PROJECT DESCRIPTION

We have implemented the research paper Weighted Guided Image Filtering with Steering Kernel (attached in the folder) and merged it with 3 other research papers, namely Guided Image Filtering, Kernel Regression and Single Haze Removal for the purpose of application in Image Dehazing and Enhancement using SKWGIF.

We have divided the project into three parts namely:

- 1. Steering Kernel WGIF Implementation
- 2. Image Dehazing Using SKWGIF and Histogram Equalization
- 3. Coloured Image Dehazing Using SKWGIF

• Steering Kernel WGIF Implementation

We have implemented WGIF with a Steering Kernel (SKWGIF). GIF and WGIF suffers from Halo Artifacts. SKWGIF takes advantage of WGIF over GIF while leveraging the edge direction more sufficiently. The code uses Steering Kernel which in turn requires local gradient matrices. The steering kernel helps us to identify the energy dominant directions. We have used different values for the radius of the local window and the regularization parameter. The comparison results clearly show the advantage of using SKWGIF over WGIF and GIF.

Code

```
Grad mat = [[dummy mat for j in range(img.shape[1])] for i in range(img.shape[0])]
  for i in range(1, img.shape[0]-1):
    for j in range(1, img.shape[1]-1):
      Gij = []
      roi = img[i-1:i+2, j-1:j+2]
      gx = cv2.Sobel(roi, cv2.CV 64F, 1, 0, ksize = 1)
      gy = cv2.Sobel(roi, cv2.CV_64F, 0, 1, ksize = 1)
      gx = np.reshape(gx,(9, ))
      gy = np.reshape(gy,(9, ))
      Gij.append(gx)
      Gij.append(gy)
      Grad_mat[i][j] = np.transpose(Gij)
  return Grad_mat
def steering_kernel(img):
  This Function Returns Steering Kernel Matrices.
  Parameters
  img: Image
  Returns
  W: 2D Numpy Matrix
    Matrix containing Steering Kernel Weight Matrices for each pixel in input image.
  Grad mat = Grad func(img*255)
  dummy mat = np.array([[0 for j in range(3)] for i in range(3)])
  W = [[dummy_mat for j in range(img.shape[1])] for i in range(img.shape[0])]
  for i in range(1, img.shape[0]-1):
    for j in range(1, img.shape[1]-1):
      u, s, v = np.linalg.svd(Grad_mat[i][j])
      v2 = v[1]
      if v2[1] == 0:
        theta = pi/2
      else:
        theta = np.arctan(v2[0]/v2[1])
      sigma = (s[0] + 1.0)/(s[1] + 1.0)
      gamma = sqrt(((s[0]*s[1]) + 0.01)/9)
      Rot_mat = np.array([[cos(theta), sin(theta)], [-(sin(theta)), cos(theta)]])
      El_mat = np.array([[sigma, 0], [0, (1/sigma)]])
      C = gamma*(np.dot(np.dot(Rot_mat, El_mat), np.transpose(Rot_mat)))
      coeff = sqrt(np.linalg.det(C))/(2*pi*(5.76))
      W_i = [[0 \text{ for q in range}(3)] \text{ for p in range}(3)]
      for n_i in range(i-1, i+2):
        for n_j in range(j-1, j+2):
           xi = np.array([i, j])
           xk = np.array([n_i, n_j])
```

```
xik = xi - xk
          wik = coeff*(exp(-(np.dot(np.transpose(xik), C), xik))/(11.52)))
          W_i[n_i-i+1][n_j-j+1] = wik
      W[i][j] = W_i
  return W
def Guided Image Filter(im,p,r,eps):
 This Function returns the output for
 Guided Image Filter applied on Input Image.
 Parameters
 im: Guidance Image
 p: Input Filter Image
 r: Radius of Kernel
 eps: Regularization parameter
 Returns
 q: Output Image after GIF application
 mean I = cv2.boxFilter(im,cv2.CV 64F,(r,r))
 mean p = cv2.boxFilter(p, cv2.CV 64F,(r,r))
 mean Ip = cv2.boxFilter(im*p,cv2.CV 64F,(r,r))
 cov lp = mean lp - mean l*mean p
 mean_II = cv2.boxFilter(im*im,cv2.CV_64F,(r,r))
 var_l = mean_ll - mean_l*mean_l
 a = cov_lp/(var_l + eps)
 b = mean_p - a*mean_I
 mean a = cv2.boxFilter(a,cv2.CV 64F,(r,r))
 mean b = cv2.boxFilter(b,cv2.CV 64F,(r,r))
 cv2.imshow("Edge GIF", mean a)
 q = mean a*im + mean b
 return q
def Weighted_Guided_Image_Filter(im, p, r, r2, eps, lamda, N):
 This Function returns the output for Weighted
 Guided Image Filter applied on Input Image.
 Parameters
  _____
 im: Guidance Image
```

```
r: Radius of Kernel
 r2 : Radius of Local Window centered at a particular pixel
 eps: Regularization parameter
 lamda: small constant dependent on dynamic range
 N: Number of Pixels in the Input image
 Returns
 q : Output Image after WGIF application
 mean I = cv2.boxFilter(im,cv2.CV 64F,(r,r))
 mean 12 = cv2.boxFilter(im, cv2.CV 64F,(r2,r2))
 mean_p = cv2.boxFilter(p, cv2.CV_64F,(r,r))
 mean_p2 = cv2.boxFilter(p, cv2.CV_64F, (r2,r2))
 corr_I = cv2.boxFilter(im*im, cv2.CV_64F,(r,r))
 corr I2 = cv2.boxFilter(im*im,cv2.CV 64F,(r2,r2))
 corr Ip = cv2.boxFilter(im*p,cv2.CV 64F,(r,r))
 var I = corr I - mean I*mean I
 var I2 = corr I2 - mean I2*mean I2
 Psil = ((var_12 + lamda)*np.sum(1/(var_12 + lamda)))/N
 cov_lp = corr_lp - mean_l*mean_p
 a_psi = cov_lp/(var_l + eps/Psil)
 b_psi = mean_p - (a_psi)*mean_I
 mean_ap = cv2.boxFilter(a_psi,cv2.CV_64F,(r2,r2))
 mean bp = cv2.boxFilter(b psi,cv2.CV 64F,(r2,r2))
 cv2.imshow("Edge WGIF", mean ap)
 qp = mean ap*im + mean bp
 return qp
def SK Weighted Guided Image Filter(im,p,r,r2,eps,lamda,N):
 This Function returns the output for Steering Kernel
 Weighted Guided Image Filter applied on Input Image.
 Parameters
 im: Guidance Image
```

p: Input Filter Image

```
p: Input Filter Image
r: Radius of Kernel
r2: Radius of Local Window centered at a particular pixel
eps: Regularization parameter
lamda: small constant dependent on dynamic range
N: Number of Pixels in the Input image
Returns
q : Output Image after SKWGIF application
mean I = cv2.boxFilter(im,cv2.CV 64F,(r,r))
mean 12 = cv2.boxFilter(im, cv2.CV 64F,(r2,r2))
mean_p = cv2.boxFilter(p, cv2.CV_64F,(r,r))
mean_p2 = cv2.boxFilter(p, cv2.CV_64F, (r2,r2))
corr_I = cv2.boxFilter(im*im, cv2.CV_64F,(r,r))
corr_I2 = cv2.boxFilter(im*im,cv2.CV_64F,(r2,r2))
corr Ip = cv2.boxFilter(im*p,cv2.CV 64F,(r,r))
var I = corr I - mean I*mean I
var I2 = corr I2 - mean I2*mean I2
Psil = ((var_l2+lamda)*np.sum(1/(var_l2+lamda)))/N
cov_lp = corr_lp - mean_l*mean_p
a_psi = cov_lp/(var_l + eps/Psil)
b_psi = mean_p - (a_psi)*mean_I
W = steering kernel(im)
mean a = [[0 for j in range(im.shape[1])] for i in range(im.shape[0])]
mean b = [[0 for j in range(im.shape[1])] for i in range(im.shape[0])]
for i in range(1, im.shape[0]-1):
  for j in range(1, im.shape[1]-1):
    Wk = W[i][j]
    roi_a = a_psi[i-1:i+2, j-1:j+2]
    roi b = b psi[i-1:i+2, j-1:j+2]
    mean a[i][j] = np.sum(Wk*roi a)
    mean b[i][j] = np.sum(Wk*roi b)
mean a = np.array(mean a)
```

```
mean b = np.array(mean b)
  mean_b = b_psi
  cv2.imshow("Edge SKWGIF", mean a)
  q = mean_a*im + mean_b
  return q
def TransmissionRefine(im, et, r, eps, lamda, N):
  Parameters
  im: Guidance Image
  et : Input Filter Image
  r: Radius of kernel
  eps: Regularization Parameter
  lamda: small constant dependent on dynamic range
  N: Number of Pixels in the Input image
  Returns
  None.
  gray = np.float64(im)/255
  rd = 3
  GIF = Guided_Image_Filter(gray, gray, r, eps)
  WGIF = Weighted_Guided_Image_Filter(gray, gray, r, rd, eps, lamda, N)
  SKWGIF = SK_Weighted_Guided_Image_Filter(gray, gray, r, rd, eps, lamda, N)
  cv2.imshow("GIF", GIF)
  cv2.imshow("WGIF", WGIF)
  cv2.imshow("SKWGIF", SKWGIF)
src = cv2.imread("cat.png")
gray = cv2.cvtColor(src, cv2.COLOR_BGR2GRAY)
cv2.imshow("gray image", gray)
minimum = np.min(gray)
maximum = np.max(gray)
L = (maximum-minimum)
lamda = (0.001*L)**2
rows, columns = gray.shape
N = rows*columns
r = [2, 4, 8]
eps = [0.01, 0.04, 0.16]
TransmissionRefine(gray, gray, r[0], eps[0], lamda, N)
```

RESULTS AND COMPARISON:

COMPARISON 1:

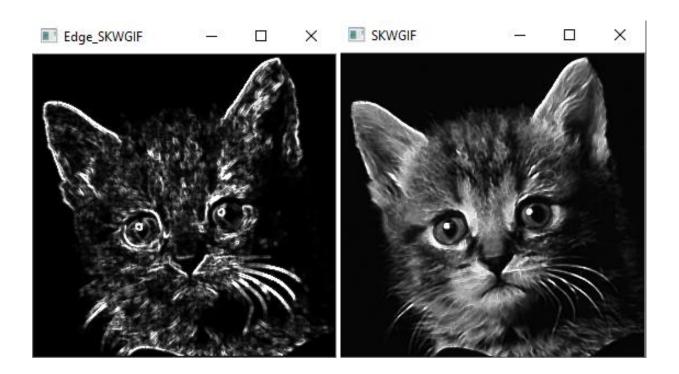
ORIGINAL IMAGE





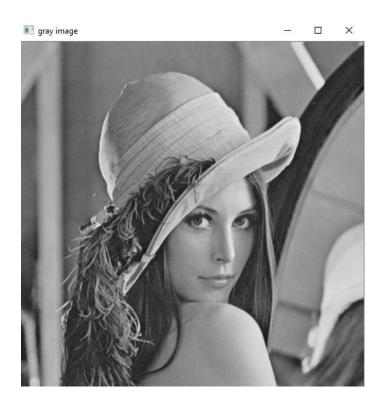
WGIF FILTERING OUTPUT

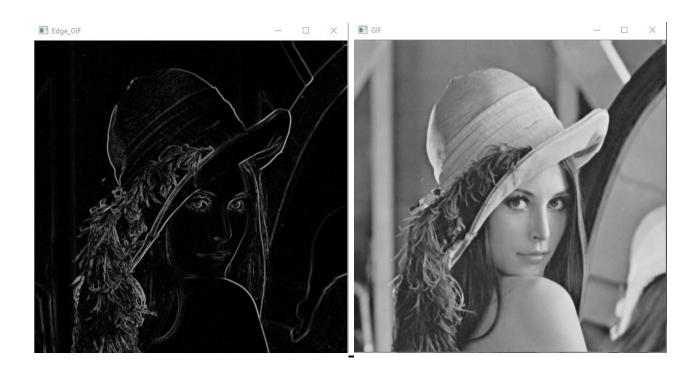




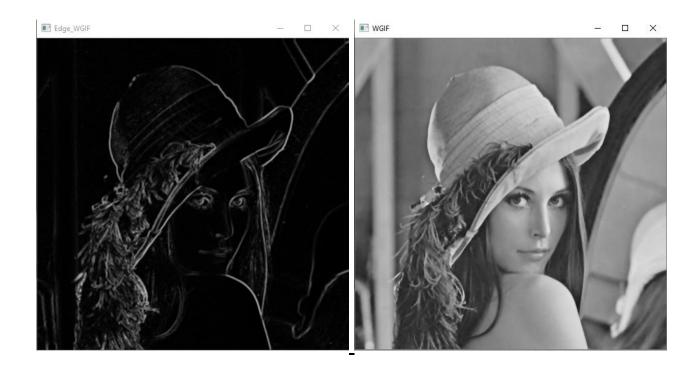
COMPARISON 2:

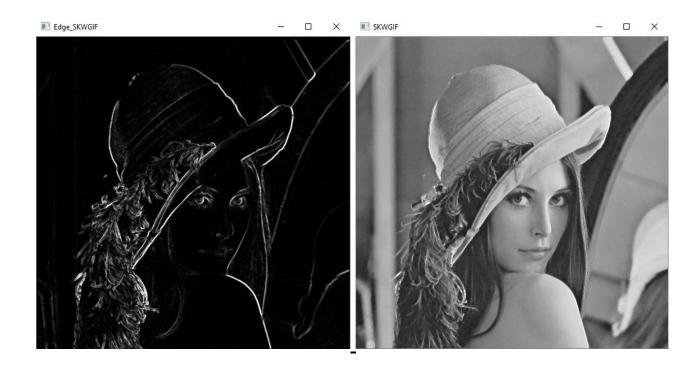
ORIGINAL IMAGE





WGIF FILTERING OUTPUT



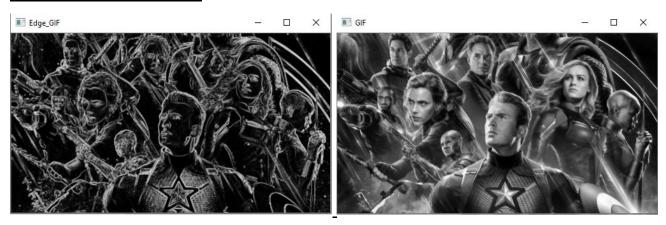


COMPARISON 3:

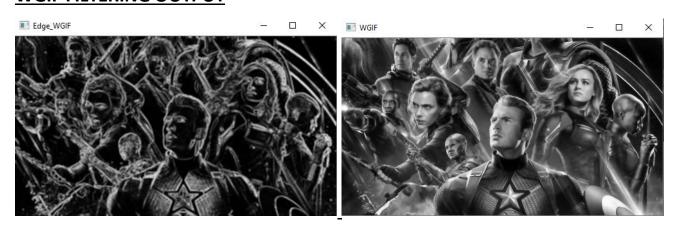
ORIGINAL IMAGE

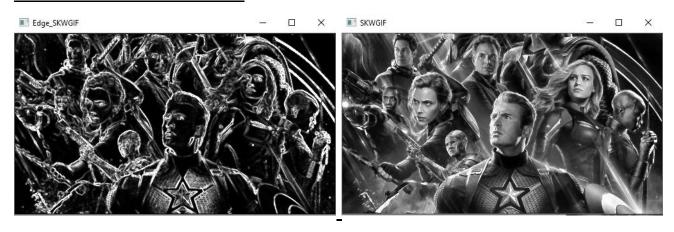


GIF FILTERING OUTPUT



WGIF FILTERING OUTPUT





• Image Dehazing Using SKWGIF and Histogram Equalization

We have implemented Image Dehazing for Grayscale Images. First, we applied Histogram Equalization to increase the dynamic range of the image. Then we have used SKWGIF for detail enhancement and edge retention which reduces the contrast of background noise. The Code uses Histogram Equalization function followed by SKWGIF function. The results are presented by varying the values for radius of local window and regularization parameter. SKWGIF gives better results than GIF and WGIF due to supreme edge detection.

Code

```
import cv2
import cv2
import numpy as np
from math import *
#Histogram equalisation
def Histogram Eq(resized image):
  This Function returns Histogram Equalised Image for Contrast Enhancement.
  Parameters
  resized image: Input Image
  Returns
  resized image: Histogram Equalized Image
  r = []
  no_of_pixel = (resized_image.shape[0] * resized_image.shape[1])
  r = np.ravel(resized image)
  unique, count = np.unique(r, return_counts=True)
  #print(unique)
  counts = np.zeros((256, ))
  val = 0
  for i in range(256):
    if i in unique:
      counts[i] = count[val]
      val += 1;
  sigma_list = []
  sigma list.append(counts[0])
  for i in range(1, 256):
    cnt = counts[i]
```

```
sigma list.append(sigma list[i - 1] + cnt)
  sigma list = np.array(sigma list)
  final_list = (sigma_list*255)/(no_of_pixel)#[(x*255)/(no_of_pixel) for x in sigma_list]
  for i in range(resized image.shape[0]):
    for j in range(resized image.shape[1]):
       temp = resized image[i][j]
       resized_image[i][j] = final_list[temp]
  return resized image
def Grad func(img):
  This Function returns Local Gradient Matrices.
  Parameters
  -----
  img: Image
     Input Image for which Local Gradient Matrices are to be found.
  Returns
  Grad_mat: 2D Numpy Matrix
        Matrix containing Local Gradient Matrix for every pixel in input image.
  dummy mat = np.array([[0.00 for j in range(2)] for i in range(9)])
  Grad mat = [[dummy mat for j in range(img.shape[1])] for i in range(img.shape[0])]
  for i in range(1, img.shape[0]-1):
    for j in range(1, img.shape[1]-1):
      Gij = []
      roi = img[i-1:i+2, j-1:j+2]
      gx = cv2.Sobel(roi, cv2.CV 64F, 1, 0, ksize = 1)
      gy = cv2.Sobel(roi, cv2.CV_64F, 0, 1, ksize = 1)
      gx = np.reshape(gx,(9, ))
      gy = np.reshape(gy,(9, ))
      Gij.append(gx)
      Gij.append(gy)
      Grad mat[i][j] = np.transpose(Gij)
  return Grad mat
def steering kernel(img):
  This Function Returns Steering Kernel Matrices.
  Parameters
  img: Image
  Returns
  W: 2D Numpy Matrix
```

```
Grad mat = Grad func(img*255)
  dummy_mat = np.array([[0 for j in range(3)] for i in range(3)])
  W = [[dummy mat for j in range(img.shape[1])] for i in range(img.shape[0])]
  for i in range(1, img.shape[0]-1):
    for j in range(1, img.shape[1]-1):
      u, s, v = np.linalg.svd(Grad_mat[i][j])
      v2 = v[1]
      if v2[1] == 0:
        theta = pi/2
      else:
        theta = np.arctan(v2[0]/v2[1])
      sigma = (s[0] + 1.0)/(s[1] + 1.0)
      gamma = sqrt(((s[0]*s[1]) + 0.01)/9)
      Rot mat = np.array([[cos(theta), sin(theta)], [-(sin(theta)), cos(theta)]])
      El_mat = np.array([[sigma, 0], [0, (1/sigma)]])
      C = gamma*(np.dot(np.dot(Rot mat, El mat), np.transpose(Rot mat)))
      coeff = sqrt(np.linalg.det(C))/(2*pi*(5.76))
      W_i = [[0 \text{ for q in range}(3)] \text{ for p in range}(3)]
      for n_i in range(i-1, i+2):
        for n_j in range(j-1, j+2):
           xi = np.array([i, j])
           xk = np.array([n_i, n_j])
           xik = xi - xk
           wik = coeff*(exp(-(np.dot(np.transpose(xik), C), xik))/(11.52)))
           W_i[n_i-i+1][n_j-j+1] = wik
      W[i][j] = W i
  return W
def Guided_Image_Filter(im,p,r,eps):
  This Function returns the output for
  Guided Image Filter applied on Input Image.
  Parameters
  im: Guidance Image
  p: Input Filter Image
  r: Radius of Kernel
  eps: Regularization parameter
  Returns
  q: Output Image after GIF application
```

Matrix containing Steering Kernel Weight Matrices for each pixel in input image.

```
mean_I = cv2.boxFilter(im,cv2.CV_64F,(r,r))
 mean_p = cv2.boxFilter(p, cv2.CV_64F,(r,r))
 mean_lp = cv2.boxFilter(im*p,cv2.CV_64F,(r,r))
 cov_lp = mean_lp - mean_l*mean_p
 mean_II = cv2.boxFilter(im*im,cv2.CV_64F,(r,r))
 var_l = mean_ll - mean_l*mean_l
 a = cov_lp/(var_l + eps)
 b = mean_p - a*mean_I
 mean_a = cv2.boxFilter(a,cv2.CV_64F,(r,r))
 mean b = cv2.boxFilter(b,cv2.CV 64F,(r,r))
 cv2.imshow("Edge_GIF", mean_a)
 q = mean a*im + mean b
 return q
def Weighted Guided Image Filter(im, p, r, r2, eps, lamda, N):
 This Function returns the output for Weighted
 Guided Image Filter applied on Input Image.
 Parameters
  -----
 im: Guidance Image
 p: Input Filter Image
 r: Radius of Kernel
 r2 : Radius of Local Window centered at a particular pixel
 eps: Regularization parameter
 lamda: small constant dependent on dynamic range
 N: Number of Pixels in the Input image
 Returns
 q: Output Image after WGIF application
 mean_I = cv2.boxFilter(im,cv2.CV_64F,(r,r))
 mean_I2 = cv2.boxFilter(im, cv2.CV_64F,(r2,r2))
```

mean_p = cv2.boxFilter(p, cv2.CV_64F,(r,r)) mean_p2 = cv2.boxFilter(p, cv2.CV_64F, (r2,r2))

```
corr I = cv2.boxFilter(im*im, cv2.CV 64F,(r,r))
 corr I2 = cv2.boxFilter(im*im,cv2.CV 64F,(r2,r2))
 corr Ip = cv2.boxFilter(im*p,cv2.CV_64F,(r,r))
 var I = corr I - mean I*mean I
 var I2 = corr I2 - mean I2*mean I2
 Psil = ((var_12 + lamda)*np.sum(1/(var_12 + lamda)))/N
 cov_lp = corr_lp - mean_l*mean_p
 a psi = cov_lp/(var_l + eps/Psil)
 b_psi = mean_p - (a_psi)*mean_I
 mean ap = cv2.boxFilter(a psi,cv2.CV 64F,(r2,r2))
 mean bp = cv2.boxFilter(b_psi,cv2.CV_64F,(r2,r2))
 cv2.imshow("Edge_WGIF", mean_ap)
 qp = mean ap*im + mean bp
 return ap
def SK_Weighted_Guided_Image_Filter(im,p,r,r2,eps,lamda,N):
 This Function returns the output for Steering Kernel
 Weighted Guided Image Filter applied on Input Image.
 Parameters
  -----
 im: Guidance Image
 p: Input Filter Image
 r: Radius of Kernel
 r2 : Radius of Local Window centered at a particular pixel
 eps: Regularization parameter
 lamda: small constant dependent on dynamic range
 N: Number of Pixels in the Input image
 Returns
 q: Output Image after SKWGIF application
 mean I = cv2.boxFilter(im,cv2.CV 64F,(r,r))
 mean 12 = cv2.boxFilter(im, cv2.CV 64F,(r2,r2))
 mean p = cv2.boxFilter(p, cv2.CV 64F,(r,r))
```

```
mean p2 = cv2.boxFilter(p, cv2.CV 64F, (r2,r2))
 corr I = cv2.boxFilter(im*im, cv2.CV 64F,(r,r))
 corr I2 = cv2.boxFilter(im*im,cv2.CV 64F,(r2,r2))
 corr Ip = cv2.boxFilter(im*p,cv2.CV 64F,(r,r))
 var I = corr I - mean I*mean I
 var_I2 = corr_I2 - mean_I2*mean_I2
 Psil = ((var_12 + lamda)*np.sum(1/(var_12 + lamda)))/N
 cov_lp = corr_lp - mean_l*mean_p
 a psi = cov lp/(var I + eps/PsiI)
 b_psi = mean_p - (a_psi)*mean_l
 W = steering kernel(im)
 mean a = [[0 for j in range(im.shape[1])] for i in range(im.shape[0])]
 mean b = [[0 for j in range(im.shape[1])] for i in range(im.shape[0])]
 for i in range(1, im.shape[0]-1):
    for j in range(1, im.shape[1]-1):
      Wk = W[i][j]
      roi_a = a_psi[i-1:i+2, j-1:j+2]
      roi b = b psi[i-1:i+2, j-1:j+2]
      mean_a[i][j] = np.sum(Wk*roi_a)
      mean b[i][j] = np.sum(Wk*roi b)
 mean a = np.array(mean a)
 mean_b = np.array(mean_b)
 mean b = b psi
 cv2.imshow("Edge_SKWGIF", mean_a)
 q = mean_a*im + mean_b
 return q
def TransmissionRefine(im, et, r, eps, lamda, N):
 Parameters
  -----
 im: Guidance Image
 et: Input Filter Image
 r: Radius of kernel
 eps: Regularization Parameter
 lamda: small constant dependent on dynamic range
```

N: Number of Pixels in the Input image

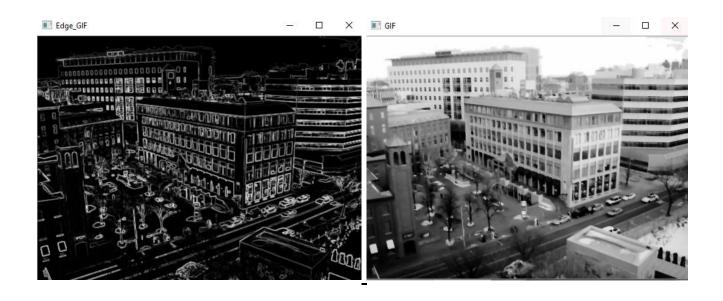
```
Returns
  None.
  gray = np.float64(im)/255
  rd = 3
  GIF = Guided Image Filter(gray, gray, r, eps)
  WGIF = Weighted_Guided_Image_Filter(gray, gray, r, rd, eps, lamda, N)
  SKWGIF = SK_Weighted_Guided_Image_Filter(gray, gray, r, rd, eps, lamda, N)
  cv2.imshow("GIF", GIF)
  cv2.imshow("WGIF", WGIF)
  cv2.imshow("SKWGIF", SKWGIF)
original image = cv2.imread('Input Images Used\Building with Haze.png', cv2.IMREAD GRAYSCALE)
cv2.imshow("original_image", original_image)
histogram equalised image = Histogram Eq(original image)
gray = histogram_equalised_image
minimum = np.min(gray)
maximum = np.max(gray)
L = (maximum-minimum)
lamda = (0.001*L)**2
rows, columns = gray.shape
N = rows*columns
r = 2
eps = 0.01
TransmissionRefine(gray, gray, r, eps, lamda, N)
```

RESULT AND ANALYSIS

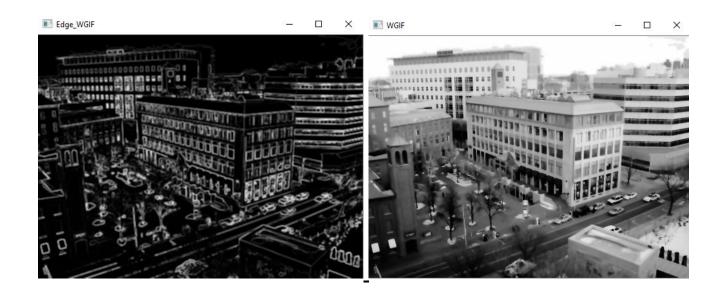
COMPARISON 1:

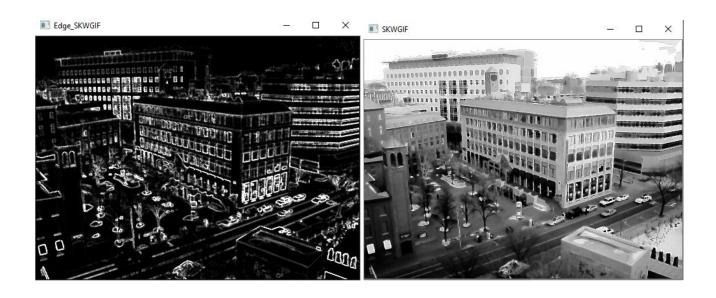
ORIGINAL IMAGE





WGIF FILTERING OUTPUT





COMPARISON 2: ORIGINAL IMAGE



GIF FILTERING OUTPUT



WGIF FILTERING OUTPUT





• Coloured Image Dehazing Using SKWGIF

We have implemented image dehazing for coloured images using SKWGIF and Dark Channel Prior. Instead of using Laplacian matrix to refine the haze transmission map, we simply use SKWGIF to filter the raw transmission map under the guidance of the hazy image. The code uses Dark Channel Function, AtmLight Function, Transmission Refine and Recovery function along with SKWGIF function for guided image filtering. The results come out with a large amount of haze removed and visually similar to the original method while being a simpler algorithm and with less overhead.

Code

```
import cv2
from math import *
import numpy as np;
def DarkChannel(im,sz):
  """ This Function is used to get the pixel values
  whose intensity is very low in the given colour channel """
  b,g,r = cv2.split(im)
  dc = cv2.min(cv2.min(r,g),b);
  kernel = cv2.getStructuringElement(cv2.MORPH RECT,(sz,sz))
  dark = cv2.erode(dc,kernel)
  return dark
def AtmLight(im,dark):
  """ This Function is used to estimate
  the atmospheric light in image"""
  [h,w] = im.shape[:2]
  imsz = h*w
  numpx = int(max(floor(imsz/1000),1))
  darkvec = dark.reshape(imsz,1);
  imvec = im.reshape(imsz,3);
  indices = darkvec.argsort();
  indices = indices[imsz-numpx::]
  atmsum = np.zeros([1,3])
  for ind in range(1,numpx):
   atmsum = atmsum + imvec[indices[ind]]
  A = atmsum / numpx;
  return A
```

```
def TransmissionEstimate(im,A,sz):
  """ This Function deletes the preliminary transmittal
  based on latent area obtained from dark channel"""
  omega = 0.95;
  im3 = np.empty(im.shape,im.dtype);
  for ind in range(0,3):
    im3[:,:,ind] = im[:,:,ind]/A[0,ind]
  transmission = 1 - omega*DarkChannel(im3,sz);
  return transmission
def Grad_func(img):
  This Function returns Local Gradient Matrices.
  Parameters
  -----
  img: Image
     Input Image for which Local Gradient Matrices are to be found.
  Returns
  Grad mat: 2D Numpy Matrix
        Matrix containing Local Gradient Matrix for every pixel in input image.
  dummy mat = np.array([[0.00 for j in range(2)] for i in range(9)])
  Grad_mat = [[dummy_mat for j in range(img.shape[1])] for i in range(img.shape[0])]
  for i in range(1, img.shape[0]-1):
    for j in range(1, img.shape[1]-1):
      Gii = []
      roi = img[i-1:i+2, j-1:j+2]
      gx = cv2.Sobel(roi,cv2.CV_64F, 1, 0, ksize = 1)
      gy = cv2.Sobel(roi, cv2.CV_64F, 0, 1, ksize = 1)
      gx = np.reshape(gx,(9, ))
      gy = np.reshape(gy,(9, ))
      Gij.append(gx)
      Gij.append(gy)
      Grad mat[i][j] = np.transpose(Gij)
  return Grad mat
def steering kernel(img):
  This Function Returns Steering Kernel Matrices.
  Parameters
  img: Image
  Returns
```

```
W: 2D Numpy Matrix
    Matrix containing Steering Kernel Weight Matrices for each pixel in input image.
  Grad mat = Grad func(img*255)
  dummy mat = np.array([[0 for j in range(3)] for i in range(3)])
  W = [[dummy mat for j in range(img.shape[1])] for i in range(img.shape[0])]
  for i in range(1, img.shape[0]-1):
    for j in range(1, img.shape[1]-1):
      u, s, v = np.linalg.svd(Grad_mat[i][j])
      v2 = v[1]
      if v2[1] == 0:
        theta = pi/2
      else:
        theta = np.arctan(v2[0]/v2[1])
      sigma = (s[0] + 1.0)/(s[1] + 1.0)
      gamma = sqrt(((s[0]*s[1]) + 0.01)/9)
      Rot mat = np.array([[cos(theta), sin(theta)], [-(sin(theta)), cos(theta)]])
      El mat = np.array([[sigma, 0], [0, (1/sigma)]])
      C = gamma*(np.dot(np.dot(Rot_mat, El_mat), np.transpose(Rot_mat)))
      coeff = sqrt(np.linalg.det(C))/(2*pi*(5.76))
      W_i = [[0 \text{ for q in range}(3)] \text{ for p in range}(3)]
      for n i in range(i-1, i+2):
        for n j in range(j-1, j+2):
           xi = np.array([i, j])
           xk = np.array([n_i, n_j])
           xik = xi - xk
           wik = coeff*(exp(-(np.dot(np.transpose(xik), C), xik))/(11.52)))
           W i[n i-i+1][n j-j+1] = wik
      W[i][j] = W i
  return W
def SK_Weighted_Guided_Image_Filter(im,p,r,r2,eps,lamda,N):
  This Function returns the output for Steering Kernel
  Weighted Guided Image Filter applied on Input Image.
  Parameters
  _____
  im: Guidance Image
  p: Input Filter Image
  r: Radius of Kernel
  r2: Radius of Local Window centered at a particular pixel
  eps: Regularization parameter
```

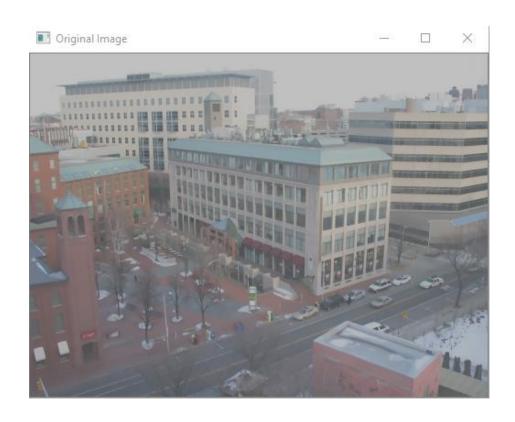
```
N: Number of Pixels in the Input image
 Returns
  _____
 q: Output Image after SKWGIF application
 mean I = cv2.boxFilter(im,cv2.CV 64F,(r,r))
 mean 12 = cv2.boxFilter(im, cv2.CV 64F,(r2,r2))
 mean_p = cv2.boxFilter(p, cv2.CV_64F,(r,r))
 mean_p2 = cv2.boxFilter(p, cv2.CV_64F, (r2,r2))
 corr_I = cv2.boxFilter(im*im, cv2.CV_64F,(r,r))
 corr 12 = cv2.boxFilter(im*im,cv2.CV 64F,(r2,r2))
 corr_Ip = cv2.boxFilter(im*p,cv2.CV_64F,(r,r))
 var I = corr I - mean I*mean I
 var I2 = corr I2 - mean I2*mean I2
 Psil = ((var_12 + lamda)*np.sum(1/(var_12 + lamda)))/N
 cov_lp = corr_lp - mean_l*mean_p
 a psi = cov lp/(var I + eps/PsiI)
 b psi = mean p - (a psi)*mean I
 W = steering kernel(im)
 mean_a = [[0 for j in range(im.shape[1])] for i in range(im.shape[0])]
 mean b = [[0 for j in range(im.shape[1])] for i in range(im.shape[0])]
 for i in range(1, im.shape[0]-1):
    for j in range(1, im.shape[1]-1):
      Wk = W[i][j]
      roi_a = a_psi[i-1:i+2, j-1:j+2]
      roi b = b psi[i-1:i+2, i-1:j+2]
      mean a[i][j] = np.sum(Wk*roi a)
      mean b[i][j] = np.sum(Wk*roi b)
 mean a = np.array(mean a)
 mean_b = np.array(mean_b)
 mean b = b psi
 #cv2.imshow("Edge_SKWGIF", mean_a)
 q = mean_a*im + mean_b
 return q
def TransmissionRefine(im,et):
 Parameters
```

```
im: Guidance Image
  et : Input Filter Image
  Returns
  t: Final image
  gray = cv2.cvtColor(im,cv2.COLOR_BGR2GRAY);
  gray = np.float64(gray)/255;
  r = 32;
  eps = 0.01;
  minimum = np.min(gray)
  maximum = np.max(gray)
  L = (maximum-minimum)
  lamda = (0.001*L)**2
  rows, columns = gray.shape
  N = rows*columns
  t = SK_Weighted_Guided_Image_Filter(gray, et, r, 3, eps, lamda, N);
  return t;
def Recover(im,t,A,tx = 0.1):
  """ This function recovers a haze-free image determined by three surface
  colour values as well as transmission value at every pixel."""
  res = np.empty(im.shape,im.dtype);
  t = cv2.max(t,tx);
  for ind in range(0,3):
    res[:,:,ind] = (im[:,:,ind]-A[0,ind])/t + A[0,ind]
  return res
fn = "Input Images Used\Building with Haze Color.jpg"
src = cv2.imread(fn);
I = src.astype('float64')/255;
dark = DarkChannel(I,15);
A = AtmLight(I,dark);
te = TransmissionEstimate(I,A,15);
t = TransmissionRefine(src,te);
J = Recover(I,t,A,0.1);
cv2.imshow("dark",dark);
cv2.imshow("Transmission Image",t);
cv2.imshow('Original Image',src);
cv2.imshow('Final Image',J);
```

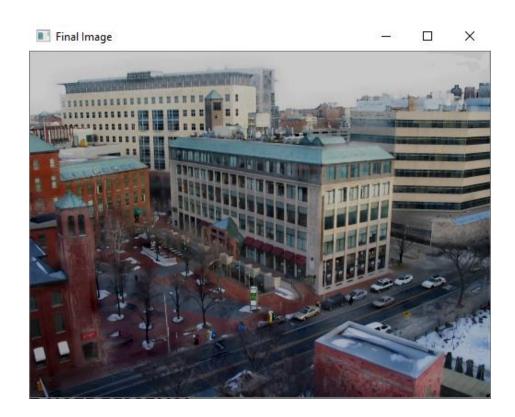
RESULT AND ANALYSIS

RESULT 1:

ORIGINAL IMAGE

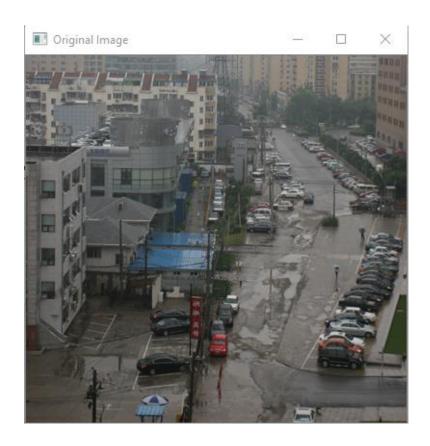


FINAL IMAGE AFTER HAZE REMOVAL



RESULT 2:

ORIGINAL IMAGE



FINAL IMAGE AFTER HAZE REMOVAL

