 4$ , then change value of output.





## Coding to learn: activity

Be sure to... work with your partner to answer these questions in your notebook. Write code in your Pyret file as needed.

1. Examine the examples and function definition for the function `gt`. Describe how the function works.
2. How could you write a contract identifying the domain and range for `gt`?
3. Write out a function `gt2()` that produces a triangle with double the size of the input.
4. Will the domain and range for `gt2()` be any different from `gt()`? Explain why or why not in a complete sentence.
5. Bonus questions:
  - A. How could you rewrite `gt2()` as the composition two functions? Describe the functions and experiment with rewriting the function in Pyret.
  - B. Write a function in Pyret for  $h(x) = \sqrt{3x^2 - 2}$ . Describe the contract for this function.

**class:** precalc **goal:** HDW define our own functions in Pyret?

+Examine the examples and function definition for the function `gt`. Describe how the function works. -> the function takes in a number and produces a solid green triangle of that size.

+How could you write a contract identifying the domain and range for `gt`? `gt :: Number -> Image`

+Write out a function `gt2()` that produces a triangle with double the size of the input.

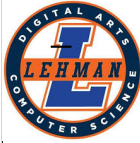
`gt(x): triangle(2 * x, "solid", "green")`

Will the domain and range for `gt2()` be any different from `gt()`? Explain why or why not in a complete sentence. No, because the function can still take any positive number and produces an image as an output.

Bonus questions:

How could you rewrite `gt2()` as the composition two functions? Describe the functions and experiment with rewriting the function in Pyret. `f(x): 2 * x` and `gt2(x): gt(f(x))`

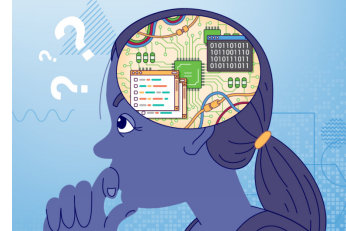
Write a function in Pyret for . Describe the contract for this function. `h(x): num-sqrt((2 * num-sqr(x)) - 2)`



## Reflection: Thinking about thinking

be sure to: Answer each question below with a complete sentence.

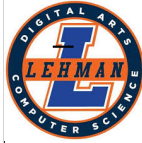
1. Why is it useful for a programmer to be able to define a function?
2. Why is it useful to be able to define a function in math?
3. How do you think functions will make it easier to build our video game?



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1. answers will vary.
2. using functions for manipulating images, e.g. `scale()`, `overlay`, etc.

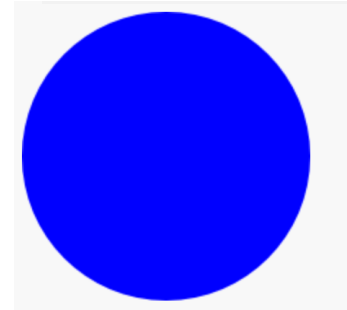


### exit ticket

be sure to: Answer each question below with a complete sentence.

Let's say we want to define a function called `bc()` that would make a solid blue circle of whatever radius we want.

1. Write out how to define this function in Pyret.
2. What would the contract for this function look like?



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1. How many times does the for loop iterate? How many times does the while loop iterate? Why are they different?
2. The for loop will iterate 5 times. The while loop will iterate 6 times. The while loop will iterate one more time because the inequality `<=` is used instead of `<`. The while loop will run when the variable = 5 whereas the for loop will not.