



Fall 2021 Pre-calculus Lesson 5.2

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Lehman High School
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students need calculators
no new vocab



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do now

be sure to: Get out your binder. Copy goal and answer do now questions below. Show all work or write a complete sentence for each answer.

1. What's the parent function for $f(x)$?
2. How's $f(x)$ being transformed from its parent function?
3. Sketch a graph for $f(x)$.

$$f(x) = (x + 2)^2 + 3$$

class: pre-calculus goal: HDW write quadratic equations in standard form?

1. The basic quadratic is x^2 .
2. It's being shifted 3 right and 2 up.
3. Sketch on board. Upward facing with vertex at (3,2)



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framing



- **what:** write quadratic equations in standard form
- **why:** The quadratic equation can be used to model things in science, engineering, and more!
- **where to:** Identifying x-intercept of a quadratic

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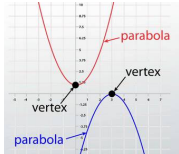
the plan: We'll go through one of the Pset #5 word problems together.
You'll work with a partner to solve some other word problems



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Vocabulary

Vertex: Minimum or maximum point of a quadratic function



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definition of quadratic function

Let a , b , and c be real numbers with $a \neq 0$. The function:

$$f(x) = ax^2 + bx + c$$

is called a quadratic function.

Write in notes.



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Example

- Trajectory of a rocket :

$$h(x) = 16t^2 + 256t + 4$$



Draw picture on board, $h(x)$ is the height of the rocket at any time t

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The problem

If you write your equation like this:

$$f(x) = ax^2 + bx + c$$

How can you figure out how it's being shifted from the parent function?

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In other words how do we identify the vertex?



$$f(x) = x^2 + 4x + 7$$

How can we rewrite this in a form where we can identify the vertex?

$$f(x) = 2x^2 + 8x + 7$$

$$f(x) = 2(x^2 + 4x) + 7$$

Use box method to show $x^2 + 4x$ is part of $x^2 + 4x + 4 - 4$

$$= (x + 2)^2 + 3$$

This is the same as the equation from the do now



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standard form for quadratic equation

$$f(x) = a(x - h)^2 + k$$

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(h, k) denotes the vertex

If a is less than 0 frown

If a is > 0 smile!



Another example

$$g(x) = 2x^2 + 8x - 9$$

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Problem set

Be sure to:

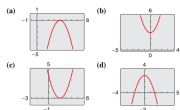
- Work at a volume 0 **first 4 minutes**
- Then you can check in with a **neighbor**
- **Do work in your notebook**
- **Show all work**

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In Exercises 1-4 match the quadratic function with its graph.

1. $f(x) = (x - 2)^2$
2. $f(x) = x^2 + 3$
3. $f(x) = 3 - x^2$
4. $f(x) = -(x - 2)^2$



For 3 and 4, sketch the graph of the function

5. $y = -x^2$
6. $y = (x + 3)^2$

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In (7-9) describe the graph of the function and identify the vertex.

7. $f(x) = 20 - x^2$

8. $f(x) = (x + 3)^2 - 4$

9. $h(x) = x^2 - 2x + 1$

10. For $f(x) = 2x^2$, $g(x) = x + 4$, (a) $f \circ g$, (b) $g \circ f$, and (c) try to find $(f \circ g)(0)$.

For (11) and (12) below, find two functions f and g such that $(f \circ g)(x) = h(x)$. There are many right answers, explain in a complete sentence why yours is correct:

11. $h(x) = \sqrt{x^2 - 4}$

12. $h(x) = \frac{4}{(5x + 3)^2}$

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+how rewrite in standard form?check notes!

How identify composite functions? Find a simpler function in the bigger one



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exit ticket

be sure to: Answer on a sheet of loose leaf paper. Show all work or write a complete sentence for each answer:

1. Rewrite $h(x) = x^2 - 2x + 1$ in **standard form**.

2. Sketch a graph for the equation, identifying the vertex.

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$$(x^2 - 2x - 1) + 1 + 1$$

$$(x - 1)^2 + 2$$

vertex = (1,2)

2. sketch an upward facing quadratic with vertex at (1,2).